1. Perimeter of rectangle = 2(i+a)=417 where a is the length of the other edge of rectangle. Area of the rectangle is = $i \times a$. Use perimeter equation

Then reformulate the area $I=i\times a=\frac{417\,i}{2}-i^2$ which turns out to be a quadratic Parabola:

and solve for $a = \frac{417-2i}{2}$

Compute the vertex $\frac{417}{4}$ and then plug the vertex into the area which will compute the maximum area.