

Vertex of the Quadratic

Given a quadratic $v(u) = au^2 + bu + c$ compute its value at

$$u_1 = -\frac{b}{2a} \text{ namely } v(u_1) = c - \frac{b^2}{4a}$$

Now compute the same quadratic at u_1+h , namely

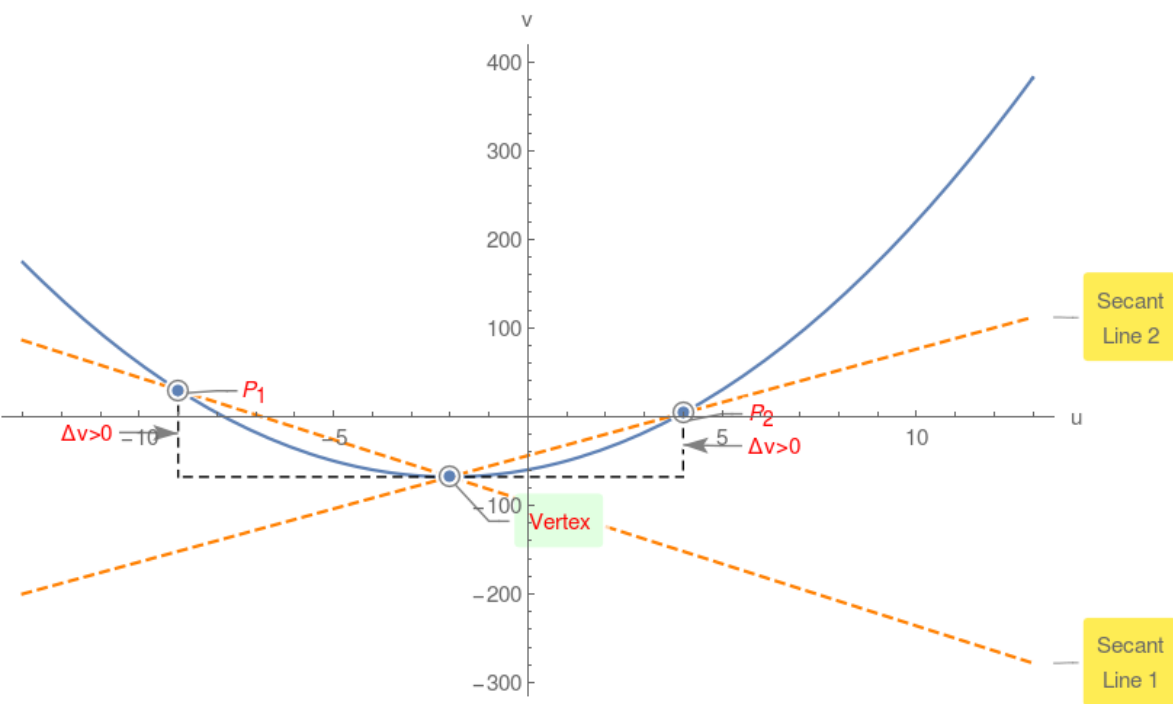
$$v(u_1+h) = -\frac{b^2}{4a} + ah^2 + c$$

$$\text{Compute } \Delta = v(u_1+h) - v(u_1) = ah^2$$

Since $h^2 > 0$, therefore if $a > 0$ then $\Delta > 0$ or vertex is the global minimum!

Example 1.

$$v(u) = 2u^2 + 8u - 60$$



However if $a < 0$ then $\Delta < 0$ or vertex is the global maximum!

Example 2.

$$v(u) = 62 - u^2$$

