4. Which of the following are correct calculations for difference quotient of: $x(n) = 9 n^2 + 5 n + 8$ $x(n) = 9 n^2 + 5 n + 8$

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\begin{array}{l} x\left(n\right) = 9 \; n^2 + 5 \; n + 8 \\ x\left(n + h\right) = 9 \; \left(h + n\right)^2 + 5 \; \left(h + n\right) \; + 8 \\ = 9 \; h^2 + 18 \; h \; n + 5 \; h + 9 \; n^2 + 5 \; n + 8 \\ \frac{x\left(n + h\right) - x\left(n\right)}{h} = \frac{\left(9 \; h^2 + 18 \; n \; h + 5 \; h + 9 \; n^2 + 5 \; n + 8\right) - \left(9 \; \left(n + 1\right)^2 + 5 \; \left(n + 1\right) + 8\right)}{h} \\ = \frac{9 \; h^2 + 18 \; n \; h + 5 \; h}{h} \\ = \frac{h \; \left(9 \; h + 18 \; n + 5\right)}{h} \\ = 9 \; h \; + \; 18 \; n \; + \; 5 \end{array}
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 \begin{array}{l} x \ (n) = 9 \ n^2 + 5 \ n + 8 \\ x \ (n+h) = 9 \ (h+n)^2 + 5 \ (h+n) + 8 \\ = 9 \ h^2 + 18 \ h \ n + 23 \ h + 9 \ n^2 + 23 \ n + 22 \\ \frac{x \ (n+h) - x \ (n)}{h} = \frac{\left(9 \ h^2 + 18 \ n \ h + 23 \ h + 9 \ n^2 + 23 \ n + 22\right) - \left(9 \ n^2 + 5 \ n + 8\right)}{h} \\ = \frac{9 \ h^2 + 18 \ n \ h + 5 \ h}{h} \\ = \frac{h \ (9 \ h + 18 \ n + 5)}{h} \\ = 9 \ h + 18 \ n + 5 \end{array}
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\begin{split} &x\left(n\right)=9\ n^{2}+5\ n+8\\ &x\left(n+h\right)=9\ \left(h+n\right)^{2}+5\ \left(h+n\right)\ +8\\ &=9\ h^{2}+18\ h\ n+5\ h+9\ n^{2}+5\ n+8\\ &\frac{x\left(n+h\right)-x\left(n\right)}{h}=\frac{\left(9\ h^{2}+18\ n\ h+5\ h+9\ n^{2}+5\ n+8\right)-\left(9\ n^{2}+5\ n+8\right)}{h}\\ &=\frac{9\ h^{2}+18\ n\ h+5\ h}{h}\\ &=\frac{h\left(9\ h+18\ n+5\right)}{h}\\ &=9\ h+18\ n+5 \end{split}
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\begin{array}{l} x\,(\,n\,) = 9\,\,n^2 \,+\, 5\,\,n \,+\, 8 \\ x\,(\,n + h\,) = 9\,\,\left(\,h \,+\, n\,\right)^{\,2} \,+\, 5\,\,\left(\,h \,+\, n\,\right) \,\,+\, 8 \\ = 9\,\,h^2 \,+\, 18\,\,h\,\,n \,-\, 13\,\,h \,+\, 9\,\,n^2 \,-\, 13\,\,n \,+\, 12 \\ \frac{x\,(\,n + h\,) \,-\, x\,(\,n\,)}{h} = \frac{\left(\,9\,\,h^2 + 18\,\,n\,\,h + 41\,\,h + 9\,\,n^2 + 41\,\,n + 54\,\right) - \left(\,9\,\,n^2 + 5\,\,n + 8\,\right)}{h} \\ = \frac{9\,\,h^2 + 18\,\,n\,\,h + 5\,\,h}{h} \\ = \frac{h\,(\,9\,\,h + 18\,\,(\,n + 1\,) \,+ 5\,)}{h} \\ = 9\,\,h \,+\, 18\,\,n \,+\, 5 \end{array}
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Solution