3. Which of the following are correct calculations for difference quotient of: $z\left(r\right)=5\ r^{2}+7\ r+1$

```
\begin{split} z\,(\,r) &= 5\,\,r^2 \,+\, 7\,\,r \,+\, 1 \\ z\,(\,r + h) &= 5\,\,\left(h \,+\, r\right)^{\,2} \,+\, 7\,\,\left(h \,+\, r\right) \,+\, 1 \\ &= 5\,\,h^2 \,+\, 10\,\,h\,\,r \,+\, 7\,\,h \,+\, 5\,\,r^2 \,+\, 7\,\,r \,+\, 1 \\ \frac{z\,(\,r + h) \,-\, z\,(\,r\,)}{h} &= \frac{\left(5\,\,h^2 \,+\, 10\,\,r\,\,h \,+\, 7\,\,h \,+\, 5\,\,r^2 \,+\, 7\,\,r \,+\, 1\right) \,-\, \left(5\,\,\left(\,r \,+\, 1\right)^{\,2} \,+\, 7\,\,\left(\,r \,+\, 1\right) \,+\, 1\right)}{h} \\ &= \frac{5\,\,h^2 \,+\, 10\,\,r\,\,h \,+\, 7\,\,h}{h} \\ &= \frac{h\,(\,5\,\,h \,+\, 10\,\,r \,+\, 7\,)}{h} \\ &= 5\,\,h \,+\, 10\,\,r \,+\, 7 \end{split}
```

```
z(r) = 5 r^{2} + 7 r + 1
z(r+h) = 5 (h+r)^{2} + 7 (h+r) + 1
= 5 h^{2} + 10 h r + 17 h + 5 r^{2} + 17 r + 13
\frac{z(r+h) - z(r)}{h} = \frac{\left(5 h^{2} + 10 r h + 17 h + 5 r^{2} + 17 r + 13\right) - \left(5 r^{2} + 7 r + 1\right)}{h}
= \frac{5 h^{2} + 10 r h + 7 h}{h}
= \frac{h(5 h + 10 r + 7)}{h}
= 5 h + 10 r + 7
```

```
\begin{split} z\,(\,r) &= 5\,\,r^2 \,+\, 7\,\,r \,+\, 1 \\ z\,(\,r + h) &= 5\,\,\left(\,h \,+\, r\,\right)^{\,2} \,+\, 7\,\,\left(\,h \,+\, r\,\right) \,\,+\, 1 \\ &= 5\,\,h^2 \,+\, 10\,\,h\,\,r \,+\, 7\,\,h \,+\, 5\,\,r^2 \,+\, 7\,\,r \,+\, 1 \\ \frac{z\,(\,r + h) \,-\, z\,(\,r\,)}{h} &= \frac{\left(\,5\,\,h^2 + 10\,\,r\,\,h + 7\,\,h + 5\,\,r^2 + 7\,\,r + 1\,\right) \,-\,\left(\,5\,\,r^2 + 7\,\,r + 1\,\right)}{h} \\ &= \frac{5\,\,h^2 + 10\,\,r\,\,h + 7\,\,h}{h} \\ &= \frac{h\,(\,5\,\,h + 10\,\,r + 7\,)}{h} \\ &= 5\,\,h \,+\, 10\,\,r \,+\, 7\, \end{split}
```

```
\begin{split} z\,(\,r) &= 5\,\,r^2 \,+\, 7\,\,r \,+\, 1 \\ z\,(\,r + h) &= 5\,\,\left(\,h \,+\, r\,\right)^{\,2} \,+\, 7\,\,\left(\,h \,+\, r\,\right) \,\,+\, 1 \\ &= 5\,\,h^2 \,+\, 10\,\,h\,\,r \,-\, 3\,\,h \,+\, 5\,\,r^2 \,-\, 3\,\,r \,-\, 1 \\ \frac{z\,(\,r + h) \,-\, z\,(\,r\,)}{h} &= \frac{\left(\,5\,\,h^2 + 10\,\,r\,\,h + 27\,\,h + 5\,\,r^2 + 27\,\,r + 35\,\right) - \left(\,5\,\,r^2 + 7\,\,r + 1\,\right)}{h} \\ &= \frac{5\,h^2 + 10\,\,r\,\,h + 7\,\,h}{h} \\ &= \frac{h\,(\,5\,\,h + 10\,\,(\,r + 1) \,+\, 7\,)}{h} \\ &= 5\,\,h \,+\, 10\,\,r \,+\, 7 \end{split}
```

Solution