SAT & PSAT Must-Know Math Formulas
LOTLOUISCHO STEM CLUB

1 Conversions and Constants

$$1 \text{ in} = 2.54 \text{ cm}, \quad 1 \text{ ft} = 12 \text{ in}, \quad 1 \text{ yd} = 3 \text{ ft}$$

$$\pi \approx 3.1416, \quad e \approx 2.718$$

2 Algebra – Linear Equations and Functions

y: Function or Graph
m: Slope
x: Variable
b: Y-Intercept

NOTE: X-intercept means when $y = 0$. Y-intercept means $x = 0$.

Standard Form $Ax + By = C$
Slope $= -\frac{A}{B}$
Slope m $= \frac{y_2 - y_1}{x_2 - x_1}$
Slope-Intercept Form: $y = mx + b$
Point-slope Form: $y - y_1 = m(x - x_1)$

Average rate of change between (a,f(a)) and (b, f(b)) can be determined by

$$m = \frac{f(b) - f(a)}{b - a}$$

Let's say we have two lines $y_1 = m_1 x + b_1$ and $y_2 = m_2 x + b_2$. We can say that:

$m_1 = m_2$ **PARALLEL LINES (SAME SLOPE)**
$m_1 \cdot m_2 = -1$ **PERPENDICULAR LINES**

When you are given something like this:

$$ax + by = c_1$$
$$ax + by = c_2$$

If $c_1 = c_2$, then there are infinite many solutions. If $c_1 \neq c_2$, then there are no solutions to the system of linear equations above.

Distance a vehicle or a person travels can be determined by

$$\textbf{Distance} = \textbf{Velocity} \times \textbf{Time}$$

The distance d between two points (x_1, y_1) and (x_2, y_2) can be computed by

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

and the midpoint M between two points can be determined by

$$M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

3   Exponent Rules & Radicals

Be aware of MADSPM or in other words Mad Steve Pours Milkshake. What does this mean and what do we do with the exponents?

Multiplying Exponents mean **ADD**
Dividing Exponents mean **SUBTRACT**
Powering Exponents mean **MULTIPLY**

$$a^m \cdot a^n = a^{m+n}$$
$$\frac{a^m}{a^n} = a^{m-n}$$
$$(a^m)^n = a^{m \cdot n}$$
$$(ab)^m = a^m \cdot b^m$$
$$a^{-m} = \frac{1}{a^m}$$
$$a^{1/n} = \sqrt[n]{a}$$
$$a^{m/n} = \sqrt[n]{a^m}$$
$$\sqrt{a} \cdot \sqrt{b} = \sqrt{ab}$$

y_0: Initial value
b: Growth/Decay Factor
t: Time
r: Rate
n: Time period

$$y = y_0 b^t$$
$$y = y_0 (1 \pm r)^t \quad \text{(Growth/decay model)}$$
$$A = P\left(1 + \frac{r}{n}\right)^{nt} \quad \text{(Compound interest)}$$
$$A = Pe^{rt} \quad \text{(Continuous growth/decay)}$$

4   Quadratics and Polynomials

$$y = ax^2 + bx + c \quad \text{(Standard form)}$$
$$y = a(x - h)^2 + k \quad \text{(Vertex form, vertex} = (h, k))$$
$$y = a(x - r_1)(x - r_2) \quad \text{(Factored form, roots } r_1, r_2)$$
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \text{(Quadratic formula)}$$

NOTE: These kind of questions shown below ALWAYS appear on the exam!

$$b^2 - 4ac > 0 \text{ **TWO Real Solutions**}$$

$$b^2 - 4ac = 0 \text{ **ONE Real Solution**}$$

$$b^2 - 4ac < 0 \text{ **NO Real Solutions**}$$

Sum of solutions $= -\dfrac{b}{a}$, **Product of Solutions** $= \dfrac{c}{a}$

DISCLAIMER: If you are currently enrolled in AP Calculus, then you will know what this part is about. For those of you not enrolled in AP Calculus, this is a quick shortcut to determine the minimum or the maximum points on the quadratic equation $y = ax^2 + bx + c$**.**

$$y = ax^2 + bx + c$$
$$\frac{dy}{dx} = 2ax + b$$
$$\frac{dy}{dx} = 0$$
$$\frac{dy}{dx} = 2ax + b = 0$$
$$2ax = -b$$
$$x = -\frac{b}{2a}$$

Thus the minimum/maximum of $f(x) = ax^2 + bx + c$ is at $\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$.

5   Factoring

$$a^2 + 2ab + b^2 = (a + b)^2$$
$$a^2 - 2ab + b^2 = (a - b)^2$$
$$a^2 - b^2 = (a - b)(a + b)$$

6 Complex Numbers

The canonical form for complex numbers is $a + bi$ where a is the real number and b is in the imaginary axis. The patterns shown below will repeat after four cycles.

$$i = \sqrt{-1}$$
$$i^2 = -1$$
$$i^3 = -i$$
$$i^4 = 1$$

Now look what happens after we pass i^4. Can you see a pattern?

$$i^5 = \sqrt{-1}$$
$$i^6 = -1$$
$$i^7 = -i$$
$$i^8 = 1$$

7 Geometry

7.1 Circles

The canonical formula for circles is shown below:

$$(x - h)^2 + (y - k)^2 = r^2$$

where **r** is the radius of the circle and (h, k) is the center of the circle. We can also compute:

$$\text{Area } A = \pi r^2$$
$$\text{Circumference } C = 2\pi r$$
$$\text{Length of Arc } l = r\theta \text{ or } l = \frac{n^\circ}{360^\circ} \times 2\pi r$$
$$\text{Area of Sector } S = \frac{n^\circ}{360^\circ} \times \pi r^2$$

