The domain is all values that z is allowed to be.
Since I can't divide by zero (division by zero isn't allowed,

I need to find all values of z that would cause division by zero.

 $2 z^4 + 9 = 0$

The domain will then be all other z-values. When is this denominator equal to zero?

impossible , then the domain of w is $(-\infty,\infty)$ i.e. $z{\in}\mathbb{R}$