



## Gradiane Online Accelerated Learning

Zayd

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1. Apply the construction in Figure 3.16 (p. 104) and Figure 3.17 (p. 105) to convert the regular expression  $(0+1)^*(0+\epsilon)$  to an epsilon-NFA. Then, identify the true statement about your epsilon-NFA from the list below:
  - a) There are 5 states with more than one arc out.
  - b) There are 14 arcs labeled  $\epsilon$ .
  - c) There are 10 states.
  - d) There are no states with more than one arc in.

[You did not answer this question.](#)

2. The classes of languages P and NP are closed under certain operations, and not closed under others, just like classes such as the regular languages or context-free languages have closure properties. Decide whether P and NP are closed under each of the following operations.
  1. Union.
  2. Intersection.
  3. Intersection with a regular language.
  4. Concatenation.
  5. Kleene closure (star).
  6. Homomorphism.
  7. Inverse homomorphism.

Then, select from the list below the true statement.

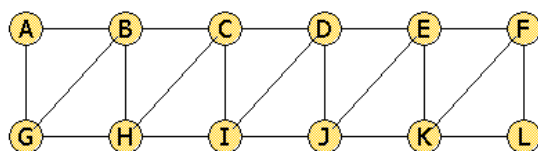
- a) NP is closed under inverse homomorphism.
- b) NP is not closed under Kleene closure.
- c) NP is closed under homomorphism.
- d) NP is not closed under union.

**Answer submitted: b)**

**Your answer is incorrect.**

The definition of the class NP is in Section 10.1.3 (p. 431). Hint: To tell whether input  $w$  is in the closure of  $L$ , start by guessing how to break  $w$  into one or more substrings, each of which is in  $L$ . If we know a bound on the running time of the test for membership in  $L$ , what can we conclude about the running time of the whole process?

3. How large can an independent set be in the graph below?



Identify one of the maximal independent sets below.

- a) {B,E,I,L}
- b) {A,C,E,H,J,L}
- c) {A,D,I,L}
- d) {B,D,F,J,K}

You did not answer this question.

4. The Boolean expression  $wxyz+u+v$  is equivalent to an expression in 3-CNF (a product of clauses, each clause being the sum of exactly three literals). Find the simplest such 3-CNF expression and then identify one of its clauses in the list below. Note:  $-e$  denotes the negation of  $e$ . Also note: we are looking for an expression that involves only  $u, v, w, x, y$ , and  $z$ , no other variables. Not all boolean expressions can be converted to 3-CNF without introducing new variables, but this one can.

- a)  $(u+v+-w)$
- b)  $(w+y+v)$
- c)  $(w+u+v)$
- d)  $(u+v+-y)$

You did not answer this question.

5. Here are seven regular expressions:

- 1.  $(0^*+10^*)^*$
- 2.  $(0+10)^*$
- 3.  $(0^*+10)^*$
- 4.  $(0^*+1^*)^*$
- 5.  $(0+1)^*$
- 6.  $(0+1^*0)^*$
- 7.  $(0+1^*)^*$

Determine the language of each of these expressions. Then, find in the list below a pair of equivalent expressions.

- a)  $(0+1)^*$  and  $(0+1^*)^*$
- b)  $(0+1)^*$  and  $(0^*+10)^*$
- c)  $(0+1)^*$  and  $(0+1^*0)^*$
- d)  $(0+1^*0)^*$  and  $(0+1^*)^*$

You did not answer this question.

6. Consider the descriptions of the following problems:

- 1. Problem  $P_1$ : Given a set  $S$  of positive integers  $\{s_1, s_2, \dots, s_n\}$  and an integer  $C$  as input, is there a subset  $T$  of  $S$  such that the integers in  $T$  add up to  $C$ ?
- 2. Problem  $P_2$ : Given a set  $S$  of positive integers  $\{s_1, s_2, \dots, s_n\}$  as input, is there a subset  $T$  of  $S$  such that the integers in  $T$  add up to  $c_0$ ? Here  $c_0$  is a positive integer constant.
- 3. Problem  $P_3$ : Given an undirected graph  $G$  and an integer  $K$  as input, is there a clique in  $G$  of size  $K$ ?
- 4. Problem  $P_4$ : Given an undirected graph  $G$  as input does  $G$  contain a clique of size  $m$ ? Here  $m$  is a positive integer constant.

