

5.

It so happens that this function can be simplified as:

$$\begin{aligned} j(e) &= \frac{-1+e^3}{-2+e+e^2} \\ &= \frac{(e-1)(e^2+e+1)}{(e-1)(e+2)} \\ &= \frac{e^2+e+1}{e+2} \end{aligned}$$

To find the vertical asymptote :

$$e+2=0$$

$$e=-2$$

There is a vertical asymptote at $e=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-1+e^3}{-2+e+e^2} = \frac{e^2+e+1}{e+2} = \frac{3}{e+2} + (e-1)$$

There is an oblique asymptote at $t=e-1$

