

4.

It so happens that this function can be simplified as:

$$\begin{aligned} m(h) &= \frac{-8+h^3}{-2-h+h^2} \\ &= \frac{(h-2)(h^2+2h+4)}{(h-2)(h+1)} \\ &= \frac{h^2+2h+4}{h+1} \end{aligned}$$

To find the vertical asymptote :

$$h+1=0$$

$$h=-1$$

There is a vertical asymptote at  $h=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator  $\frac{-8+h^3}{-2-h+h^2} = \frac{h^2+2h+4}{h+1} = \frac{3}{h+1} + (h+1)$

There is an oblique asymptote at  $w=h+1$

