



Gradiane Online Accelerated Learning

Zayd

- [Home Page](#)
- [Assignments Due](#)
- [Progress Report](#)
- [Handouts](#)
- [Tutorials](#)
- [Homeworks](#)
- [Lab Projects](#)
- [Log Out](#)

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Based on Sections 7.2, 7.3, and 7.4 of HMU.

Help

1. The intersection of two CFL's need not be a CFL. Identify in the list below a pair of CFL's such that their intersection is not a CFL.

- a) $L_1 = \{aba^n b^n c^n ba \mid n > 0, i > 0\}$
 $L_2 = \{aba^n b^i c^j ba \mid n > 0, i > 0, j > 0\}$
- b) $L_1 = \{aba^i b^n c^i ba \mid n > 0, i > 0\}$
 $L_2 = \{aba^n b^i c^j ba \mid n > 0, i > 0, j > 0\}$
- c) $L_1 = \{aba^n b^n c^i \mid n > 0, i > 0\}$
 $L_2 = \{aba^n b^j c^i \mid n > 0, i > 0, j > 0\}$
- d) $L_1 = \{aba^n b^n c^i ba \mid n > 0, i > 0\}$
 $L_2 = \{aba^n b^i c^i ba \mid n > 0, i > 0\}$

Answer submitted: **d)**

You have answered the question correctly.

Question Explanation:

The incorrect choices fall in two categories: either one of the two given languages is not a CFL, or one is a CFL and the other is a regular language, in which case we know that their intersection is a CFL (see Section 7.3.4 on p. 291).

For the four correct choices the intersections of the two given languages are:

1. $\{a^n b^n c^n \mid n > 0\}$.
2. $\{aba^n b^n c^n \mid n > 0\}$.
3. $\{aba^n b^n c^n ba \mid n > 0\}$.
4. $\{a^n b^n c^n \mid n > 0\}$.

In all cases we can prove the language not to be context-free by using the pumping lemma on a word $a^n b^n c^n$ for sufficiently large n . If we pump any pair of strings (of length much smaller than n) then the balance on the number of a 's, b 's and c 's will be ruined.

2. If h is the homomorphism defined by $h(a) = 0$ and $h(b) = \epsilon$, which of the following strings is in $h^{-1}(000)$?
- a) aabbaa
 - b) babab
 - c) aababb
 - d) abbbabaab

Answer submitted: **c)**

You have answered the question correctly.

Question Explanation:

Since there are three 0's in $h(w)$, w must have exactly three a 's. It can have any number of b 's, since $h(b) = \epsilon$. Of the choices, only aababb has exactly three a 's.

3. G_1 is a context-free grammar with start symbol S_1 , and no other nonterminals whose name begins with "S." Similarly, G_2 is a context-free grammar with start symbol S_2 , and no other nonterminals whose name begins with "S." S_1 and S_2 appear on the right side of no productions. Also, no nonterminal appears in both G_1 and G_2 .

We wish to combine the symbols and productions of G_1 and G_2 to form a new grammar G , whose language is the concatenation of the languages of G_1 and G_2 . The start symbol of G will be S . All productions and symbols of G_1 and G_2 will be symbols and productions of G . Which of the following sets of productions, added to those of G , is guaranteed to make $L(G)$ be $L(G_1)L(G_2)$?

- a) $S \rightarrow S_1 S_1, S_1 \rightarrow S_2$
- b) $S \rightarrow S_1 S_2 S$
- c) $S \rightarrow S_1 S_3, S_3 \rightarrow S_2$
- d) $S \rightarrow S_1, S_1 \rightarrow S_1 S_2$

Answer submitted: **c)**

You have answered the question correctly.

Question Explanation:

Each of the choices involves only S, S_1, S_2 , and in some cases other nonterminals whose names begin with "S" and that therefore are known not to appear in G_1 or G_2 . As a result, we need only to look at the strings involving S_1 and S_2 only, that are

derivable from S , using the new productions. In order for $L(G)$ to be $L(G_1)L(G_2)$, it is necessary and sufficient that the strings involving only symbols S_1 and S_2 that are derived from S using only the additional productions be exactly the one string $\{S_1S_2\}$.

For example, adding $S \rightarrow S_1S_2$ obviously has this property. So does the set of productions

$$S \rightarrow S_1S_3S_2$$

$$S_3 \rightarrow e$$

4. The language $L = \{ss \mid s \text{ is a string of a's and b's}\}$ is not a context-free language. In order to prove that L is not context-free we need to show that for every integer n , there is some string z in L , of length at least n , such that no matter how we break z up as $z = uvwxy$, subject to the constraints $|vwx| \leq n$ and $|vx| > 0$, there is some $i \geq 0$ such that uv^iwx^iy is not in L .

