7. Which of the following are correct calculations for difference quotient of:  $w(t) = 3t^2 + 9t + 8$   $w(t) = 3t^2 + 9t + 8$   $w(t+h) = 3(h+t)^2 + 9(h+t) + 8$   $2h^2 = 6h + 9h + 3t^2 = 0 + 8$ 

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\begin{split} &w(t) = 3\ t^2 + 9\ t + 8 \\ &w(t+h) = 3\ (h+t)^2 + 9\ (h+t) + 8 \\ &= 3\ h^2 + 6\ h\ t + 9\ h + 3\ t^2 + 9\ t + 8 \\ &\frac{w(t+h) - w(t)}{h} = \frac{\left(3\ h^2 + 6\ t\ h + 9\ h + 3\ t^2 + 9\ t + 8\right) - \left(3\ (t+1)^2 + 9\ (t+1) + 8\right)}{h} \\ &= \frac{3\ h^2 + 6\ t\ h + 9\ h}{h} \\ &= \frac{3\ h^2 + 6\ t\ h + 9\ h}{h} \\ &= 3\ h + 6\ t + 9 \end{split}
```

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\begin{split} &w\left(t\right)=3\ t^{2}+9\ t+8\\ &w\left(t+h\right)=3\ \left(h+t\right)^{2}+9\ \left(h+t\right)+8\\ &=3\ h^{2}+6\ h\ t+15\ h+3\ t^{2}+15\ t+20\\ &\frac{w\left(t+h\right)-w\left(t\right)}{h}=\frac{\left(3\ h^{2}+6\ t\ h+15\ h+3\ t^{2}+15\ t+20\right)-\left(3\ t^{2}+9\ t+8\right)}{h}\\ &=\frac{3\ h^{2}+6\ t\ h+9}{h}\\ &=\frac{h\left(3\ h+6\ t+9\right)}{h}\\ &=3\ h+6\ t+9 \end{split}
```

```
\begin{split} &w(t) = 3\ t^2 + 9\ t + 8 \\ &w(t+h) = 3\ (h+t)^2 + 9\ (h+t) + 8 \\ &= 3\ h^2 + 6\ h\ t + 9\ h + 3\ t^2 + 9\ t + 8 \\ &\frac{w(t+h) - w(t)}{h} = \frac{\left(3\ h^2 + 6\ t\ h + 9\ h + 3\ t^2 + 9\ t + 8\right) - \left(3\ t^2 + 9\ t + 8\right)}{h} \\ &= \frac{3\ h^2 + 6\ t\ h + 9\ h}{h} \\ &= \frac{h\ (3\ h + 6\ t + 9)}{h} \\ &= 3\ h + 6\ t + 9 \end{split}
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\begin{split} &w(t)=3\ t^2+9\ t+8\\ &w(t+h)=3\ (h+t)^2+9\ (h+t)+8\\ &=3\ h^2+6\ h\ t+3\ h+3\ t^2+3\ t+2\\ &\frac{w(t+h)-w(t)}{h}=\frac{\left(3\ h^2+6\ t\ h+21\ h+3\ t^2+21\ t+38\right)-\left(3\ t^2+9\ t+8\right)}{h}\\ &=\frac{3\ h^2+6\ t\ h+9\ h}{h}\\ &=\frac{h\left(3\ h+6\ (t+1)+9\right)}{h}\\ &=3\ h+6\ t+9 \end{split}
```

## Solution