

Assignment 3

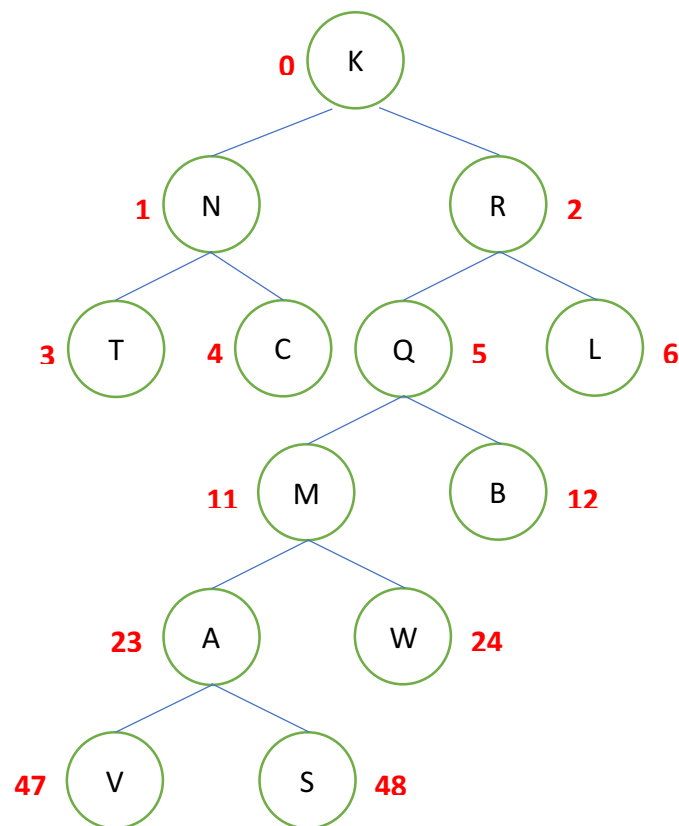
Rui Zhao

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Writing questions:

Question 1:

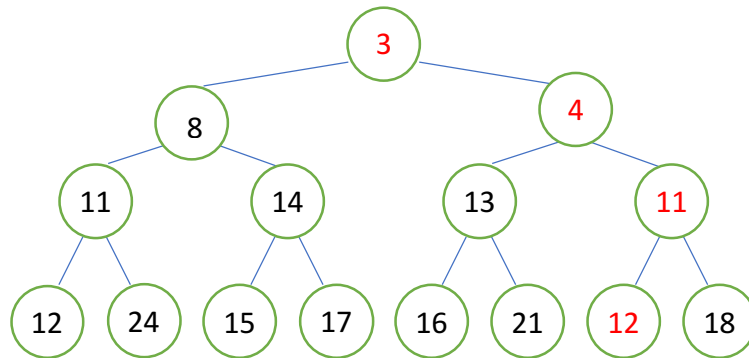
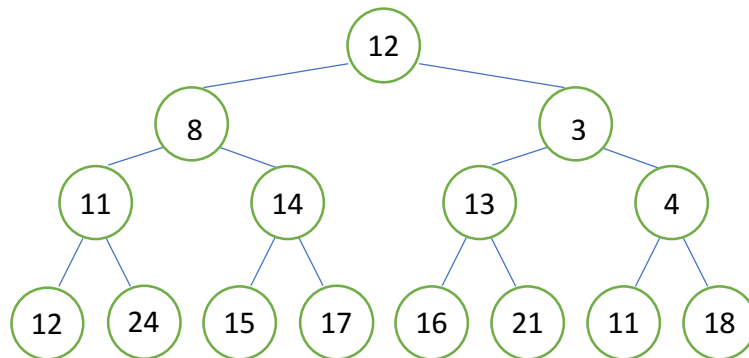
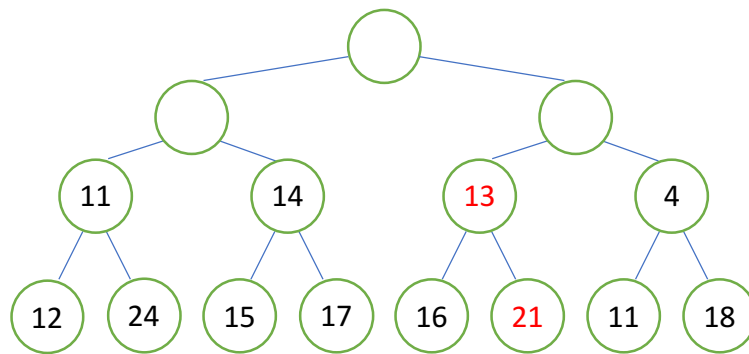
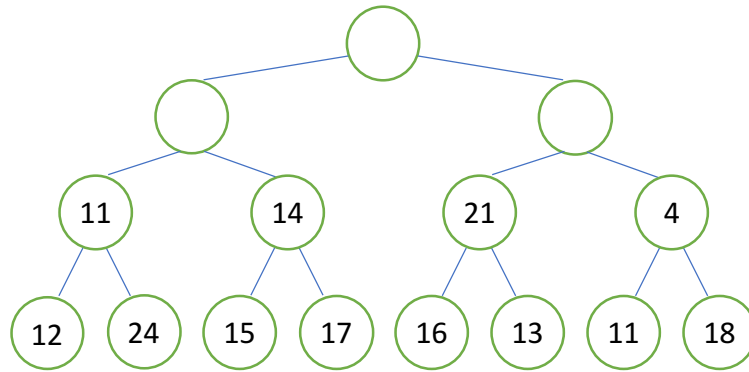
a)



