

# Vertex of the Quadratic

Given a quadratic  $m(u) = au^2 + bu + c$  compute its value at

$$u_1 = -\frac{b}{2a} \text{ namely } m(u_1) = c - \frac{b^2}{4a}$$

Now compute the same quadratic at  $u_1+h$ , namely

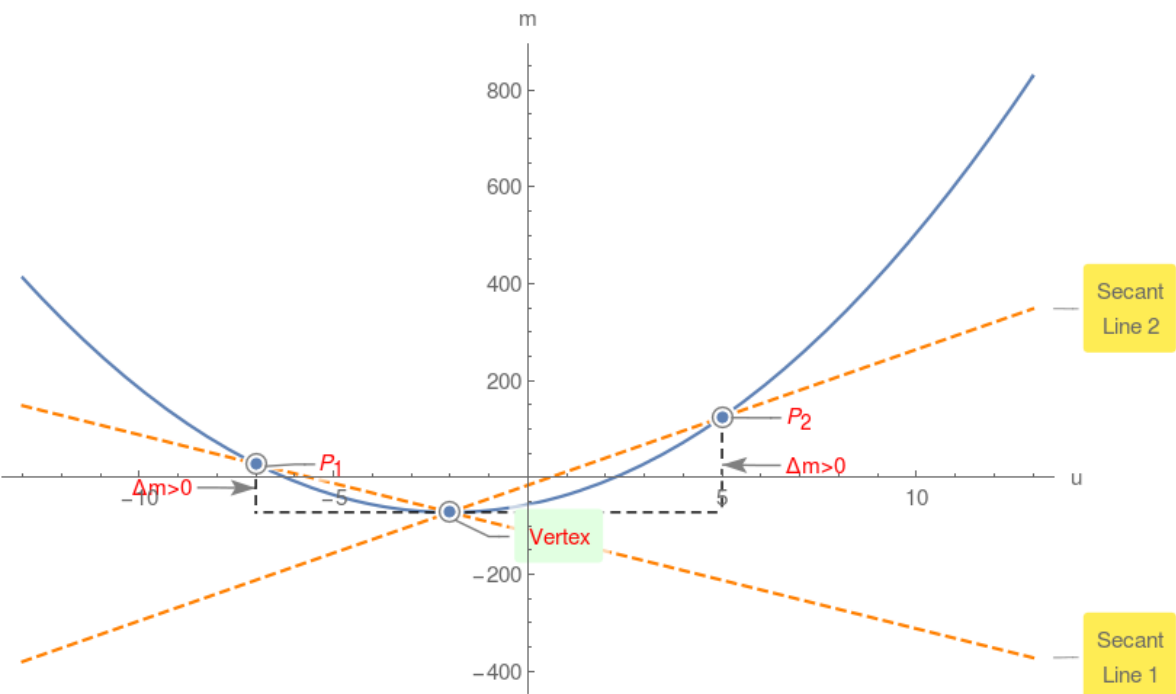
$$m(u_1+h) = -\frac{b^2}{4a} + ah^2 + c$$

$$\text{Compute } \Delta = m(u_1+h) - m(u_1) = ah^2$$

Since  $h^2 > 0$ , therefore if  $a > 0$  then  $\Delta > 0$  or vertex is the global minimum!

## Example 1.

$$m(u) = 4u^2 + 16u - 56$$



However if  $a < 0$  then  $\Delta < 0$  or vertex is the global maximum!

## Example 2.

$$m(u) = -u^2 + 6u + 38$$

