

$$\Delta U > 0$$

$$\rightarrow \left. \frac{\partial^2 U}{\partial x^2} \right|_{x, z} > 0$$

$$x = \{S, N, V\}$$

gen. force

$$\left. \frac{\partial T}{\partial S} \right|_{N, V} > 0 ; - \left. \frac{\partial P}{\partial V} \right|_{S, N} > 0 ; \left. \frac{\partial \mu}{\partial N} \right|_{S, V} > 0$$

gen. displ. ||

$$C_V = T \left. \frac{\partial S}{\partial T} \right|_V > 0 ; \kappa_S = - \frac{1}{V} \left. \frac{\partial V}{\partial P} \right|_{S, N} > 0$$

Same for  $F, G, H$ :

Show  $G(T, P, N)$

$\Rightarrow \Delta G > 0$  MINIMUM WRT  
EXTENSIVE STATE VARIABLES  
NOT FIXED BY EXTERNAL  
CONSTRAINTS.

$$\rightarrow \left. \frac{\partial^2 G}{\partial N^2} \right|_{P, T} > 0 \quad \rightarrow \left. \frac{\partial \mu}{\partial N} \right|_{P, T} > 0$$

$$\left. \frac{\partial^2 G}{\partial T^2} \right|_{p, N} = - \left. \frac{\partial S}{\partial T} \right|_{p, N} = - \frac{C_p}{T} < 0$$

BECAUSE

$$C_p > 0$$

$$F(T, V, N) \Rightarrow K_T > 0 ; \left. \frac{\partial \mu}{\partial N} \right|_{T, V} > 0$$

$$H(S, p, N) \Rightarrow C_p > 0 ; \left. \frac{\partial \mu}{\partial N} \right|_{S, p} > 0$$

$$\frac{T}{V K_S C_V} > \frac{\alpha^2 T^2}{C_V^2 K_T}$$

$$C_V > \frac{K_S}{K_T} \alpha^2 T V$$

$$C_p - C_V = \frac{\alpha^2 T V}{K_T} \rightarrow C_V > \frac{K_S}{K_T} (C_p - C_V)$$

$$\downarrow$$

$$C_p - C_V > 0 \quad (+) \quad C_V > 0$$

$$\rightarrow C_p > C_V > 0$$

$$K_T - K_S = \frac{V T \alpha^2}{C_p} > 0$$

$$K_T > K_S > 0$$

SUMMARY:  $\frac{\partial Y}{\partial X} \Big|_{\substack{\text{not } Y \\ \text{not } X}} > 0$

WHERE  $(Y, X)$  ARE CONJUGATE GENERALIZED FORCE/DISPLACEMENT PAIR.

$$\rightarrow \frac{\partial X}{\partial Y} = \frac{1}{\frac{\partial Y}{\partial X}} > 0$$

1. 4.

5. Maxwell  $\rightarrow$  2 p. deriv

$\rightarrow$  correct in Triple product rule

$$\left( \begin{array}{c} \phantom{Y} \end{array} \right) \left( \begin{array}{c} \phantom{X} \end{array} \right) \left( \begin{array}{c} \phantom{P} \end{array} \right) = -1$$

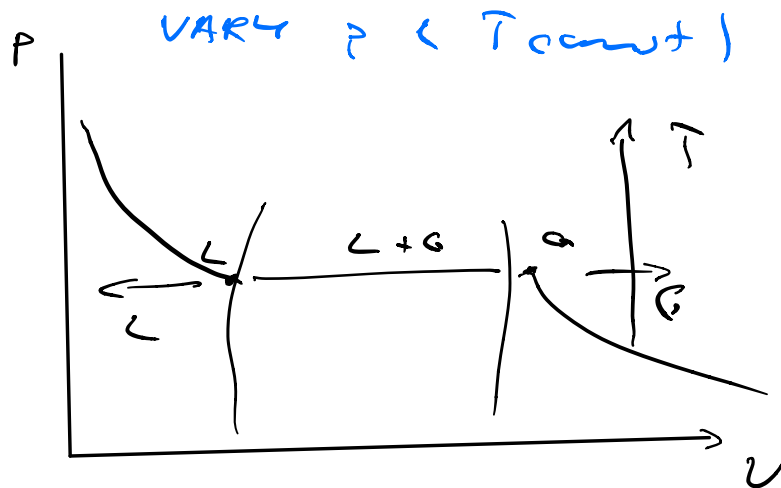
$\left\{ \begin{array}{l} \text{given by} \\ \text{relations} \end{array} \right.$