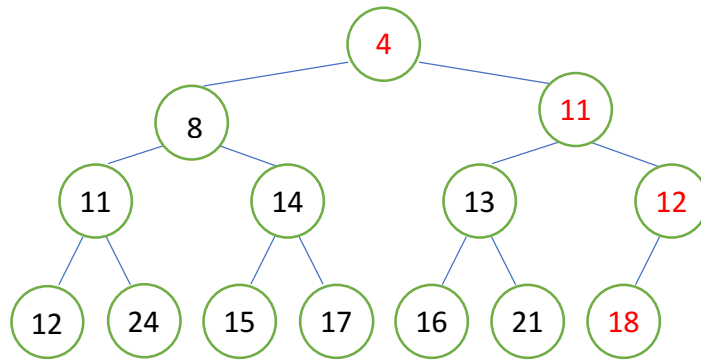
b) For array-based binary tree, the index of left child is  $2 \times \text{index of root} + 1$ , and the index of right child is  $2 \times \text{index of root} + 2$ . Therefore, the array for storing the given tree is illustrated above. The red numbers indicate the indices of the array in which corresponding values are stored.

**Question 2:**

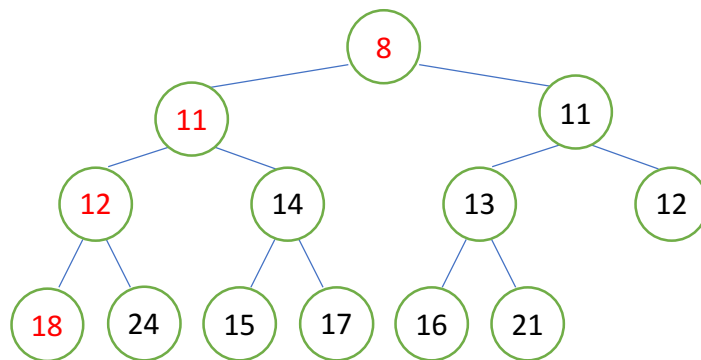
a)



