

3.

It so happens that this function can be simplified as:

$$\begin{aligned}q(f) &= \frac{-27+f^3}{-6-f+f^2} \\&= \frac{(f-3)(f^2+3f+9)}{(f-3)(f+2)} \\&= \frac{f^2+3f+9}{f+2}\end{aligned}$$

To find the vertical asymptote :

$$f+2=0$$

$$f=-2$$

There is a vertical asymptote at $f=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-27+f^3}{-6-f+f^2} = \frac{f^2+3f+9}{f+2} = \frac{7}{f+2} + (f+1)$$

There is an oblique asymptote at $v=f+1$

