5. Which of the following are correct calculations for difference quotient of:  $t(d)=2\ d^2+5\ d+9$   $t(d)=2\ d^2+5\ d+9$   $t(d+h)=2\ (d+h)^2+5\ (d+h)+9$ 

$$\begin{split} &t\left(d\right)=2\;d^2+5\;d+9\\ &t\left(d+h\right)=2\;\left(d+h\right)^2+5\;\left(d+h\right)+9\\ &=2\;d^2+4\;d\;h+5\;d+2\;h^2+5\;h+9\\ &\frac{t\left(d+h\right)-t\left(d\right)}{h}=\frac{\left(2\;d^2+4\;h\;d+5\;d+2\;h^2+5\;h+9\right)-\left(2\;\left(d+1\right)^2+5\;\left(d+1\right)+9\right)}{h}\\ &=\frac{2\;h^2+4\;d\;h+5\;h}{h}\\ &=\frac{h\;(4\;d+2\;h+5)}{h}\\ &=4\;d+2\;h+5 \end{split}$$

$$\begin{split} &t\left(d\right)=2\;d^2+5\;d+9\\ &t\left(d+h\right)=2\;\left(d+h\right)^2+5\;\left(d+h\right)\,+9\\ &=2\;d^2+4\;d\;h+9\;d+2\;h^2+9\;h+16\\ &\frac{t\left(d+h\right)-t\left(d\right)}{h}=\frac{\left(2\;d^2+4\;h\;d+9\;d+2\;h^2+9\;h+16\right)-\left(2\;d^2+5\;d+9\right)}{h}\\ &=\frac{2\;h^2+4\;d\;h+5\;h}{h}\\ &=\frac{h\left(4\;d+2\;h+5\right)}{h}\\ &=4\;d+2\;h+5 \end{split}$$

$$\begin{array}{l} t \ (d) = 2 \ d^2 + 5 \ d + 9 \\ t \ (d+h) = 2 \ (d+h)^2 + 5 \ (d+h) + 9 \\ = 2 \ d^2 + 4 \ d \ h + 5 \ d + 2 \ h^2 + 5 \ h + 9 \\ \\ \frac{t \ (d+h) - t \ (d)}{h} = \frac{\left(2 \ d^2 + 4 \ h \ d + 5 \ d + 2 \ h^2 + 5 \ h + 9\right) - \left(2 \ d^2 + 5 \ d + 9\right)}{h} \\ = \frac{2 \ h^2 + 4 \ d \ h + 5 \ h}{h} \\ = \frac{h \ (4 \ d + 2 \ h + 5)}{h} \\ = 4 \ d + 2 \ h + 5 \end{array}$$

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\begin{split} t\,(d) &= 2\,\,d^2\,+\,5\,\,d\,+\,9 \\ t\,(d+h) &= 2\,\,(d+h)^{\,2}\,+\,5\,\,(d+h)\,+\,9 \\ &= 2\,\,d^2\,+\,4\,\,d\,\,h\,+\,d\,+\,2\,\,h^2\,+\,h\,+\,6 \\ \frac{t\,(d+h)\,-\,t\,(d)}{h} &= \frac{\left(2\,d^2+4\,h\,d+13\,d+2\,h^2+13\,h+27\right)-\left(2\,d^2+5\,d+9\right)}{h} \\ &= \frac{2\,h^2+4\,d\,h+5\,h}{h} \\ &= \frac{h\,(4\,\,(d+1)\,+2\,h+5)}{h} \\ &= 4\,d\,+\,2\,h\,+\,5 \end{split}
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## Solution