3. Which of the following are correct calculations for difference quotient of:  $q(u) = 6 u^2 + 5 u + 6$   $q(u) = 6 u^2 + 5 u + 6$   $q(u+h) = 6 (h+u)^2 + 5 (h+u) + 6$ 

```
\begin{split} q\left(u\right) &= 6\ u^2 + 5\ u + 6 \\ q\left(u + h\right) &= 6\ \left(h + u\right)^2 + 5\ \left(h + u\right) + 6 \\ &= 6\ h^2 + 12\ h\ u + 5\ h + 6\ u^2 + 5\ u + 6 \\ \frac{q\left(u + h\right) - q\left(u\right)}{h} &= \frac{\left(6\ h^2 + 12\ u\ h + 5\ h + 6\ u^2 + 5\ u + 6\right) - \left(6\ \left(u + 1\right)^2 + 5\ \left(u + 1\right) + 6\right)}{h} \\ &= \frac{6\ h^2 + 12\ u\ h + 5\ h}{h} \\ &= \frac{h\left(6\ h + 12\ u + 5\right)}{h} \\ &= 6\ h + 12\ u + 5 \end{split}
```

```
\begin{split} q\left(u\right) &= 6\ u^2 + 5\ u + 6 \\ q\left(u + h\right) &= 6\ \left(h + u\right)^2 + 5\ \left(h + u\right) + 6 \\ &= 6\ h^2 + 12\ h\ u + 17\ h + 6\ u^2 + 17\ u + 17 \\ \frac{q\left(u + h\right) - q\left(u\right)}{h} &= \frac{\left(6\ h^2 + 12\ u\ h + 17\ h + 6\ u^2 + 17\ u + 17\right) - \left(6\ u^2 + 5\ u + 6\right)}{h} \\ &= \frac{6\ h^2 + 12\ u\ h + 5\ h}{h} \\ &= \frac{h\left(6\ h + 12\ u + 5\right)}{h} \\ &= 6\ h + 12\ u + 5 \end{split}
```

```
q(u) = 6 u^{2} + 5 u + 6
q(u+h) = 6 (h + u)^{2} + 5 (h + u) + 6
= 6 h^{2} + 12 h u + 5 h + 6 u^{2} + 5 u + 6
\frac{q(u+h) - q(u)}{h} = \frac{\left(6 h^{2} + 12 u h + 5 h + 6 u^{2} + 5 u + 6\right) - \left(6 u^{2} + 5 u + 6\right)}{h}
= \frac{6 h^{2} + 12 u h + 5 h}{h}
= \frac{h(6 h + 12 u + 5)}{h}
= 6 h + 12 u + 5
```

```
\begin{split} q\left(u\right) &= 6\ u^2 + 5\ u + 6 \\ q\left(u + h\right) &= 6\ \left(h + u\right)^2 + 5\ \left(h + u\right) + 6 \\ &= 6\ h^2 + 12\ h\ u - 7\ h + 6\ u^2 - 7\ u + 7 \\ \frac{q\left(u + h\right) - q\left(u\right)}{h} &= \frac{\left(6\ h^2 + 12\ u\ h + 29\ h + 6\ u^2 + 29\ u + 40\right) - \left(6\ u^2 + 5\ u + 6\right)}{h} \\ &= \frac{6\ h^2 + 12\ u\ h + 5\ h}{h} \\ &= \frac{h\left(6\ h + 12\ \left(u + 1\right) + 5\right)}{h} \\ &= 6\ h + 12\ u + 5 \end{split}
```

## Solution