$\uparrow$  stability  $> 0$

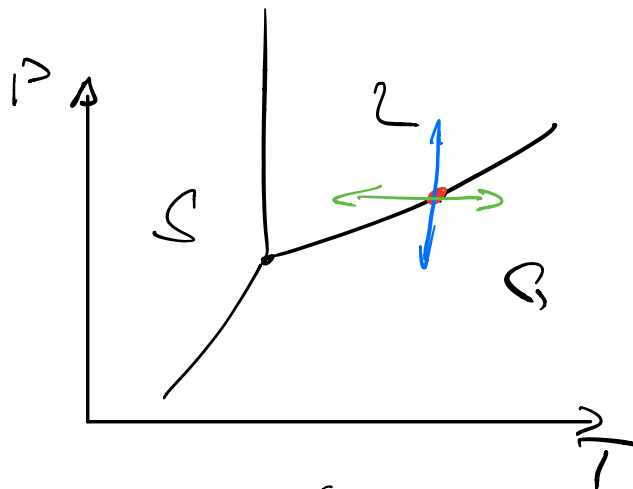
$> 0$

5. fudge.

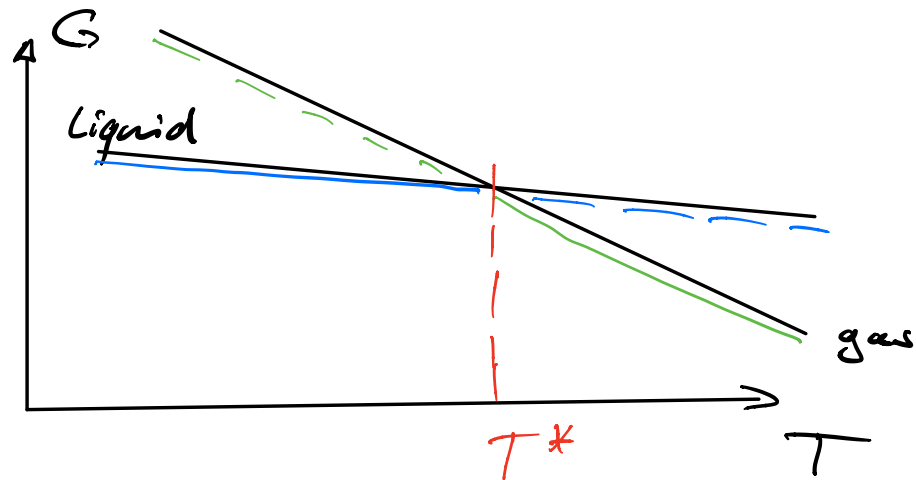
$$\alpha = \frac{1}{V} \frac{\partial V}{\partial T} \Big|_P \geq 0$$



CONSIDER VARYING  $T$  HOLDING  $p, N$  CONSTANT



$$p, T, N \rightarrow G(T, p, N)$$



$$-\frac{\partial G}{\partial T} = S \quad \rightarrow \quad S_{\text{gas}} > S_{\text{liquid}}$$

$N = \text{const}$ , system is extensive

$$G = \mu N \quad \rightarrow \quad G_L = G_g$$

$$\rightarrow \mu_L = \mu_g$$

CALCULATE CHANGE IN ENTROPY

$$\Delta S = \int \frac{dQ}{T} \quad \uparrow \quad T = T^* = \text{const} \quad = \frac{1}{T^*} \int dQ = \frac{Q}{T^*} = \frac{L \cdot N}{T^*}$$

$L$ : Latent heat per particle.

$$L = \frac{\Delta S \cdot T^*}{N}$$

MODEL OF A PHASE  
TRANSITION

IDEAL GAS  $pV = NkT$   
no phase transition

good approximation to DILUTE  
REAL GASES

REAL GASES: STARTING FROM IDEAL  
GAS AND ADD CORRECTIONS IN  
POWERS OF DENSITY  $n = \frac{N}{V}$ :

$$P = kT \left( \frac{N}{V} \right)$$

$$= kT \frac{N}{V} \left( 1 + B_2(T) \frac{N}{V} + B_3(T) \left( \frac{N}{V} \right)^2 + \dots \right)$$

known as VIRIAL expansion.

$B_n(T)$  : VIRIAL COEFFICIENTS.

→ SIMPLE APPROXIMATION FOR A REAL GAS

$$PV = NkT$$

1)  $V \rightarrow V - V_{\text{excl.}}$

↳ from finite size of molecules

$$V_{\text{excl}} \propto N \cdot b$$

2) ATTRACTIVE INTERACTION BETWEEN PARTICLES

potential energy per particle DUE TO THE ATTRACTION

$$u_{\text{attr}} \propto \frac{N}{V} \quad \text{--- from nearby molecules}$$

$$U_{\text{attr}} \propto N u_{\text{attr}}$$

$$= -a N \cdot \frac{N}{V} = -a \frac{N^2}{V}$$

$a > 0$

$$P_{\text{attr}} = - \left. \frac{\partial U}{\partial V} \right|_{N, S} = - \left( -a \frac{N^2}{V} \right) \left( -\frac{1}{V} \right) \\ = -a \frac{N^2}{V^2}$$

