

5.

It so happens that this function can be simplified as:

$$\begin{aligned}s(e) &= \frac{-27+e^3}{-6-e+e^2} \\&= \frac{(e-3)(e^2+3e+9)}{(e-3)(e+2)} \\&= \frac{e^2+3e+9}{e+2}\end{aligned}$$

To find the vertical asymptote :

$$e+2=0$$

$$e=-2$$

There is a vertical asymptote at  $e=-2$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3<sup>rd</sup> degree polynomial while the

denominator contains a 2<sup>nd</sup> degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-27+e^3}{-6-e+e^2} = \frac{e^2+3e+9}{e+2} = \frac{7}{e+2} + (e+1)$$

There is an oblique asymptote at  $h=e+1$

