

2.

It so happens that this function can be simplified as:

$$\begin{aligned}f(r) &= \frac{-1+r^3}{-2+r+r^2} \\&= \frac{(r-1)(r^2+r+1)}{(r-1)(r+2)} \\&= \frac{r^2+r+1}{r+2}\end{aligned}$$

To find the vertical asymptote :

$$r+2=0$$

$$r=-2$$

There is a vertical asymptote at $r=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-1+r^3}{-2+r+r^2} = \frac{r^2+r+1}{r+2} = \frac{3}{r+2} + (r-1)$$

There is an oblique asymptote at $h=r-1$

