



Gradiance Online Accelerated Learning

Zayd

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Submission number: 87811
Submission certificate: GA947111
Submission time: 2014-05-17 18:07:13 PST (GMT - 8:00)

Number of questions: 25
Positive points per question: 4.0
Negative points per question: 0.0
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1. Consider the descriptions of the following problems:

1. Problem P_1 : Given a set S of positive integers $\{s_1, s_2, \dots, s_n\}$ and an integer C as input, is there a subset T of S such that the integers in T add up to C ?
2. Problem P_2 : Given a set S of positive integers $\{s_1, s_2, \dots, s_n\}$ as input, is there a subset T of S such that the integers in T add up to c_0 ? Here c_0 is a positive integer constant.
3. Problem P_3 : Given an undirected graph G and an integer K as input, is there a clique in G of size K ?
4. Problem P_4 : Given an undirected graph G as input does G contain a clique of size m ? Here m is a positive integer constant.

Now consider some additional propositions about the above problems (These may be TRUE or FALSE):

1. Proposition F_1 : There is an algorithm A_1 that solves problem P_1 in $O(nC)$ time.
2. Proposition F_2 : There is an algorithm A_2 that solves problem P_2 in $O(n)$ time.
3. Proposition F_3 : P_3 is NP-complete.
4. Proposition F_4 : There is an algorithm A_3 that solves problem P_4 in $O(m^2n^m)$ time.

Choose a correct statement from the choices below:

- a) F_1 must be FALSE. Such an algorithm A_1 cannot exist.
- b) F_4 must be FALSE. Such an algorithm A_3 cannot exist.
- c) P_2 is reducible to P_1 .
- d) If F_1 and F_2 are both TRUE, then P_1 is in P but we cannot conclude so about P_2 .

Answer submitted: **c)**

You have answered the question correctly.

2. If h is the homomorphism defined by $h(a) = 0$ and $h(b) = \epsilon$, which of the following strings is in $h^{-1}(000)$?
 - a) abbbabaab
 - b) baabbbabb
 - c) babab
 - d) abbba

Answer submitted: **b)**

You have answered the question correctly.

3. Let L_1 and L_2 be two languages produced by grammars of a certain type. Let L be the language which is the concatenation of L_1 and L_2 . We want to tell for various types of grammars that produce L_1 and L_2 what type is the concatenation L . Choose the triple $(\text{type}_1, \text{type}_2, \text{type}_3)$ so that when the grammar that produces the language L_1 is of type₁ and the grammar that produces the language L_2 is of type₂, then the grammar that produces the concatenation language L may not be of type₃.

Note: A *linear grammar* is a context-free grammar in which no production body has more than one occurrence of one variable. For example, $A \rightarrow 0B1$ or $A \rightarrow 001$ could be productions of a linear grammar, but $A \rightarrow BB$ or $A \rightarrow A0B$ could not. A *linear language* is a language that has at least one linear grammar.

- a) (regular, context-free, context-free)
- b) (linear, linear, linear)
- c) (linear, regular, context-free)
- d) (linear, regular, linear)

Answer submitted: **b)**

You have answered the question correctly.

4. Here are eight simple grammars, each of which generates an infinite language of strings. These strings tend to look like alternating a 's and b 's, although there are some exceptions, and not all grammars generate all such strings.

- 1. $S \rightarrow abS \mid ab$
- 2. $S \rightarrow SS \mid ab$
- 3. $S \rightarrow aB; B \rightarrow bS \mid a$
- 4. $S \rightarrow aB; B \rightarrow bS \mid b$
- 5. $S \rightarrow aB; B \rightarrow bS \mid ab$
- 6. $S \rightarrow aB \mid b; B \rightarrow bS$
- 7. $S \rightarrow aB \mid a; B \rightarrow bS$
- 8. $S \rightarrow aB \mid ab; B \rightarrow bS$

The initial symbol is S in all cases. Determine the language of each of these grammars. Then, find, in the list below, the pair of grammars that define the same language.

