2. Which of the following are correct calculations for difference quotient of: $a(v)=8\ v^2+9\ v+4$ $a(v)=8\ v^2+9\ v+4$ $a(v+h)=8\ (h+v)^2+9\ (h+v)+4$

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\begin{array}{l} a \ (v) = 8 \ v^2 + 9 \ v + 4 \\ a \ (v+h) = 8 \ (h+v)^2 + 9 \ (h+v) + 4 \\ = 8 \ h^2 + 16 \ h \ v + 9 \ h + 8 \ v^2 + 9 \ v + 4 \\ \frac{a \ (v+h) - a \ (v)}{h} = \frac{\left(8 \ h^2 + 16 \ v \ h + 9 \ h + 8 \ v^2 + 9 \ v + 4\right) - \left(8 \ (v+1)^2 + 9 \ (v+1) + 4\right)}{h} \\ = \frac{8 \ h^2 + 16 \ v \ h + 9 \ h}{h} \\ = \frac{h \ (8 \ h + 16 \ v + 9)}{h} \\ = 8 \ h + 16 \ v + 9 \end{array}
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$$\begin{array}{l} a\left(v\right) = 8 \,\, v^2 \, + \, 9 \,\, v \, + \, 4 \\ \\ a\left(v + h\right) = 8 \,\, \left(h \, + \, v\right)^{\,2} \, + \, 9 \,\, \left(h \, + \, v\right) \, + \, 4 \\ \\ = 8 \,\, h^2 \, + \, 16 \,\, h \,\, v \, + \, 25 \,\, h \, + \, 8 \,\, v^2 \, + \, 25 \,\, v \, + \, 21 \\ \\ \frac{a\left(v + h\right) - a\left(v\right)}{h} = \frac{\left(8 \,\, h^2 + 16 \,\, v \,\, h + 25 \,\, h + 8 \,\, v^2 + 25 \,\, v + 21\right) - \left(8 \,\, v^2 + 9 \,\, v + 4\right)}{h} \\ \\ = \frac{8 \,\, h^2 + 16 \,\, v \,\, h + 9 \,\, h}{h} \\ \\ = \frac{h\left(8 \,\, h + 16 \,\, v + 9\right)}{h} \\ \\ = 8 \,\, h \, + \,\, 16 \,\, v \, + \,\, 9 \end{array}$$

$$a(v) = 8 v^{2} + 9 v + 4$$

$$a(v+h) = 8 (h + v)^{2} + 9 (h + v) + 4$$

$$= 8 h^{2} + 16 h v + 9 h + 8 v^{2} + 9 v + 4$$

$$\frac{a(v+h) - a(v)}{h} = \frac{\left(8 h^{2} + 16 v h + 9 h + 8 v^{2} + 9 v + 4\right) - \left(8 v^{2} + 9 v + 4\right)}{h}$$

$$= \frac{8 h^{2} + 16 v h + 9 h}{h}$$

$$= \frac{h(8 h + 16 v + 9)}{h}$$

$$= 8 h + 16 v + 9$$

$$a (v) = 8 v^{2} + 9 v + 4$$

$$a (v+h) = 8 (h + v)^{2} + 9 (h + v) + 4$$

$$= 8 h^{2} + 16 h v - 7 h + 8 v^{2} - 7 v + 3$$

$$\frac{a (v+h) - a (v)}{h} = \frac{\left(8 h^{2} + 16 v h + 41 h + 8 v^{2} + 41 v + 54\right) - \left(8 v^{2} + 9 v + 4\right)}{h}$$

$$= \frac{8 h^{2} + 16 v h + 9 h}{h}$$

$$= \frac{h (8 h + 16 (v+1) + 9)}{h}$$

$$= 8 h + 16 v + 9$$

Solution