

1.

It so happens that this function can be simplified as:

$$\begin{aligned} q(d) &= \frac{-1+d^3}{-2+d+d^2} \\ &= \frac{(d-1)(d^2+d+1)}{(d-1)(d+2)} \\ &= \frac{d^2+d+1}{d+2} \end{aligned}$$

To find the vertical asymptote :

$$d+2=0$$

$$d=-2$$

There is a vertical asymptote at $d=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator $\frac{-1+d^3}{-2+d+d^2} = \frac{d^2+d+1}{d+2} = \frac{3}{d+2} + (d-1)$

There is an oblique asymptote at $a=d-1$

