3. Which of the following are correct calculations for difference quotient of: $u\left(v\right)=7\ v^2+8\ v+1$ $u\left(v\right)=7\ v^2+8\ v+1$ $u\left(v+h\right)=7\ \left(h+v\right)^2+8\ \left(h+v\right)+1$

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\begin{array}{l} u\left(v\right) = 7 \ v^2 + 8 \ v + 1 \\ u\left(v + h\right) = 7 \ \left(h + v\right)^2 + 8 \ \left(h + v\right) \ + 1 \\ = 7 \ h^2 + 14 \ h \ v + 8 \ h + 7 \ v^2 + 8 \ v + 1 \\ \frac{u\left(v + h\right) - u\left(v\right)}{h} = \frac{\left(7 \ h^2 + 14 \ v \ h + 8 \ h + 7 \ v^2 + 8 \ v + 1\right) - \left(7 \ \left(v + 1\right)^2 + 8 \ \left(v + 1\right) + 1\right)}{h} \\ = \frac{7 \ h^2 + 14 \ v \ h + 8 \ h}{h} \\ = \frac{h \ \left(7 \ h + 14 \ v + 8\right)}{h} \\ = 7 \ h + 14 \ v + 8 \end{array}
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$$\begin{array}{l} u\left(v\right) = 7 \; v^2 + 8 \; v + 1 \\ u\left(v + h\right) = 7 \; \left(h + v\right)^2 + 8 \; \left(h + v\right) \; + 1 \\ = 7 \; h^2 + 14 \; h \; v + 22 \; h + 7 \; v^2 + 22 \; v + 16 \\ \frac{u\left(v + h\right) - u\left(v\right)}{h} = \frac{\left(7 \; h^2 + 14 \; v \; h + 22 \; h + 7 \; v^2 + 22 \; v + 16\right) - \left(7 \; v^2 + 8 \; v + 1\right)}{h} \\ = \frac{7 \; h^2 + 14 \; v \; h + 8 \; h}{h} \\ = \frac{h \; (7 \; h + 14 \; v + 8)}{h} \\ = 7 \; h \; + \; 14 \; v \; + \; 8 \end{array}$$

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\begin{split} &\frac{u\,(v+h)\,-u\,(v)}{h} = \frac{\left(7\,\,h^2+14\,v\,\,h+8\,\,h+7\,\,v^2+8\,\,v+1\right)\,-\left(7\,\,v^2+8\,\,v+1\right)}{h} \\ &= \frac{7\,\,h^2+14\,v\,\,h+8\,\,h}{h} \\ &= \frac{h\,(7\,\,h+14\,\,v+8)}{h} \\ &= 7\,\,h\,+\,\,14\,\,v\,+\,\,8 \end{split}
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=7 h + 14 v + 8 **Solution**

 $= \frac{7 h^2 + 14 v h + 8 h}{}$

 $= \frac{h(7 h+14 (v+1)+8)}{}$

 $u(v) = 7v^2 + 8v + 1$

 $u(v+h) = 7(h+v)^2 + 8(h+v) + 1$

 $=7 h^2 + 14 h v + 8 h + 7 v^2 + 8 v + 1$