Now consider some additional propositions about the above problems (These may be TRUE or FALSE):

1. Proposition  $F_1$ : There is an algorithm  $A_1$  that solves problem  $P_1$  in  $O(nC)$  time.
2. Proposition  $F_2$ : There is an algorithm  $A_2$  that solves problem  $P_2$  in  $O(n)$  time.
3. Proposition  $F_3$ :  $P_3$  is NP-complete.
4. Proposition  $F_4$ : There is an algorithm  $A_3$  that solves problem  $P_4$  in  $O(m^2n^m)$  time.

Choose a correct statement from the choices below:

- a) If  $F_1$  and  $F_2$  are both TRUE,  $P_1$  is in P and  $P_2$  is in P.
- b) If  $F_1$  and  $F_2$  are both TRUE, then  $P_1$  is in P but we cannot conclude so about  $P_2$ .
- c)  $F_4$  must be FALSE. Such an algorithm  $A_3$  cannot exist.
- d)  $P_2$  is reducible to  $P_1$ .

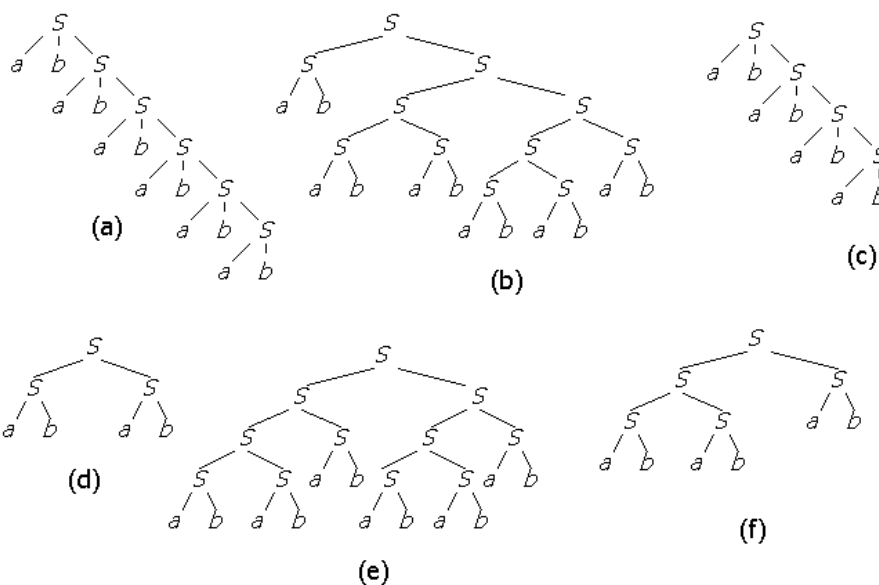
Answer submitted: **b)**

Your answer is incorrect.

Whether something is part of the input or not may make a difference in whether a problem is solvable in polynomial time. The algorithm  $A_1$  will not count as a polynomial time algorithm for problem  $P_1$ , where  $C$  is part of the input. This is because the integer  $C$  requires  $O(\log C)$  bits to encode and is therefore exponential in the size of the input. But algorithm  $A_2$  is a polynomial time algorithm for  $P_2$ .

Some of the issues regarding "size" of inputs are illustrated in Section 10.1.2 (p. 426).

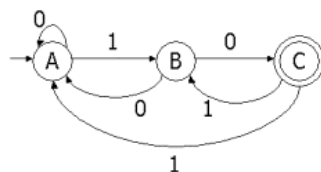
7. Consider the grammar:  $S \rightarrow SS$ ,  $S \rightarrow ab$ . Identify in the list below the one set of parse trees which includes a tree that is NOT a parse tree of this grammar?



- a)  $\{(b),(d)\}$
- b)  $\{(a),(f)\}$
- c)  $\{(b),(f)\}$
- d)  $\{(e)\}$

You did not answer this question.

8. The following nondeterministic finite automaton:



accepts which of the following strings?

- a) 10001010
- b) 0110011
- c) 0110110
- d) 00010111

You did not answer this question.

