5. Which of the following are correct calculations for difference quotient of: $z(x) = 9 x^{2} + 4 x + 1$ $z(x) = 9 x^{2} + 4 x + 1$ $z(x+h) = 9 (h+x)^{2} + 4 (h+x) + 1$

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\begin{split} &z\left(x\right) = 9 \,\, x^2 \,+\, 4 \,\, x \,+\, 1 \\ &z\left(x + h\right) = 9 \,\, \left(h \,+\, x\right)^{\,2} \,+\, 4 \,\, \left(h \,+\, x\right) \,\,+\, 1 \\ &= 9 \,\, h^2 \,+\, 18 \,\, h \,\, x \,+\, 4 \,\, h \,+\, 9 \,\, x^2 \,+\, 4 \,\, x \,+\, 1 \\ &\frac{z \,(x + h) \,-\, z \,(x)}{h} = \frac{\left(9 \,\, h^2 + 18 \,x \,\, h + 4 \,\, h + 9 \,\, x^2 + 4 \,\, x + 1\right) - \left(9 \,\, \left(x + 1\right)^{\,2} + 4 \,\, \left(x + 1\right) \,+\, 1\right)}{h} \\ &= \frac{9 \,\, h^2 + 18 \,x \,\, h + 4 \,\, h}{h} \\ &= \frac{h \,(9 \,h + 18 \,x + 4)}{h} \\ &= 9 \,\, h \,+\, 18 \,\, x \,+\, 4 \end{split}
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\begin{split} z\left(x\right) &= 9 \; x^2 \; + \; 4 \; x \; + \; 1 \\ z\left(x + h\right) &= 9 \; \left(h \; + \; x\right)^2 \; + \; 4 \; \left(h \; + \; x\right) \; + \; 1 \\ &= 9 \; h^2 \; + \; 18 \; h \; x \; + \; 22 \; h \; + \; 9 \; x^2 \; + \; 22 \; x \; + \; 14 \\ \frac{z\left(x + h\right) \; - z\left(x\right)}{h} &= \frac{\left(9 \; h^2 + 18 \; x \; h + \; 22 \; h + \; 9 \; x^2 + \; 22 \; x \; + \; 14\right) \; - \left(9 \; x^2 + \; 4 \; x \; + \; 1\right)}{h} \\ &= \frac{9 \; h^2 + 18 \; x \; h + \; 4 \; h}{h} \\ &= \frac{h \; (9 \; h + \; 18 \; x \; + \; 4)}{h} \\ &= 9 \; h \; + \; 18 \; x \; + \; 4 \end{split}
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\begin{split} z &(x) = 9 \ x^2 + 4 \ x + 1 \\ z &(x+h) = 9 \ (h+x)^2 + 4 \ (h+x) + 1 \\ &= 9 \ h^2 + 18 \ h \ x - 14 \ h + 9 \ x^2 - 14 \ x + 6 \\ &\frac{z \, (x+h) - z \, (x)}{h} = \frac{\left(9 \ h^2 + 18 \, x \, h + 40 \ h + 9 \ x^2 + 40 \ x + 45\right) - \left(9 \ x^2 + 4 \ x + 1\right)}{h} \\ &= \frac{9 \ h^2 + 18 \, x \, h + 4 \ h}{h} \\ &= \frac{h \, (9 \ h + 18 \ (x+1) + 4)}{h} \\ &= 9 \ h + 18 \ x + 4 \end{split}
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Solution