4. Which of the following are correct calculations for difference quotient of: $d\left(w\right)=2\;w^2\,+\,5\;w\,+\,6$ $d\left(w\right)=2\;w^2\,+\,5\;w\,+\,6$

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\begin{split} d\left(w\right) &= 2\ w^2 + 5\ w + 6 \\ d\left(w + h\right) &= 2\ \left(h + w\right)^2 + 5\ \left(h + w\right) + 6 \\ &= 2\ h^2 + 4\ h\ w + 5\ h + 2\ w^2 + 5\ w + 6 \\ \frac{d\left(w + h\right) - d\left(w\right)}{h} &= \frac{\left(2\ h^2 + 4\ w\ h + 5\ h + 2\ w^2 + 5\ w + 6\right) - \left(2\ \left(w + 1\right)^2 + 5\ \left(w + 1\right) + 6\right)}{h} \\ &= \frac{2\ h^2 + 4\ w\ h + 5\ h}{h} \\ &= \frac{h\left(2\ h + 4\ w + 5\right)}{h} \\ &= 2\ h + 4\ w + 5 \end{split}
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$$\begin{split} d\left(w\right) &= 2\ w^2 + 5\ w + 6 \\ d\left(w + h\right) &= 2\ (h + w)^2 + 5\ (h + w) + 6 \\ &= 2\ h^2 + 4\ h\ w + 9\ h + 2\ w^2 + 9\ w + 13 \\ \frac{d\left(w + h\right) - d\left(w\right)}{h} &= \frac{\left(2\ h^2 + 4\ w\ h + 9\ h + 2\ w^2 + 9\ w + 13\right) - \left(2\ w^2 + 5\ w + 6\right)}{h} \\ &= \frac{2\ h^2 + 4\ w\ h + 5\ h}{h} \\ &= \frac{h\left(2\ h + 4\ w + 5\right)}{h} \\ &= 2\ h + 4\ w + 5 \end{split}$$

$$d(w) = 2 w^{2} + 5 w + 6$$

$$d(w+h) = 2 (h+w)^{2} + 5 (h+w) + 6$$

$$= 2 h^{2} + 4 h w + 5 h + 2 w^{2} + 5 w + 6$$

$$\frac{d(w+h) - d(w)}{h} = \frac{\left(2 h^{2} + 4 w h + 5 h + 2 w^{2} + 5 w + 6\right) - \left(2 w^{2} + 5 w + 6\right)}{h}$$

$$= \frac{2 h^{2} + 4 w h + 5 h}{h}$$

$$= \frac{h(2 h + 4 w + 5)}{h}$$

$$= 2 h + 4 w + 5$$

$$\begin{split} d\left(w\right) &= 2\ w^2 + 5\ w + 6 \\ d\left(w + h\right) &= 2\ (h + w)^2 + 5\ (h + w) + 6 \\ &= 2\ h^2 + 4\ h\ w + h + 2\ w^2 + w + 3 \\ \frac{d\left(w + h\right) - d\left(w\right)}{h} &= \frac{\left(2\ h^2 + 4\ w\ h + 13\ h + 2\ w^2 + 13\ w + 24\right) - \left(2\ w^2 + 5\ w + 6\right)}{h} \\ &= \frac{2\ h^2 + 4\ w\ h + 5\ h}{h} \\ &= \frac{h\left(2\ h + 4\ (w + 1) + 5\right)}{h} \\ &= 2\ h + 4\ w + 5 \end{split}$$

Solution