

INTRODUCTION

Analysis of 5 different algorithms for stock trading optimization

Tasks covered:

Problem-1

- Brute Force (Task 1) \rightarrow O (m \times n²)
- Greedy (Task 2) \rightarrow O (m \times n)
- Single-Transaction DP (Task 3) \rightarrow O (m×n)

Problem-2

• Multi-Transaction DP (Task 5) \rightarrow O (m×n×k)

Problem-3

• Multi-Transaction DP With Cooldown Period (Task 6) \rightarrow O (m×n²)

Focus: Algorithm design, performance analysis, and practical trade-offs
Learning objective: Understanding how algorithm choice impacts real-world performance



THE STOCK TRADING PROBLEM

Input: Matrix $A[m \times n]$ where m = stocks, n = days

Goal: Maximize profit from buy/sell transactions

Example:

• Stock 4, buy day 2 (\$3) \rightarrow sell day 3 (\$14) = \$11 profit

Constraints: Must buy before selling, temporal ordering matters

Variations: Single transaction vs. multiple transactions (up to k)

Task 1 - Brute Force Approach: Check Everything

Algorithm

Three nested loops (stocks \rightarrow buy days \rightarrow sell days)

Time Complexity

 $O(m \times n^2)$

Example

1000 stocks \times 1000 days = \sim 1 billion operations

Advantages

Simple to understand, guaranteed correct answer

Disadvantages

Extremely slow for large datasets

Best Use

Learning, small problems, algorithm verification

```
def MaxProfitBruteForce(A, m, n):
    Brute force algorithm to find the maximum profit from a single buy/sell trans.
    Parameters:
       A (List[List[int]]): Matrix representing stock prices (m stocks * n days)
       m (int): Number of stocks (rows)
       n (int): Number of days (columns)
        Tuple[int, int, int, int]: (bestStock, bestBuyDay, bestSellDay, maxProfit)
       All values are 1-based indices.
        Returns (0, 0, 0, 0) if no profit is possible.
    if m \le 0 or n \le 1 or not A or n \le 2:
        return (0, 0, 0, 0)
    # --- edge case: check if matrix has proper dimensions
   if len(A) != m or any(len(row) != n for row in A):
        return (0, 0, 0, 0)
    # --- initialize variables to store the best result found ---
    maxProfit = 0
    bestStock = 0
    for i in range(m): # stock index (0-based)
       for j1 in range(n - 1): # buy day
            # --- try every possible sell day after the buy day ---
            for j2 in range(j1 + 1, n): # sell day
                if profit > maxProfit:
                    # 1-based index
                   bestSellDay = j2 + 1
    if maxProfit == 0:
       return (0, 0, 0, 0) # if no profitable transaction found
        return (bestStock, bestBuyDay, bestSellDay, maxProfit)
```

Task 2 - Greedy Optimization

For any sell day, optimal buy day = lowest previous price

Algorithm

Track minimum price while processing days sequentially

Time Complexity

 $O(m \times n)$ - 1000× improvement!

Example

 1000×1000 dataset = ~ 1 million operations

Advantages

Fast, elegant, mathematically optimal

Best Use

Production systems, single-transaction scenarios

```
def MaxProfitGreedySolution(A, m, n):
    Greedy algorithm to find the maximum profit from a single buy/sell transaction.
    Parameters:
       A (List[List[int]]): Matrix representing stock prices (m stocks * n days)
       m (int): Number of stocks
       n (int): Number of days
    Returns:
        Tuple[int, int, int]: (bestStock, bestBuyDay, bestSellDay, maxProfit)
       All values use 1-based indexing.
        Returns (0, 0, 0, 0) if no profit is possible.
    if m \le 0 or n \le 1 or not A or n \le 2:
        return (0, 0, 0, 0)
       return (0, 0, 0, 0)
    maxProfit = 0
    bestStock = 0
    bestBuvDav = 0
    bestSellDay = 0
    for i in range(m):
       minDav = 0
                               # track the day of the minimum price
        for j in range(1, n): # start from day 1 (second day)
                bestSellDay = j + 1
    if maxProfit == 0:
        return (0, 0, 0, 0)
```

```
def MaxProfitDynamicProgramming(A, m, n):
    DP approach to find the maximum profit from a single buy/sell transaction.
    Parameters:
       A (List[List[int]]): Matrix representing stock prices (m stocks * n days)
       m (int): Number of stocks
       n (int): Number of days
    Returns:
        Tuple[int, int, int] : (bestStock, bestBuyDay, bestSellDay, maxProfit)
       All values use 1-based indexing.
       Returns (0, 0, 0, 0) if no profit is possible.
    if m \le 0 or n \le 1 or not A:
        return (0, 0, 0, 0)
    if len(A) != m or any(len(row) != n for row in A):
        return (0, 0, 0, 0)
    maxProfit = 0
    bestStock = 0
    bestSellDay = 0
    for i in range(m):
                           # day when the lowest price occurred
        for j in range(1, n):
           if A[i][j] < minPrice:</pre>
               minPrice = A[i][j]
    if maxProfit == 0:
        return (0, 0, 0, 0) # if no profitable transaction found
        return (bestStock, bestBuyDay, bestSellDay, maxProfit)
```

Task 3 - Single Transaction DP

Dynamic Programming Foundation

Approach:

DP principles applied to single-transaction problem

Performance:

 $O(m \times n)$ - identical to greedy algorithm

Purpose:

Framework for extensibility, not immediate speed gains

Value:

Foundation for complex multi-transaction scenarios

Comparison:

Same performance as greedy, better structure for extensions

Best Use:

