3. Which of the following are correct calculations for difference quotient of: $r(x) = 9 x^2 + 5 x + 8$ $r(x) = 9 x^2 + 5 x + 8$ $r(x+h) = 9 (h+x)^2 + 5 (h+x) + 8$

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\begin{split} & r\left(x\right) = 9 \,\, x^2 \, + \, 5 \,\, x \, + \, 8 \\ & r\left(x + h\right) = 9 \,\, \left(h \, + \, x\right)^{\,2} \, + \, 5 \,\, \left(h \, + \, x\right) \,\, + \, 8 \\ & = 9 \,\, h^2 \, + \, 18 \,\, h \,\, x \, + \, 5 \,\, h \, + \, 9 \,\, x^2 \, + \, 5 \,\, x \, + \, 8 \\ & \frac{r\left(x + h\right) - r\left(x\right)}{h} = \frac{\left(9 \,\, h^2 + 18 \, x \, h + 5 \,\, h + 9 \,\, x^2 + 5 \,\, x + 8\right) - \left(9 \,\, \left(x + 1\right)^{\,2} + 5 \,\, \left(x + 1\right) + 8\right)}{h} \\ & = \frac{9 \,\, h^2 + 18 \, x \,\, h + 5 \,\, h}{h} \\ & = \frac{h \,\, (9 \,\, h + 18 \,\, x + 5)}{h} \\ & = 9 \,\, h \,\, + \,\, 18 \,\, x \,\, + \,\, 5 \end{split}
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r(x) = 9 x^{2} + 5 x + 8
r(x+h) = 9 (h + x)^{2} + 5 (h + x) + 8
= 9 h^{2} + 18 h x + 23 h + 9 x^{2} + 23 x + 22
\frac{r(x+h) - r(x)}{h} = \frac{\left(9 h^{2} + 18 x h + 23 h + 9 x^{2} + 23 x + 22\right) - \left(9 x^{2} + 5 x + 8\right)}{h}
= \frac{9 h^{2} + 18 x h + 5 h}{h}
= \frac{h (9 h + 18 x + 5)}{h}
= 9 h + 18 x + 5
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\begin{split} r\left(x\right) &= 9 \; x^2 + 5 \; x + 8 \\ r\left(x + h\right) &= 9 \; \left(h + x\right)^2 + 5 \; \left(h + x\right) \; + 8 \\ &= 9 \; h^2 + 18 \; h \; x + 5 \; h + 9 \; x^2 + 5 \; x + 8 \\ \frac{r\left(x + h\right) - r\left(x\right)}{h} &= \frac{\left(9 \; h^2 + 18 \; x \; h + 5 \; h + 9 \; x^2 + 5 \; x + 8\right) - \left(9 \; x^2 + 5 \; x + 8\right)}{h} \\ &= \frac{9 \; h^2 + 18 \; x \; h + 5 \; h}{h} \\ &= \frac{h \; (9 \; h + 18 \; x + 5)}{h} \\ &= 9 \; h \; + \; 18 \; x \; + \; 5 \end{split}
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\begin{split} &r\left(x\right)=9\;x^{2}+5\;x+8\\ &r\left(x+h\right)=9\;\left(h+x\right)^{2}+5\;\left(h+x\right)+8\\ &=9\;h^{2}+18\;h\;x-13\;h+9\;x^{2}-13\;x+12\\ &\frac{r\left(x+h\right)-r\left(x\right)}{h}=\frac{\left(9\;h^{2}+18\;x\;h+41\;h+9\;x^{2}+41\;x+54\right)-\left(9\;x^{2}+5\;x+8\right)}{h}\\ &=\frac{9\;h^{2}+18\;x\;h+5\;h}{h}\\ &=\frac{h\left(9\;h+18\;\left(x+1\right)+5\right)}{h}\\ &=9\;h+18\;x+5 \end{split}
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Solution