3. Which of the following are correct calculations for difference quotient of:  $f(v) = 5\ v^2 + 6\ v + 1$   $f(v) = 5\ v^2 + 6\ v + 1$   $f(v+h) = 5\ (h+v)^2 + 6\ (h+v) + 1$ 

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\begin{split} &f\left(v\right)=5\ v^2+6\ v+1\\ &f\left(v\!+\!h\right)=5\ \left(h+v\right)^2+6\ \left(h+v\right)\ +1\\ &=5\ h^2+10\ h\ v+6\ h+5\ v^2+6\ v+1\\ &\frac{f\left(v\!+\!h\right)-f\left(v\right)}{h}=\frac{\left(5\ h^2\!+\!10\ v\ h\!+\!6\ h\!+\!5\ v^2\!+\!6\ v\!+\!1\right)\!-\!\left(5\ \left(v\!+\!1\right)^2\!+\!6\ \left(v\!+\!1\right)\!+\!1\right)}{h}\\ &=\frac{5\ h^2\!+\!10\ v\ h\!+\!6\ h}{h}\\ &=\frac{h\left(5\ h\!+\!10\ v\!+\!6\right)}{h}\\ &=5\ h+10\ v+6 \end{split}
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$$\begin{split} f\left(v\right) &= 5 \ v^2 + 6 \ v + 1 \\ f\left(v + h\right) &= 5 \ \left(h + v\right)^2 + 6 \ \left(h + v\right) \ + 1 \\ &= 5 \ h^2 + 10 \ h \ v + 16 \ h + 5 \ v^2 + 16 \ v + 12 \\ &\frac{f\left(v + h\right) - f\left(v\right)}{h} = \frac{\left(5 \ h^2 + 10 \ v \ h + 16 \ h + 5 \ v^2 + 16 \ v + 12\right) - \left(5 \ v^2 + 6 \ v + 1\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ v \ h + 6 \ h}{h} \\ &= \frac{h \ (5 \ h + 10 \ v + 6)}{h} \\ &= 5 \ h + 10 \ v + 6 \end{split}$$

$$\begin{split} f(v) &= 5 \ v^2 + 6 \ v + 1 \\ f(v+h) &= 5 \ (h+v)^2 + 6 \ (h+v) + 1 \\ &= 5 \ h^2 + 10 \ h \ v + 6 \ h + 5 \ v^2 + 6 \ v + 1 \\ \frac{f(v+h) - f(v)}{h} &= \frac{\left(5 \ h^2 + 10 \ v \ h + 6 \ h + 5 \ v^2 + 6 \ v + 1\right) - \left(5 \ v^2 + 6 \ v + 1\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ v \ h + 6 \ h}{h} \\ &= \frac{h \ (5 \ h + 10 \ v + 6)}{h} \\ &= 5 \ h + 10 \ v + 6 \end{split}$$

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\begin{split} f\left(v\right) &= 5 \ v^2 + 6 \ v + 1 \\ f\left(v + h\right) &= 5 \ \left(h + v\right)^2 + 6 \ \left(h + v\right) \ + 1 \\ &= 5 \ h^2 + 10 \ h \ v - 4 \ h + 5 \ v^2 - 4 \ v \\ &\frac{f\left(v + h\right) - f\left(v\right)}{h} = \frac{\left(5 \ h^2 + 10 \ v \ h + 26 \ h + 5 \ v^2 + 26 \ v + 33\right) - \left(5 \ v^2 + 6 \ v + 1\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ v \ h + 6 \ h}{h} \\ &= \frac{h \left(5 \ h + 10 \ \left(v + 1\right) + 6\right)}{h} \\ &= 5 \ h + 10 \ v + 6 \end{split}
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## Solution