3. Which of the following are correct calculations for difference quotient of: $f(q) = 3 q^2 + 2 q + 8$ $f(q) = 3 q^2 + 2 q + 8$ $f(q+h) = 3 (h+q)^2 + 2 (h+q) + 8$

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\begin{split} f\left(q\right) &= 3\ q^2 + 2\ q + 8 \\ f\left(q+h\right) &= 3\ \left(h+q\right)^2 + 2\ \left(h+q\right) + 8 \\ &= 3\ h^2 + 6\ h\ q + 2\ h + 3\ q^2 + 2\ q + 8 \\ \frac{f\left(q+h\right) - f\left(q\right)}{h} &= \frac{\left(3\ h^2 + 6\ q\ h + 2\ h + 3\ q^2 + 2\ q + 8\right) - \left(3\ \left(q+1\right)^2 + 2\ \left(q+1\right) + 8\right)}{h} \\ &= \frac{3\ h^2 + 6\ q\ h + 2\ h}{h} \\ &= \frac{h\left(3\ h + 6\ q + 2\right)}{h} \\ &= 3\ h + 6\ q + 2 \end{split}
```

$$\begin{split} f\left(q\right) &= 3\ q^2 + 2\ q + 8 \\ f\left(q+h\right) &= 3\ \left(h+q\right)^2 + 2\ \left(h+q\right) + 8 \\ &= 3\ h^2 + 6\ h\ q + 8\ h + 3\ q^2 + 8\ q + 13 \\ &\frac{f\left(q+h\right) - f\left(q\right)}{h} = \frac{\left(3\ h^2 + 6\ q\ h + 8\ h + 3\ q^2 + 8\ q + 13\right) - \left(3\ q^2 + 2\ q + 8\right)}{h} \\ &= \frac{3\ h^2 + 6\ q\ h + 2\ h}{h} \\ &= \frac{h\left(3\ h + 6\ q + 2\right)}{h} \\ &= 3\ h + 6\ q + 2 \end{split}$$

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f(q) = 3 q^{2} + 2 q + 8
f(q+h) = 3 (h+q)^{2} + 2 (h+q) + 8
= 3 h^{2} + 6 h q + 2 h + 3 q^{2} + 2 q + 8
\frac{f(q+h) - f(q)}{h} = \frac{\left(3 h^{2} + 6 q h + 2 h + 3 q^{2} + 2 q + 8\right) - \left(3 q^{2} + 2 q + 8\right)}{h}
= \frac{3 h^{2} + 6 q h + 2 h}{h}
= \frac{h (3 h + 6 q + 2)}{h}
= 3 h + 6 q + 2
```

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\begin{split} f\left(q\right) &= 3\ q^2 + 2\ q + 8 \\ f\left(q+h\right) &= 3\ \left(h+q\right)^2 + 2\ \left(h+q\right) + 8 \\ &= 3\ h^2 + 6\ h\ q - 4\ h + 3\ q^2 - 4\ q + 9 \\ &\frac{f\left(q+h\right) - f\left(q\right)}{h} = \frac{\left(3\ h^2 + 6\ q\ h + 14\ h + 3\ q^2 + 14\ q + 24\right) - \left(3\ q^2 + 2\ q + 8\right)}{h} \\ &= \frac{3\ h^2 + 6\ q\ h + 2\ h}{h} \\ &= \frac{h\left(3\ h + 6\ (q+1) + 2\right)}{h} \\ &= 3\ h + 6\ q + 2 \end{split}
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Solution