

2.

It so happens that this function can be simplified as:

$$\begin{aligned} s(d) &= \frac{-125+d^3}{-20-d+d^2} \\ &= \frac{(d-5)(d^2+5d+25)}{(d-5)(d+4)} \\ &= \frac{d^2+5d+25}{d+4} \end{aligned}$$

To find the vertical asymptote :

$$d + 4 = 0$$

$$d = -4$$

There is a vertical asymptote at  $d = -4$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-125+d^3}{-20-d+d^2} = \frac{d^2+5d+25}{d+4} = \frac{21}{d+4} + (d+1)$$

There is an oblique asymptote at  $j = d + 1$