- a) G1: $S \rightarrow abS, S \rightarrow ab$
G2: $S \rightarrow SS, S \rightarrow ab$
- b) G1: $S \rightarrow aB, B \rightarrow bS, B \rightarrow b$
G2: $S \rightarrow aB, B \rightarrow bS, S \rightarrow a$
- c) G1: $S \rightarrow aB, B \rightarrow bS, B \rightarrow ab$
G2: $S \rightarrow SS, S \rightarrow ab$
- d) G1: $S \rightarrow abS, S \rightarrow ab$
G2: $S \rightarrow aB, B \rightarrow bS, S \rightarrow a$

Answer submitted: **a)**

You have answered the question correctly.

5. Apply the CYK algorithm to the input ababaa and the grammar:

$S \rightarrow AB \mid BC$
 $A \rightarrow BA \mid a$
 $B \rightarrow CC \mid b$
 $C \rightarrow AB \mid a$

Compute the table of entries X_{ij} = the set of nonterminals that derive positions i through j , inclusive, of the string ababaa. Then, identify a true assertion about one of the X_{ij} 's in the list below.

- a) $X_{15} = \{S, C\}$
- b) $X_{25} = \{A\}$
- c) $X_{36} = \{S, A, C\}$
- d) $X_{16} = \{B\}$

Answer submitted: **d)**

You have answered the question correctly.

6. The classes of languages P and NP are closed under certain operations, and not closed under others, just like classes such as the regular languages or context-free languages have closure properties. Decide whether P and NP are closed under each of the following operations.

1. Union.
2. Intersection.
3. Intersection with a regular language.
4. Concatenation.
5. Kleene closure (star).
6. Homomorphism.
7. Inverse homomorphism.

Then, select from the list below the true statement.

- a) P is not closed under intersection with a regular language.
- b) P is not closed under homomorphism.
- c) P is closed under homomorphism.
- d) NP is not closed under union.

Answer submitted: **b)**

You have answered the question correctly.

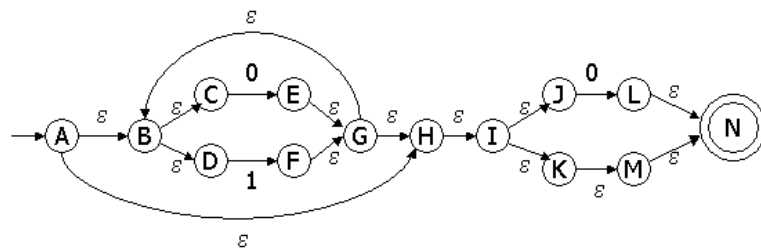
7. Which of the following pairs of grammars define the same language?

- a) $G_1: S \rightarrow SaScSa|aca|\epsilon$
 $G_2: S \rightarrow SaSAaS|aca, A \rightarrow cS|\epsilon$
- b) $G_1: S \rightarrow AB, A \rightarrow aAA|\epsilon, B \rightarrow baB|\epsilon$
 $G_2: S \rightarrow CB|C|B, C \rightarrow aCC|aC|a, B \rightarrow baBB|baB|ba$
- c) $G_1: S \rightarrow AB|a, A \rightarrow b$
 $G_2: S \rightarrow a|b$
- d) $G_1: S \rightarrow AB|a, A \rightarrow b$
 $G_2: S \rightarrow a$

Answer submitted: **d)**

You have answered the question correctly.

8. Here is an epsilon-NFA:



Suppose we construct an equivalent DFA by the construction of Section 2.5.5 (p. 77). That is, start with the epsilon-closure of the start state A. For each set of states S we construct (which becomes one state of the DFA), look at the transitions from this set of states on input symbol 0. See where those transitions lead, and take the union of the epsilon-closures of all the states reached on 0. This set of states becomes a state of the DFA. Do the same for the transitions out of S on input 1. When we have found all the sets of epsilon-NFA states that are constructed in this way, we have the DFA and its transitions.

Carry out this construction of a DFA, and identify one of the states of this DFA (as a subset of the epsilon-NFA's states) from the list below.

- BCDFGHIJKMN
- BCDGHIIJKMN
- LN
- IJKMN

Answer submitted: **a)**

You have answered the question correctly.

