

Intercepts of the Quadratic

Given a quadratic $m(u) = a u^2 + b u + c$ compute its discriminant Δ :

$$\Delta = \sqrt{b^2 - 4ac}$$

Case1: $\Delta > 0$

$u_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ computes the u-intercepts of multiplicity 1.

$m(0) = c$ computes the single m-intercept.

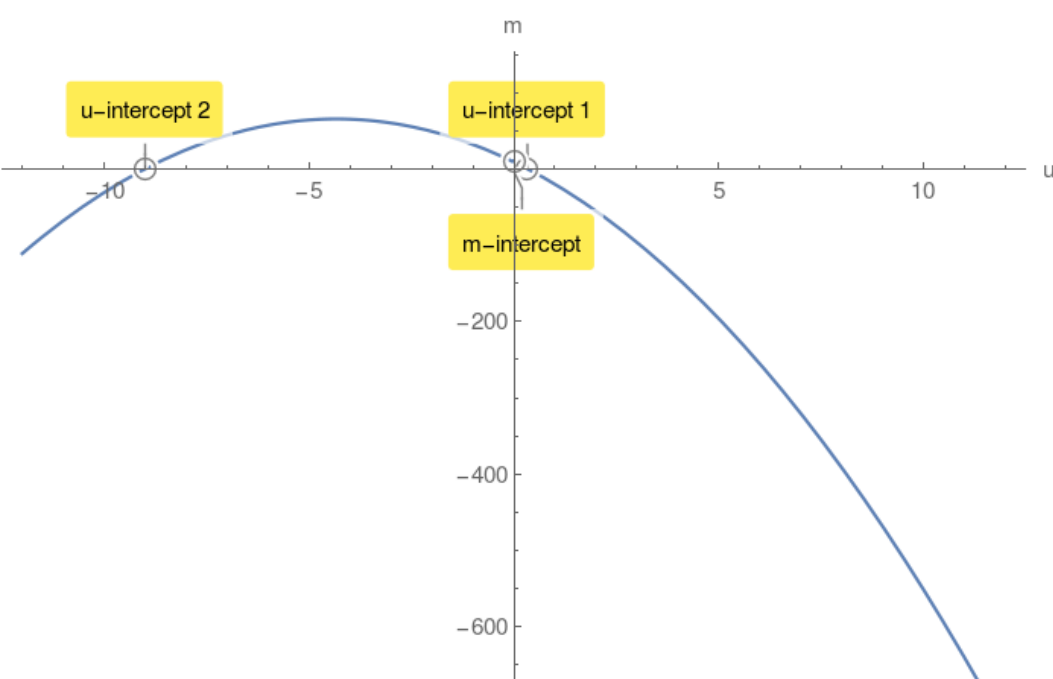
Example 1.

$m(u) = -3u^2 - 26u + 9$ compute its discriminant Δ :

$$\Delta = 784 > 0$$

$$u_{1,2} = \frac{1}{3}, -9$$

$m(0) = 9$ m-intercept.



Case2: $\Delta = 0$

$u_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-b \pm 0}{2a} = \frac{-b}{2a}$ single u-intercept of multiplicity 2.

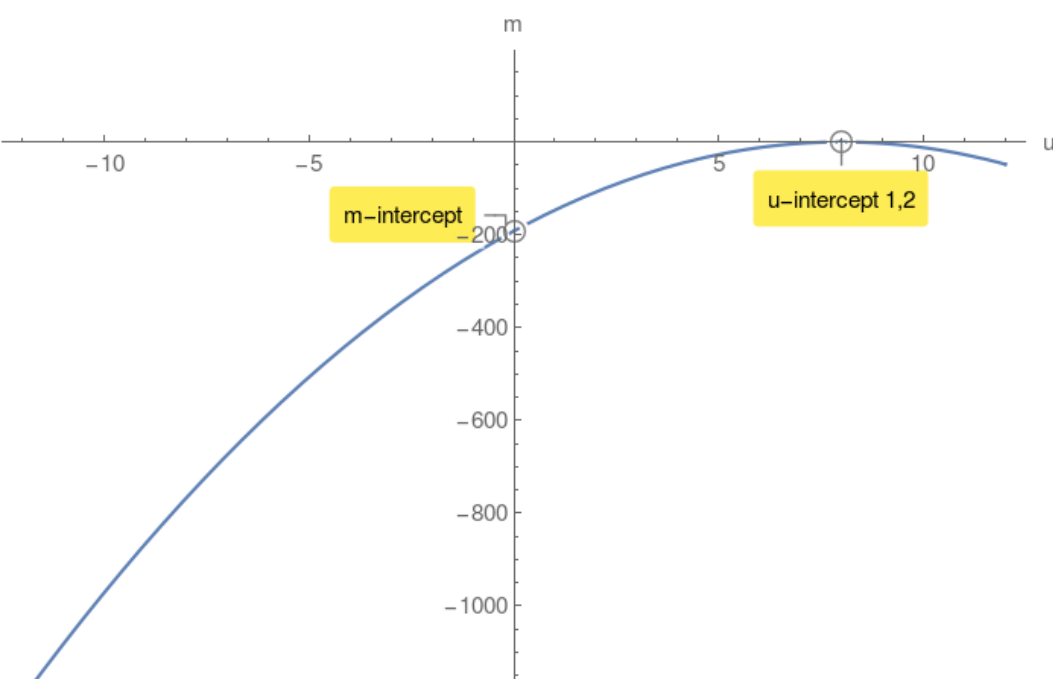
Example 2.

$m(u) = -3u^2 + 48u - 192$ compute its discriminant Δ :

$$\Delta = 0$$

$$u_{1,2} = 8, 8$$

$m(0) = -192$ m-intercept.



Case3: $\Delta < 0$

$\sqrt{b^2 - 4ac}$ has no value in Real Numbers. Therefore there are no u-intercepts.

However there is a m-intercept.

Example 3.

$m(u) = 4u^2 - 80u + 500$ compute its discriminant Δ :

$$\Delta = -1600 < 0$$

$m(0) = 500$ m-intercept.

