

Average Rate of Change & Secant Line

$$\text{Average Rate of Change} = \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(x_1) - f(x_2)}{x_1 - x_2}$$

Average Rate of Change is a single number indicating a rough amount computed for some measurable entity that changes or varies with time.

A **Secant Line**, also simply called a secant, is a line passing through two points of a curve.

Therefore **slope of a secant line** is the same as the Average Rate of Change.

Equation for Secant Line, if **A** indicates Average Rate of Change

while **f(x)** indicates horizontal axis value for secant line

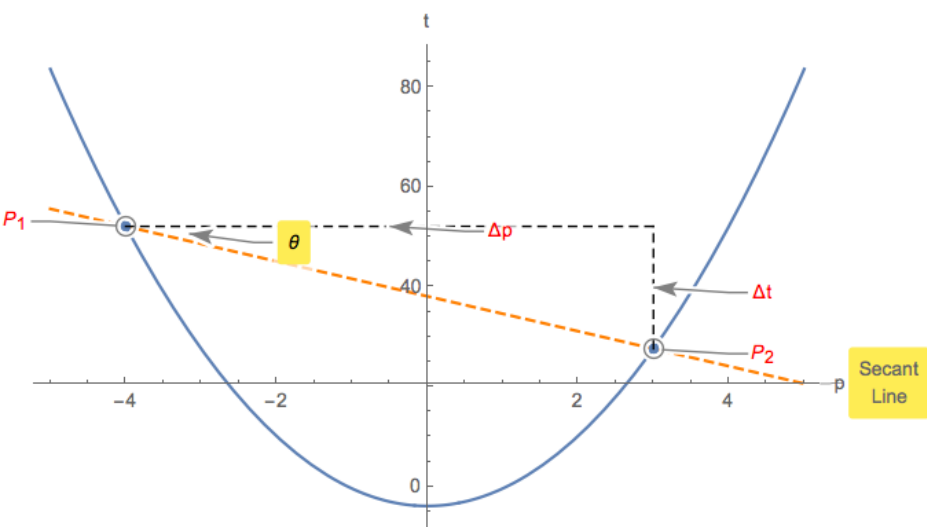
computes as follows:

$$A = \frac{f(x) - f(x_1)}{x - x_1} \Rightarrow A(x - x_1) = f(x) - f(x_1) \Rightarrow A(x - x_1) + f(x_1) = f(x)$$

$$f(x) = Ax + (f(x_1) - Ax_1)$$

Example 1.

$$t = \frac{7p^2}{2} - \frac{39}{10} \text{ average between } -4, 3$$



$$\Delta t = t(3) - t(-4) = \frac{7(3)^2}{2} - \frac{39}{10} - \left(\frac{7(-4)^2}{2} - \frac{39}{10} \right) = -\frac{49}{2}$$

$$\text{Secant Slope} = \tan(\theta) = \frac{t(3) - t(-4)}{3 - (-4)} = -\frac{7}{2}$$

$$\text{Average Rate of Change} = A = -\frac{7}{2}$$

$$\text{Secant Line: } t = -\frac{7}{2}p + \frac{381}{10}$$

t could be temperature of a cup of tea and p time.

t could be speed of a car and p time.

t could be gasoline amount and p distance traveled.