

1.

It so happens that this function can be simplified as:

$$\begin{aligned}b(c) &= \frac{-1+c^3}{-2+c+c^2} \\&= \frac{(c-1)(c^2+c+1)}{(c-1)(c+2)} \\&= \frac{c^2+c+1}{c+2}\end{aligned}$$

To find the vertical asymptote :

$$c+2=0$$

$$c=-2$$

There is a vertical asymptote at  $c=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-1+c^3}{-2+c+c^2} = \frac{c^2+c+1}{c+2} = \frac{3}{c+2} + (c-1)$$

There is an oblique asymptote at  $p=c-1$