9. Consider the pushdown automaton with the following transition rules:

1.  $\delta(q, 0, Z_0) = \{(q, XZ_0)\}$
2.  $\delta(q, 0, X) = \{(q, XX)\}$
3.  $\delta(q, 1, X) = \{(q, X)\}$
4.  $\delta(q, \epsilon, X) = \{(p, \epsilon)\}$
5.  $\delta(p, \epsilon, X) = \{(p, \epsilon)\}$
6.  $\delta(p, 1, X) = \{(p, XX)\}$
7.  $\delta(p, 1, Z_0) = \{(p, \epsilon)\}$

From the ID  $(p, 1101, XXZ_0)$ , which of the following ID's can NOT be reached?

- a)  $(q, 01, XXZ_0)$
- b)  $(p, 01, XZ_0)$
- c)  $(p, 01, XXXZ_0)$
- d)  $(p, 1101, XZ_0)$

You did not answer this question.

10. Here is a context-free grammar G:

$S \rightarrow AB$   
 $A \rightarrow 0A1 \mid 2$   
 $B \rightarrow 1B \mid 3A$

Which of the following strings is in  $L(G)$ ?

- a) 002111300211
- b) 0021113002111
- c) 0021131100211
- d) 00021132

You did not answer this question.

11. Here is a context-free grammar:

$S \rightarrow AB \mid CD$   
 $A \rightarrow BG \mid 0$   
 $B \rightarrow AD \mid \epsilon$   
 $C \rightarrow CD \mid 1$   
 $D \rightarrow BB \mid E$   
 $E \rightarrow AF \mid B1$   
 $F \rightarrow EG \mid 0C$   
 $G \rightarrow AG \mid BD$

Find all the nullable symbols (those that derive  $\epsilon$  in one or more steps). Then, identify the true statement from the list below.

- a) C is nullable.

- b) A is nullable.
- c) B is not nullable.
- d) G is not nullable.

You did not answer this question.

12. Consider the grammars:

$G_1: S \rightarrow AB \mid a \mid abC, A \rightarrow b, C \rightarrow abC \mid c$

$G_2: S \rightarrow a \mid b \mid cC, C \rightarrow cC \mid c$

These grammars do not define the same language. To prove, we use a string that is generated by one but not by the other grammar. Which of the following strings can be used for this proof?

- a) cabaca
- b) ababccc
- c) abac
- d) ccc

You did not answer this question.

13. Let  $L_1$  and  $L_2$  be two languages produced by grammars of a certain type. Let  $L$  be the language which is the concatenation of  $L_1$  and  $L_2$ . We want to tell for various types of grammars that produce  $L_1$  and  $L_2$  what type is the concatenation  $L$ . Choose the triple  $(type_1, type_2, type_3)$  so that when the grammar that produces the language  $L_1$  is of type<sub>1</sub> and the grammar that produces the language  $L_2$  is of type<sub>2</sub>, then the grammar that produces the concatenation language  $L$  may not be of type<sub>3</sub>.

Note: A *linear grammar* is a context-free grammar in which no production body has more than one occurrence of one variable. For example,  $A \rightarrow 0B1$  or  $A \rightarrow 001$  could be productions of a linear grammar, but  $A \rightarrow BB$  or  $A \rightarrow A0B$  could not. A *linear language* is a language that has at least one linear grammar.

- a) (regular, regular, context-free)
- b) (regular, regular, linear)
- c) (linear, regular, regular)
- d) (context-free, context-free, context-free)

You did not answer this question.

14. If  $h$  is the homomorphism defined by  $h(a) = 0$  and  $h(b) = \varepsilon$ , which of the following strings is in  $h^{-1}(000)$ ?

- a) abbabaab
- b) babab
- c) abbbabaab
- d) baabba

You did not answer this question.

15. For the purpose of this question, we assume that all languages are over input alphabet  $\{0,1\}$ . Also, we assume that a Turing machine can have any fixed number of tapes.

Sometimes restricting what a Turing machine can do does not affect the class of languages that can be recognized --- the restricted Turing machines can still be designed to accept any recursively enumerable language. Other restrictions limit what languages the Turing machine can accept. For example, it might limit the languages to some subset of the recursive languages, which we know is smaller than the recursively enumerable languages. Here are some of the possible restrictions:

1. Limit the number of states the TM may have.
2. Limit the number of tape symbols the TM may have.
3. Limit the number of times any tape cell may change.

4. Limit the amount of tape the TM may use.
5. Limit the number of moves the TM may make.
6. Limit the way the tape heads may move.

