

2. Given the function $e(a)=a^2+4a$,
find an equation of the secant line containing $(1,e(1))$
and $(5,e(5))$. Express the equation in slope-intercept form.

$$n = -15 + 10a$$

$$n = 15 - 10a$$

$$n = -5 + 10a$$

$$n = -4 + \frac{41a}{4}$$

Solution

The line passing through the two points has the slope:

$$\begin{aligned} & \frac{e(5)-e(1)}{5-1} \\ &= \frac{(1(5)^2+4(5))-(1(1)^2+4(1))}{4} \\ &= \frac{45-5}{4} \\ &= 10 \end{aligned}$$

using one of the points, say $(1,5)$ and the slope to get the equation of the secant line:

$$n-5 = 10(a-1)$$

The equation in slope-intercept form:

$$n = -5 + 10a$$