

2.

It so happens that this function can be simplified as:

$$\begin{aligned}m(j) &= \frac{-8+j^3}{-8+2j+j^2} \\&= \frac{(j-2)(j^2+2j+4)}{(j-2)(j+4)} \\&= \frac{j^2+2j+4}{j+4}\end{aligned}$$

To find the vertical asymptote :

$$j+4=0$$

$$j=-4$$

There is a vertical asymptote at  $j=-4$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator  $\frac{-8+j^3}{-8+2j+j^2} = \frac{j^2+2j+4}{j+4} = \frac{12}{j+4} + (j-2)$

There is an oblique asymptote at  $u=j-2$

