

3.

Solution

Quadratic function: is a function that can be written in the form:

$y(r) = ar^2 + br + c$ where a , b , and c are real numbers and $a \neq 0$

we have $y(r) = -r^2 + 11r + 19$, note: $-r^2 + 11r + 19$ is in ry -plane

Here, we know that $a = -1$, $b = 11$, $c = 19$

Since $a < 0$, we know that the y -coordinate of the vertex is a maximum. However, to find the y -coordinate of our vertex we first need to find the r -coordinate of the vertex by using $r = -\frac{b}{2a} = -\frac{11}{-2} = \frac{11}{2}$ Now that we have the r -coordinate, we can find the y -coordinate

of the vertex by finding $y\left(\frac{11}{2}\right) = -1\left(\frac{11}{2}\right)^2 + 11\left(\frac{11}{2}\right) + 19 = -\frac{121}{4} + \frac{121}{2} + 19 = \frac{197}{4}$ Maximum = $\frac{197}{4}$