When planning to extend to Tasks 5-6 later

Task 5 - Multiple Transactions DP

Section 1: Algorithm Overview & Input Validation

```
# --- edge case: check if the input is empty or missing ---
if m <= 0 or n <= 1 or not A or k <= 0:
    return []

# --- edge case: check if matrix has proper dimensions
if len(A) != m or any(len(row) != n for row in A):
    return []</pre>
```

Section 2: DP Table Initialization

```
# --- initialize DP tables ---
# DP table to store the best profit at each day for up to t transactions
max_profit = []
for transaction_num in range(k + 1):
    day_profits = []
    for day in range(n):
        day_profits.append(0) # start with 0 profit for each day
    max_profit.append(day_profits)

# DP table to remember which (buy, sell) days gave us that profit
best_days = []
for transaction_num in range(k + 1):
    day_pairs = []
    for day in range(n):
        day_pairs.append(None) # no transaction yet
    best_days.append(day_pairs)
```

Section 3: Core DP Algorithm

```
for t in range(1, k + 1):
    max diff = -prices[0]
                                 # best value of (max_profit[t-1][d] - prices[d])
    best buy day = 1
                                 # start with day 1 (1-based)
    for day in range(1, n):
       current_profit = prices[day] + max_diff
        if max profit[t][day - 1] >= current profit:
            max profit[t][day] = max profit[t][day - 1]
           best_days[t][day] = best_days[t][day - 1]
            # --- option 2: sell today using the best past buy day ---
            max profit[t][day] = current profit
            best_days[t][day] = (best_buy_day, day + 1) # store 1-based
        # --- update max diff and corresponding buy day ---
       prev = max_profit[t - 1][day] - prices[day]
        if prev > max diff:
            max diff = prev
            best buy day = day + 1
```

Task 5 - Multiple Transactions DP

Section 4: Transaction Reconstruction

```
# --- reconstruct transactions for this stock ---
t = k
day = n - 1
while t > 0 and day > 0:
    if best_days[t][day]:
        buy_day, sell_day = best_days[t][day]
        profit = prices[sell_day - 1] - prices[buy_day - 1]
        all_transactions.append((stock_index + 1, buy_day, sell_day, profit))
        day = buy_day - 2  # go to the day before the buy_day
        t -= 1
    else:
        day -= 1
```

Test Result

```
Selected Non-Overlapping Transactions:

ID (Stock, Buy, Sell) Profit

T1 (2, 1, 2) 7

T2 (2, 3, 5) 6

T3 (1, 2, 3) 4

[(2, 1, 2), (2, 3, 5), (1, 2, 3)] with total profit = 17
```

Section 5: Global Selection & Return

```
# --- sort all transactions by profit in descending order ---
all_transactions.sort(key=lambda x: x[3], reverse=True )

# --- pick top-k non-overlapping transactions ---
selected = []
for stock, buy1, sell1, profit in all_transactions:
    overlaps = False
    for _, buy2, sell2, _ in selected:
        if not (sell1 <= buy2 or buy1 >= sell2): # overlapping interval
            overlaps = True
            break

if not overlaps:
        selected.append((stock, buy1, sell1, profit))
        if len(selected) == k:
            break

return selected
```

Task 6 - Multiple Transactions With Cooldown period DP

Problem Overview

Challenge: Cannot buy any stock for c days after selling any stock

Real-World Application: Models trading restrictions, settlement periods, or regulatory constraints

Example: If you sell on day 3 with cooldown=2, you cannot buy until day 6

buy until day 6

Algorithm: Dynamic Programming with constraint handling

Section 2: Find all profitable transactions

Section 1: Input Validation

Similar to Task-5

Section 3:Dynamic Programming Optimization

```
# --- 3: DP table where dp[day] = (max_profit, best_sequence) ---
dp = [(0, []) for _ in range(n + 2)] # allows access to sell + cooldown + 1
prefix_max = [(0, []) for _ in range(n + 2)]

for t in transactions:
    stock, buy, sell, profit, next_day = t
    next_day = min(next_day, n) # cap to make sute next_day does not exceed n

# --- compute the best result before or on the buy day ---
best_profit_before = prefix_max[buy]
    total_profit = best_profit_before[0] + profit
    sequence = best_profit_before[1] + [(stock, buy, sell)]

if total_profit > dp[next_day][0]:
    dp[next_day] = (total_profit, sequence)

# --- update prefix max at next_day ---
    prefix_max[next_day] = max(prefix_max[next_day], dp[next_day], key=lambda x: x[0])
```

Performance Comparison

Complexity Overview

Task	Problem	Algorithm Type	Time Complexity	Problem Description
Task 1	Problem 1	Brute Force	$O(m \times n^2)$	Single transaction
Task 2	Problem 1	Greedy	$O(m \times n)$	Single transaction
Task 3	Problem 1	Dynamic Programming	$O(m \times n)$	Single transaction
Task 5	Problem 2	Dynamic Programming	$O(m \times n \times k)$	Multiple transactions
Task 6	Problem 3	Dynamic Programming	$O(m \times n^2)$	Cooldown constraints

Performance Analysis (1000×1000 Dataset)

Task	Operations Required	Relative Speed	Best Use Case
Task 2/3	~1 million	1000× faster	Production single-transaction
Task 1	~1 billion	Baseline (slowest)	Learning/verification
Task 6	~1 billion	Similar to Task 1	Cooldown scenarios
Task 5 (k=10)	~10 million	100× faster than brute force	Multiple transactions

Algorithm Selection Guide

Brute Force: Learning, datasets <100×100, algorithm verification

Greedy: Production systems, single transactions, speed priority

Single DP: Planning future extensions to multi-transaction problems

Multi DP: Realistic trading, portfolio optimization, k-transaction scenarios, cooldown period

Decision Factors:

Dataset size, performance requirements, future extensibility needs Understanding level, maintenance complexity, correctness guarantees

THANK YOU