

3.

Solution

Quadratic function: is a function that can be written in the form:

$r(s) = as^2 + bs + c$ where a , b , and c are real numbers and $a \neq 0$

we have $r(s) = 3s^2 - 14s - 22$, note: $3s^2 - 14s - 22$ is in sr -plane

Here, we know that $a=3$, $b=-14$, $c=-22$

Since $a > 0$, we know that the r -coordinate of the vertex is a minimum. However, to find the r -coordinate of our vertex we first need to find the s -coordinate of the vertex by using $s = -\frac{b}{2a} = -\frac{-14}{2 \cdot 3} = \frac{7}{3}$ Now that we have the s -coordinate, we can find the r -coordinate

of the vertex by finding $r\left(\frac{7}{3}\right) = 3\left(\frac{7}{3}\right)^2 - 14\left(\frac{7}{3}\right) - 22 = \frac{49}{3} - \frac{98}{3} - 22 = -\frac{115}{3}$ Minimum $= -\frac{115}{3}$