5. Which of the following are correct calculations for difference quotient of:  $e(c)=2\ c^2+c+8$   $e(c)=2\ c^2+c+8$   $e(c+h)=2\ (c+h)^2+c+h+8$   $=2\ c^2+4\ c\ h+c+2\ h^2+h+8$ 

$$e(C+n) = 2(C+n)^{-1} + C + n + 8$$

$$= 2c^{2} + 4ch + c + 2h^{2} + h + 8$$

$$\frac{e(c+h) - e(c)}{h} = \frac{(2c^{2} + 4hc + c + 2h^{2} + h + 8) - (2(c+1)^{2} + c + 9)}{h}$$

$$= \frac{2h^{2} + 4ch + h}{h}$$

$$= \frac{h(4c + 2h + 1)}{h}$$

$$= 4c + 2h + 1$$

$$\begin{array}{l} e\left(\,c\,\right) = 2\,\,c^2 \,+\,c\,+\,8 \\ e\left(\,c + h\,\right) = 2\,\,\left(\,c \,+\,h\,\right)^{\,2} \,+\,c\,+\,h\,+\,8 \\ = 2\,\,c^2 \,+\,4\,\,c\,\,h\,+\,5\,\,c\,+\,2\,\,h^2 \,+\,5\,\,h\,+\,11 \\ \\ \frac{e\left(\,c + h\,\right) - e\left(\,c\,\right)}{h} = \frac{\left(\,2\,\,c^2 + 4\,h\,\,c + 5\,\,c + 2\,\,h^2 + 5\,\,h + 11\,\right) - \left(\,2\,\,c^2 + c + 8\,\right)}{h} \\ = \frac{2\,h^2 + 4\,c\,\,h + h}{h} \\ = \frac{h\left(\,4\,\,c + 2\,\,h + 1\,\right)}{h} \\ = 4\,\,c\,+\,2\,\,h\,+\,1 \end{array}$$

$$\begin{array}{l} e\left(c\right)=2\;c^{2}+c+8\\ e\left(c+h\right)=2\;\left(c+h\right)^{2}+c+h+8\\ =2\;c^{2}+4\;c\;h+c+2\;h^{2}+h+8\\ \\ \frac{e\left(c+h\right)-e\left(c\right)}{h}=\frac{\left(2\;c^{2}+4\;h\;c+c+2\;h^{2}+h+8\right)-\left(2\;c^{2}+c+8\right)}{h}\\ =\frac{2\;h^{2}+4\;c\;h+h}{h}\\ =\frac{h\left(4\;c+2\;h+1\right)}{h}\\ =4\;c+2\;h+1 \end{array}$$

$$\begin{array}{l} e\left(c\right) = 2\;c^2 + c + 8 \\ e\left(c + h\right) = 2\;\left(c + h\right)^2 + c + h + 8 \\ = 2\;c^2 + 4\;c\;h - 3\;c + 2\;h^2 - 3\;h + 9 \\ \frac{e\left(c + h\right) - e\left(c\right)}{h} = \frac{\left(2\;c^2 + 4\;h\;c + 9\;c + 2\;h^2 + 9\;h + 18\right) - \left(2\;c^2 + c + 8\right)}{h} \\ = \frac{2\;h^2 + 4\;c\;h + h}{h} \\ = \frac{h\left(4\;\left(c + 1\right) + 2\;h + 1\right)}{h} \\ = 4\;c\;+\;2\;h\;+\;1 \end{array}$$

## Solution