3. Which of the following are correct calculations for difference quotient of: $d\left(s\right)=4\;s^{2}+3\;s+8$

$$\begin{split} &d\left(s\right) = 4\ s^2 + 3\ s + 8 \\ &d\left(s + h\right) = 4\ \left(h + s\right)^2 + 3\ \left(h + s\right) + 8 \\ &= 4\ h^2 + 8\ h\ s + 3\ h + 4\ s^2 + 3\ s + 8 \\ &\frac{d\left(s + h\right) - d\left(s\right)}{h} = \frac{\left(4\ h^2 + 8\ s\ h + 3\ h + 4\ s^2 + 3\ s + 8\right) - \left(4\ \left(s + 1\right)^2 + 3\ \left(s + 1\right) + 8\right)}{h} \\ &= \frac{4\ h^2 + 8\ s\ h + 3\ h}{h} \\ &= \frac{h\left(4\ h + 8\ s + 3\right)}{h} \\ &= 4\ h + 8\ s + 3 \end{split}$$

$$\begin{split} d\left(s\right) &= 4\ s^2 + 3\ s + 8 \\ d\left(s + h\right) &= 4\ \left(h + s\right)^2 + 3\ \left(h + s\right) + 8 \\ &= 4\ h^2 + 8\ h\ s + 11\ h + 4\ s^2 + 11\ s + 15 \\ \frac{d\left(s + h\right) - d\left(s\right)}{h} &= \frac{\left(4\ h^2 + 8\ s\ h + 11\ h + 4\ s^2 + 11\ s + 15\right) - \left(4\ s^2 + 3\ s + 8\right)}{h} \\ &= \frac{4\ h^2 + 8\ s\ h + 3\ h}{h} \\ &= \frac{h\left(4\ h + 8\ s + 3\right)}{h} \\ &= 4\ h + 8\ s + 3 \end{split}$$

$$\begin{split} &d\left(s\right) = 4\ s^2 + 3\ s + 8\\ &d\left(s + h\right) = 4\ \left(h + s\right)^2 + 3\ \left(h + s\right) + 8\\ &= 4\ h^2 + 8\ h\ s + 3\ h + 4\ s^2 + 3\ s + 8\\ &\frac{d\left(s + h\right) - d\left(s\right)}{h} = \frac{\left(4\ h^2 + 8\ s\ h + 3\ h + 4\ s^2 + 3\ s + 8\right) - \left(4\ s^2 + 3\ s + 8\right)}{h}\\ &= \frac{4\ h^2 + 8\ s\ h + 3\ h}{h}\\ &= \frac{h\left(4\ h + 8\ s + 3\right)}{h}\\ &= 4\ h + 8\ s + 3 \end{split}$$

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d(s) = 4 s^{2} + 3 s + 8
d(s+h) = 4 (h+s)^{2} + 3 (h+s) + 8
= 4 h^{2} + 8 h s - 5 h + 4 s^{2} - 5 s + 9
\frac{d(s+h) - d(s)}{h} = \frac{\left(4 h^{2} + 8 s h + 19 h + 4 s^{2} + 19 s + 30\right) - \left(4 s^{2} + 3 s + 8\right)}{h}
= \frac{4 h^{2} + 8 s h + 3 h}{h}
= \frac{h(4 h + 8 (s+1) + 3)}{h}
= 4 h + 8 s + 3
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Solution