

1.

To find the vertical asymptote :

We must set the denominator equal to 0 and solve:

$$f^4 - 1 = 0$$

$$(f^2 - 1)(f^2 + 1) = 0$$

$$(f^2 - 1) = 0$$

$$(f - 1)(f + 1) = 0$$

$$f = 1 \text{ or } f = -1$$

There is vertical asymptote at  $f=1$  and at  $f=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the denominator contains a 4<sup>th</sup> degree polynomial.

Since the polynomial in the numerator is a lower degree than the denominator, the horizontal asymptote is located at  $r=0$ .

To find the oblique asymptote :

Since the degrees of the numerator are less than the degrees of the denominator, this rational does not have an oblique asymptote

