

# Intercepts of the Quadratic

Given a quadratic  $m(v) = a v^2 + b v + c$  compute its discriminant  $\Delta$ :

$$\Delta = \sqrt{b^2 - 4ac}$$

**Case1:  $\Delta > 0$**

$v_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$  computes the v-intercepts of multiplicity 1.

$m(0) = c$  computes the single m-intercept.

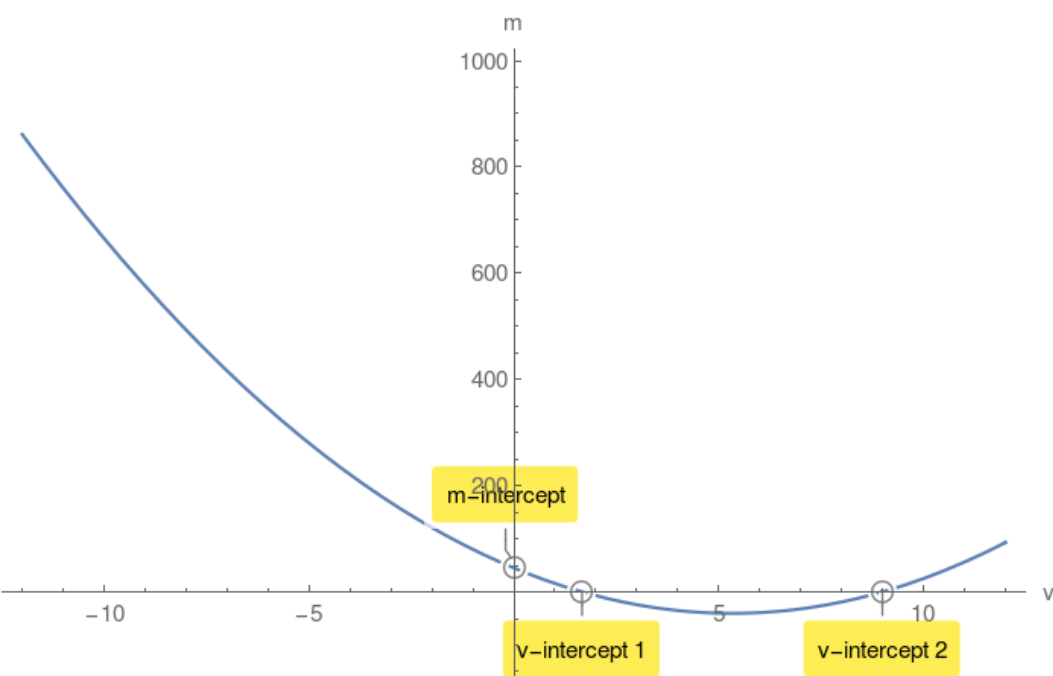
**Example 1.**

$m(v) = 3v^2 - 32v + 45$  compute its discriminant  $\Delta$ :

$$\Delta = 484 > 0$$

$$v_{1,2} = \frac{5}{3}, 9$$

$m(0) = 45$  m-intercept.



**Case2:  $\Delta = 0$**

$v_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-b \pm 0}{2a} = \frac{-b}{2a}$  single v-intercept of multiplicity 2.

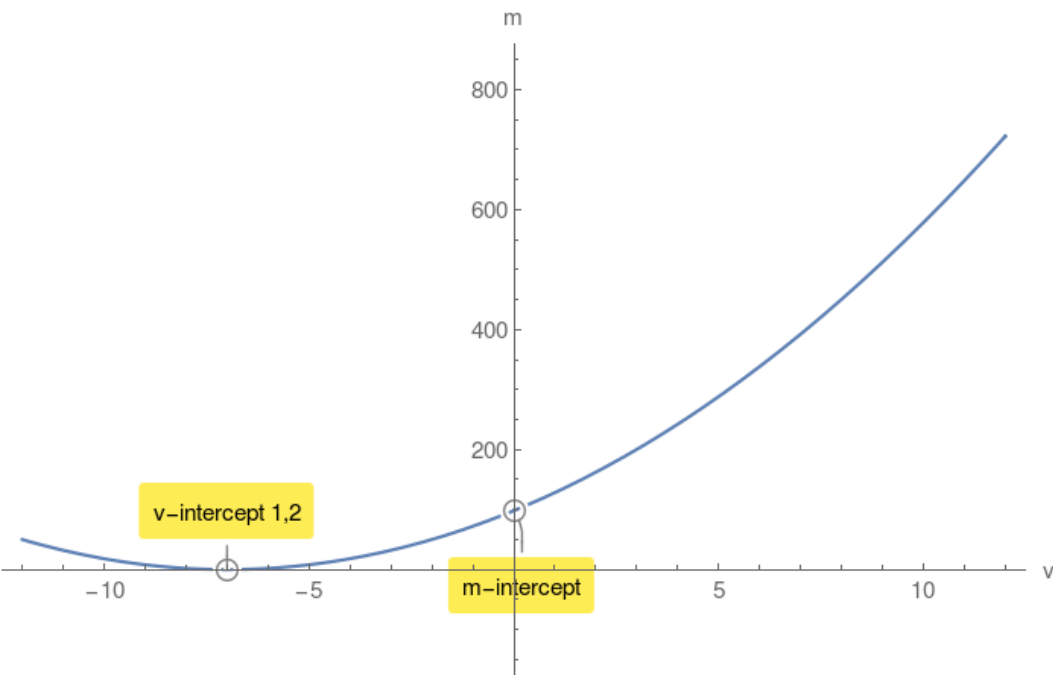
**Example 2.**

$m(v) = 2v^2 + 28v + 98$  compute its discriminant  $\Delta$ :

$$\Delta = 0$$

$$v_{1,2} = -7, -7$$

$m(0) = 98$  m-intercept.



**Case3:  $\Delta < 0$**

$\sqrt{b^2 - 4ac}$  has no value in Real Numbers. Therefore there are no v-intercepts.

However there is a m-intercept.

**Example 3.**

$m(v) = -9v^2 + 180v - 1000$  compute its discriminant  $\Delta$ :

$$\Delta = -3600 < 0$$

$m(0) = -1000$  m-intercept.

