5. Which of the following are correct calculations for difference quotient of:  $k(z) = 2 z^2 + 3 z + 4$   $k(z) = 2 z^2 + 3 z + 4$   $k(z+h) = 2 (h+z)^2 + 3 (h+z) + 4$ 

$$\begin{split} & k\left(z\right) = 2\ z^{2} + 3\ z + 4 \\ & k\left(z+h\right) = 2\ \left(h+z\right)^{2} + 3\ \left(h+z\right) + 4 \\ & = 2\ h^{2} + 4\ h\ z + 3\ h + 2\ z^{2} + 3\ z + 4 \\ & \frac{k\left(z+h\right) - k\left(z\right)}{h} = \frac{\left(2\ h^{2} + 4\ z\ h + 3\ h + 2\ z^{2} + 3\ z + 4\right) - \left(2\ \left(z+1\right)^{2} + 3\ \left(z+1\right) + 4\right)}{h} \\ & = \frac{2\ h^{2} + 4\ z\ h + 3\ h}{h} \\ & = \frac{h\left(2\ h + 4\ z + 3\right)}{h} \\ & = 2\ h + 4\ z + 3 \end{split}$$

$$\begin{array}{l} k\left(z\right) = 2\ z^2 + 3\ z + 4 \\ k\left(z + h\right) = 2\ \left(h + z\right)^2 + 3\ \left(h + z\right) + 4 \\ = 2\ h^2 + 4\ h\ z + 7\ h + 2\ z^2 + 7\ z + 9 \\ \frac{k\left(z + h\right) - k\left(z\right)}{h} = \frac{\left(2\ h^2 + 4\ z\ h + 7\ h + 2\ z^2 + 7\ z + 9\right) - \left(2\ z^2 + 3\ z + 4\right)}{h} \\ = \frac{2\ h^2 + 4\ z\ h + 3\ h}{h} \\ = \frac{h\left(2\ h + 4\ z + 3\right)}{h} \\ = 2\ h + 4\ z + 3 \end{array}$$

$$\begin{array}{c} k\left(z\right) = 2\ z^2 + 3\ z + 4 \\ k\left(z + h\right) = 2\ \left(h + z\right)^2 + 3\ \left(h + z\right) + 4 \\ = 2\ h^2 + 4\ h\ z + 3\ h + 2\ z^2 + 3\ z + 4 \\ \frac{k\left(z + h\right) - k\left(z\right)}{h} = \frac{\left(2\ h^2 + 4\ z\ h + 3\ h + 2\ z^2 + 3\ z + 4\right) - \left(2\ z^2 + 3\ z + 4\right)}{h} \\ = \frac{2\ h^2 + 4\ z\ h + 3\ h}{h} \\ = \frac{h\left(2\ h + 4\ z + 3\right)}{h} \\ = 2\ h + 4\ z + 3 \end{array}$$

$$\begin{array}{c} k\left(z\right) = 2\ z^2 + 3\ z + 4 \\ k\left(z + h\right) = 2\ \left(h + z\right)^2 + 3\ \left(h + z\right) + 4 \\ = 2\ h^2 + 4\ h\ z - h + 2\ z^2 - z + 3 \\ \frac{k\left(z + h\right) - k\left(z\right)}{h} = \frac{\left(2\ h^2 + 4\ z\ h + 11\ h + 2\ z^2 + 11\ z + 18\right) - \left(2\ z^2 + 3\ z + 4\right)}{h} \\ = \frac{2\ h^2 + 4\ z\ h + 3\ h}{h} \\ = \frac{h\left(2\ h + 4\ (z + 1) + 3\right)}{h} \\ = 2\ h + 4\ z + 3 \end{array}$$

## Solution