

3.

It so happens that this function can be simplified as:

$$\begin{aligned} a(e) &= \frac{-125+e^3}{-5-4e+e^2} \\ &= \frac{(e-5)(e^2+5e+25)}{(e-5)(e+1)} \\ &= \frac{e^2+5e+25}{e+1} \end{aligned}$$

To find the vertical asymptote :

$$e+1=0$$

$$e=-1$$

There is a vertical asymptote at  $e=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator  $\frac{-125+e^3}{-5-4e+e^2} = \frac{e^2+5e+25}{e+1} = \frac{21}{e+1} + (e+4)$

There is an oblique asymptote at  $b=e+4$

