4. Which of the following are correct calculations for difference quotient of: $s(b) = 3b^2 + 3b + 6$ $s(b) = 3b^2 + 3b + 6$

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\begin{split} s\;(b) &= 3\;b^2 + 3\;b + 6 \\ s\;(b+h) &= 3\;(b+h)^2 + 3\;(b+h) + 6 \\ &= 3\;b^2 + 6\;b\;h + 3\;b + 3\;h^2 + 3\;h + 6 \\ \frac{s\;(b+h) - s\;(b)}{h} &= \frac{\left(3\;b^2 + 6\;h\;b + 3\;b + 3\;h^2 + 3\;h + 6\right) - \left(3\;(b+1)^2 + 3\;(b+1) + 6\right)}{h} \\ &= \frac{3\;h^2 + 6\;b\;h + 3\;h}{h} \\ &= \frac{h\;(6\;b + 3\;h + 3)}{h} \\ &= 6\;b + 3\;h + 3 \end{split}
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$$\begin{split} s &(b) = 3 \ b^2 + 3 \ b + 6 \\ s &(b+h) = 3 \ (b+h)^2 + 3 \ (b+h) + 6 \\ = 3 \ b^2 + 6 \ b \ h + 9 \ b + 3 \ h^2 + 9 \ h + 12 \\ \frac{s \, (b+h) - s \, (b)}{h} &= \frac{\left(3 \, b^2 + 6 \ h \ b + 9 \ b + 3 \ h^2 + 9 \ h + 12\right) - \left(3 \, b^2 + 3 \ b + 6\right)}{h} \\ &= \frac{3 \, h^2 + 6 \, b \, h + 3 \, h}{h} \\ &= \frac{h \, (6 \, b + 3 \, h + 3)}{h} \\ &= 6 \, b + 3 \, h + 3 \end{split}$$

$$s(b) = 3b^{2} + 3b + 6$$

$$s(b+h) = 3(b+h)^{2} + 3(b+h) + 6$$

$$= 3b^{2} + 6bh + 3b + 3h^{2} + 3h + 6$$

$$\frac{s(b+h) - s(b)}{h} = \frac{\left(3b^{2} + 6hb + 3b + 3h^{2} + 3h + 6\right) - \left(3b^{2} + 3b + 6\right)}{h}$$

$$= \frac{3h^{2} + 6bh + 3h}{h}$$

$$= \frac{h(6b + 3h + 3)}{h}$$

$$= 6b + 3h + 3$$

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\begin{split} s &(b) = 3 \ b^2 + 3 \ b + 6 \\ s &(b+h) = 3 \ (b+h)^2 + 3 \ (b+h) + 6 \\ = 3 \ b^2 + 6 \ b \ h - 3 \ b + 3 \ h^2 - 3 \ h + 6 \\ \frac{s \ (b+h) - s \ (b)}{h} &= \frac{\left(3 \ b^2 + 6 \ h \ b + 15 \ b + 3 \ h^2 + 15 \ h + 24\right) - \left(3 \ b^2 + 3 \ b + 6\right)}{h} \\ &= \frac{3 \ h^2 + 6 \ b \ h + 3 \ h}{h} \\ &= \frac{h \ (6 \ (b+1) + 3 \ h + 3)}{h} \\ = 6 \ b + 3 \ h + 3 \end{split}
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Solution