

1.

It so happens that this function can be simplified as:

$$\begin{aligned}m(g) &= \frac{-64+g^3}{-12-g+g^2} \\&= \frac{(g-4)(g^2+4g+16)}{(g-4)(g+3)} \\&= \frac{g^2+4g+16}{g+3}\end{aligned}$$

To find the vertical asymptote :

$$g+3=0$$

$$g=-3$$

There is a vertical asymptote at $g=-3$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-64+g^3}{-12-g+g^2} = \frac{g^2+4g+16}{g+3} = \frac{13}{g+3} + (g+1)$$

There is an oblique asymptote at $j=g+1$