9. Here are seven regular expressions:

- $(0^*+10^*)^*$
- $(0+10)^*$
- $(0^*+10)^*$
- $(0^*+1^*)^*$
- $(0+1)^*$
- $(0+1^*0)^*$
- $(0+1^*)^*$

Determine the language of each of these expressions. Then, find in the list below a pair of equivalent expressions.

- $(0^*+10^*)^*$ and $(0^*+10)^*$
- $(0+1)^*$ and $(0+10)^*$
- $(0+10)^*$ and $(0+1^*)^*$
- $(0+1)^*$ and $(0+1^*)^*$

Answer submitted: **d)**

You have answered the question correctly.

10. The Turing machine M has:

- States q and p; q is the start state.
- Tape symbols 0, 1, and B; 0 and 1 are input symbols, and B is the blank.
- The following next-move function:

State	Tape	Move
	Symbol	
q	0	(q,0,R)
q	1	(p,0,R)
q	B	(q,B,R)
p	0	(q,0,L)
p	1	none (halt)
p	B	(q,0,L)

Your problem is to describe the property of an input string that makes M halt. Identify a string that makes M halt from the list below.

- 00100
- 1010
- 0011
- 00001

Answer submitted: **c)**

You have answered the question correctly.

11. Here is a context-free grammar G:

$S \rightarrow AB$
 $A \rightarrow 0A1 \mid 2$
 $B \rightarrow 1B \mid 3A$

Which of the following strings is in $L(G)$?

- a) 00211100211
- b) 002111300211
- c) 00021132
- d) 0002111112

Answer submitted: **b)**

You have answered the question correctly.

12. Apply the construction in Figure 3.16 (p. 104) and Figure 3.17 (p. 105) to convert the regular expression $(0+1)^*(0+\epsilon)$ to an epsilon-NFA. Then, identify the true statement about your epsilon-NFA from the list below:

- a) There are no states with more than one arc in.
- b) There are 16 states.
- c) There are 4 states with more than one arc in.
- d) There are 12 arcs labeled ϵ .

Answer submitted: **c)**

You have answered the question correctly.

13. Design the minimum-state DFA that accepts all and only the strings of 0's and 1's that have 110 as a substring. To verify that you have designed the correct automaton, we will ask you to identify the true statement in a list of choices. These choices will involve:

- 1. The number of *loops* (transitions from a state to itself).
- 2. The number of transitions into a state (including loops) on input 1.
- 3. The number of transitions into a state (including loops) on input 0.

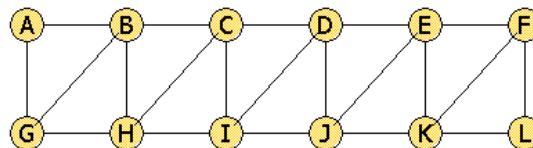
Count the number of transitions into each of your states ("in-transitions") on input 1 and also on input 0. Count the number of loops on input 1 and on input 0. Then, find the true statement in the following list.

- a) There is one state that has no in-transitions on input 0.
- b) There is one state that has one in-transition on input 0.
- c) There are no states that have two in-transitions on input 1.
- d) There are two states that have two in-transitions on input 0.

Answer submitted: **d)**

You have answered the question correctly.

14. How large can an independent set be in the graph below?



Identify one of the maximal independent sets below.

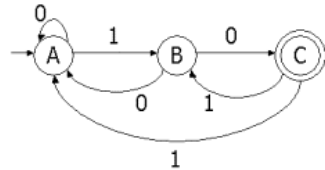
- a) $\{A, D, F, H\}$
- b) $\{A, D, I, L\}$
- c) $\{A, C, H, J, L\}$

d) {B,D,F}

Answer submitted: a)

You have answered the question correctly.

15. The following nondeterministic finite automaton:



accepts which of the following strings?

- a) 10001010
- b) 1100101
- c) 0110011
- d) 0110110

Answer submitted: a)

You have answered the question correctly.

16. For the purpose of this question, we assume that all languages are over input alphabet $\{0,1\}$. Also, we assume that a Turing machine can have any fixed number of tapes.

