

5.

It so happens that this function can be simplified as:

$$\begin{aligned}m(r) &= \frac{-2+8r^2}{2+4r} \\&= \frac{(2r-1)(4r+2)}{4r+2} \\&= 2r-1\end{aligned}$$

To find the vertical asymptote :

There is no vertical asymptote

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 2nd degree polynomial while the denominator contains a 1st degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator and so the oblique asymptote $f=2r-1$

