

1.

Solution

To find the vertex, we look at the coefficients in the function $e(z) = az^2 + bz + c$ in this equation, $a = 1$ and $b = 9$

The first coordinate of the vertex has the formula: $\frac{-b}{2a}$ now, plugging into formula to get:

$$\frac{-b}{2a} = -\frac{9}{2(1)} = -\frac{9}{2}$$

$$\begin{aligned} \text{The second coordinate of the vertex is } e\left(-\frac{9}{2}\right) &= 1\left(-\frac{9}{2}\right)^2 + 9\left(-\frac{9}{2}\right) - 5 \\ &= -\frac{101}{4} \end{aligned}$$

Therefore, the vertex of the graph of f is $\left(-\frac{9}{2}, -\frac{101}{4}\right)$