Sometimes restricting what a Turing machine can do does not affect the class of languages that can be recognized --- the restricted Turing machines can still be designed to accept any recursively enumerable language. Other restrictions limit what languages the Turing machine can accept. For example, it might limit the languages to some subset of the recursive languages, which we know is smaller than the recursively enumerable languages. Here are some of the possible restrictions:

1. Limit the number of states the TM may have.
2. Limit the number of tape symbols the TM may have.
3. Limit the number of times any tape cell may change.
4. Limit the amount of tape the TM may use.
5. Limit the number of moves the TM may make.
6. Limit the way the tape heads may move.

Consider the effect of limitations of these types, perhaps in pairs. Then, from the list below, identify the combination of restrictions that allows the restricted form of Turing machine to accept all recursively enumerable languages.

- a) Allow only two input symbols, 0 and 1, and one other tape symbol, B.
- b) Allow the TM to use only n^2 tape cells when the input is of length n .
- c) Allow the TM to use only 2^n tape cells when the input is of length n .
- d) Allow the TM to run for only n^2 moves when the input is of length n .

Answer submitted: a)

You have answered the question correctly.

17. Consider the pushdown automaton with the following transition rules:

1. $\delta(q, 0, Z_0) = \{(q, XZ_0)\}$
2. $\delta(q, 0, X) = \{(q, XX)\}$
3. $\delta(q, 1, X) = \{(q, X)\}$
4. $\delta(q, \epsilon, X) = \{(p, \epsilon)\}$
5. $\delta(p, \epsilon, X) = \{(p, \epsilon)\}$
6. $\delta(p, 1, X) = \{(p, XX)\}$

$$7. \delta(p, 1, Z_0) = \{(p, \epsilon)\}$$

From the ID $(p, 1101, XXZ_0)$, which of the following ID's can NOT be reached?

- a) $(p, 1101, XZ_0)$
- b) (p, ϵ, ϵ)
- c) $(p, 01, \epsilon)$
- d) $(p, 1101, Z_0)$

Answer submitted: **b)**

You have answered the question correctly.

18. Consider the grammars:

$G_1: S \rightarrow AB \mid a \mid abC, A \rightarrow b, C \rightarrow abC \mid c$

$G_2: S \rightarrow a \mid b \mid cC, C \rightarrow cC \mid c$

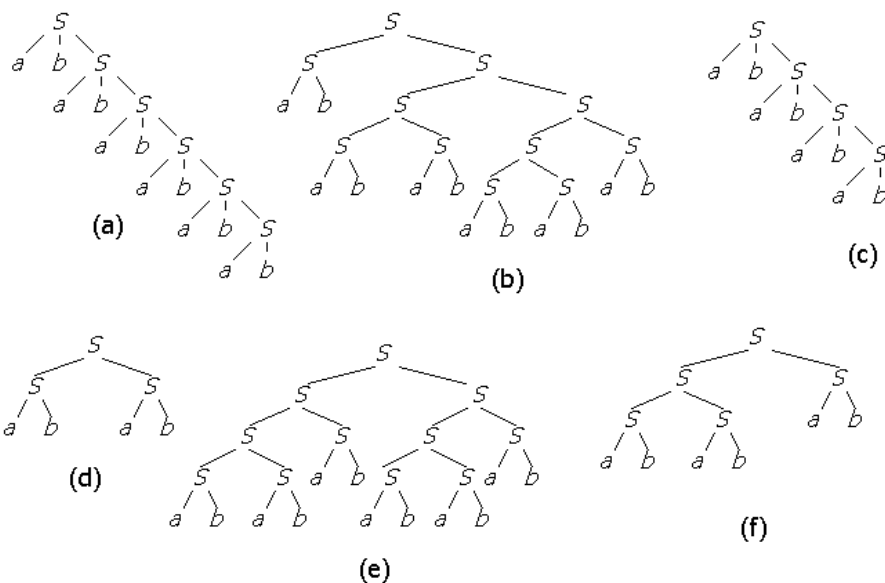
These grammars do not define the same language. To prove, we use a string that is generated by one but not by the other grammar. Which of the following strings can be used for this proof?

