1. Which of the following are correct calculations for difference quotient of: $d(v) = 2 v^2 + 8 v + 1$ $d(v) = 2 v^2 + 8 v + 1$ $d(v+h) = 2 (h+v)^2 + 8 (h+v) + 1$

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\begin{split} &d\left(v\right)=2\;v^2+8\;v+1\\ &d\left(v\!+\!h\right)=2\;\left(h+v\right)^2+8\;\left(h+v\right)+1\\ &=2\;h^2+4\;h\;v+8\;h+2\;v^2+8\;v+1\\ &\frac{d\left(v\!+\!h\right)-d\left(v\right)}{h}=\frac{\left(2\;h^2\!+\!4\;v\;h\!+\!8\;h\!+\!2\;v^2\!+\!8\;v\!+\!1\right)-\left(2\;\left(v\!+\!1\right)^2\!+\!8\;\left(v\!+\!1\right)\!+\!1\right)}{h}\\ &=\frac{2\;h^2\!+\!4\;v\;h\!+\!8\;h}{h}\\ &=\frac{h\left(2\;h\!+\!4\;v\!+\!8\right)}{h}\\ &=2\;h+4\;v+8 \end{split}
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$$\begin{split} &d\left(v\right)=2\ v^2+8\ v+1\\ &d\left(v\!+\!h\right)=2\ \left(h+v\right)^2+8\ \left(h+v\right)\ +1\\ &=2\ h^2+4\ h\ v+12\ h+2\ v^2+12\ v+11\\ &\frac{d\left(v\!+\!h\right)-d\left(v\right)}{h}=\frac{\left(2\ h^2\!+\!4\ v\ h\!+\!12\ h\!+\!2\ v^2\!+\!12\ v\!+\!11\right)-\left(2\ v^2\!+\!8\ v\!+\!1\right)}{h}\\ &=\frac{2\ h^2\!+\!4\ v\ h\!+\!8\ h}{h}\\ &=\frac{h\left(2\ h\!+\!4\ v\!+\!8\right)}{h}\\ &=2\ h+4\ v+8 \end{split}$$

$$\begin{split} d\left(v\right) &= 2\ v^2 + 8\ v + 1 \\ d\left(v + h\right) &= 2\ \left(h + v\right)^2 + 8\ \left(h + v\right) + 1 \\ &= 2\ h^2 + 4\ h\ v + 8\ h + 2\ v^2 + 8\ v + 1 \\ \frac{d\left(v + h\right) - d\left(v\right)}{h} &= \frac{\left(2\ h^2 + 4\ v\ h + 8\ h + 2\ v^2 + 8\ v + 1\right) - \left(2\ v^2 + 8\ v + 1\right)}{h} \\ &= \frac{2\ h^2 + 4\ v\ h + 8\ h}{h} \\ &= \frac{h\left(2\ h + 4\ v + 8\right)}{h} \\ &= 2\ h + 4\ v + 8 \end{split}$$

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\begin{split} d\left(v\right) &= 2\ v^2 + 8\ v + 1 \\ d\left(v + h\right) &= 2\ \left(h + v\right)^2 + 8\ \left(h + v\right) + 1 \\ &= 2\ h^2 + 4\ h\ v + 4\ h + 2\ v^2 + 4\ v - 5 \\ \frac{d\left(v + h\right) - d\left(v\right)}{h} &= \frac{\left(2\ h^2 + 4\ v\ h + 16\ h + 2\ v^2 + 16\ v + 25\right) - \left(2\ v^2 + 8\ v + 1\right)}{h} \\ &= \frac{2\ h^2 + 4\ v\ h + 8\ h}{h} \\ &= \frac{h\left(2\ h + 4\ \left(v + 1\right) + 8\right)}{h} \\ &= 2\ h + 4\ v + 8 \end{split}
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Solution