3. Which of the following are correct calculations for difference quotient of:  $s(e) = 5e^2 + 2e + 4$   $s(e) = 5e^2 + 2e + 4$   $s(e+h) = 5(e+h)^2 + 2(e+h) + 4$ 

```
\begin{split} s\;(e) &= 5\;e^2 + 2\;e + 4 \\ s\;(e+h) &= 5\;\left(e+h\right)^2 + 2\;\left(e+h\right) + 4 \\ &= 5\;e^2 + 10\;e\;h + 2\;e + 5\;h^2 + 2\;h + 4 \\ \frac{s\;(e+h) - s\;(e)}{h} &= \frac{\left(5\;e^2 + 10\;h\;e + 2\;e + 5\;h^2 + 2\;h + 4\right) - \left(5\;\left(e+1\right)^2 + 2\;\left(e+1\right) + 4\right)}{h} \\ &= \frac{5\;h^2 + 10\;e\;h + 2\;h}{h} \\ &= \frac{h\;(10\;e + 5\;h + 2)}{h} \\ &= 10\;e + 5\;h + 2 \end{split}
```

```
s(e) = 5e^{2} + 2e + 4
s(e+h) = 5(e+h)^{2} + 2(e+h) + 4
= 5e^{2} + 10eh + 12e + 5h^{2} + 12h + 11
\frac{s(e+h) - s(e)}{h} = \frac{\left(5e^{2} + 10h + e + 12e + 5h^{2} + 12h + 11\right) - \left(5e^{2} + 2e + 4\right)}{h}
= \frac{5h^{2} + 10eh + 2h}{h}
= \frac{h(10e + 5h + 2)}{h}
= 10e + 5h + 2
```

```
\begin{split} &s \ (e+h) = 5 \ (e+h)^2 + 2 \ (e+h) + 4 \\ &= 5 \ e^2 + 10 \ e \ h + 2 \ e + 5 \ h^2 + 2 \ h + 4 \\ &\frac{s \ (e+h) - s \ (e)}{h} = \frac{\left(5 \ e^2 + 10 \ h \ e + 2 \ e + 5 \ h^2 + 2 \ h + 4\right) - \left(5 \ e^2 + 2 \ e + 4\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ e \ h + 2 \ h}{h} \\ &= \frac{h \ (10 \ e + 5 \ h + 2)}{h} \\ &= 10 \ e + 5 \ h + 2 \end{split}
```

$$\begin{split} s &(e) = 5 \, e^2 + 2 \, e + 4 \\ s &(e+h) = 5 \, (e+h)^2 + 2 \, (e+h) + 4 \\ = 5 \, e^2 + 10 \, e \, h - 8 \, e + 5 \, h^2 - 8 \, h + 7 \\ \frac{s \, (e+h) - s \, (e)}{h} &= \frac{\left(5 \, e^2 + 10 \, h \, e + 22 \, e + 5 \, h^2 + 22 \, h + 28\right) - \left(5 \, e^2 + 2 \, e + 4\right)}{h} \\ &= \frac{5 \, h^2 + 10 \, e \, h + 2 \, h}{h} \\ &= \frac{h \, (10 \, (e+1) + 5 \, h + 2)}{h} \\ &= 10 \, e + 5 \, h + 2 \end{split}$$

## Solution