5. Which of the following are correct calculations for difference quotient of:  $r(w) = 9 \ w^2 + 4 \ w + 9$   $r(w) = 9 \ w^2 + 4 \ w + 9$   $r(w+h) = 9 \ (h+w)^2 + 4 \ (h+w) + 9$ 

```
\begin{split} r\left(w\right) &= 9 \; w^2 \; + \; 4 \; w \; + \; 9 \\ r\left(w + h\right) &= 9 \; \left(h \; + \; w\right)^2 \; + \; 4 \; \left(h \; + \; w\right) \; + \; 9 \\ &= 9 \; h^2 \; + \; 18 \; h \; w \; + \; 4 \; h \; + \; 9 \; w^2 \; + \; 4 \; w \; + \; 9 \\ \frac{r\left(w + h\right) - r\left(w\right)}{h} &= \frac{\left(9 \; h^2 + 18 \; w \; h + \; 4 \; h + \; 9 \; w^2 + \; 4 \; w + \; 9\right) - \left(9 \; \left(w + 1\right)^2 + \; 4 \; \left(w + 1\right) \; + \; 9\right)}{h} \\ &= \frac{9 \; h^2 + 18 \; w \; h + \; 4 \; h}{h} \\ &= \frac{h \; (9 \; h + 18 \; w + \; 4)}{h} \\ &= 9 \; h \; + \; 18 \; w \; + \; 4 \end{split}
```

```
\begin{split} r\left(w\right) &= 9 \; w^2 \; + \; 4 \; w \; + \; 9 \\ r\left(w + h\right) &= 9 \; \left(h \; + \; w\right)^2 \; + \; 4 \; \left(h \; + \; w\right) \; + \; 9 \\ &= 9 \; h^2 \; + \; 18 \; h \; w \; + \; 22 \; h \; + \; 9 \; w^2 \; + \; 22 \; w \; + \; 22 \\ \frac{r\left(w + h\right) \; - r\left(w\right)}{h} &= \frac{\left(9 \; h^2 + 18 \; w \; h + \; 22 \; h + \; 9 \; w^2 + \; 22 \; w + \; 22\right) \; - \left(9 \; w^2 + \; 4 \; w + \; 9\right)}{h} \\ &= \frac{9 \; h^2 + 18 \; w \; h + \; 4 \; h}{h} \\ &= \frac{h \; (9 \; h + \; 18 \; w + \; 4)}{h} \\ &= 9 \; h \; + \; 18 \; w \; + \; 4 \end{split}
```

```
\begin{split} r\left(w\right) &= 9\ w^2 + 4\ w + 9 \\ r\left(w + h\right) &= 9\ \left(h + w\right)^2 + 4\ \left(h + w\right) + 9 \\ &= 9\ h^2 + 18\ h\ w + 4\ h + 9\ w^2 + 4\ w + 9 \\ \frac{r\left(w + h\right) - r\left(w\right)}{h} &= \frac{\left(9\ h^2 + 18\ w\ h + 4\ h + 9\ w^2 + 4\ w + 9\right) - \left(9\ w^2 + 4\ w + 9\right)}{h} \\ &= \frac{9\ h^2 + 18\ w\ h + 4\ h}{h} \\ &= \frac{h\left(9\ h + 18\ w + 4\right)}{h} \\ &= 9\ h + 18\ w + 4 \end{split}
```

```
\begin{split} r\left(w\right) &= 9 \; w^2 \; + \; 4 \; w \; + \; 9 \\ r\left(w + h\right) &= 9 \; \left(h \; + \; w\right)^2 \; + \; 4 \; \left(h \; + \; w\right) \; + \; 9 \\ &= 9 \; h^2 \; + \; 18 \; h \; w \; - \; 14 \; h \; + \; 9 \; w^2 \; - \; 14 \; w \; + \; 14 \\ \frac{r\left(w + h\right) - r\left(w\right)}{h} &= \frac{\left(9 \; h^2 + 18 \; w \; h + \; 40 \; h + \; 9 \; w^2 + \; 40 \; w + \; 53\right) - \left(9 \; w^2 + \; 4 \; w + \; 9\right)}{h} \\ &= \frac{9 \; h^2 + 18 \; w \; h + \; 4 \; h}{h} \\ &= \frac{h \; (9 \; h + \; 18 \; \left(w + 1\right) \; + \; 4)}{h} \\ &= 9 \; h \; + \; 18 \; w \; + \; 4 \end{split}
```

## Solution