2. Which of the following are correct calculations for difference quotient of: $d(k) = k^2 + 6k + 3$ $d(k) = k^2 + 6k + 3$ $d(k + k) = (k + k)^2 + 6(k + k) + 3$

$$\begin{split} &d(k) = k^2 + 6 \ k + 3 \\ &d(k+h) = (h+k)^2 + 6 \ (h+k) + 3 \\ &= h^2 + 2 \ h \ k + 6 \ h + k^2 + 6 \ k + 3 \\ &\frac{d(k+h) - d(k)}{h} = \frac{\left(h^2 + 2 \ k \ h + 6 \ h + k^2 + 6 \ k + 3\right) - \left((k+1)^2 + 6 \ (k+1) + 3\right)}{h} \\ &= \frac{h^2 + 2 \ k \ h + 6 \ h}{h} \\ &= \frac{h \ (h+2 \ k + 6)}{h} \\ &= h + 2 \ k + 6 \end{split}$$

$$\begin{split} &d\left(\,k\,\right) = k^2 \,+\, 6\,\,k \,+\, 3 \\ &d\left(\,k + h\,\right) = \left(\,h \,+\, k\,\right)^{\,2} \,+\, 6\,\,\left(\,h \,+\, k\,\right) \,\,+\, 3 \\ &= h^2 \,+\, 2\,\,h\,\,k \,+\, 8\,\,h \,+\, k^2 \,+\, 8\,\,k \,+\, 10 \\ &\frac{d\,(k + h)\,-d\,(k)}{h} = \frac{\left(\,h^2 + 2\,\,k\,\,h + 8\,\,h + k^2 + 8\,\,k + 10\,\right)\,-\,\left(\,k^2 + 6\,\,k + 3\,\right)}{h} \\ &= \frac{h^2 + 2\,\,k\,\,h + 6\,\,h}{h} \\ &= \frac{h\,(h + 2\,\,k + 6)}{h} \\ &= h \,+\, 2\,\,k \,+\, 6 \end{split}$$

$$\begin{split} d\left(k\right) &= k^2 + 6 \ k + 3 \\ d\left(k + h\right) &= (h + k)^2 + 6 \ (h + k) + 3 \\ &= h^2 + 2 \ h \ k + 6 \ h + k^2 + 6 \ k + 3 \\ \frac{d\left(k + h\right) - d\left(k\right)}{h} &= \frac{\left(h^2 + 2 \ k \ h + 6 \ h + k^2 + 6 \ k + 3\right) - \left(k^2 + 6 \ k + 3\right)}{h} \\ &= \frac{h^2 + 2 \ k \ h + 6 \ h}{h} \\ &= \frac{h \ (h + 2 \ k + 6)}{h} \\ &= h + 2 \ k + 6 \end{split}$$

$$\begin{split} d\left(k\right) &= k^2 + 6 \ k + 3 \\ d\left(k + h\right) &= (h + k)^2 + 6 \ (h + k) + 3 \\ &= h^2 + 2 \ h \ k + 4 \ h + k^2 + 4 \ k - 2 \\ \frac{d\left(k + h\right) - d\left(k\right)}{h} &= \frac{\left(h^2 + 2 \ k \ h + 10 \ h + k^2 + 10 \ k + 19\right) - \left(k^2 + 6 \ k + 3\right)}{h} \\ &= \frac{h^2 + 2 \ k \ h + 6 \ h}{h} \\ &= \frac{h \ (h + 2 \ (k + 1) + 6)}{h} \\ &= h + 2 \ k + 6 \end{split}$$

Solution