$$P = \frac{NkT}{V - Nb} + P_{\text{attr}}$$

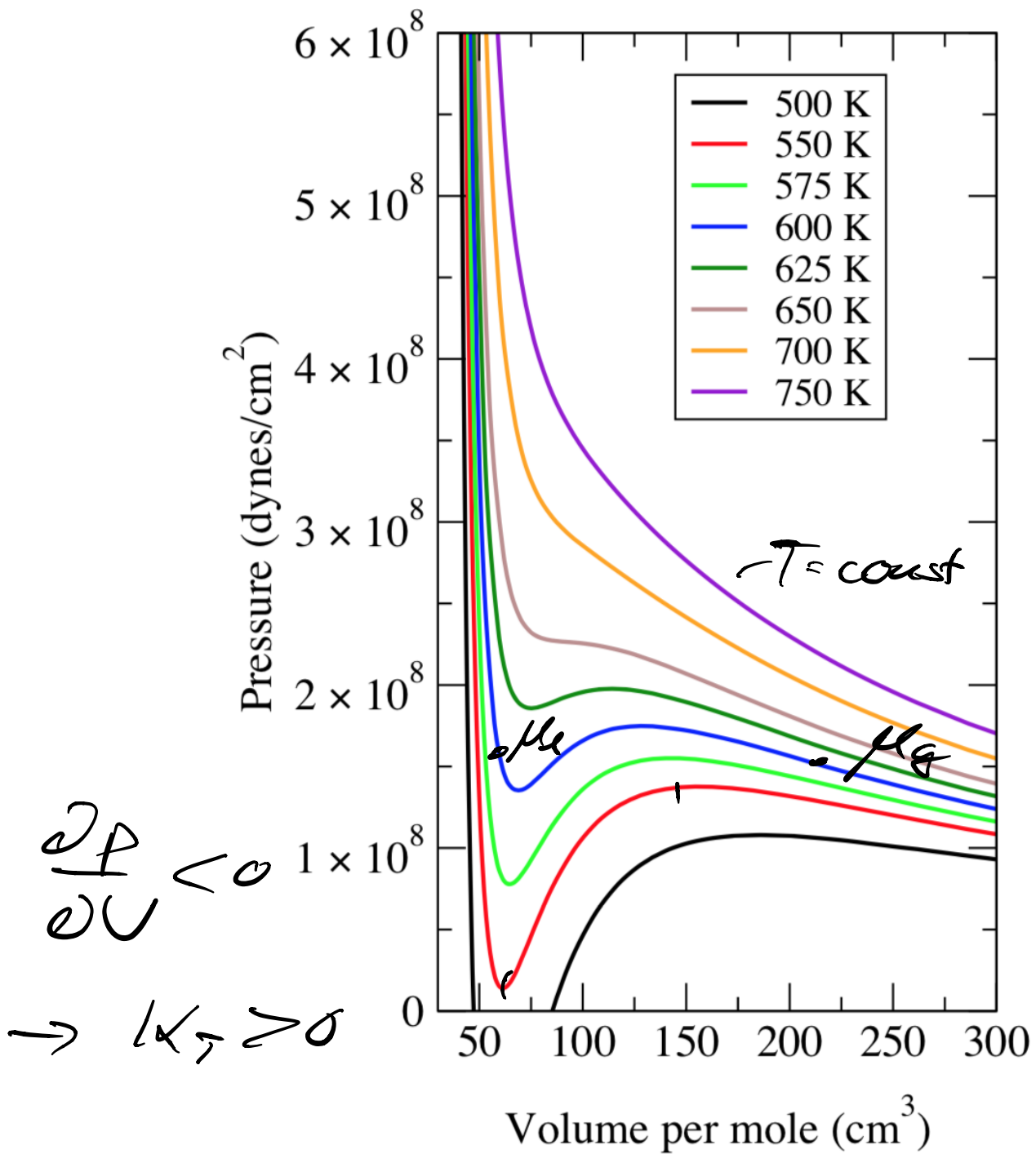
$$\Rightarrow \left[ \left( P + \frac{aN^2}{V^2} \right) (V - Nb) = NkT \right]$$

van der Waals EOS

Quiz 5, due 5pm, Tuesday 4/21

1. Intro to van der Waals EOS

Do problems 11.1 and 11.2 a) (not b) in EOPC.





