5. Which of the following are correct calculations for difference quotient of: $d(x) = 7x^{2} + 3x + 7$

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\begin{split} &d\left(x\right)=7\ x^{2}+3\ x+7\\ &d\left(x+h\right)=7\ \left(h+x\right)^{2}+3\ \left(h+x\right)+7\\ &=7\ h^{2}+14\ h\ x+3\ h+7\ x^{2}+3\ x+7\\ &\frac{d\left(x+h\right)-d\left(x\right)}{h}=\frac{\left(7\ h^{2}+14\ x\ h+3\ h+7\ x^{2}+3\ x+7\right)-\left(7\ \left(x+1\right)^{2}+3\ \left(x+1\right)+7\right)}{h}\\ &=\frac{7\ h^{2}+14\ x\ h+3\ h}{h}\\ &=\frac{h\left(7\ h+14\ x+3\right)}{h}\\ &=7\ h+14\ x+3 \end{split}
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\begin{split} &d\left(x\right)=7\ x^{2}+3\ x+7\\ &d\left(x+h\right)=7\ \left(h+x\right)^{2}+3\ \left(h+x\right)+7\\ &=7\ h^{2}+14\ h\ x+17\ h+7\ x^{2}+17\ x+17\\ &\frac{d\left(x+h\right)-d\left(x\right)}{h}=\frac{\left(7\ h^{2}+14\ x\ h+17\ h+7\ x^{2}+17\ x+17\right)-\left(7\ x^{2}+3\ x+7\right)}{h}\\ &=\frac{7\ h^{2}+14\ x\ h+3\ h}{h}\\ &=\frac{h\left(7\ h+14\ x+3\right)}{h}\\ &=7\ h+14\ x+3 \end{split}
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$$d(x) = 7 x^{2} + 3 x + 7$$

$$d(x+h) = 7 (h + x)^{2} + 3 (h + x) + 7$$

$$= 7 h^{2} + 14 h x + 3 h + 7 x^{2} + 3 x + 7$$

$$\frac{d(x+h) - d(x)}{h} = \frac{(7 h^{2} + 14 x h + 3 h + 7 x^{2} + 3 x + 7) - (7 x^{2} + 3 x + 7)}{h}$$

$$= \frac{7 h^{2} + 14 x h + 3 h}{h}$$

$$= \frac{h(7 h + 14 x + 3)}{h}$$

$$= 7 h + 14 x + 3$$

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\begin{split} d\left(x\right) &= 7 \, x^2 + 3 \, x + 7 \\ d\left(x + h\right) &= 7 \, \left(h + x\right)^2 + 3 \, \left(h + x\right) \, + 7 \\ &= 7 \, h^2 + 14 \, h \, x - 11 \, h + 7 \, x^2 - 11 \, x + 11 \\ \frac{d\left(x + h\right) - d\left(x\right)}{h} &= \frac{\left(7 \, h^2 + 14 \, x \, h + 31 \, h + 7 \, x^2 + 31 \, x + 41\right) - \left(7 \, x^2 + 3 \, x + 7\right)}{h} \\ &= \frac{7 \, h^2 + 14 \, x \, h + 3 \, h}{h} \\ &= \frac{h \, (7 \, h + 14 \, \left(x + 1\right) + 3)}{h} \\ &= 7 \, h \, + \, 14 \, x \, + \, 3 \end{split}
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Solution