- a) ababababcc
- b) cccc
- c) ababababccccc
- d) aba

Answer submitted: **b)**

You have answered the question correctly.

19. Consider the grammar: $S \rightarrow SS, S \rightarrow ab$. Identify in the list below the one set of parse trees which includes a tree that is NOT a parse tree of this grammar?



- a) $\{(c), (e), (d)\}$
- b) $\{(d), (f)\}$
- c) $\{(d), (e)\}$
- d) $\{(b), (f)\}$

Answer submitted: **a)**

You have answered the question correctly.

20. Consider the grammar G with start symbol S :

$$S \rightarrow bS \mid aA \mid b$$

$$A \rightarrow bA \mid aB$$

$$B \rightarrow bB \mid aS \mid a$$

Which of the following is a word in $L(G)$?

- a) ababbbbbb
- b) ababbbbbbbb
- c) ababbbb
- d) aababbabbabba

Answer submitted: **d)**

You have answered the question correctly.

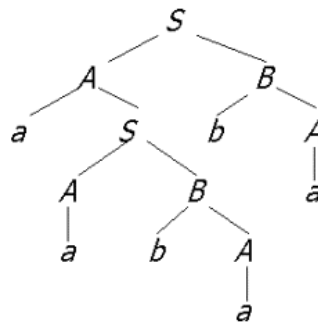
21. The Boolean expression $wxyz+u+v$ is equivalent to an expression in 3-CNF (a product of clauses, each clause being the sum of exactly three literals). Find the simplest such 3-CNF expression and then identify one of its clauses in the list below. Note: $\neg e$ denotes the negation of e . Also note: we are looking for an expression that involves only u, v, w, x, y , and z , no other variables. Not all boolean expressions can be converted to 3-CNF without introducing new variables, but this one can.

- a) $(w+z+v)$
- b) $(u+v+\neg x)$
- c) $(y+z+v)$
- d) $(y+u+v)$

Answer submitted: **d)**

You have answered the question correctly.

22. The parse tree below represents a rightmost derivation according to the grammar $S \rightarrow AB$, $A \rightarrow aS \mid a$, $B \rightarrow bA$.



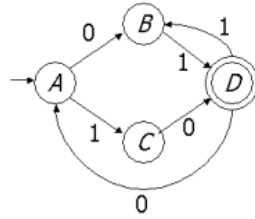
Which of the following is a right-sentential form in this derivation?

- a) aSbA
- b) abaAba
- c) Aba
- d) aaBba

Answer submitted: **c)**

You have answered the question correctly.

23. The finite automaton below:



accepts no word of length zero, no word of length one, and only two words of length two (01 and 10). There is a fairly simple recurrence equation for the number $N(k)$ of words of length k that this automaton accepts. Discover this recurrence and demonstrate your understanding by identifying the correct value of $N(k)$ for some particular k . Note: the recurrence does not have an easy-to-use closed form, so you will have to compute the first few values by hand. You do not have to compute $N(k)$ for any k greater than 14.

- a) $N(13) = 2730$
- b) $N(14) = 114$
- c) $N(13) = 624$
- d) $N(11) = 682$

Answer submitted: **b)**

You have answered the question correctly.

24. Identify from the list below the regular expression that generates all and only the strings over alphabet $\{0,1\}$ that end in 1.

- a) $1*0*1$
- b) $(0*+1)^+$
- c) $(0+1)^*1^+$
- d) $(0*+1)^*$

Answer submitted: **c)**

You have answered the question correctly.

25. Here is a context-free grammar:

```

S → AB | CD
A → BG | 0
B → AD | ε
C → CD | 1
D → BB | E
E → AF | B1
F → EG | 0C
G → AG | BD
  
```

Find all the nullable symbols (those that derive ϵ in one or more steps). Then, identify the true statement from the list below.

- a) G is not nullable.
- b) D is not nullable.
- c) S is nullable.
- d) B is not nullable.

Answer submitted: **c)**

You have answered the question correctly.