

2.

It so happens that this function can be simplified as:

$$\begin{aligned}g(q) &= \frac{-64+q^3}{-16+q^2} \\&= \frac{(q-4)(q^2+4q+16)}{(q-4)(q+4)} \\&= \frac{q^2+4q+16}{q+4}\end{aligned}$$

To find the vertical asymptote :

$$q+4=0$$

$$q=-4$$

There is a vertical asymptote at  $q=-4$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator  $\frac{-64+q^3}{-16+q^2} = \frac{q^2+4q+16}{q+4} = \frac{16}{q+4} + q$

There is an oblique asymptote at  $b=q$

