

4.

It so happens that this function can be simplified as:

$$\begin{aligned} t(a) &= \frac{-1+a^3}{-1+a^2} \\ &= \frac{(a-1)(a^2+a+1)}{(a-1)(a+1)} \\ &= \frac{a^2+a+1}{a+1} \end{aligned}$$

To find the vertical asymptote :

$$a+1=0$$

$$a=-1$$

There is a vertical asymptote at  $a=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator  $\frac{-1+a^3}{-1+a^2} = \frac{a^2+a+1}{a+1} = \frac{1}{a+1} + a$

There is an oblique asymptote at  $s=a$

