

3.

It so happens that this function can be simplified as:

$$\begin{aligned} f(s) &= \frac{-64+s^3}{-8-2s+s^2} \\ &= \frac{(s-4)(s^2+4s+16)}{(s-4)(s+2)} \\ &= \frac{s^2+4s+16}{s+2} \end{aligned}$$

To find the vertical asymptote :

$$s+2=0$$

$$s=-2$$

There is a vertical asymptote at $s=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator $\frac{-64+s^3}{-8-2s+s^2} = \frac{s^2+4s+16}{s+2} = \frac{12}{s+2} + (s+2)$

There is an oblique asymptote at $g=s+2$

