2. Which of the following are correct calculations for difference quotient of: $z\left(y\right)=9\;y^2+5\;y+1$ $z\left(y\right)=9\;y^2+5\;y+1$ $z\left(y+h\right)=9\;\left(h+y\right)^2+5\;\left(h+y\right)+1$

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\begin{split} &z\left(y\right)=9\;y^2+5\;y+1\\ &z\left(y+h\right)=9\;\left(h+y\right)^2+5\;\left(h+y\right)+1\\ &=9\;h^2+18\;h\;y+5\;h+9\;y^2+5\;y+1\\ &\frac{z\left(y+h\right)-z\left(y\right)}{h}=\frac{\left(9\;h^2+18\;y\;h+5\;h+9\;y^2+5\;y+1\right)-\left(9\;\left(y+1\right)^2+5\;\left(y+1\right)+1\right)}{h}\\ &=\frac{9\;h^2+18\;y\;h+5\;h}{h}\\ &=\frac{h\left(9\;h+18\;y+5\right)}{h}\\ &=9\;h+18\;y+5 \end{split}
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\begin{split} z &(y) = 9 \ y^2 + 5 \ y + 1 \\ z &(y+h) = 9 \ (h+y)^2 + 5 \ (h+y) + 1 \\ &= 9 \ h^2 + 18 \ h \ y + 23 \ h + 9 \ y^2 + 23 \ y + 15 \\ \frac{z &(y+h) - z &(y)}{h} &= \frac{\left(9 \ h^2 + 18 \ y \ h + 23 \ h + 9 \ y^2 + 23 \ y + 15\right) - \left(9 \ y^2 + 5 \ y + 1\right)}{h} \\ &= \frac{9 \ h^2 + 18 \ y \ h + 5 \ h}{h} \\ &= \frac{h &(9 \ h + 18 \ y + 5)}{h} \\ &= 9 \ h + 18 \ y + 5 \end{split}
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\begin{split} z\left(y\right) &= 9\ y^2 + 5\ y + 1 \\ z\left(y + h\right) &= 9\ \left(h + y\right)^2 + 5\ \left(h + y\right) + 1 \\ &= 9\ h^2 + 18\ h\ y + 5\ h + 9\ y^2 + 5\ y + 1 \\ \frac{z\left(y + h\right) - z\left(y\right)}{h} &= \frac{\left(9\ h^2 + 18\ y\ h + 5\ h + 9\ y^2 + 5\ y + 1\right) - \left(9\ y^2 + 5\ y + 1\right)}{h} \\ &= \frac{9\ h^2 + 18\ y\ h + 5\ h}{h} \\ &= \frac{h\left(9\ h + 18\ y + 5\right)}{h} \\ &= 9\ h + 18\ y + 5 \end{split}
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\begin{split} z &(y) = 9 \ y^2 + 5 \ y + 1 \\ z &(y+h) = 9 \ (h+y)^2 + 5 \ (h+y) + 1 \\ = 9 \ h^2 + 18 \ h \ y - 13 \ h + 9 \ y^2 - 13 \ y + 5 \\ \frac{z \, (y+h) - z \, (y)}{h} &= \frac{\left(9 \ h^2 + 18 \ y \ h + 41 \ h + 9 \ y^2 + 41 \ y + 47\right) - \left(9 \ y^2 + 5 \ y + 1\right)}{h} \\ &= \frac{9 \ h^2 + 18 \ y \ h + 5 \ h}{h} \\ &= \frac{h \, (9 \ h + 18 \ (y+1) + 5)}{h} \\ = 9 \ h + 18 \ y + 5 \end{split}
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Solution