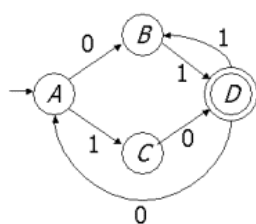
Consider the effect of limitations of these types, perhaps in pairs. Then, from the list below, identify the combination of restrictions that allows the restricted form of Turing machine to accept all recursively enumerable languages.

- a) Allow the TM to use only  $n^2$  tape cells when the input is of length  $n$ .
- b) Limit the number of states to 1,000,000 and the number of tape symbols to 1,000,000.
- c) Allow tape heads to move only right or remain stationary on their tape.
- d) Allow the TM to run for only  $n^{10}$  moves when the input is of length  $n$ .

Answer submitted: **b)**

You have answered the question correctly.

16. The finite automaton below:



accepts no word of length zero, no word of length one, and only two words of length two (01 and 10). There is a fairly simple recurrence equation for the number  $N(k)$  of words of length  $k$  that this automaton accepts. Discover this recurrence and demonstrate your understanding by identifying the correct value of  $N(k)$  for some particular  $k$ . Note: the recurrence does not have an easy-to-use closed form, so you will have to compute the first few values by hand. You do not have to compute  $N(k)$  for any  $k$  greater than 14.

- a)  $N(11) = 32$
- b)  $N(12) = 10$
- c)  $N(12) = 1366$
- d)  $N(13) = 16$

You did not answer this question.

17. Apply the CYK algorithm to the input ababaa and the grammar:

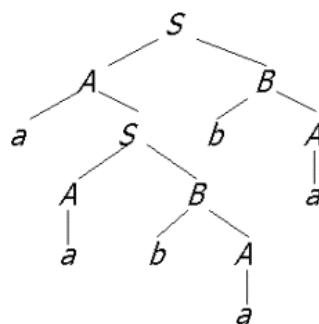
$S \rightarrow AB \mid BC$   
 $A \rightarrow BA \mid a$   
 $B \rightarrow CC \mid b$   
 $C \rightarrow AB \mid a$

Compute the table of entries  $X_{ij}$  = the set of nonterminals that derive positions  $i$  through  $j$ , inclusive, of the string ababaa. Then, identify a true assertion about one of the  $X_{ij}$ 's in the list below.

- a)  $X_{36} = \{S, A, C\}$
- b)  $X_{36} = \{S, A\}$
- c)  $X_{26} = \{B\}$
- d)  $X_{34} = \{S\}$

You did not answer this question.

18. The parse tree below represents a rightmost derivation according to the grammar  $S \rightarrow AB$ ,  $A \rightarrow aS \mid a$ ,  $B \rightarrow bA$ .



Which of the following is a right-sentential form in this derivation?

- a) aaBB
- b) aabAba
- c) Aba
- d) aABbA

You did not answer this question.

19. Design the minimum-state DFA that accepts all and only the strings of 0's and 1's that have 110 as a substring. To verify that you have designed the correct automaton, we will ask you to identify the true statement in a list of choices. These choices will involve:

- 1. The number of *loops* (transitions from a state to itself).
- 2. The number of transitions into a state (including loops) on input 1.
- 3. The number of transitions into a state (including loops) on input 0.

Count the number of transitions into each of your states ("in-transitions") on input 1 and also on input 0. Count the number of loops on input 1 and on input 0. Then, find the true statement in the following list.

- a) There is one loop on input 0 and two loops on input 1.
- b) There are no states that have two in-transitions on input 1.
- c) There are three states that have one in-transition on input 1.
- d) There are two states that have two in-transitions on input 0.

You did not answer this question.

20. The Turing machine M has:

- States q and p; q is the start state.
- Tape symbols 0, 1, and B; 0 and 1 are input symbols, and B is the blank.
- The following next-move function:

State	Tape	Move
	Symbol	
q	0	(q,0,R)
q	1	(p,0,R)
q	B	(q,B,R)
p	0	(q,0,L)
p	1	none (halt)
p	B	(q,0,L)

Your problem is to describe the property of an input string that makes M halt. Identify a string that makes M halt from the list below.

- a) 001010
- b) 010001
- c) 1001
- d) 0011

You did not answer this question.

21. Here are eight simple grammars, each of which generates an infinite language of strings. These strings tend to look like alternating *a*'s and *b*'s, although there are some exceptions, and not all grammars generate all such strings.

