

Vertex of the Quadratic

Given a quadratic $s(g) = ag^2 + bg + c$ compute its value at

$$g_1 = -\frac{b}{2a} \text{ namely } s(g_1) = c - \frac{b^2}{4a}$$

Now compute the same quadratic at g_1+h , namely

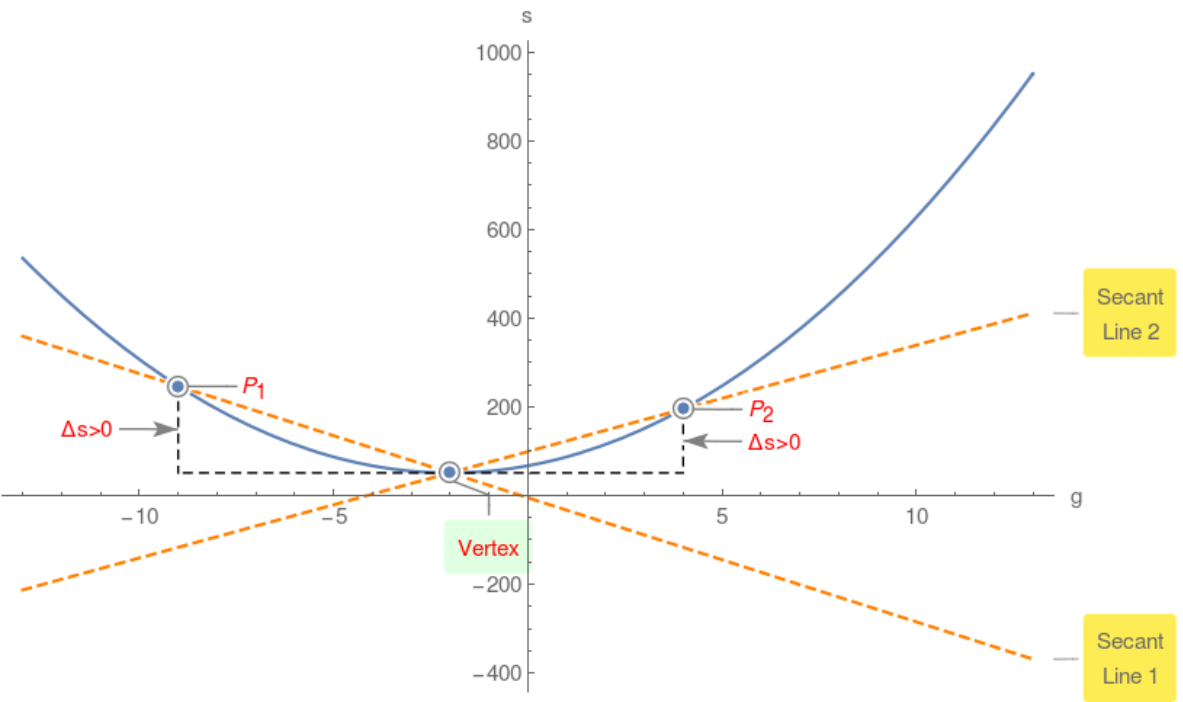
$$s(g_1+h) = -\frac{b^2}{4a} + ah^2 + c$$

$$\text{Compute } \Delta = s(g_1+h) - s(g_1) = ah^2$$

Since $h^2 > 0$, therefore if $a > 0$ then $\Delta > 0$ or vertex is the global minimum!

Example 1.

$$s(g) = 4g^2 + 16g + 67$$



However if $a < 0$ then $\Delta < 0$ or vertex is the global maximum!

Example 2.

$$s(g) = -2g^2 - 4g - 44$$

