

3.

It so happens that this function can be simplified as:

$$\begin{aligned}C(W) &= \frac{-1+W^3}{-1+W^2} \\&= \frac{(W-1)(W^2+W+1)}{(W-1)(W+1)} \\&= \frac{W^2+W+1}{W+1}\end{aligned}$$

To find the vertical asymptote :

$$W+1=0$$

$$W=-1$$

There is a vertical asymptote at  $W=-1$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-1+W^3}{-1+W^2} = \frac{W^2+W+1}{W+1} = \frac{1}{W+1} + W$$

There is an oblique asymptote at  $a=W$

