

3.

## Solution

Quadratic function: is a function that can be written in the form:

$$p(z) = az^2 + bz + c \quad \text{where } a, b, \text{ and } c \text{ are real numbers and } a \neq 0$$

we have  $p(z) = -3z^2 + 13z + 1$ , note:  $-3z^2 + 13z + 1$  is in  $zp$ -plane

Here, we know that  $a = -3$ ,  $b = 13$ ,  $c = 1$

Since  $a < 0$ , we know that the  $p$ -coordinate of the vertex is a maximum. However, to find the  $p$ -coordinate of our vertex we first need to find the  $z$ -coordinate of the vertex by using  $z = -\frac{b}{2a} = -\frac{13}{-6} = \frac{13}{6}$ . Now that we have the  $z$ -coordinate, we can find the  $p$ -coordinate

of the vertex by finding  $p\left(\frac{13}{6}\right) = -3\left(\frac{13}{6}\right)^2 + 13\left(\frac{13}{6}\right) + 1 = -\frac{169}{12} + \frac{169}{6} + 1 = \frac{181}{12}$ . Maximum =  $\frac{181}{12}$