2. Since the fences enclose a rectangular plot without one side, two sides have length b and one side has length a: $a+b+b=2511 \implies a=2511-2b$

 $area=a \times b = (l-2b)b= 2511b-2b^2$

the area:

Note that the equation is for parabola. Now find the vertex:

vertex= $(\frac{2511}{4} \text{ ft }, \frac{6305121}{9} \text{ ft}^2)$

Square the unit for vertex's vertical coordinate since it is a quadratic.