

3.

It so happens that this function can be simplified as:

$$\begin{aligned}t(j) &= \frac{-64+j^3}{-12-j+j^2} \\&= \frac{(j-4)(j^2+4j+16)}{(j-4)(j+3)} \\&= \frac{j^2+4j+16}{j+3}\end{aligned}$$

To find the vertical asymptote :

$$j+3=0$$

$$j=-3$$

There is a vertical asymptote at $j=-3$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-64+j^3}{-12-j+j^2} = \frac{j^2+4j+16}{j+3} = \frac{13}{j+3} + (j+1)$$

There is an oblique asymptote at $k=j+1$

