

7. Given the function $e(y)=2y^2+3y$,
find an equation of the secant line containing $(3,e(3))$
and $(4,e(4))$. Express the equation in slope-intercept form.

$$t = -78 + 17y$$

$$t = 78 - 17y$$

$$t = -24 + 17y$$

$$t = -23 + 18y$$

Solution

The line passing through the two points has the slope:

$$\begin{aligned} & \frac{e(4)-e(3)}{4-3} \\ &= \frac{(2(4)^2+3(4))-(2(3)^2+3(3))}{1} \\ &= \frac{44-27}{1} \\ &= 17 \end{aligned}$$

using one of the points, say $(3,27)$ and the slope to get the equation of the secant line:

$$t-27 = 17(y-3)$$

The equation in slope-intercept form:

$$t = -24 + 17y$$