1. Which of the following are correct calculations for difference quotient of:  $x(w) = 9 w^2 + 8 w + 9$   $x(w) = 9 w^2 + 8 w + 9$   $x(w+h) = 9 (h+w)^2 + 8 (h+w) + 9$ 

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 \begin{array}{l} x \left( w \right) = 9 \; w^2 \; + \; 8 \; w \; + \; 9 \\ x \left( w + h \right) = 9 \; \left( h \; + \; w \right)^2 \; + \; 8 \; \left( h \; + \; w \right) \; \; + \; 9 \\ = 9 \; h^2 \; + \; 18 \; h \; w \; + \; 8 \; h \; + \; 9 \; w^2 \; + \; 8 \; w \; + \; 9 \\ \frac{x \left( w + h \right) \; - x \left( w \right)}{h} = \frac{\left( 9 \; h^2 + 18 \; w \; h + \; 8 \; h + \; 9 \; w^2 + \; 8 \; w + \; 9 \right) - \left( 9 \; \left( w + \; 1 \right)^2 + \; 8 \; \left( w + \; 1 \right) \; + \; 9 \right)}{h} \\ = \frac{9 \; h^2 + 18 \; w \; h + \; 8 \; h}{h} \\ = \frac{h \; (9 \; h + \; 18 \; w + \; 8)}{h} \\ = 9 \; h \; + \; 18 \; w \; + \; 8 \end{array}
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\begin{split} x &(w) = 9 \ w^2 + 8 \ w + 9 \\ x &(w+h) = 9 \ (h+w)^2 + 8 \ (h+w) + 9 \\ &= 9 \ h^2 + 18 \ h \ w + 26 \ h + 9 \ w^2 + 26 \ w + 26 \\ &\frac{x \ (w+h) - x \ (w)}{h} = \frac{\left(9 \ h^2 + 18 \ w \ h + 26 \ h + 9 \ w^2 + 26 \ w + 26\right) - \left(9 \ w^2 + 8 \ w + 9\right)}{h} \\ &= \frac{9 \ h^2 + 18 \ w \ h + 8 \ h}{h} \\ &= \frac{h \ (9 \ h + 18 \ w + 8)}{h} \\ &= 9 \ h + 18 \ w + 8 \end{split}
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 \begin{array}{l} x \ (w) = 9 \ w^2 + 8 \ w + 9 \\ x \ (w+h) = 9 \ (h+w)^2 + 8 \ (h+w) + 9 \\ = 9 \ h^2 + 18 \ h \ w + 8 \ h + 9 \ w^2 + 8 \ w + 9 \\ \frac{x \ (w+h) - x \ (w)}{h} = \frac{\left(9 \ h^2 + 18 \ w \ h + 8 \ h + 9 \ w^2 + 8 \ w + 9\right) - \left(9 \ w^2 + 8 \ w + 9\right)}{h} \\ = \frac{9 \ h^2 + 18 \ w \ h + 8 \ h}{h} \\ = \frac{h \ (9 \ h + 18 \ w + 8)}{h} \\ = 9 \ h + 18 \ w + 8 \\ \end{array}
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\begin{split} x &(w) = 9 \ w^2 + 8 \ w + 9 \\ x &(w+h) = 9 \ (h+w)^2 + 8 \ (h+w) + 9 \\ &= 9 \ h^2 + 18 \ h \ w - 10 \ h + 9 \ w^2 - 10 \ w + 10 \\ \frac{x \, (w+h) - x \, (w)}{h} &= \frac{\left(9 \ h^2 + 18 \ w \ h + 44 \ h + 9 \ w^2 + 44 \ w + 61\right) - \left(9 \ w^2 + 8 \ w + 9\right)}{h} \\ &= \frac{9 \ h^2 + 18 \ w \ h + 8 \ h}{h} \\ &= \frac{h \, (9 \ h + 18 \ (w+1) + 8)}{h} \\ &= 9 \ h + 18 \ w + 8 \end{split}
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## Solution