

3.

It so happens that this function can be simplified as:

$$\begin{aligned}d(z) &= \frac{-4-11z+3z^2}{1+3z} \\&= \frac{(z-4)(3z+1)}{3z+1} \\&= z - 4\end{aligned}$$

To find the vertical asymptote :

There is no vertical asymptote

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 2nd degree polynomial while the denominator contains a 1st degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator and so the oblique asymptote $r = z - 4$

