

# Average Rate of Change & Secant Line

$$\text{Average Rate of Change} = \frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(x_1) - f(x_2)}{x_1 - x_2}$$

Average Rate of Change is a single number indicating a rough amount computed for some measurable entity that changes or varies with time.

A **Secant Line**, also simply called a secant, is a line passing through two points of a curve.

Therefore **slope of a secant line** is the same as the Average Rate of Change.

Equation for Secant Line, if **A** indicates Average Rate of Change

while **f(x)** indicates horizontal axis value for secant line

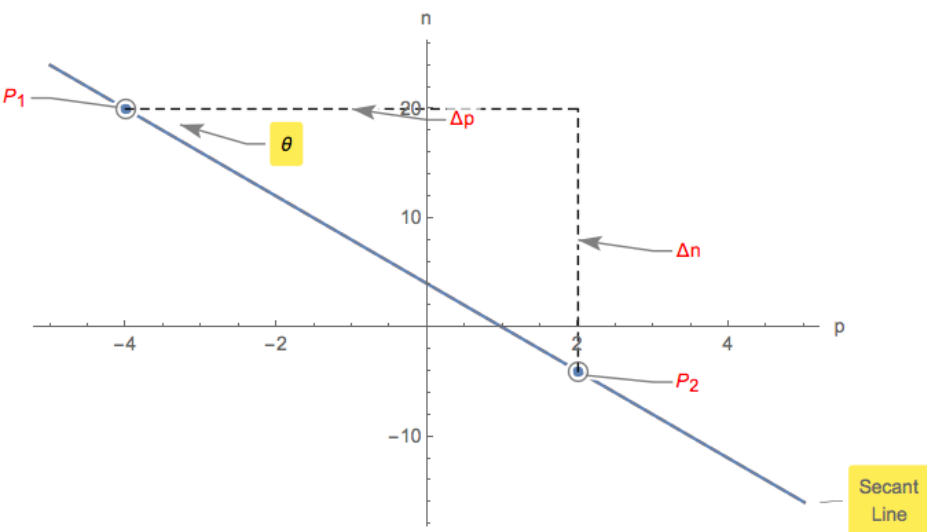
computes as follows:

$$A = \frac{f(x) - f(x_1)}{x - x_1} \Rightarrow A(x - x_1) = f(x) - f(x_1) \Rightarrow A(x - x_1) + f(x_1) = f(x)$$

$$f(x) = Ax + (f(x_1) - Ax_1)$$

## Example 1.

$n = 4 - 4p$  average between  $-4, 2$



$$\Delta n = n(2) - n(-4) = 4 - 4(2) - (4 - 4(-4)) = -24$$

$$\text{Secant Slope} = \tan(\theta) = \frac{n(2) - n(-4)}{2 - (-4)} = -4$$

$$\text{Average Rate of Change} = A = -4$$

$$\text{Secant Line: } n = -4p + 4$$

$n$  could be temperature of a cup of tea and  $p$  time.

$n$  could be speed of a car and  $p$  time.

$n$  could be gasoline amount and  $p$  distance traveled.