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6. Which of the following are correct calculations for difference quotient of: p(x) = 5 x^2 + 6 x + 4 p(x) = 5 x^2 + 6 x + 4 p(x+h) = 5 (h+x)^2 + 6 (h+x) + 4 = 5 h^2 + 10 h x + 6 h + 5 x^2 + 6 x + 4 \frac{p(x+h) - p(x)}{h} = \frac{\left(5 h^2 + 10 x h + 6 h + 5 x^2 + 6 x + 4\right) - \left(5 (x+1)^2 + 6 (x+1) + 4\right)}{h}
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\begin{split} p\left(x\right) &= 5 \,\, x^2 \,+\, 6 \,\, x \,+\, 4 \\ p\left(x\!+\!h\right) &= 5 \,\, \left(h \,+\, x\right)^2 \,+\, 6 \,\, \left(h \,+\, x\right) \,\,+\, 4 \\ &= 5 \,\, h^2 \,+\, 10 \,\, h \,\, x \,+\, 16 \,\, h \,+\, 5 \,\, x^2 \,+\, 16 \,\, x \,+\, 15 \\ \frac{p\left(x\!+\!h\right) - p\left(x\right)}{h} &= \frac{\left(5 \,h^2 + 10 \,x \,h + 16 \,h + 5 \,x^2 + 16 \,x + 15\right) - \left(5 \,x^2 + 6 \,x + 4\right)}{h} \\ &= \frac{5 \,h^2 + 10 \,x \,h + 6 \,h}{h} \\ &= \frac{h\left(5 \,h + 10 \,x + 6\right)}{h} \\ &= 5 \,\, h \,+\, 10 \,\, x \,+\, 6 \end{split}
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 $= \frac{5 h^2 + 10 \times h + 6 h}{1}$

_ <u>h (5 h+10 x+6)</u>

=5 h + 10 x + 6

```
\begin{split} p\left(x\right) &= 5 \; x^2 + 6 \; x + 4 \\ p\left(x + h\right) &= 5 \; \left(h + x\right)^2 + 6 \; \left(h + x\right) \; + 4 \\ &= 5 \; h^2 + 10 \; h \; x + 6 \; h + 5 \; x^2 + 6 \; x + 4 \\ &\frac{p\left(x + h\right) - p\left(x\right)}{h} = \frac{\left(5 \; h^2 + 10 \; x \; h + 6 \; h + 5 \; x^2 + 6 \; x + 4\right) - \left(5 \; x^2 + 6 \; x + 4\right)}{h} \\ &= \frac{5 \; h^2 + 10 \; x \; h + 6 \; h}{h} \\ &= \frac{h \; (5 \; h + 10 \; x + 6)}{h} \\ &= 5 \; h \; + \; 10 \; x \; + \; 6 \end{split}
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\begin{split} p(x) &= 5 \ x^2 + 6 \ x + 4 \\ p(x+h) &= 5 \ (h+x)^2 + 6 \ (h+x) + 4 \\ &= 5 \ h^2 + 10 \ h \ x - 4 \ h + 5 \ x^2 - 4 \ x + 3 \\ \frac{p(x+h) - p(x)}{h} &= \frac{\left(5 \ h^2 + 10 \ x \ h + 26 \ h + 5 \ x^2 + 26 \ x + 36\right) - \left(5 \ x^2 + 6 \ x + 4\right)}{h} \\ &= \frac{5 \ h^2 + 10 \ x \ h + 6 \ h}{h} \\ &= \frac{h(5 \ h + 10 \ (x+1) + 6)}{h} \\ &= 5 \ h + 10 \ x + 6 \end{split}
```

Solution