4. Which of the following are correct calculations for difference quotient of: $w(g) = 9 g^2 + 9 g + 5$ $w(g) = 9 g^2 + 9 g + 5$ $w(g+h) = 9 (g+h)^2 + 9 (g+h) + 5$ $-9 g^2 + 18 g h + 9 g + 9 h^2 + 9 h + 5$

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\begin{split} &w\left(g\right) = 9\ g^2 + 9\ g + 5 \\ &w\left(g + h\right) = 9\ \left(g + h\right)^2 + 9\ \left(g + h\right) + 5 \\ &= 9\ g^2 + 18\ g\ h + 9\ g + 9\ h^2 + 9\ h + 5 \\ &\frac{w\left(g + h\right) - w\left(g\right)}{h} = \frac{\left(9\ g^2 + 18\ h\ g + 9\ g + 9\ h^2 + 9\ h + 5\right) - \left(9\ \left(g + 1\right)^2 + 9\ \left(g + 1\right) + 5\right)}{h} \\ &= \frac{9\ h^2 + 18\ g\ h + 9\ h}{h} \\ &= \frac{h\left(18\ g + 9\ h + 9\right)}{h} \\ &= 18\ g + 9\ h + 9 \end{split}
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\begin{split} &w\left(g\right) = 9\ g^{2} + 9\ g + 5 \\ &w\left(g + h\right) = 9\ \left(g + h\right)^{2} + 9\ \left(g + h\right) + 5 \\ &= 9\ g^{2} + 18\ g\ h + 27\ g + 9\ h^{2} + 27\ h + 23 \\ &\frac{w\left(g + h\right) - w\left(g\right)}{h} = \frac{\left(9\ g^{2} + 18\ h\ g + 27\ g + 9\ h^{2} + 27\ h + 23\right) - \left(9\ g^{2} + 9\ g + 5\right)}{h} \\ &= \frac{9\ h^{2} + 18\ g\ h + 9\ h}{h} \\ &= \frac{h\left(18\ g + 9\ h + 9\right)}{h} \\ &= 18\ g + 9\ h + 9 \end{split}
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\begin{split} &w\left(g\right) = 9\ g^{2} + 9\ g + 5 \\ &w\left(g + h\right) = 9\ \left(g + h\right)^{2} + 9\ \left(g + h\right) + 5 \\ &= 9\ g^{2} + 18\ g\ h + 9\ g + 9\ h^{2} + 9\ h + 5 \\ &\frac{w\left(g + h\right) - w\left(g\right)}{h} = \frac{\left(9\ g^{2} + 18\ h\ g + 9\ g + 9\ h^{2} + 9\ h + 5\right) - \left(9\ g^{2} + 9\ g + 5\right)}{h} \\ &= \frac{9\ h^{2} + 18\ g\ h + 9\ h}{h} \\ &= \frac{h\left(18\ g + 9\ h + 9\right)}{h} \\ &= 18\ g + 9\ h + 9 \end{split}
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\begin{split} &w\left(g\right) = 9\ g^2 + 9\ g + 5 \\ &w\left(g + h\right) = 9\ \left(g + h\right)^2 + 9\ \left(g + h\right) + 5 \\ &= 9\ g^2 + 18\ g\ h - 9\ g + 9\ h^2 - 9\ h + 5 \\ &\frac{w\left(g + h\right) - w\left(g\right)}{h} = \frac{\left(9\ g^2 + 18\ h\ g + 45\ g + 9\ h^2 + 45\ h + 59\right) - \left(9\ g^2 + 9\ g + 5\right)}{h} \\ &= \frac{9\ h^2 + 18\ g\ h + 9\ h}{h} \\ &= \frac{h\left(18\ \left(g + 1\right) + 9\ h + 9\right)}{h} \\ &= 18\ g + 9\ h + 9 \end{split}
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Solution