

# Learning from noisy demonstrations: compliance-based tradeoff

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#### Plan

- 1 Motivations
- 2 Background
  - Reinforcement learning
  - Transfer learning
- 3 Approach
  - Sandbox state space
  - Compliance-based learning
  - Method comparaison
- 4 Future work

#### Motivations

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#### Motivations

- ► For long and complex tasks : common machine learning algorithm are usually very slow to converge
- ► Accelerate learning via prior knowledge of the environment or task : provide a demonstration of the task
- ▶ Framework of *learning from demonstration* (LfD)¹

 $\longrightarrow$  Ex. : robotic arm grabbing a cup

: maze solver

#### Motivations

- ▶ How to take the teacher's demonstration into account?
  - Exactly reproduce the teacher's actions
  - Use demonstration data to build a representation of the environment's dynamics
  - ▶ Use the teacher demonstration as an exploration baseline

- Child learning to dance: first follow its dance teacher moves, before trying out new ones once he feels he has exploited the teacher's recommandation
  - ⇒ notion of compliance w.r.t the teacher.

### ■ Goal :

- Introduce a theoretical framework for compliance-based learning
- Grasp ideas and intuition about how such an approach can
  - ► Speed up the learning
  - Overcome some possible mentor's sub-optimality.
  - ► Generalize to transfer learning

in a reinforcement learning framework.

# ■ Approach :

- Create a simple but generic environment and task
- Solve it using classical RL method
- Implement compliant-based learning method
- ► Compare them with classical methods, evaluate their pros and cons

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#### RL:

- Framework in which an agent (or a learner) learns its actions from interaction with its environment
- ▶ The environment generates scalar values called rewards, that the agent is seeking to maximize over time.

Under a Markovian asumption for the dynamics and reward system, the reinforcement learning problem can be formulated as a Markov Decision Process:

$$(\mathcal{S}, \mathcal{A}(\mathcal{S}), \mathcal{P}_{ss'}^{a}, \mathcal{R}_{ss'}^{a}) \tag{1}$$

where:

$$\mathcal{P}_{ss'}^{a} = \underbrace{\mathbb{P}(s_{t+1} = s' \mid s_{t} = s, \ a_{t} = a)}_{\textit{dynamics}} \qquad \mathcal{S} : \text{ state space}$$

$$\mathcal{R}_{ss'}^{a} = \underbrace{\mathbb{E}\left[r_{t} \mid s_{t+1} = s', \ s_{t} = s, \ a_{t} = a\right]}_{\textit{dynamics}} \qquad \mathcal{A}(\mathcal{S}) : \text{ action space}$$
(2)

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immediate reward

#### ■ RL :

▶ Define state value and action value function under a policy (probabilistic decision rule)  $\pi: \mathcal{S} \to \mathcal{A}$ :

$$V^{\pi}(s) = \mathbb{E}_{\pi} \left[ \sum_{i} \gamma^{i} r_{t+i+1} | s_{t} = s \right]$$

$$Q^{\pi}(s, a) = \mathbb{E}_{\pi} \left[ \sum_{i} \gamma^{i} r_{t+i+1} | s_{t} = s, a_{t} = a \right]$$
(3)

- ► All algorithm computing optimal policies rely on various mix of a Generalized Policy Iteration :
  - 1. Evaluate the current policy (DP,..)
  - 2. Improve the current policy (greedization)
  - 3. Repeat

# ■ Solving RL : Two baseline methods :

- ▶ Model-based ( $\mathcal{P}_{ss'}^a$  and  $\mathcal{R}_{ss'}^a$  are known) : dynamic programming (value iteration algorithm, ...)
- ► Model-free : exploitation vs exploration paradigm for computing the optimal policy's Q-values :

$$\{Q(s,a)\}_{s\in\mathcal{S},a\in\mathcal{A}(s)}\tag{4}$$

- ► Bootstrap from initial value
- Update in direction of the sampled expected return

$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + \alpha \mathbb{E}\left[R_t|s, a\right]$$
 (5)

► Many different variations : SARSA, Q-learning, R-learning, eligibiliy traces,...



- Transfer learning: speeding a learning process thanks to another learning experience.
  - ▶ Provide the learner with a mentor that is another learner
  - ► In homogeneous settings<sup>2</sup>
  - Study how convergence is affected

and eventually generalize to

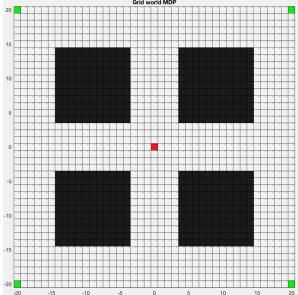
- multiple teacher
- inhomogeneous settings

<sup>&</sup>lt;sup>2</sup>Bob Price and Craig Boutilier. "Accelerating reinforcement learning through implicit imitation". *Journal of Artificial Intelligence Research* 19 (2003);5569–629. Print. ₹ → Q

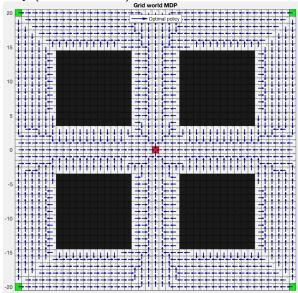
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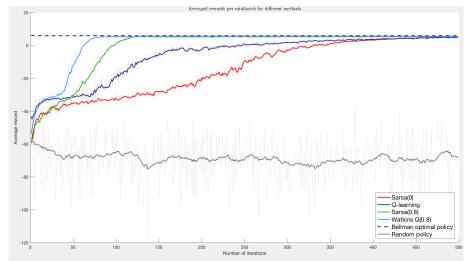
■ Generic and simple state space :



