difference quotient of:  $v(u) = 3 u^2 + u + 8$   $v(u) = 3 u^2 + u + 8$   $v(u+h) = 3 (h+u)^2 + h + u + 8$   $= 3 h^2 + 6 h u + h + 3 u^2 + u + 8$   $\frac{v(u+h) - v(u)}{h} = \frac{\left(3 h^2 + 6 u h + h + 3 u^2 + u + 8\right) - \left(3 (u+1)^2 + u + 9\right)}{h}$   $\frac{3 h^2 + 6 u h + h}{h}$ 

7. Which of the following are correct calculations for

```
 \begin{array}{l} = 3 \; h + 6 \; u + 1 \\ \\ v \, (u) = 3 \; u^2 + u + 8 \\ v \, (u + h) = 3 \; (h + u)^2 + h + u + 8 \\ = 3 \; h^2 + 6 \; h \; u + 7 \; h + 3 \; u^2 + 7 \; u + 12 \\ \\ \frac{v \, (u + h) - v \, (u)}{h} = \frac{\left(3 \; h^2 + 6 \; u \; h + 7 \; h + 3 \; u^2 + 7 \; u + 12\right) - \left(3 \; u^2 + u + 8\right)}{h} \\ = \frac{3 \; h^2 + 6 \; u \; h + h}{h} \\ = \frac{h \, (3 \; h + 6 \; u + 1)}{h} \\ = 3 \; h + 6 \; u + 1 \\ \end{array}
```

 $=\frac{h(3h+6u+1)}{}$ 

```
\begin{array}{c} v\left(u\right) = 3 \; u^2 + u + 8 \\ v\left(u + h\right) = 3 \; \left(h + u\right)^2 + h + u + 8 \\ = 3 \; h^2 + 6 \; h \; u + h + 3 \; u^2 + u + 8 \\ \frac{v\left(u + h\right) - v\left(u\right)}{h} = \frac{\left(3 \; h^2 + 6 \; u \; h + h + 3 \; u^2 + u + 8\right) - \left(3 \; u^2 + u + 8\right)}{h} \\ = \frac{3 \; h^2 + 6 \; u \; h + h}{h} \\ = \frac{h \; (3 \; h + 6 \; u + 1)}{h} \\ = 3 \; h + 6 \; u + 1 \end{array}
```

```
\begin{split} v\left(u\right) &= 3\ u^2 + u + 8 \\ v\left(u + h\right) &= 3\ \left(h + u\right)^2 + h + u + 8 \\ &= 3\ h^2 + 6\ h\ u - 5\ h + 3\ u^2 - 5\ u + 10 \\ &\frac{v\left(u + h\right) - v\left(u\right)}{h} = \frac{\left(3\ h^2 + 6\ u\ h + 13\ h + 3\ u^2 + 13\ u + 22\right) - \left(3\ u^2 + u + 8\right)}{h} \\ &= \frac{3\ h^2 + 6\ u\ h + h}{h} \\ &= \frac{h\left(3\ h + 6\ \left(u + 1\right) + 1\right)}{h} \\ &= 3\ h + 6\ u + 1 \end{split}
```

## Solution