

2.

It so happens that this function can be simplified as:

$$\begin{aligned} s(b) &= \frac{-64+b^3}{-20+b+b^2} \\ &= \frac{(b-4)(b^2+4b+16)}{(b-4)(b+5)} \\ &= \frac{b^2+4b+16}{b+5} \end{aligned}$$

To find the vertical asymptote :

$$b+5=0$$

$$b=-5$$

There is a vertical asymptote at $b=-5$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-64+b^3}{-20+b+b^2} = \frac{b^2+4b+16}{b+5} = \frac{21}{b+5} + (b-1)$$

There is an oblique asymptote at $q=b-1$