# ■ Optimal Policy (value iteration) :



# ■ Learning the optimal policy :



- Compliance learning
- $\rightarrow$  We only have access to the teacher's actions over  $\mathcal{A}(\mathcal{S})$ .
- → Intuitively :
  - Follow the teacher
  - Gain some knowledge about the environment and the task
  - Take our own actions
- → The teacher should only influence our action selection

- ▶ Global compliance term  $p \in [0, 1]$
- **>** p-greedy action selection w.r.t the teacher's action :  $\forall s \in \mathcal{S}$

$$\pi(s) = \begin{cases} a_m \text{ with probability } p \text{ independent of } s \\ a \in \mathcal{A}(s) \text{ (Gibbs softmax)} \end{cases}$$
 (6)

### ■ Naive approach :

Constantly decreasing compliance :

$$\begin{vmatrix} p_0 \in [0,1] \\ p_{t+1} = \beta p_t, \quad \beta < 1 \end{aligned}$$
 (7)

Along with SARSA update :

$$Q(s,a) \leftarrow Q(s,a) + \alpha(r + \gamma Q(s',a') - Q(s,a))$$
 (8)

## ■ Constantly decreasing compliance :

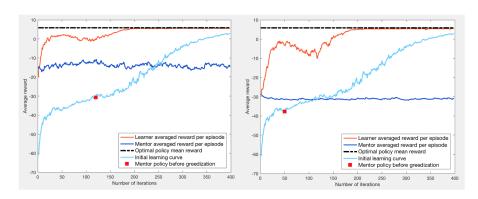


Figure: Average reward for two naive compliance learners

■ Constantly decreasing compliance :

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Easy to implement	Undershoot
Fast convergence (200 vs 500)	Precise tuning

Tuning between the dynamics of p and of the Gibbs sampling temperature is hard!

Could we *learn p* instead of using a fixed dynamic ?

### ■ Learning the compliance term

 $\forall s \in \mathcal{S}$ , define p(s) - compliance term that impact the action selection :

$$\pi(s) = \begin{cases} a_m \text{ with probability } p(s) \\ a \in \mathcal{A}(s) \setminus a_m \text{ with probabiliy } 1\text{-p(s)} \end{cases}$$
 (9)

**Goal**: learn p(s),  $\forall s \in S \rightarrow$  measure how right the teacher seems to be

- Learning the compliance term
- ► Actor-critic approach :
  - ▶  $\forall s \in S$ , provide p(s) with a Beta prior :

$$p(s) \sim B(\alpha(s), \beta(s))$$
 (10)

► Given a (s,a,r,s',a') 5-tuple, compute the critic TD value :

$$\delta_t = r + \gamma Q(s', a') - Q(s, a_m) \tag{11}$$

▶ Compute posterior distribution over p(s):

$$\alpha_t(s) \leftarrow \alpha_t(s) + \mathbb{1}_{a=a_m} \delta_t \varepsilon_t \beta_t(s) \leftarrow \beta_t(s) + \mathbb{1}_{a \neq a_m} \delta_t \varepsilon_t$$
(12)

## ► Actor-critic approach :

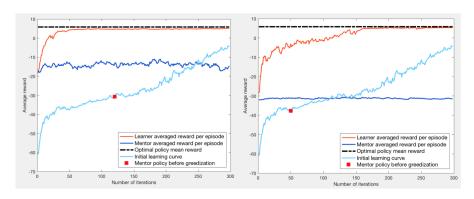
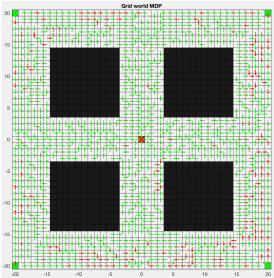


Figure: Average reward for two actor-critic compliance learners

- ► Faster convergence
- ▶ No undershoot + tuning is intuitive

# ► Actor-critic approach :



- Learning the compliance term
- ► Action-value approach :
  - Adds a hierarchical MDP :

$$\forall s \in \mathcal{S}, \, \mathcal{A}_c(s) = \{' listen', \, 'discard' \}$$
 (13)

▶ Define exploration based on  $\{Q_c(s, l), Q_c(s, d)\}$ :

$$\forall s \in \mathcal{S}, \quad \pi_c(s) = \begin{cases} 'l' \text{ with probability } p = \sigma \left( \frac{Q_c(s, l) - Q_c(s, d)}{\tau} \right) \\ 'd' \text{ with probability } 1 - p \end{cases}$$

$$\tag{14}$$

- Action-value approach :
  - Perform SARSA update
  - Update:

$$\begin{cases}
Q_c(s, l) \leftarrow \beta Q_c(s, l) + (1 - \beta) Q(s, a_m) \\
Q_c(s, d) = \beta Q_c(s, d) + (1 - \beta) \max_{a \neq a_m} Q(s, a)
\end{cases}$$
(15)

Introduce prior knowledge by setting

$$Q_c^0(s,l) - Q_c^0(s,d) = \log\{\frac{p}{1-p}\}\tag{16}$$

## ► Action-value approach :

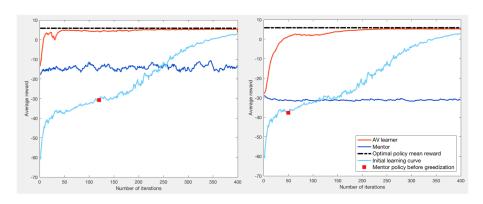
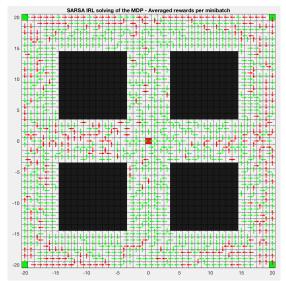


Figure: Average reward for two action-value compliance learners

# ► Action-value approach :



#### Future work

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