Rational Polynomials: Graphing and Asymptotes

Find the intercepts, if there are any.

Step 1: Set the numerator to 0 to solve for horizontal intercepts.

Step 2: Set the x to 0 to solve for vertical intercept.

Step 3: Set the denominator to 0 to solve for vertical asymptotes.

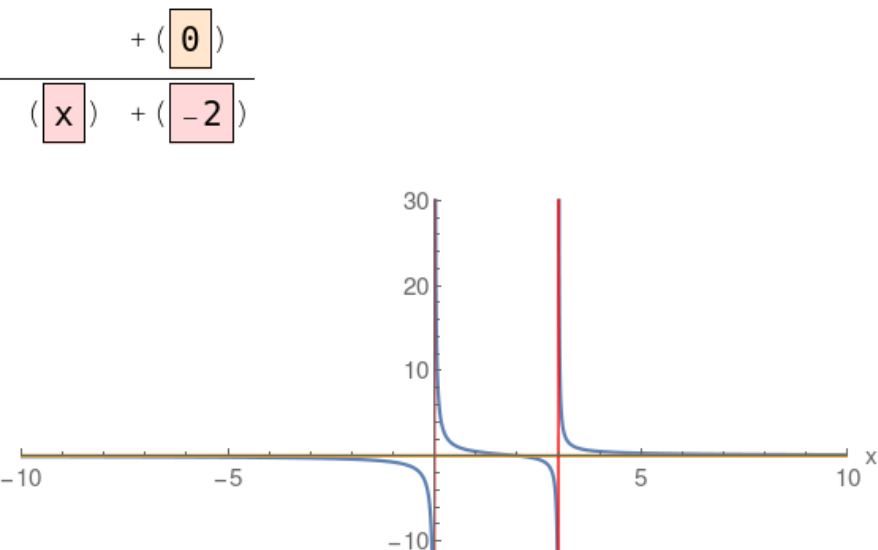
Step 4: Perform a long division to find the quotient which specifies the oblique asymptote.

Note: Blue curve the actual Rational function.
Red and Gold asymptotes.

Example: Horizontal Asymptote

$$\frac{x-5}{3x-4}$$

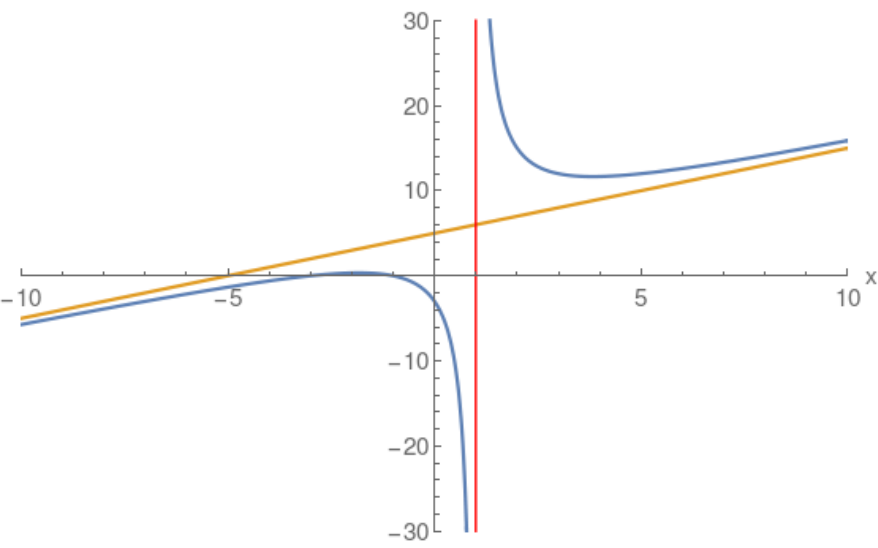
$$\begin{array}{r|l} & +\left(\frac{1}{3}\right) \\ \hline 3x-4 & (1)\,x \;+(-5) \\ & \left(x\right) \;+\left(-\frac{4}{3}\right) \\ & +\left(-\frac{11}{3}\right) \end{array}$$



Example: Oblique Linear Asymptote

$$\frac{(x+1)\,(x+3)}{x-1}$$

$$\begin{array}{r|l} & +(x) \quad +(5) \\ \hline x-1 & (1)\,x^2 \;+(4)\,x \quad +(3) \\ & \left(x^2\right) \;+(-x) \\ & +(5)\,x \quad +(3) \\ & +(5x) \quad +(-5) \\ & +(8) \end{array}$$



Example: Multiple Vertical Asymptotes

$$\frac{x-2}{(x-3)\,x}$$

$$\begin{array}{r|l} & +(0) \\ \hline (x) \;+(-2) \end{array}$$