

1.

To find the vertical asymptote :

We must set the denominator equal to 0 and solve:

$$e^4 - 256 = 0$$

$$(e^2 - 16)(e^2 + 16) = 0$$

$$(e^2 - 16) = 0$$

$$(e - 4)(e + 4) = 0$$

$$e = 4 \text{ or } e = -4$$

There is vertical asymptote at $e = 4$ and at $e = -4$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the denominator contains a 4th degree polynomial.

Since the polynomial in the numerator is a lower degree than the denominator, the horizontal asymptote is located at $n = 0$.

To find the oblique asymptote :

Since the degrees of the numerator are less than the degrees of the denominator, this rational does not have an oblique asymptote

