Intercepts of the Quadratic

Given a quadratic $s(w)=a\,w^2+b\,w+c$ compute its discriminant $\triangle$:

$\triangle=\sqrt{b^2-4\,ac}$

Case1: $\triangle>0$

$w_{1,2}=\frac{-b\pm\sqrt{b^2-4\,ac}}{2a}$ computes the w-intercepts of multiplicity 1.

$s(0)=c$ computes the single s-intercept.

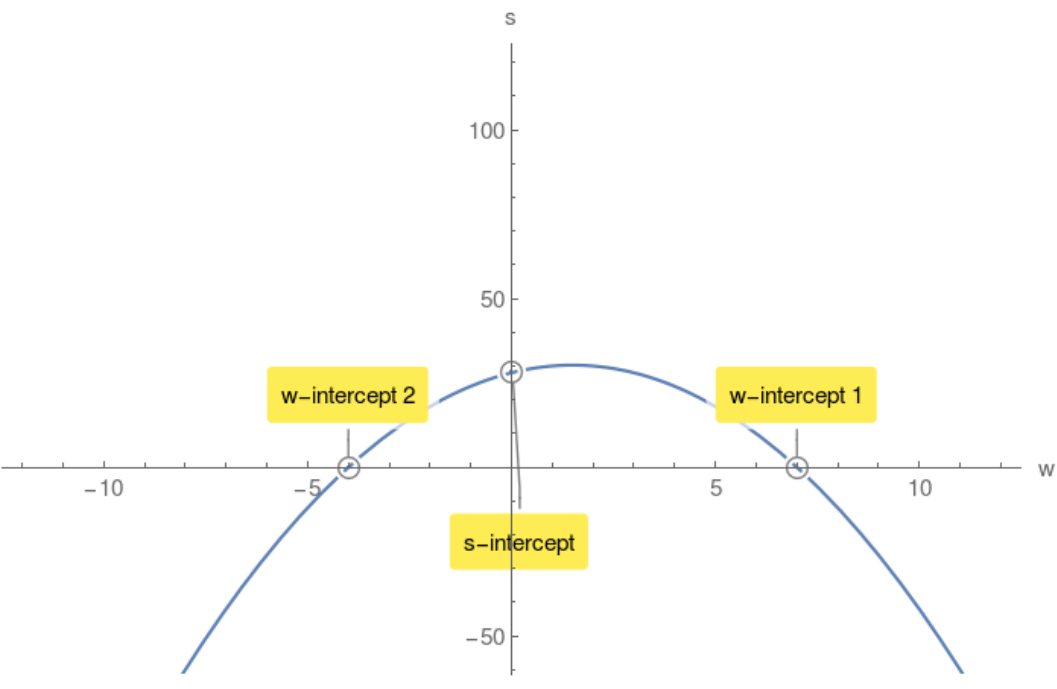
Example 1.

$s(w)=-w^2+3\,w+28$ compute its discriminant $\triangle$:

$\triangle=121>0$

$w_{1,2}=7,-4$

$s(0)=28$ s-intercept.



Case2: $\triangle=0$

$w_{1,2}=\frac{-b\pm\sqrt{b^2-4\,ac}}{2a}=\frac{-b\pm0}{2a}=\frac{-b}{2a}$ single w-intercept of multiplicity 2.

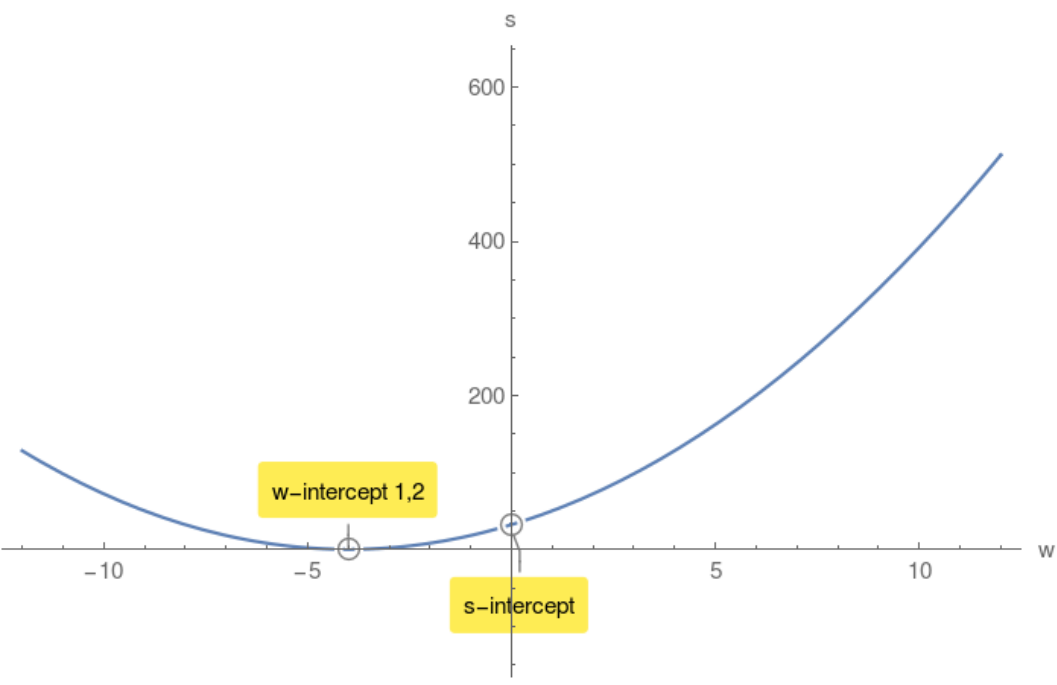
Example 2.

$s(w)=2\,w^2+16\,w+32$ compute its discriminant $\triangle$:

$\triangle=0$

$w_{1,2}=-4,-4$

$s(0)=32$ s-intercept.



Case3: $\triangle<0$

$\sqrt{b^2-4\,ac}$ has no value in Real Numbers. Therefore there are no w-intercepts.

However there is a s-intercept.

Example 3.

$s(w)=4\,w^2-56\,w+245$ compute its discriminant $\triangle$:

$\triangle=-784<0$

$s(0)=245$ s-intercept.