Let us focus on a particular $z = aabaaaba$ and $n = 7$. It turns out that this is the wrong choice of z for $n = 7$, since there are some ways to break z up for which

we can find the desired i , and for others, we cannot. Identify from the list below the choice of u, v, w, x, y for which there is an i that makes uv^iwx^iy not be in L . We show the breakup of $aabaaaba$ by placing four $|$'s among the a's and b's. The resulting five pieces (some of which may be empty), are the five strings. For instance, $aa|b|aaaba|$ means $u=aa$, $v=b$, $w=\epsilon$, $x=aaaba$, and $y=\epsilon$.

- a) $aa|ba|aa|ba|$
- b) $a|ab|aa|ab|a$
- c) $a|a|ba|a|aba$
- d) $a|ab|aaa|b|a$

Answer submitted: **d)**

You have answered the question correctly.

Question Explanation:

In all cases for this problem, $i = 0$ works if anything works. For example one correct choice is $aab|a|a|ba$, where if we remove the second and 4th pieces, we get $aababa$, which is not of the form ss . That is, the first half, aab , is not the same as the second half, and therefore $aababa$ is not in L .

For each of the incorrect choices, the choice explanation gives an argument as to why no "pumping" of v and x will lead to a string whose first half differs from the second half.

5. Apply the CYK algorithm to the input $ababaa$ and the grammar:

$$\begin{array}{lcl} S & \rightarrow & AB \mid BC \\ A & \rightarrow & BA \mid a \\ B & \rightarrow & CC \mid b \\ C & \rightarrow & AB \mid a \end{array}$$

Compute the table of entries X_{ij} = the set of nonterminals that derive positions i through j , inclusive, of the string ababaa. Then, identify a true assertion about one of the X_{ij} 's in the list below.

- a) $X_{15} = \{S, A, C\}$
- b) $X_{16} = \{S, A, C\}$
- c) $X_{15} = \{S, C\}$
- d) $X_{36} = \{S, A, C\}$

Answer submitted: **a)**

You have answered the question correctly.

Question Explanation:

Here is the table:

B					
SAC	SA				
B	B	SA			
B	SC	B	-		
SC	SA	SC	SA	B	
AC	B	AC	B	AC	AC
a	b	a	b	a	a

6. G_1 is a context-free grammar with start symbol S_1 , and no other nonterminals whose name begins with "S." Similarly, G_2 is a context-free grammar with start symbol S_2 , and no other nonterminals whose name begins with "S." S_1 and S_2 appear on the right side of no productions. Also, no nonterminal appears in both G_1 and G_2 .

We wish to combine the symbols and productions of G_1 and G_2 to form a new grammar G , whose language is the union of the languages of G_1 and G_2 . The start symbol of G will be S . All productions and symbols of G_1 and G_2 will be symbols and productions of G . Which of the following sets of productions, added to those of G , is guaranteed to make $L(G)$ be $L(G_1) \cup L(G_2)$?

- a) $S \rightarrow S_3, S_3 \rightarrow S_1 S_2$
- b) $S \rightarrow S_1 S_3, S_3 \rightarrow S_2 \mid \varepsilon$
- c) $S \rightarrow S_1 S_2 \mid S_2 S_1$
- d) $S \rightarrow S_1 S_3 \mid S_2 S_3, S_3 \rightarrow \varepsilon$

Answer submitted: **d)**

You have answered the question correctly.

Question Explanation:

Each of the choices involves only S , S_1 , S_2 , and in some cases other nonterminals whose names begin with "S" and that therefore are known not to appear in G_1 or G_2 . As a result, we need only to look at the strings involving S_1 and S_2 only, that are derivable from S , using the new productions. In order for $L(G)$ to be $L(G_1) \cup L(G_2)$, it is necessary and sufficient that the strings involving only symbols S_1 and S_2 that are derived from S using only the additional productions be exactly the two strings $\{S_1, S_2\}$.

For example, adding $S \rightarrow S_1 \mid S_2$ obviously has this property. So does the set of productions

$$S \rightarrow S_1$$

$$S_1 \rightarrow S_2$$

Note that if S_1 could appear on the right side of productions of G_1 , then this choice would not work --- derivations of G_2 could suddenly appear in the middle of derivations that should be in G_1 only.

$$S \rightarrow S_1 \mid S_3$$

$$S_3 \rightarrow S_2$$