

Intercepts of the Quadratic

Given a quadratic $p(t) = at^2 + bt + c$ compute its discriminant Δ :

$$\Delta = \sqrt{b^2 - 4ac}$$

Case1: $\Delta > 0$

$t_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ computes the t-intercepts of multiplicity 1.
 $p(0) = c$ computes the single p-intercept.

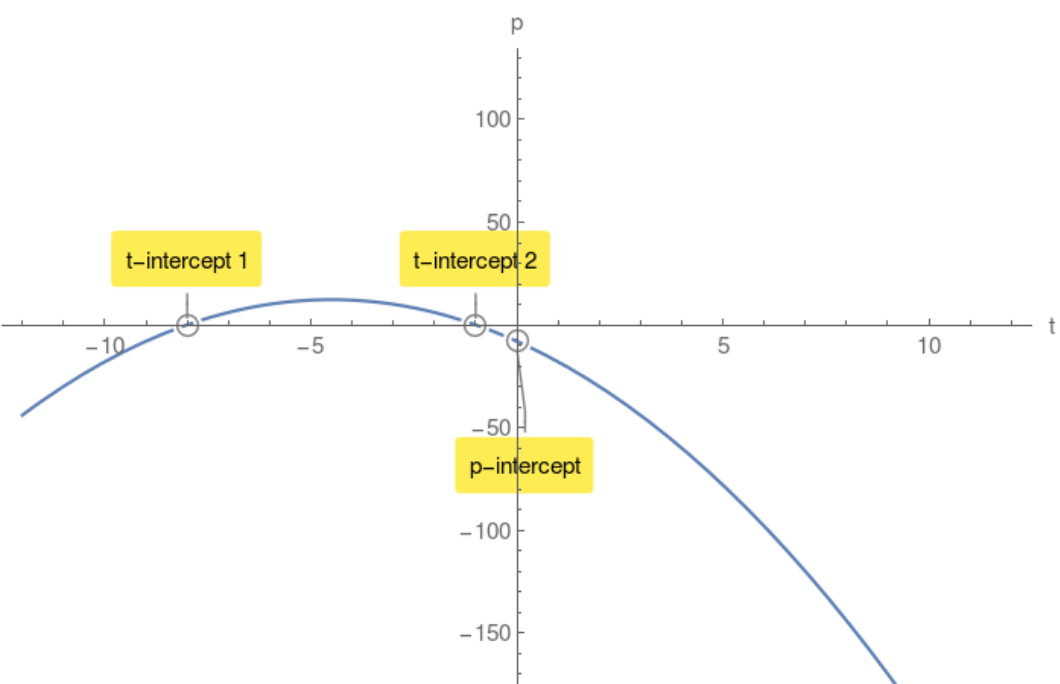
Example 1.

$p(t) = -t^2 - 9t - 8$ compute its discriminant Δ :

$$\Delta = 49 > 0$$

$$t_{1,2} = -8, -1$$

$p(0) = -8$ p-intercept.



Case2: $\Delta = 0$

$t_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-b \pm 0}{2a} = \frac{-b}{2a}$ single t-intercept of multiplicity 2.

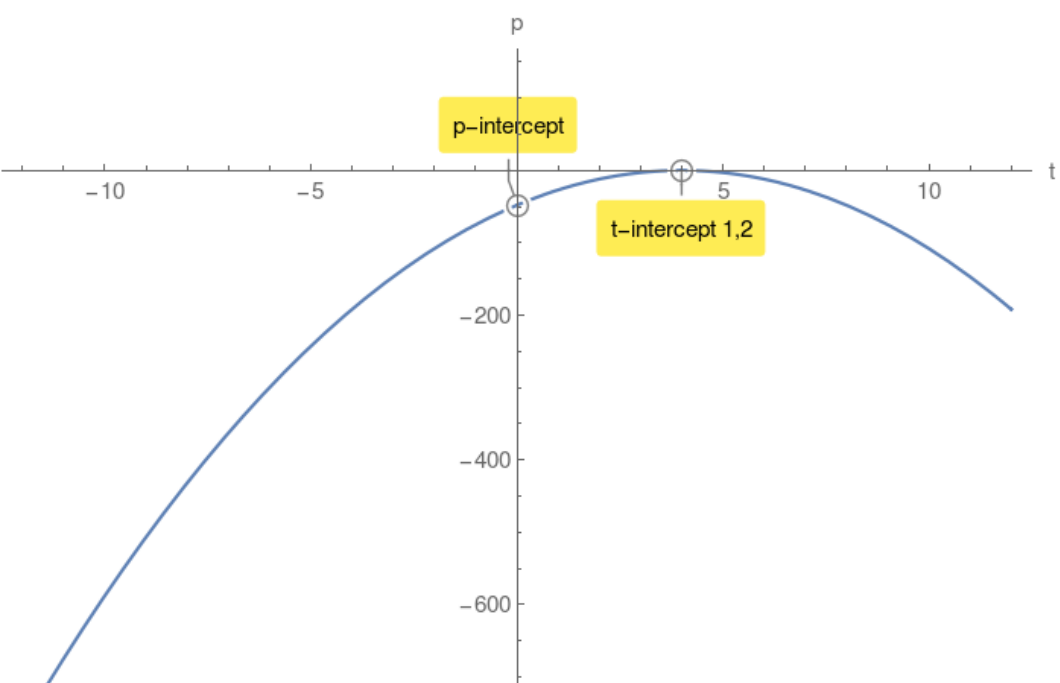
Example 2.

$p(t) = -3t^2 + 24t - 48$ compute its discriminant Δ :

$$\Delta = 0$$

$$t_{1,2} = 4, 4$$

$p(0) = -48$ p-intercept.



Case3: $\Delta < 0$

$\sqrt{b^2 - 4ac}$ has no value in Real Numbers. Therefore there are no t-intercepts.

However there is a p-intercept.

Example 3.

$p(t) = -4t^2 - 80t - 500$ compute its discriminant Δ :

$$\Delta = -1600 < 0$$

$p(0) = -500$ p-intercept.