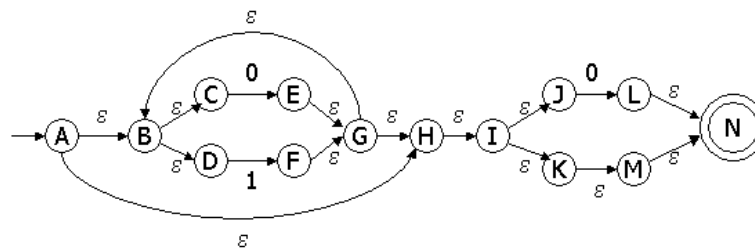
- 1.  $S \rightarrow abS \mid ab$
- 2.  $S \rightarrow SS \mid ab$
- 3.  $S \rightarrow aB; B \rightarrow bS \mid a$
- 4.  $S \rightarrow aB; B \rightarrow bS \mid b$
- 5.  $S \rightarrow aB; B \rightarrow bS \mid ab$
- 6.  $S \rightarrow aB \mid b; B \rightarrow bS$
- 7.  $S \rightarrow aB \mid a; B \rightarrow bS$
- 8.  $S \rightarrow aB \mid ab; B \rightarrow bS$

The initial symbol is *S* in all cases. Determine the language of each of these grammars. Then, find, in the list below, the pair of grammars that define the same language.

- a) G1:  $S \rightarrow abS, S \rightarrow ab$   
G2:  $S \rightarrow aB, B \rightarrow bS, B \rightarrow ab$
- b) G1:  $S \rightarrow aB, B \rightarrow bS, B \rightarrow b$   
G2:  $S \rightarrow aB, B \rightarrow bS, S \rightarrow a$
- c) G1:  $S \rightarrow SS, S \rightarrow ab$   
G2:  $S \rightarrow aB, B \rightarrow bS, B \rightarrow b$
- d) G1:  $S \rightarrow abS, S \rightarrow ab$   
G2:  $S \rightarrow aB, B \rightarrow bS, S \rightarrow a$

You did not answer this question.

22. Here is an epsilon-NFA:



Suppose we construct an equivalent DFA by the construction of Section 2.5.5 (p. 77). That is, start with the epsilon-closure of the start state *A*. For each set of states *S* we construct (which becomes one state of the DFA), look at the transitions from this set of states on input symbol 0. See where those transitions lead, and take the union of the epsilon-closures of all the states reached on 0. This set of states becomes a state of the DFA. Do the same for the transitions out of *S* on input 1. When we have found all the sets of epsilon-NFA states that are constructed in this way, we have the DFA and its transitions.

Carry out this construction of a DFA, and identify one of the states of this DFA (as a subset of the epsilon-NFA's states) from the list below.

- a) IJKMN
- b) BCDEGHIJKMN



- c) BCDFGHIJKMN
- d) ABCD

You did not answer this question.

23. Consider the grammar G with start symbol S:

$S \rightarrow bS \mid aA \mid b$   
 $A \rightarrow bA \mid aB$   
 $B \rightarrow bB \mid aS \mid a$

Which of the following is a word in  $L(G)$ ?

- a) ababbbbbbbbbbb
- b) ababba
- c) babbbbaaab
- d) bababaababaa

You did not answer this question.

24. Identify from the list below the regular expression that generates all and only the strings over alphabet  $\{0,1\}$  that end in 1.

- a)  $(0^?+1^+)^*1$
- b)  $(0+1)^*1^+1$
- c)  $(0^+1^+)^*1$
- d)  $(0^*+1)^*$

Answer submitted: a)

You have answered the question correctly.

25. Which of the following pairs of grammars define the same language?

- a)  $G_1: S \rightarrow AB|a, A \rightarrow b$   
 $G_2: S \rightarrow a|b$
- b)  $G_1: S \rightarrow AB, A \rightarrow aAA|\epsilon, B \rightarrow baBB|\epsilon$   
 $G_2: S \rightarrow CB|B|\epsilon, C \rightarrow aCC|aC|a, B \rightarrow baBB|baB|ba$
- c)  $G_1: S \rightarrow SaScSaS|\epsilon$   
 $G_2: S \rightarrow SaBaS|\epsilon, B \rightarrow ScS$
- d)  $G_1: S \rightarrow SaScSa|aca|\epsilon$   
 $G_2: S \rightarrow SaSAaS|aca, A \rightarrow cS|\epsilon$

You did not answer this question.