

3.

It so happens that this function can be simplified as:

$$\begin{aligned} a(s) &= \frac{-125+s^3}{-25+s^2} \\ &= \frac{(s-5)(s^2+5s+25)}{(s-5)(s+5)} \\ &= \frac{s^2+5s+25}{s+5} \end{aligned}$$

To find the vertical asymptote :

$$s+5=0$$

$$s=-5$$

There is a vertical asymptote at $s=-5$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-125+s^3}{-25+s^2} = \frac{s^2+5s+25}{s+5} = \frac{25}{s+5} + s$$

There is an oblique asymptote at $g=s$

