

4.

Solution

Quadratic function: is a function that can be written in the form:

$f(d) = ad^2 + bd + c$ where a , b , and c are real numbers and $a \neq 0$

we have $f(d) = 3d^2 - 14d$, note: $3d^2 - 14d$ is in df -plane

Here, we know that $a = 3$, $b = -14$, $c = 0$

Since $a > 0$, we know that the f -coordinate of the vertex is a minimum. However, to find the f -coordinate of our vertex we first need to find the d -coordinate of the vertex by using $d = -\frac{b}{2a} = -\frac{-14}{2 \cdot 3} = \frac{7}{3}$ Now that we have the d -coordinate, we can find the f -coordinate

of the vertex by finding $f\left(\frac{7}{3}\right) = 3\left(\frac{7}{3}\right)^2 - 14\left(\frac{7}{3}\right) + 0 = \frac{49}{3} - \frac{98}{3} + 0 = -\frac{49}{3}$ Minimum = $-\frac{49}{3}$