

1.

It so happens that this function can be simplified as:

$$\begin{aligned}u(c) &= \frac{-27+c^3}{-3-2c+c^2} \\&= \frac{(c-3)(c^2+3c+9)}{(c-3)(c+1)} \\&= \frac{c^2+3c+9}{c+1}\end{aligned}$$

To find the vertical asymptote :

$$c+1=0$$

$$c=-1$$

There is a vertical asymptote at $c=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-27+c^3}{-3-2c+c^2} = \frac{c^2+3c+9}{c+1} = \frac{7}{c+1} + (c+2)$$

There is an oblique asymptote at $r=c+2$

