

3.

### Solution

Quadratic function: is a function that can be written in the form:

$x(j) = aj^2 + bj + c$  where  $a$ ,  $b$ , and  $c$  are real numbers and  $a \neq 0$

we have  $x(j) = j^2 - 5j - 7$ , note:  $j^2 - 5j - 7$  is in  $j$ -plane

Here, we know that  $a=1$ ,  $b=-5$ ,  $c=-7$

Since  $a > 0$ , we know that the  $x$ -coordinate of the vertex is a minimum. However, to find the  $x$ -coordinate of our vertex we first need to find the  $j$ -coordinate of the vertex by using  $j = -\frac{b}{2a} = -\frac{-5}{2} = \frac{5}{2}$  Now that we have the  $j$ -coordinate, we can find the  $x$ -coordinate

of the vertex by finding  $x(\frac{5}{2}) = 1(\frac{5}{2})^2 - 5(\frac{5}{2}) - 7 = \frac{25}{4} - \frac{25}{2} - 7 = -\frac{33}{4}$  Minimum  $= -\frac{33}{4}$