

Intercepts of the Quadratic

Given a quadratic $s(y) = ay^2 + by + c$ compute its discriminant Δ :

$$\Delta = \sqrt{b^2 - 4ac}$$

Case1: $\Delta > 0$

$y_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ computes the y-intercepts of multiplicity 1.
 $s(0) = c$ computes the single s-intercept.

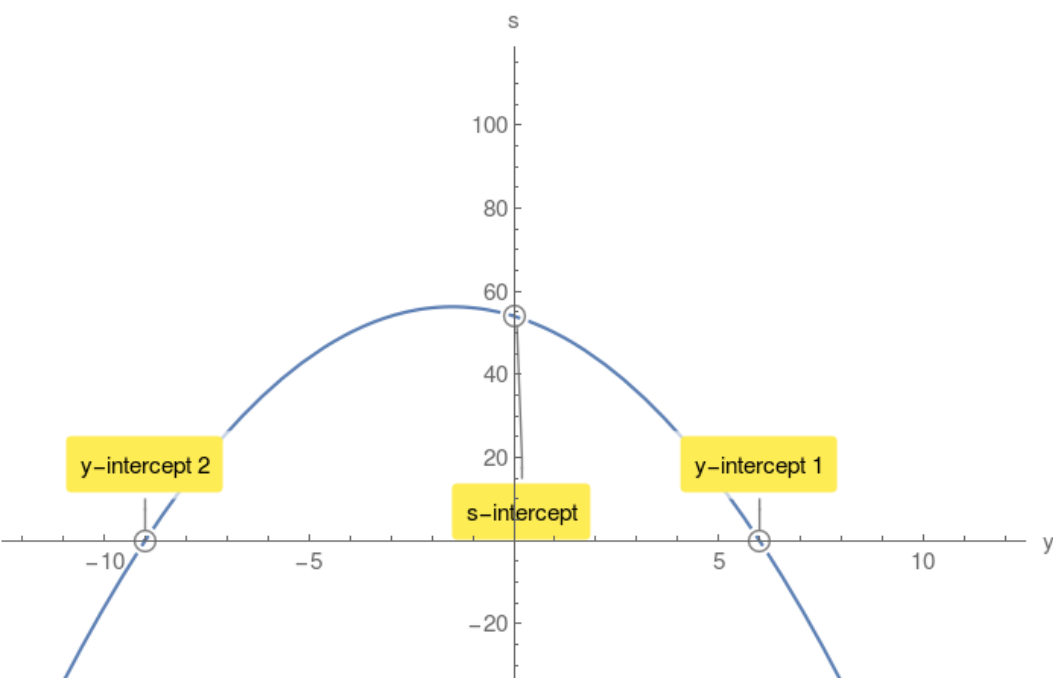
Example 1.

$s(y) = -y^2 - 3y + 54$ compute its discriminant Δ :

$$\Delta = 225 > 0$$

$$y_{1,2} = 6, -9$$

$s(0) = 54$ s-intercept.



Case2: $\Delta = 0$

$y_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-b \pm 0}{2a} = \frac{-b}{2a}$ single y-intercept of multiplicity 2.

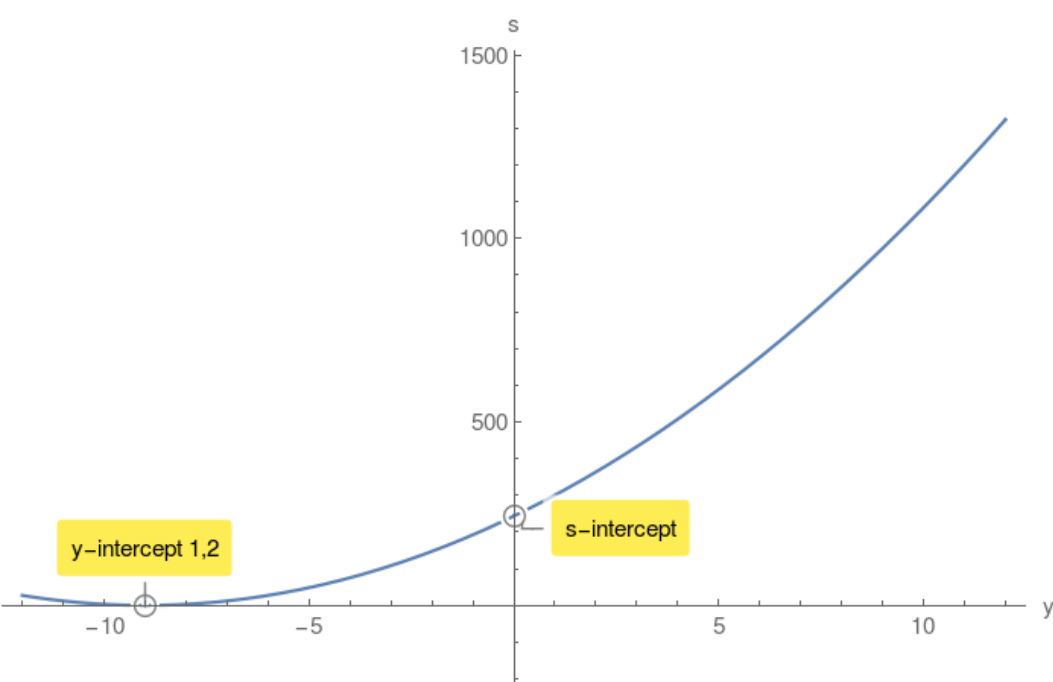
Example 2.

$s(y) = 3y^2 + 54y + 243$ compute its discriminant Δ :

$$\Delta = 0$$

$$y_{1,2} = -9, -9$$

$s(0) = 243$ s-intercept.



Case3: $\Delta < 0$

$\sqrt{b^2 - 4ac}$ has no value in Real Numbers. Therefore there are no y-intercepts.
However there is a s-intercept.

Example 3.

$s(y) = 9y^2 - 144y + 640$ compute its discriminant Δ :

$$\Delta = -2304 < 0$$

$s(0) = 640$ s-intercept.

