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1. Which of the following are correct calculations for difference quotient of: j(v) = 4 v^2 + 8 v + 7
j(v) = 4 v^2 + 8 v + 7
j(v+h) = 4 (h+v)^2 + 8 (h+v) + 7
4 h^2 + 8 h + 4 v^2 + 8 v + 7
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\begin{split} &j \ (v) = 4 \ v^2 + 8 \ v + 7 \\ &j \ (v+h) = 4 \ (h+v)^2 + 8 \ (h+v) + 7 \\ &= 4 \ h^2 + 8 \ h \ v + 8 \ h + 4 \ v^2 + 8 \ v + 7 \\ &\frac{j \ (v+h) - j \ (v)}{h} = \frac{\left(4 \ h^2 + 8 \ v \ h + 8 \ h + 4 \ v^2 + 8 \ v + 7\right) - \left(4 \ (v+1)^2 + 8 \ (v+1) + 7\right)}{h} \\ &= \frac{4 \ h^2 + 8 \ v \ h + 8 \ h}{h} \\ &= \frac{h \ (4 \ h + 8 \ v + 8)}{h} \\ &= 4 \ h + 8 \ v + 8 \end{split}
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$$\begin{split} j &(v) = 4 \ v^2 + 8 \ v + 7 \\ j &(v+h) = 4 \ (h+v)^2 + 8 \ (h+v) + 7 \\ = 4 \ h^2 + 8 \ h \ v + 16 \ h + 4 \ v^2 + 16 \ v + 19 \\ \frac{j &(v+h) - j &(v)}{h} &= \frac{\left(4 \ h^2 + 8 \ v \ h + 16 \ h + 4 \ v^2 + 16 \ v + 19\right) - \left(4 \ v^2 + 8 \ v + 7\right)}{h} \\ &= \frac{4 \ h^2 + 8 \ v \ h + 8 \ h}{h} \\ &= \frac{h &(4 \ h + 8 \ v + 8)}{h} \\ &= 4 \ h + 8 \ v + 8 \end{split}$$

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\begin{split} j &(v) = 4 \ v^2 + 8 \ v + 7 \\ j &(v+h) = 4 \ (h+v)^2 + 8 \ (h+v) + 7 \\ = 4 \ h^2 + 8 \ h \ v + 8 \ h + 4 \ v^2 + 8 \ v + 7 \\ \frac{j \ (v+h) - j \ (v)}{h} &= \frac{\left(4 \ h^2 + 8 \ v \ h + 8 \ h + 4 \ v^2 + 8 \ v + 7\right) - \left(4 \ v^2 + 8 \ v + 7\right)}{h} \\ &= \frac{4 \ h^2 + 8 \ v \ h + 8 \ h}{h} \\ &= \frac{h \ (4 \ h + 8 \ v + 8)}{h} \\ &= 4 \ h + 8 \ v + 8 \end{split}
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\begin{split} j &(v) = 4 \ v^2 + 8 \ v + 7 \\ j &(v+h) = 4 \ (h+v)^2 + 8 \ (h+v) + 7 \\ = 4 \ h^2 + 8 \ h \ v + 4 \ v^2 + 3 \\ \frac{j &(v+h) - j &(v)}{h} &= \frac{\left(4 \ h^2 + 8 \ v \ h + 24 \ h + 4 \ v^2 + 24 \ v + 39\right) - \left(4 \ v^2 + 8 \ v + 7\right)}{h} \\ &= \frac{4 \ h^2 + 8 \ v \ h + 8 \ h}{h} \\ &= \frac{h &(4 \ h + 8 \ (v+1) + 8)}{h} \\ &= 4 \ h + 8 \ v + 8 \end{split}
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## Solution