1. Which of the following are correct calculations for difference quotient of:  $g(r)=4\ r^2+4\ r+3$   $g(r)=4\ r^2+4\ r+3$   $g(r+h)=4\ (h+r)^2+4\ (h+r)+3$ 

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g(r) = 4 r^{2} + 4 r + 3
g(r+h) = 4 (h+r)^{2} + 4 (h+r) + 3
= 4 h^{2} + 8 h r + 4 h + 4 r^{2} + 4 r + 3
\frac{g(r+h) - g(r)}{h} = \frac{\left(4 h^{2} + 8 r h + 4 h + 4 r^{2} + 4 r + 3\right) - \left(4 (r+1)^{2} + 4 (r+1) + 3\right)}{h}
= \frac{4 h^{2} + 8 r h + 4 h}{h}
= \frac{h(4 h + 8 r + 4)}{h}
= 4 h + 8 r + 4
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\begin{split} g\left(\,r\,\right) &= 4\,\,r^2\,+\,4\,\,r\,+\,3 \\ g\left(\,r\,+\,h\,\right) &= 4\,\,\left(\,h\,+\,r\,\right)^{\,2}\,+\,4\,\,\left(\,h\,+\,r\,\right)^{\,}\,+\,3 \\ &= 4\,\,h^2\,+\,8\,\,h\,\,r\,+\,12\,\,h\,+\,4\,\,r^2\,+\,12\,\,r\,+\,11 \\ \frac{g\left(\,r\,+\,h\,\right)\,-\,g\left(\,r\,\right)}{h} &= \frac{\left(\,4\,\,h^2\,+\,8\,\,r\,\,h\,+\,12\,\,h\,+\,4\,\,r^2\,+\,12\,\,r\,+\,11\,\right)\,-\,\left(\,4\,\,r^2\,+\,4\,\,r\,+\,3\,\right)}{h} \\ &= \frac{4\,\,h^2\,+\,8\,\,r\,\,h\,+\,4\,\,h}{h} \\ &= \frac{h\,(\,4\,\,h\,+\,8\,\,r\,+\,4\,\right)}{h} \\ &= 4\,\,h\,+\,8\,\,r\,+\,4 \end{split}
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g(r) = 4 r^{2} + 4 r + 3
g(r+h) = 4 (h+r)^{2} + 4 (h+r) + 3
= 4 h^{2} + 8 h r + 4 h + 4 r^{2} + 4 r + 3
\frac{g(r+h) - g(r)}{h} = \frac{\left(4 h^{2} + 8 r h + 4 h + 4 r^{2} + 4 r + 3\right) - \left(4 r^{2} + 4 r + 3\right)}{h}
= \frac{4 h^{2} + 8 r h + 4 h}{h}
= \frac{h(4 h + 8 r + 4)}{h}
= 4 h + 8 r + 4
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\begin{split} g &(r) = 4 \ r^2 + 4 \ r + 3 \\ g &(r+h) = 4 \ (h+r)^2 + 4 \ (h+r) + 3 \\ = 4 \ h^2 + 8 \ h \ r - 4 \ h + 4 \ r^2 - 4 \ r + 3 \\ \frac{g &(r+h) - g &(r)}{h} &= \frac{\left(4 \ h^2 + 8 \ r \ h + 20 \ h + 4 \ r^2 + 20 \ r + 27\right) - \left(4 \ r^2 + 4 \ r + 3\right)}{h} \\ &= \frac{4 \ h^2 + 8 \ r \ h + 4 \ h}{h} \\ &= \frac{h &(4 \ h + 8 \ (r+1) + 4)}{h} \\ &= 4 \ h + 8 \ r + 4 \end{split}
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## Solution