

Rational Polynomials: Graphing and Asymptotes

Find the intercepts, if there are any.

Step 1: Set the numerator to 0 to solve for horizontal intercepts.

Step 2: Set the x to 0 to solve for vertical intercept.

Step 3: Set the denominator to 0 to solve for vertical asymptotes.

Step 4: Perform a long division to find the quotient which specifies the oblique asymptote.

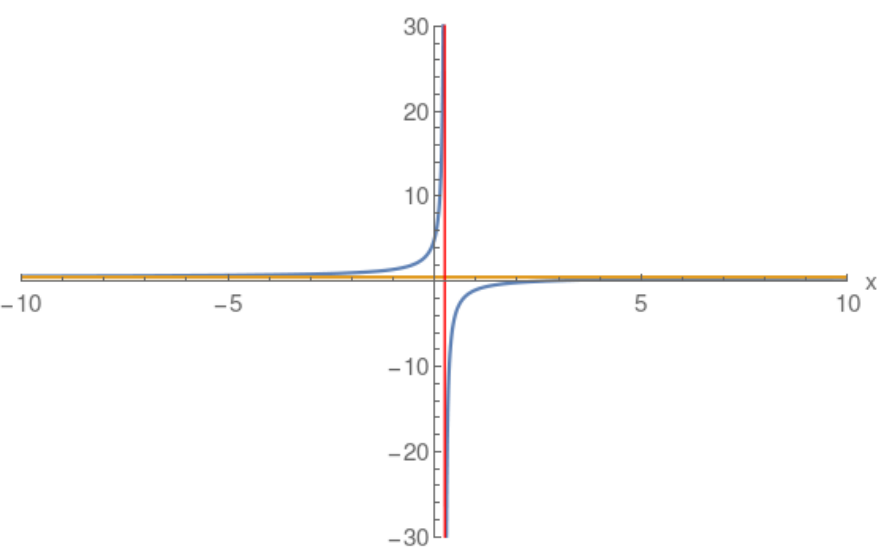
Note: Blue curve the actual Rational function.

Red and Gold asymptotes.

Example: Horizontal Asymptote

$$\frac{2x-5}{4x-1}$$

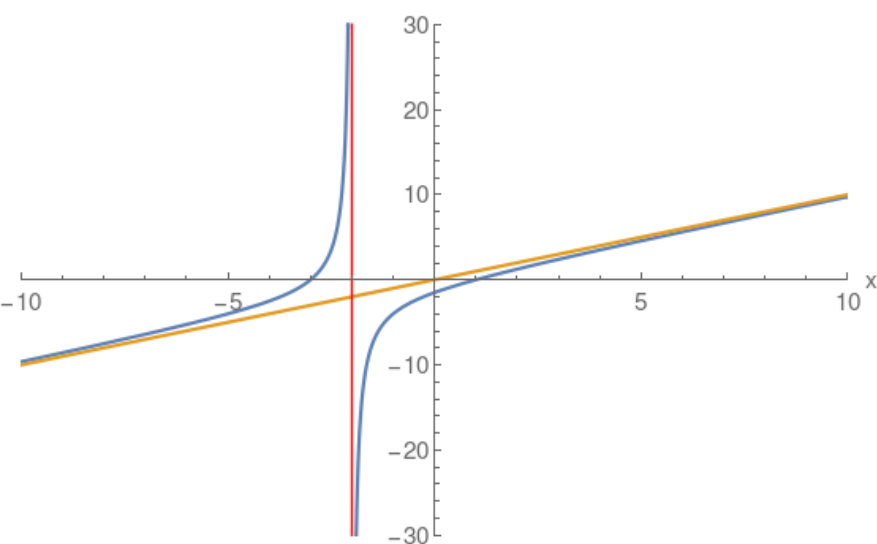
$$\begin{array}{r} + \left(\frac{1}{2} \right) \\ \hline \boxed{4x-1} \quad (2)x \quad + (-5) \\ \quad \left(\frac{2x}{2} \right) + \left(\frac{-1}{2} \right) \\ \quad \quad + \left(\frac{-9}{2} \right) \end{array}$$



Example: Oblique Linear Asymptote

$$\frac{(x-1)(x+3)}{x+2}$$

$$\begin{array}{r} + \left(x \right) \\ \hline \boxed{x+2} \quad (1)x^2 + (2)x + (-3) \\ \quad \left(\frac{x^2}{1} \right) + \left(\frac{2x}{1} \right) \\ \quad \quad + \left(\frac{-3}{1} \right) \end{array}$$



Example: Multiple Vertical Asymptotes

$$\frac{x+2}{(x-1)(x+3)}$$

$$\begin{array}{r} + \left(0 \right) \\ \hline \left(\frac{x}{1} \right) + \left(\frac{2}{1} \right) \end{array}$$