7.2 Triangle Theorems

The inequality theorem states that when you have sides a, b and c, then $a + b > c$.

$$\text{Equilateral Triangle: ALL sides are EQUAL}$$
$$\text{Isosceles Triangle: Two sides are EQUAL}$$
$$\text{Scalene Triangle: ALL unequal sides}$$
$$\text{Acute angle means less than } 90^\circ$$
$$\text{Right angle means } 90^\circ$$
$$\text{Obtuse angle means greater than } 90^\circ$$
$$\text{Sum of interior angles add up to } 180^\circ$$

7.3 Common Formulas
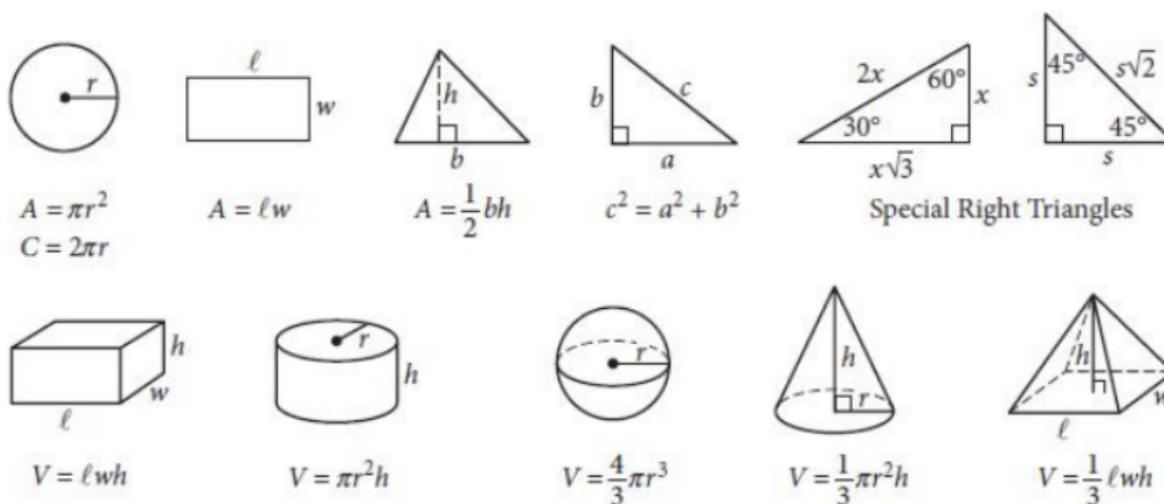
The number of degrees of arc in a circle is 360.
The number of radians of arc in a circle is 2π.
The sum of the measures in degrees of the angles of a triangle is 180.

Figure 1: Geometry Formulas from Official College Board SAT and PSAT Exams.

7.3.1 Areas A

$$A_{Square} = \textbf{Length}^2$$
$$A_{Rectangle} = \text{Length} \times \text{Width}$$
$$A_{Triangle} = \frac{1}{2} \times \text{base} \times \text{height}$$
$$\text{Sphere Surface Area} = 4\pi r^2$$

7.3.2 Perimeters P – Sum of All Sides of Shapes

$$P_{Square} = 4 \times \text{Length}$$
$$P_{Rectangle} = 2 \times (\text{Length} + \text{Width})$$
$$P_{Triangle} = a + b + c$$

7.3.3 Volumes V

$$V_{\text{Rectangular Prism}} = \text{Length} \times \text{Width} \times \text{Height}$$
$$V_{\text{Cylinder}} = \pi r^2 \times \text{Height}$$
$$V_{\text{Cone}} = \frac{1}{3}\pi r^2 \times \text{Height}$$
$$V_{\text{Sphere}} = \frac{4}{3}\pi r^3$$

7.3.4 Pythagorean Theorem

$$a^2 + b^2 = c^2$$

8 Trigonometry

Always remember **SOHCAHTOA** which means:

$$\sin\theta = \frac{\textbf{Opposite}}{\textbf{Hypotenuse}}$$
$$\cos\theta = \frac{\textbf{Adjacent}}{\textbf{Hypotenuse}}$$
$$\tan\theta = \frac{\textbf{Opposite}}{\textbf{Adjacent}}$$

Another thing to note is that when θ is in degrees:

$$\sin\theta = \cos\left(90° - \theta\right)$$
$$\cos\theta = \sin\left(90° - \theta\right)$$
$$\sin^2\theta + \cos^2\theta = 1$$

9 Statistics and Data

$$\text{Mean (Average) } \mu = \frac{\text{Sum of Data}}{\text{Number of Data Points}}$$
$$\text{Median} = \text{Middle value}$$
$$\text{Mode} = \text{Most Frequent Value}$$
$$\text{Range R} = \text{Max - Min}$$
$$\text{Standard Deviation } \sigma = \text{Spread of data and how far apart from mean value}$$
$$\text{Line of best fit: } y = mx + b$$
$$\text{Percent} = \frac{Part}{Whole} \times 100$$
$$\text{Percent change: } \frac{\text{new} - \text{old}}{\text{old}} \times 100\%$$

10 Probability and Counting

$$\text{P} = \frac{\text{Favorable Outcomes}}{\text{Total Outcomes}}$$
$$P(A \cap B) = P(A)P(B) \textbf{ (Independent Events)}$$
$$P(A \cup B) = P(A) + P(B) \textbf{ (Mutually Exclusive Events)}$$

11 Bonus: Quick Test Tips

- Memorize special right triangle ratios.

- Know how to use the built-in Desmos calculator efficiently.

- Check units for geometry problems.

- For variables, plug in easy numbers.

- Estimate magnitude to spot unreasonable answers.