2. Which of the following are correct calculations for difference quotient of: $r(z) = 2z^2 + 4z + 6$ $r(z) = 2z^2 + 4z + 6$ $r(z+h) = 2(h+z)^2 + 4(h+z) + 6$ $= 2h^2 + 4hz + 4h + 2z^2 + 4z + 6$

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r(z) = 2z + 4z + 6
r(z+h) = 2(h+z)^{2} + 4(h+z) + 6
= 2h^{2} + 4hz + 4h + 2z^{2} + 4z + 6
\frac{r(z+h) - r(z)}{h} = \frac{(2h^{2} + 4zh + 4h + 2z^{2} + 4z + 6) - (2(z+1)^{2} + 4(z+1) + 6)}{h}
= \frac{2h^{2} + 4zh + 4h}{h}
= \frac{h(2h + 4z + 4)}{h}
= 2h + 4z + 4
r(z) = 2z^{2} + 4z + 6
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$$\begin{split} & r\left(z+h\right)=2\;\left(h+z\right)^{\,2}+4\;\left(h+z\right)\,+6\\ & = 2\;h^2\,+4\;h\;z\,+8\;h\,+2\;z^2\,+8\;z\,+12\\ & \frac{r\left(z+h\right)-r\left(z\right)}{h}=\frac{\left(2\;h^2+4\;z\;h+8\;h+2\;z^2+8\;z+12\right)-\left(2\;z^2+4\;z+6\right)}{h}\\ & = \frac{2\;h^2+4\;z\;h+4\;h}{h}\\ & = \frac{h\left(2\;h+4\;z+4\right)}{h}\\ & = 2\;h\,+4\;z\,+4 \end{split}$$

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r(z+h) = 2 (h+z)^{2} + 4 (h+z) + 6
= 2 h^{2} + 4 h z + 4 h + 2 z^{2} + 4 z + 6
\frac{r(z+h) - r(z)}{h} = \frac{\left(2 h^{2} + 4 z h + 4 h + 2 z^{2} + 4 z + 6\right) - \left(2 z^{2} + 4 z + 6\right)}{h}
= \frac{2 h^{2} + 4 z h + 4 h}{h}
= \frac{h(2 h + 4 z + 4)}{h}
= 2 h + 4 z + 4
r(z) = 2 z^{2} + 4 z + 6
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$$\begin{split} r\left(z\right) &= 2\ z^2 + 4\ z + 6 \\ r\left(z + h\right) &= 2\ \left(h + z\right)^2 + 4\ \left(h + z\right) + 6 \\ &= 2\ h^2 + 4\ h\ z + 2\ z^2 + 4 \\ \frac{r\left(z + h\right) - r\left(z\right)}{h} &= \frac{\left(2\ h^2 + 4\ z\ h + 12\ h + 2\ z^2 + 12\ z + 22\right) - \left(2\ z^2 + 4\ z + 6\right)}{h} \\ &= \frac{2\ h^2 + 4\ z\ h + 4\ h}{h} \\ &= \frac{h\left(2\ h + 4\ z + 4\right)}{h} \\ &= 2\ h + 4\ z + 4 \end{split}$$

Solution