

2.

It so happens that this function can be simplified as:

$$\begin{aligned} m(u) &= \frac{-125+u^3}{-15-2u+u^2} \\ &= \frac{(u-5)(u^2+5u+25)}{(u-5)(u+3)} \\ &= \frac{u^2+5u+25}{u+3} \end{aligned}$$

To find the vertical asymptote :

$$u+3=0$$

$$u=-3$$

There is a vertical asymptote at $u=-3$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

we must divide the numerator by the denominator $\frac{-125+u^3}{-15-2u+u^2} = \frac{u^2+5u+25}{u+3} = \frac{19}{u+3} + (u+2)$

There is an oblique asymptote at $t=u+2$

