2. Which of the following are correct calculations for difference quotient of:  $f(s)=2\ s^2+4\ s+2$   $f(s)=2\ s^2+4\ s+2$   $f(s+h)=2\ (h+s)^2+4\ (h+s)+2$   $=2\ h^2+4\ h\ s+4\ h+2\ s^2+4\ s+2$ 

$$f(s) = 2 s^{2} + 4 s + 2$$

$$f(s+h) = 2 (h+s)^{2} + 4 (h+s) + 2$$

$$= 2 h^{2} + 4 h s + 4 h + 2 s^{2} + 4 s + 2$$

$$\frac{f(s+h) - f(s)}{h} = \frac{\left(2 h^{2} + 4 s h + 4 h + 2 s^{2} + 4 s + 2\right) - \left(2 (s+1)^{2} + 4 (s+1) + 2\right)}{h}$$

$$= \frac{2 h^{2} + 4 s h + 4 h}{h}$$

$$= \frac{h(2 h + 4 s + 4)}{h}$$

$$= 2 h + 4 s + 4$$

$$f(s) = 2 s^{2} + 4 s + 2$$

$$\begin{split} f\left(s+h\right) &= 2 \; \left(h+s\right)^{\,2} + 4 \; \left(h+s\right) \; + 2 \\ &= 2 \; h^2 + 4 \; h \; s \; + 8 \; h \; + 2 \; s^2 \; + 8 \; s \; + 8 \\ \frac{f\left(s+h\right) - f\left(s\right)}{h} &= \frac{\left(2 \; h^2 + 4 \; s \; h + 8 \; h + 2 \; s^2 + 8 \; s + 8\right) - \left(2 \; s^2 + 4 \; s + 2\right)}{h} \\ &= \frac{2 \; h^2 + 4 \; s \; h + 4 \; h}{h} \\ &= \frac{h \; (2 \; h + 4 \; s + 4)}{h} \\ &= 2 \; h \; + \; 4 \; s \; + \; 4 \end{split}$$

 $\frac{f\left(s+h\right)-f\left(s\right)}{-}\left(2\;h^{2}+4\;s\;h+4\;h+2\;s^{2}+4\;s+2\right)-\left(2\;s^{2}+4\;s+2\right)$ 

 $=2 h^2 + 4 h s + 4 h + 2 s^2 + 4 s + 2$ 

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 = \frac{2 h^2 + 4 s h + 4 h}{h} 
 = \frac{h (2 h + 4 s + 4)}{h} 
 = 2 h + 4 s + 4 
 f(s) = 2 s^2 + 4 s + 2 
 f(s+h) = 2 (h+s)^2 + 4 (h+s) + 2 
 = 2 h^2 + 4 h s + 2 s^2 
 \frac{f(s+h) - f(s)}{h} = \frac{\left(2 h^2 + 4 s h + 12 h + 2 s^2 + 12 s + 18\right) - \left(2 s^2 + 4 s + 2\right)}{h} 
 = \frac{2 h^2 + 4 s h + 4 h}{h}
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## Solution

 $= \frac{h(2 h+4 (s+1)+4)}{}$ 

=2h+4s+4