4. Which of the following are correct calculations for difference quotient of: $k(p) = 8p^2 + 3p + 7$ $k(p) = 8p^2 + 3p + 7$ $k(p+h) = 8(h+p)^2 + 3(h+p) + 7$ $= 8h^2 + 16hp + 3h + 8p^2 + 3p + 7$ $= 8h^2 + 16hp + 3h + 8p^2 + 3p + 7$ $= 8h^2 + 16hp + 3h + 8p^2 + 3p + 7$

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\begin{split} &\frac{k\,(p+h)-k\,(p)}{h} = \frac{\left(8\,h^2+16\,p\,h+3\,h+8\,p^2+3\,p+7\right)-\left(8\,\left(p+1\right)^{\,2}+3\,\left(p+1\right)+7\right)}{h} \\ &= \frac{8\,h^2+16\,p\,h+3\,h}{h} \\ &= \frac{h\,(8\,h+16\,p+3)}{h} \\ &= 8\,h+16\,p+3 \end{split} &= 8\,h+16\,p+3 \end{split} &= 8\,h+16\,p+3 \end{split} &\qquad \qquad k\,(p)=8\,p^2+3\,p+7 \\ &\qquad \qquad k\,(p+h)=8\,\left(h+p\right)^2+3\,\left(h+p\right)+7 \\ &= 8\,h^2+16\,h\,p+19\,h+8\,p^2+19\,p+18 \\ &\qquad \qquad \frac{k\,(p+h)-k\,(p)}{h} = \frac{\left(8\,h^2+16\,p\,h+19\,h+8\,p^2+19\,p+18\right)-\left(8\,p^2+3\,p+7\right)}{h} \end{split}
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\begin{array}{c} k\left(p\right) = 8\ p^2 + 3\ p + 7 \\ k\left(p+h\right) = 8\ \left(h+p\right)^2 + 3\ \left(h+p\right) + 7 \\ = 8\ h^2 + 16\ h\ p - 13\ h + 8\ p^2 - 13\ p + 12 \\ \frac{k\left(p+h\right) - k\left(p\right)}{h} = \frac{\left(8\ h^2 + 16\ p\ h + 35\ h + 8\ p^2 + 35\ p + 45\right) - \left(8\ p^2 + 3\ p + 7\right)}{h} \\ = \frac{8\ h^2 + 16\ p\ h + 3\ h}{h} \\ = \frac{h\left(8\ h + 16\ \left(p + 1\right) + 3\right)}{h} \\ = 8\ h + 16\ p + 3 \end{array}
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Solution

 $= \frac{8 h^2 + 16 p h + 3 h}{}$

= h (8 h+16 p+3)