## Comments

I also read through the part on recursions and I thought the recursive definitions of well-formed formulas as n-ary functions taking in n arguments (each of which may be a function applied to its arguments) made a lot of sense.

On the other hand, polish notation without parenthesizing the arguments felt more complicated than the infix notation we have been using thus far. I understand how it reduces ambiguity, but I found it more tasking to process and mentally parse the wffs written in polish notation.

## Questions

In the section about 0-ary connectives, we say that  $\top$  and  $\bot$  can be thought of as the constants T and F having  $\overline{v}(\bot) = F$  and  $\overline{v}(\top) = T$  for every v. Wouldn't we get a contradiction if we have a function that negates v? For instance, if  $w = \neg v$  for some function v, doesn't  $\overline{w}(\bot) = \neg \overline{v}(\bot)$  imply that  $\overline{w}(\bot) = T$ ?

## **Exercises**

1. Let G be the following three-place Boolean function.

$$G(F,F,F)=T,$$
  $G(T,F,F)=T,$   $G(F,F,T)=T,$   $G(F,T,F)=T,$   $G(F,T,T)=F,$   $G(F,T,T)=F,$   $G(T,T,T)=F.$ 

(a) Find a wff using at most the connectives  $\land$ ,  $\lor$ , and  $\neg$ , that realizes G.

 $G(\alpha, \beta, \gamma)$  always disagrees with the majority of  $\alpha, \beta$ , and  $\gamma$ .

That is,

$$G(\alpha, \beta, \gamma) = \neg((\alpha \land \beta) \lor (\alpha \land \gamma) \lor (\beta \land \gamma))$$

(b) Then find such a wff in which connective symbols occur at not more than  $5\ \mathrm{places}.$ 

$$G(\alpha, \beta, \gamma) = \neg(\#\alpha\beta\gamma)$$

Using only  $\land, \lor, \lnot$ :

$$G(\alpha,\beta,\gamma) = \neg (\ (\alpha \wedge (\beta \vee \gamma)) \ \vee \ (\beta \wedge \gamma))$$