

1.

It so happens that this function can be simplified as:

$$\begin{aligned} z(g) &= \frac{-125+g^3}{-25+g^2} \\ &= \frac{(g-5)(g^2+5g+25)}{(g-5)(g+5)} \\ &= \frac{g^2+5g+25}{g+5} \end{aligned}$$

To find the vertical asymptote :

$$g+5=0$$

$$g=-5$$

There is a vertical asymptote at $g=-5$

To find the horizontal asymptote :

First we must compare the degrees of the polynomials.

The numerator contains a 3rd degree polynomial while the

denominator contains a 2nd degree polynomial.

Since the polynomial in the numerator is a higher degree than the denominator, there is no horizontal asymptote.

To find the oblique asymptote :

$$\text{we must divide the numerator by the denominator } \frac{-125+g^3}{-25+g^2} = \frac{g^2+5g+25}{g+5} = \frac{25}{g+5} + g$$

There is an oblique asymptote at $w=g$

