5. Which of the following are correct calculations for difference quotient of: $u(k) = k^2 + 3k + 4$ $u(k) = k^2 + 3k + 4$ $u(k+h) = (h+k)^2 + 3(h+k) + 4$ $= h^2 + 2hk + 3h + k^2 + 3k + 4$

$$\begin{array}{l} u\;(\;k\;) = k^2 + 3\;k + 4 \\ u\;(\;k+h\;) = (\;h\;+\;k\;)^2 + 3\;(\;h\;+\;k\;) + 4 \\ = h^2 + 2\;h\;k + 3\;h + k^2 + 3\;k + 4 \\ \frac{u\;(\;k+h\;) - u\;(\;k\;)}{h} = \frac{\left(h^2 + 2\;k\;h + 3\;h + k^2 + 3\;k + 4\right) - \left(\;(\;k+1\;)^2 + 3\;(\;k+1\;) + 4\right)}{h} \\ = \frac{h^2 + 2\;k\;h + 3\;h}{h} \\ = \frac{h\;(\;h + 2\;k + 3\;)}{h} \\ = h\;+\;2\;k\;+\;3 \end{array}$$

$$\begin{array}{l} u\left(\,k\,\right) = k^2 \,+\, 3\,\,k \,+\, 4 \\ \\ u\left(\,k + h\,\right) = \left(\,h \,+\, k\,\right)^{\,2} \,+\, 3\,\,\left(\,h \,+\, k\,\right) \,\,+\, 4 \\ \\ = h^2 \,+\, 2\,\,h\,\,k \,+\, 5\,\,h \,+\, k^2 \,+\, 5\,\,k \,+\, 8 \\ \\ \frac{u\left(\,k + h\,\right) \,-\, u\left(\,k\,\right)}{h} = \frac{\left(\,h^2 + 2\,\,k\,\,h + 5\,\,h + k^2 + 5\,\,k + 8\,\right) \,-\,\left(\,k^2 + 3\,\,k + 4\,\right)}{h} \\ \\ = \frac{h^2 + 2\,\,k\,\,h + 3\,\,h}{h} \\ \\ = \frac{h\left(\,h + 2\,\,k + 3\,\right)}{h} \\ \\ = h \,+\, 2\,\,k \,+\, 3 \end{array}$$

$$\begin{array}{l} u\left(k\right)=k^{2}+3\ k+4\\ u\left(k\!+\!h\right)=\left(h+k\right)^{2}+3\ \left(h+k\right)+4\\ =\!h^{2}+2\ h\ k+3\ h+k^{2}+3\ k+4\\ \frac{u\left(k\!+\!h\right)-u\left(k\right)}{h}=\frac{\left(\!h^{2}\!+\!2\ k\ h\!+\!3\ h\!+\!k^{2}\!+\!3\ k\!+\!4\!\right)\!-\!\left(\!k^{2}\!+\!3\ k\!+\!4\!\right)}{h}\\ =\!\frac{h^{2}\!+\!2\ k\ h\!+\!3\ h}{h}\\ =\!\frac{h\left(h\!+\!2\ k\!+\!3\right)}{h}\\ =\!h+2\ k+3 \end{array}$$

$$\begin{array}{l} u\left(k\right) = k^2 + 3 \ k + 4 \\ u\left(k + h\right) = \left(h + k\right)^2 + 3 \ \left(h + k\right) + 4 \\ = h^2 + 2 \ h \ k + h + k^2 + k + 2 \\ \frac{u\left(k + h\right) - u\left(k\right)}{h} = \frac{\left(h^2 + 2 \ k \ h + 7 \ h + k^2 + 7 \ k + 14\right) - \left(k^2 + 3 \ k + 4\right)}{h} \\ = \frac{h^2 + 2 \ k \ h + 3 \ h}{h} \\ = \frac{h \ \left(h + 2 \ \left(k + 1\right) + 3\right)}{h} \\ = h + 2 \ k + 3 \end{array}$$

Solution