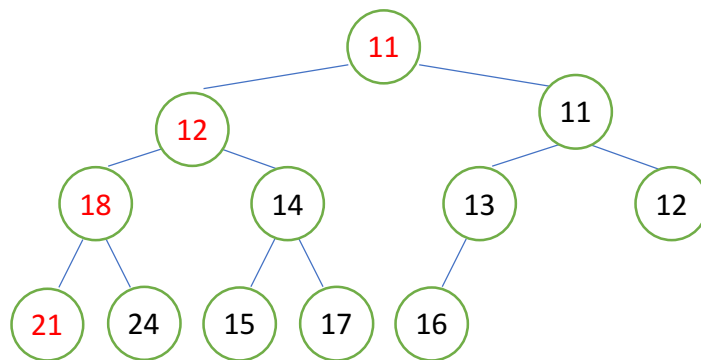
**After 1<sup>st</sup> removeMin**



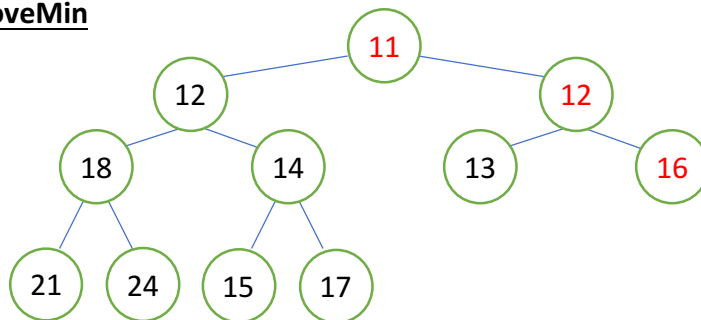
**After 2<sup>nd</sup> removeMin**



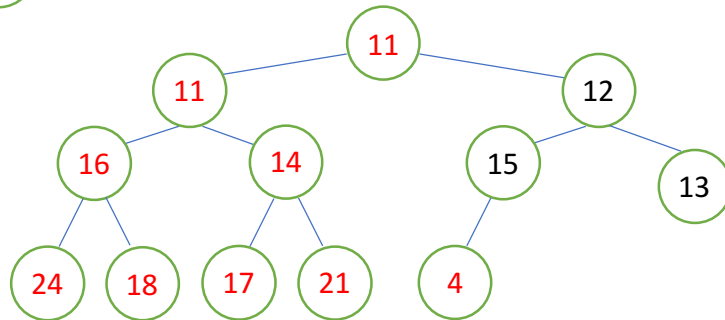
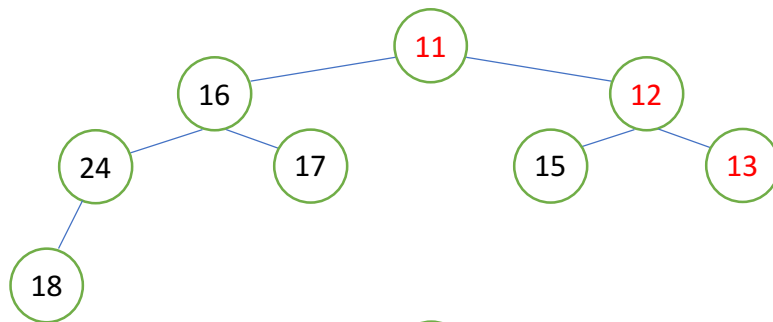
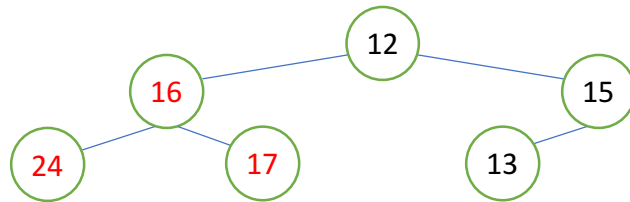
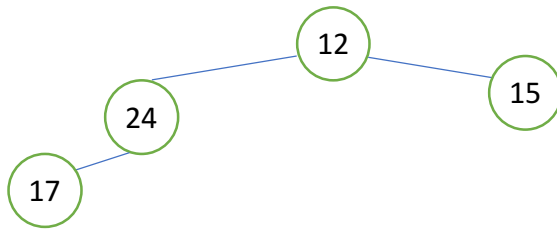
**After 3<sup>rd</sup> removeMin**



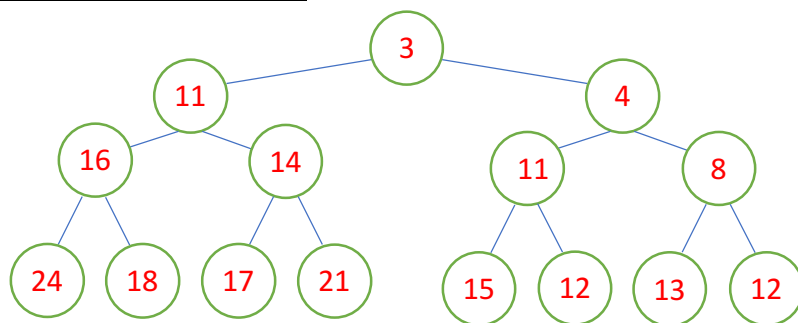
**After 4<sup>th</sup> removeMin**



b)



**Final tree (some steps are omitted):**



**Question 3:**

**Algorithm computeDepth(Tree T, Node v)**

**Input:** tree T with n nodes, v is a node of T

**Output:** the depth of each node in the subtree of T rooted at v

**if** T.isRoot(v) **then**

    setDepth(v,0)

**else then**

    setDepth(v,1+getDepth(T.parent(v)))

children  $\leftarrow$  T.children(v)

**while** (children.hasNext()) **do**

    computeDepth(T, children.next())

- a) the time complexity of this algorithm is  $O(n)$ , because it is a linear recursion function and will make n recursive calls in total.
- b) The best possible complexity that can be achieved to compute the depth of all nodes of the tree T should be  $O(n)$ , because we have to visit each node at least once in order to compute its depth.
- c) My algorithm is  $O(n)$  in terms of time complexity.