

4.

### Solution

Quadratic function: is a function that can be written in the form:

$u(y) = ay^2 + by + c$  where  $a$ ,  $b$ , and  $c$  are real numbers and  $a \neq 0$

we have  $u(y) = y^2 - 2y + 19$ , note:  $y^2 - 2y + 19$  is in  $yu$ -plane

Here, we know that  $a=1$ ,  $b=-2$ ,  $c=19$

Since  $a > 0$ , we know that the  $u$ -coordinate of the vertex is a minimum. However, to find the  $u$ -coordinate of our vertex we first need to find the  $y$ -coordinate of the vertex by using  $y = -\frac{b}{2a} = -\frac{-2}{2} = 1$  Now that we have the  $y$ -coordinate, we can find the  $u$ -coordinate

of the vertex by finding  $u(1) = 1(1)^2 - 2(1) + 19 = 1 - 2 + 19 = 18$  Minimum = 18