4. Which of the following are correct calculations for difference quotient of: $g(f) = 5 \ f^2 + 6 \ f + 8$ $g(f) = 5 \ f^2 + 6 \ f + 8$ $g(f+h) = 5 \ (f+h)^2 + 6 \ (f+h) + 8$

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\begin{split} g\left(f\right) &= 5 \ f^2 + 6 \ f + 8 \\ g\left(f + h\right) &= 5 \ \left(f + h\right)^2 + 6 \ \left(f + h\right) + 8 \\ &= 5 \ f^2 + 10 \ f \ h + 6 \ f + 5 \ h^2 + 6 \ h + 8 \\ \frac{g\left(f + h\right) - g\left(f\right)}{h} &= \frac{\left(5 \ f^2 + 10 \ h \ f + 6 \ f + 5 \ h^2 + 6 \ h + 8\right) - \left(5 \ \left(f + 1\right)^2 + 6 \ \left(f + 1\right) + 8\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ f \ h + 6 \ h}{h} \\ &= \frac{h \left(10 \ f + 5 \ h + 6\right)}{h} \\ &= 10 \ f + 5 \ h + 6 \end{split}
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\begin{split} g\left(f\right) &= 5 \ f^2 + 6 \ f + 8 \\ g\left(f + h\right) &= 5 \ \left(f + h\right)^2 + 6 \ \left(f + h\right) + 8 \\ &= 5 \ f^2 + 10 \ f \ h + 16 \ f + 5 \ h^2 + 16 \ h + 19 \\ \frac{g\left(f + h\right) - g\left(f\right)}{h} &= \frac{\left(5 \ f^2 + 10 \ h \ f + 16 \ f + 5 \ h^2 + 16 \ h + 19\right) - \left(5 \ f^2 + 6 \ f + 8\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ f \ h + 6 \ h}{h} \\ &= \frac{h \left(10 \ f + 5 \ h + 6\right)}{h} \\ &= 10 \ f + 5 \ h + 6 \end{split}
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\begin{split} g\left(f\right) &= 5 \ f^2 + 6 \ f + 8 \\ g\left(f + h\right) &= 5 \ \left(f + h\right)^2 + 6 \ \left(f + h\right) + 8 \\ &= 5 \ f^2 + 10 \ f \ h + 6 \ f + 5 \ h^2 + 6 \ h + 8 \\ &\frac{g\left(f + h\right) - g\left(f\right)}{h} = \frac{\left(5 \ f^2 + 10 \ h \ f + 6 \ f + 5 \ h^2 + 6 \ h + 8\right) - \left(5 \ f^2 + 6 \ f + 8\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ f \ h + 6 \ h}{h} \\ &= \frac{h \left(10 \ f + 5 \ h + 6\right)}{h} \\ &= 10 \ f + 5 \ h + 6 \end{split}
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\begin{split} g(f) &= 5 \ f^2 + 6 \ f + 8 \\ g(f+h) &= 5 \ (f+h)^2 + 6 \ (f+h) + 8 \\ &= 5 \ f^2 + 10 \ f \ h - 4 \ f + 5 \ h^2 - 4 \ h + 7 \\ \frac{g(f+h) - g(f)}{h} &= \frac{\left(5 \ f^2 + 10 \ h \ f + 26 \ f + 5 \ h^2 + 26 \ h + 40\right) - \left(5 \ f^2 + 6 \ f + 8\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ f \ h + 6 \ h}{h} \\ &= \frac{h \ (10 \ (f+1) + 5 \ h + 6)}{h} \\ &= 10 \ f + 5 \ h + 6 \end{split}
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Solution