

3. Given the function $e(b)=b^2+3b$, find an equation of the secant line containing $(1,e(1))$ and $(4,e(4))$. Express the equation in slope-intercept form.

$$d = -12 + 8b$$

$$d = 12 - 8b$$

$$d = -4 + 8b$$

$$d = -3 + \frac{25b}{3}$$

Solution

The line passing through the two points has the slope:

$$\begin{aligned} & \frac{e(4)-e(1)}{4-1} \\ &= \frac{(1(4)^2+3(4))-(1(1)^2+3(1))}{3} \\ &= \frac{28-4}{3} \\ &= 8 \end{aligned}$$

using one of the points, say $(1,4)$ and the slope to get the equation of the secant line:

$$d-4 = 8(b-1)$$

The equation in slope-intercept form:

$$d = -4 + 8b$$