

3.

It so happens that this function can be simplified as:

$$\begin{aligned}g(h) &= \frac{-64+h^3}{-16+h^2} \\&= \frac{(h-4)(h^2+4h+16)}{(h-4)(h+4)} \\&= \frac{h^2+4h+16}{h+4}\end{aligned}$$

To find the vertical asymptote :

$$h+4=0$$

$$h=-4$$

There is a vertical asymptote at  $h=-4$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-64+h^3}{-16+h^2} = \frac{h^2+4h+16}{h+4} = \frac{16}{h+4} + h$$

There is an oblique asymptote at  $c=h$

