5. Which of the following are correct calculations for difference quotient of:  $r(a) = 8 \ a^2 + 4 \ a + 5$   $r(a) = 8 \ a^2 + 4 \ a + 5$   $r(a+h) = 8 \ (a+h)^2 + 4 \ (a+h) + 5$ 

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\begin{split} & r\left(a\right) = 8\;a^2 \,+\, 4\;a \,+\, 5 \\ & r\left(a + h\right) = 8\;\left(a \,+\, h\right)^{\,2} \,+\, 4\;\left(a \,+\, h\right) \,+\, 5 \\ & = 8\;a^2 \,+\, 16\;a\;h \,+\, 4\;a \,+\, 8\;h^2 \,+\, 4\;h \,+\, 5 \\ & \frac{r\left(a + h\right) - r\left(a\right)}{h} = \frac{\left(8\;a^2 + 16\;h\;a + 4\;a + 8\;h^2 + 4\;h + 5\right) - \left(8\;\left(a + 1\right)^{\,2} + 4\;\left(a + 1\right) \,+\, 5\right)}{h} \\ & = \frac{8\;h^2 + 16\;a\;h + 4\;h}{h} \\ & = \frac{h\left(16\;a + 8\;h + 4\right)}{h} \\ & = 16\;a \,+\, 8\;h \,+\, 4 \end{split}
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\begin{split} & r\left(a\right) = 8 \; a^2 \; + \; 4 \; a \; + \; 5 \\ & r\left(a + h\right) = 8 \; \left(a \; + \; h\right)^2 \; + \; 4 \; \left(a \; + \; h\right) \; + \; 5 \\ & = 8 \; a^2 \; + \; 16 \; a \; h \; + \; 20 \; a \; + \; 8 \; h^2 \; + \; 20 \; h \; + \; 17 \\ & \frac{r\left(a + h\right) - r\left(a\right)}{h} = \frac{\left(8 \; a^2 + 16 \; h \; a + \; 20 \; a + \; 8 \; h^2 + \; 20 \; h + \; 17\right) - \left(8 \; a^2 + \; 4 \; a + \; 5\right)}{h} \\ & = \frac{8 \; h^2 + 16 \; a \; h + \; 4 \; h}{h} \\ & = \frac{h \; (16 \; a + \; 8 \; h + \; 4)}{h} \\ & = 16 \; a \; + \; 8 \; h \; + \; 4 \end{split}
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\begin{split} r\left(a\right) &= 8\ a^2 + 4\ a + 5 \\ r\left(a + h\right) &= 8\ \left(a + h\right)^2 + 4\ \left(a + h\right) + 5 \\ &= 8\ a^2 + 16\ a\ h + 4\ a + 8\ h^2 + 4\ h + 5 \\ \frac{r\left(a + h\right) - r\left(a\right)}{h} &= \frac{\left(8\ a^2 + 16\ h\ a + 4\ a + 8\ h^2 + 4\ h + 5\right) - \left(8\ a^2 + 4\ a + 5\right)}{h} \\ &= \frac{8\ h^2 + 16\ a\ h + 4\ h}{h} \\ &= \frac{h\left(16\ a + 8\ h + 4\right)}{h} \\ &= 16\ a + 8\ h + 4 \end{split}
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\begin{split} r\left(a\right) &= 8\ a^2 + 4\ a + 5 \\ r\left(a + h\right) &= 8\ \left(a + h\right)^2 + 4\ \left(a + h\right) + 5 \\ &= 8\ a^2 + 16\ a\ h - 12\ a + 8\ h^2 - 12\ h + 9 \\ &\frac{r\left(a + h\right) - r\left(a\right)}{h} = \frac{\left(8\ a^2 + 16\ h\ a + 36\ a + 8\ h^2 + 36\ h + 45\right) - \left(8\ a^2 + 4\ a + 5\right)}{h} \\ &= \frac{8\ h^2 + 16\ a\ h + 4\ h}{h} \\ &= \frac{h\left(16\ \left(a + 1\right) + 8\ h + 4\right)}{h} \\ &= 16\ a + 8\ h + 4 \end{split}
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## Solution