

4.

It so happens that this function can be simplified as:

$$\begin{aligned} t(d) &= \frac{-125+d^3}{-5-4d+d^2} \\ &= \frac{(d-5)(d^2+5d+25)}{(d-5)(d+1)} \\ &= \frac{d^2+5d+25}{d+1} \end{aligned}$$

To find the vertical asymptote :

$$d+1=0$$

$$d=-1$$

There is a vertical asymptote at $d=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator $\frac{-125+d^3}{-5-4d+d^2} = \frac{d^2+5d+25}{d+1} = \frac{21}{d+1} + (d+4)$

There is an oblique asymptote at $h=d+4$

