

Intercepts of the Quadratic

Given a quadratic $f(t) = at^2 + bt + c$ compute its discriminant Δ :

$$\Delta = \sqrt{b^2 - 4ac}$$

Case1: $\Delta > 0$

$t_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ computes the t-intercepts of multiplicity 1.
 $f(0) = c$ computes the single f-intercept.

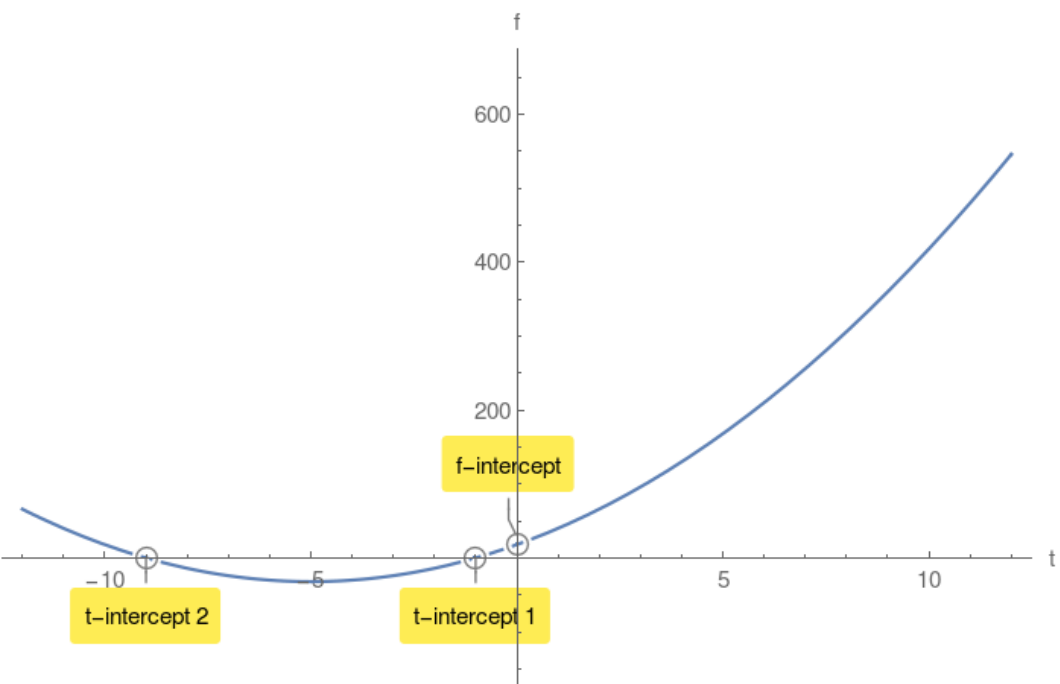
Example 1.

$f(t) = 2t^2 + 20t + 18$ compute its discriminant Δ :

$$\Delta = 256 > 0$$

$$t_{1,2} = -1, -9$$

$f(0) = 18$ f-intercept.



Case2: $\Delta = 0$

$t_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-b \pm 0}{2a} = \frac{-b}{2a}$ single t-intercept of multiplicity 2.

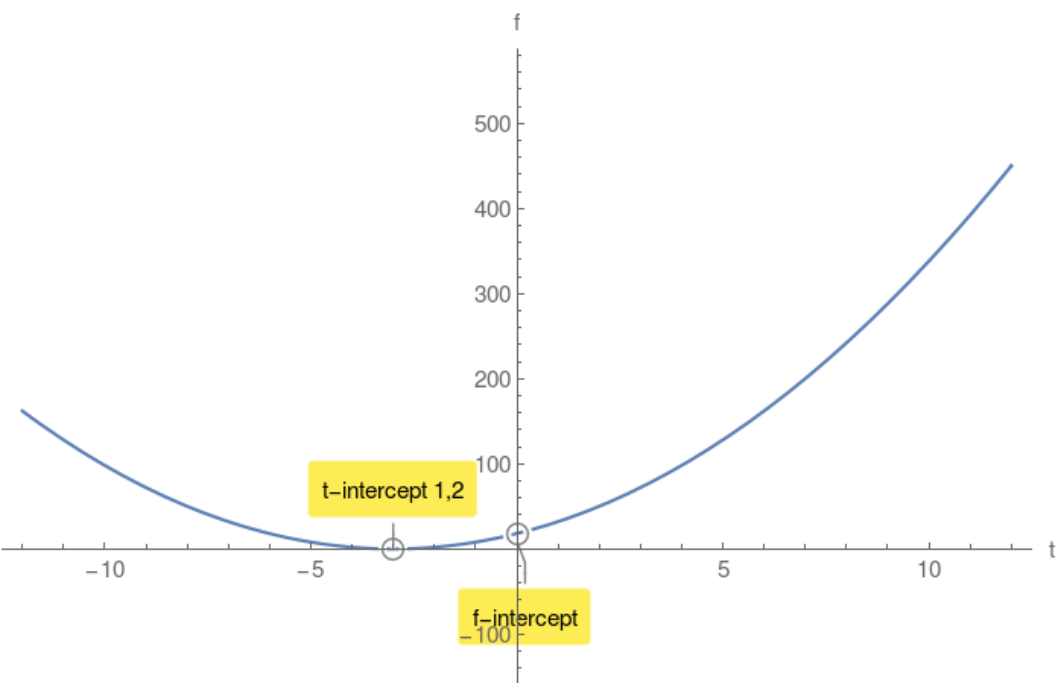
Example 2.

$f(t) = 2t^2 + 12t + 18$ compute its discriminant Δ :

$$\Delta = 0$$

$$t_{1,2} = -3, -3$$

$f(0) = 18$ f-intercept.



Case3: $\Delta < 0$

$\sqrt{b^2 - 4ac}$ has no value in Real Numbers. Therefore there are no t-intercepts.
However there is a f-intercept.

Example 3.

$f(t) = -4t^2 - 72t - 405$ compute its discriminant Δ :

$$\Delta = -1296 < 0$$

$f(0) = -405$ f-intercept.

