6. Which of the following are correct calculations for difference quotient of:  $b(q) = 9 q^{2} + 3 q + 7$   $b(q) = 9 q^{2} + 3 q + 7$   $b(q+h) = 9 (h+q)^{2} + 3 (h+q) + 7$   $= 9 h^{2} + 18 h q + 3 h + 9 q^{2} + 3 q + 7$   $(9 h^{2} + 18 q h + 3 h + 9 q^{2} + 3 q + 7) + (9 (q+1)^{2} + 3 (q+1) + 7)$ 

```
= 9 h^{2} + 18 h q + 3 h + 9 q^{2} + 3 q + 7
\frac{b (q+h) - b (q)}{h} = \frac{\left(9 h^{2} + 18 q h + 3 h + 9 q^{2} + 3 q + 7\right) - \left(9 (q+1)^{2} + 3 (q+1) + 7\right)}{h}
= \frac{9 h^{2} + 18 q h + 3 h}{h}
= \frac{h (9 h + 18 q + 3)}{h}
= 9 h + 18 q + 3
b (q) = 9 q^{2} + 3 q + 7
b (q + h) - 9 (h + q)^{2} + 3 (h + q) + 7
```

$$\begin{array}{l} b \ (q) = 9 \ q^2 + 3 \ q + 7 \\ b \ (q+h) = 9 \ (h+q)^2 + 3 \ (h+q) + 7 \\ = 9 \ h^2 + 18 \ h \ q + 21 \ h + 9 \ q^2 + 21 \ q + 19 \\ \frac{b \ (q+h) - b \ (q)}{h} = \frac{\left(9 \ h^2 + 18 \ q \ h + 21 \ h + 9 \ q^2 + 21 \ q + 19\right) - \left(9 \ q^2 + 3 \ q + 7\right)}{h} \\ = \frac{9 \ h^2 + 18 \ q \ h + 3 \ h}{h} \\ = \frac{h \ (9 \ h + 18 \ q + 3)}{h} \\ = 9 \ h + 18 \ q + 3 \end{array}$$

$$\begin{array}{c} b \ (q) = 9 \ q^2 + 3 \ q + 7 \\ b \ (q+h) = 9 \ (h+q)^2 + 3 \ (h+q) + 7 \\ = 9 \ h^2 + 18 \ h \ q + 3 \ h + 9 \ q^2 + 3 \ q + 7 \\ \frac{b \ (q+h) - b \ (q)}{h} = \frac{\left(9 \ h^2 + 18 \ q \ h + 3 \ h + 9 \ q^2 + 3 \ q + 7\right) - \left(9 \ q^2 + 3 \ q + 7\right)}{h} \\ = \frac{9 \ h^2 + 18 \ q \ h + 3 \ h}{h} \\ = \frac{h \ (9 \ h + 18 \ q + 3)}{h} \\ = 9 \ h + 18 \ q + 3 \end{array}$$

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\begin{array}{c} b \ (q) = 9 \ q^2 + 3 \ q + 7 \\ b \ (q+h) = 9 \ (h+q)^2 + 3 \ (h+q) + 7 \\ = 9 \ h^2 + 18 \ h \ q - 15 \ h + 9 \ q^2 - 15 \ q + 13 \\ \frac{b \ (q+h) - b \ (q)}{h} = \frac{\left(9 \ h^2 + 18 \ q \ h + 39 \ h + 9 \ q^2 + 39 \ q + 49\right) - \left(9 \ q^2 + 3 \ q + 7\right)}{h} \\ = \frac{9 \ h^2 + 18 \ q \ h + 3 \ h}{h} \\ = \frac{h \ (9 \ h + 18 \ (q+1) + 3)}{h} \\ = 9 \ h + 18 \ q + 3 \end{array}
```

## Solution