



Calcul Scientifique

Projet de Calcul Scientifique

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1.

Matrix dimension	Matrix type	Exec. time for <code>eig</code> (s)	Exec. time for <code>power_v11</code> , (s)
200×200	Type 1	9.000e-02	1.510e+00
400×400	Type 1	4.000e-02	1.831e+01
600×600	Type 1	6.000e-02	6.021e+01
200×200	Type 2	3.000e-02	3.000e-02
400×400	Type 2	4.000e-02	4.000e-02
600×600	Type 2	7.000e-02	1.700e-01
200×200	Type 3	1.000e-02	5.000e-02
400×400	Type 3	3.000e-02	5.200e-01
600×600	Type 3	7.000e-02	1.270e+00
200×200	Type 4	2.000e-02	1.670e+00
400×400	Type 4	3.000e-02	2.094e+01
600×600	Type 4	6.000e-02	5.456e+01

Table 1: Execution time for different sizes and types of matrices

We can see that the `power_v11` algorithm is generally slower than the `eigen` function especially for the type 2 and 4 matrices.

2.

```

1  nb_it = 1;
2  norme = norm(beta*v - z, 2)/norm(beta,2);
3
4  while(norme > eps && nb_it < maxit)
5      beta_old = beta;
6      v = z/norm(z, 2);
7      z = A*v;
8      beta = (v'*z)/(v'*v);
9      norme = abs(beta-beta_old)/abs(beta_old);
10     nb_it = nb_it + 1;
11 end

```

Listing 1: Inner loop of the new algorithm

Matrix dimension	Matrix type	Exec. time for <code>power_v11</code> , (s)	Exec. time for <code>power_v12</code> , (s)
200×200	Type 1	1.960e+00	3.200e-01
400×400	Type 1	1.888e+01	2.660e+00
600×600	Type 1	5.031e+01	7.070e+00
200×200	Type 2	1.000e-02	1.000e-02
400×400	Type 2	7.000e-02	1.000e-02
600×600	Type 2	1.800e-01	4.000e-02
200×200	Type 3	3.000e-02	1.000e-02
400×400	Type 3	6.100e-01	1.100e-01
600×600	Type 3	1.270e+00	2.600e-01
200×200	Type 4	1.530e+00	2.900e-01

400×400	Type 4	2.113e+01	3.060e+00
600×600	Type 4	5.914+e01	6.480e+00

We can see that the `power_v12` algorithm is globally faster than the `power_v11`.

3.

The main drawback of the deflated power method is the numerous matrix-vector products required to compute the eigenvectors as well as the fact that each iteration compute only one eigenvalue which can be slow if a lot of eigenvalues are desired.

4.

If we apply Algorithm 1 to m vectors, there is no reason for the columns of V to converge to a base. Each vector will converge toward a different projection of the dominant eigenvalue.

5.

In Algorithm 2, the matrix H is a smaller matrix, with dimension $n \times m$, therefore, even for larger matrices A , computing the spectral decomposition of H will not be computationally expensive.