

1.

1. Since the fences enclose a rectangular plot without one side, two sides have length b and one side has length a :

$$a + b + b = 1458 \implies a = 1458 - 2b$$

the area:

$$\text{area} = a \times b = (1458 - 2b)b = 1458b - 2b^2$$

Note that the equation is for parabola. Now solve for the vertex:

$$\text{vertex} = \left(\frac{729}{2} \text{ feet}, \frac{531441}{2} \text{ feet}^2 \right)$$

Square the unit for vertex's vertical coordinate since it is a quadratic.