1. Which of the following are correct calculations for difference quotient of: $y(v) = 4 v^2 + 9 v + 5$ $y(v) = 4 v^2 + 9 v + 5$ $y(v+h) = 4 (h+v)^2 + 9 (h+v) + 5$ $= 4 h^2 + 8 h v + 9 h + 4 v^2 + 9 v + 5$

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\begin{split} &\frac{y \, (v + h) \, - y \, (v)}{h} = \frac{\left(4 \, h^2 + 8 \, v \, h + 9 \, h + 4 \, v^2 + 9 \, v + 5\right) - \left(4 \, (v + 1)^2 + 9 \, (v + 1) + 5\right)}{h} \\ &= \frac{4 \, h^2 + 8 \, v \, h + 9 \, h}{h} \\ &= \frac{h \, (4 \, h + 8 \, v + 9)}{h} \\ &= 4 \, h \, + \, 8 \, v \, + \, 9 \end{split}
\begin{aligned} &y \, (v) \, = 4 \, v^2 \, + \, 9 \, v \, + \, 5 \\ &y \, (v + h) \, = 4 \, \left(h \, + \, v\right)^2 \, + \, 9 \, \left(h \, + \, v\right) \, + \, 5 \\ &= 4 \, h^2 \, + \, 8 \, h \, v \, + \, 17 \, h \, + \, 4 \, v^2 \, + \, 17 \, v \, + \, 18 \\ &\frac{y \, (v + h) \, - y \, (v)}{h} \, = \frac{\left(4 \, h^2 + 8 \, v \, h + \, 17 \, h + \, 4 \, v^2 + \, 17 \, v + \, 18\right) - \left(4 \, v^2 + 9 \, v + 5\right)}{h} \end{split}
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$$y(v) = 4 v^{2} + 9 v + 5$$

$$y(v+h) = 4 (h + v)^{2} + 9 (h + v) + 5$$

$$= 4 h^{2} + 8 h v + 9 h + 4 v^{2} + 9 v + 5$$

$$\frac{y(v+h) - y(v)}{h} = \frac{(4 h^{2} + 8 v h + 9 h + 4 v^{2} + 9 v + 5) - (4 v^{2} + 9 v + 5)}{h}$$

$$= \frac{4 h^{2} + 8 v h + 9 h}{h}$$

$$= \frac{h(4 h + 8 v + 9)}{h}$$

$$= 4 h + 8 v + 9$$

$$\begin{split} y &(v) = 4 \ v^2 + 9 \ v + 5 \\ y &(v+h) = 4 \ (h+v)^2 + 9 \ (h+v) + 5 \\ = 4 \ h^2 + 8 \ h \ v + h + 4 \ v^2 + v \\ \frac{y &(v+h) - y &(v)}{h} &= \frac{\left(4 \ h^2 + 8 \ v \ h + 25 \ h + 4 \ v^2 + 25 \ v + 39\right) - \left(4 \ v^2 + 9 \ v + 5\right)}{h} \\ &= \frac{4 \ h^2 + 8 \ v \ h + 9 \ h}{h} \\ &= \frac{h &(4 \ h + 8 \ (v+1) + 9)}{h} \\ &= 4 \ h + 8 \ v + 9 \end{split}$$

Solution

 $= \frac{4 \, h^2 + 8 \, v \, h + 9 \, h}{}$

 $=\frac{h(4h+8v+9)}{}$