# MAXWELL CONSTRUCTION

$$\mu_l(V_l) = \mu_g(V_g) \quad | \cdot N$$

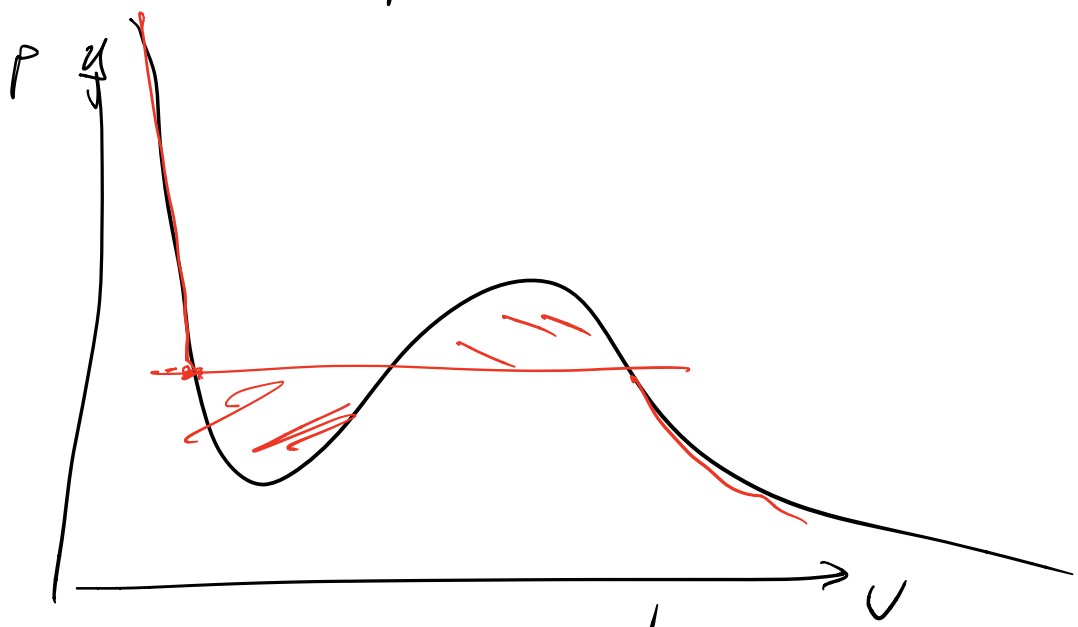
$$G_l(V_l) = G_g(V_g)$$

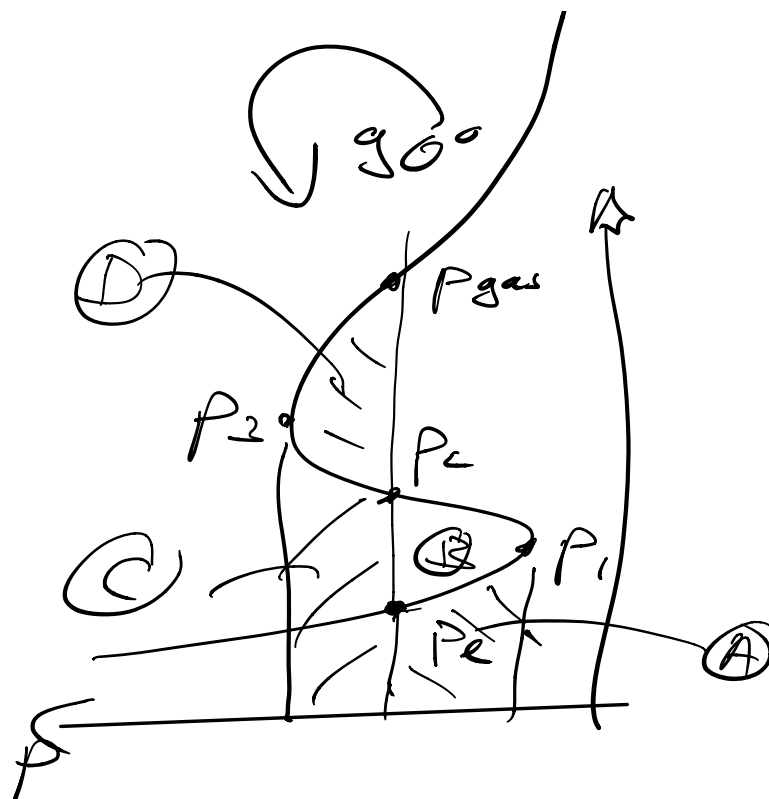
$$dG = -SdT + Vdp + \mu dN$$

$$T = \text{const}, N = \text{const}$$

$$dG = +Vdp$$

$$\Delta G = \int_{G_l}^{G_g} dG = \int_{P_l}^{P_g} V dp$$





$$\int_{P_2}^{P_1} V dP = \int_{P_2}^{P_1} V dP + \int_{P_1}^{P_2} V dP + \int_{P_2}^{P_1} V dP + \int_{P_1}^{P_2} V dP$$

~~- (A)~~    + (A) + (B)    ~~(C)~~    - ~~(D)~~    (D)

(Area B) = (Area D)  
 ≡ Maxwell construction