

Anomalous electron-phonon coupling probed on the surface of superconductor ZrB_{12} R. Khasanov,^{1,2,3} D. Di Castro,^{1,4} M. Belogolovskii,⁵ Yu. Paderno,⁶ V. Filippov,⁶ R. Brütsch,⁷ and H. Keller¹¹*Physik-Institut der Universität Zürich, Winterthurerstrasse 190, CH-8057, Zürich, Switzerland*²*DPMC, Université de Genève, 24 Quai Ernest-Ansermet, 1211 Genève 4, Switzerland*³*Laboratory for Neutron Scattering, ETH Zürich and Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland*⁴*INFN-Coherentia and Dipartimento di Fisica, Università di Roma "La Sapienza," P.le A. Moro 2, I-00185 Roma, Italy*⁵*Donetsk Physical and Technical Institute, National Academy of Science of Ukraine, 83114 Donetsk, Ukraine*⁶*Institute for Problems of Materials Science, National Academy of Science of Ukraine, 03680 Kiev, Ukraine*⁷*Laboratory for Material Behaviour, Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland*

(Received 22 September 2005; published 14 December 2005)

Magnetization measurements under hydrostatic pressure up to 10.5 kbar in zirconium dodecaboride ZrB_{12} superconductor ($T_c \approx 6.0$ K at $p=0$) were carried out. A negative pressure effect on T_c with $dT_c/dp = -0.0225(3)$ K/kbar was observed. The electron-phonon coupling constant $\lambda_{\text{el-ph}}$ decreases with increasing pressure with $d \ln \lambda_{\text{el-ph}}/dp \approx -0.20\%$ /kbar. The magnetic field penetration depth λ was studied in the Meissner state and, therefore, probes mainly the surface of the sample. The absolute values of λ and the superconducting energy gap at ambient pressure and zero temperature were found to be $\lambda(0) = 140(30)$ nm and $\Delta_0 = 1.251(9)$ meV, respectively. Δ_0 scales linearly with T_c as $2\Delta_0/k_B T_c = 4.79(1)$. The studies of the pressure effect on λ reveal that λ^{-2} increases with pressure with $d \ln \lambda^{-2}(0)/dp = 0.60(23)\%$ /kbar. This effect cannot be explained within the framework of conventional adiabatic electron-phonon pairing, suggesting the possibility that close to the surface an unconventional nonadiabatic character of the electron-phonon coupling takes place.

DOI: [10.1103/PhysRevB.72.224509](https://doi.org/10.1103/PhysRevB.72.224509)

PACS number(s): 74.70.Ad, 74.25.Ha, 74.62.Fj, 83.80.Fg

I. INTRODUCTION

The traditional concept of superconductivity is strictly associated with the electron-phonon interaction. The conventional theory is based on the Migdal-Eliashberg adiabatic approximation¹ that, in fact, leads to the prediction of many peculiar features which are a direct evidence of a phonon mediated superconductivity. The adiabatic approximation is valid if the parameter ω_0/E_f is small (ω_0 is the relevant phonon frequency and E_f is the Fermi energy). Usually this parameter is regarded as a measure of nonadiabaticity. However, crossover from a conventional adiabatic to an unconventional nonadiabatic regime does not depend only on the value of the ω_0/E_f ratio. Paci *et al.*⁸ show that even in a case of small "adiabatic" ratio one would expect the nonadiabatic coupling in superconductors having high value of the electron-phonon coupling constant $\lambda_{\text{el-ph}}$. Among BCS superconductors the zirconium dodecaboride (ZrB_{12}) is probably a candidate for the observation of such type of anomalous coupling. It stems from the rather small value of the Fermi energy ~ 1 eV (Ref. 3) that, together with the Debye temperature ~ 20 meV,⁴ leads to a ratio $\omega_0/E_f \sim 0.02$. A strong coupling ratio $2\Delta/k_B T_c \approx 4.8$ was observed by surface sensitive techniques.^{3,6} This suggests that the electron-phonon coupling constant, which has a bulk value $\lambda_{\text{el-ph}} \approx 0.67$,³ increases at the surface. From the comparison with strongly coupled metallic superconductors⁷ one would expect $\lambda_{\text{el-ph}}^{\text{surf}} \approx 1.7-1.9$. Moreover, it was pointed out by Cappelluti *et al.*² that nonadiabatic character can be further enhanced by low charge carrier density, that is the case for ZrB_{12} .^{4,5}

One of the key features of nonadiabatic superconductivity is the observation of unconventional isotope and pressure effects on the magnetic field penetration depth λ . Note that

in adiabatic superconductors (or in the superconductors where the nonadiabatic effects are small) the pressure effect (PE)^{9,10} as well as the isotope effect (IE)¹¹ on λ was found to be almost negligible in comparison with substantial PE¹² and IE¹³ on λ observed in highly nonadiabatic high- T_c cuprates. In this paper we report on PE on T_c and λ studies in ZrB_{12} superconductor. The magnetic penetration depth measured in the Meissner state is largely determined by the surface characteristics. The absolute value of λ at zero temperature and zero pressure was found to be $\lambda(0) = 140(30)$ nm. The transition temperature T_c and the electron-phonon coupling constant decrease with pressure with the pressure effect coefficients $dT_c/dp = -0.0225(3)$ K/kbar and $d \ln \lambda_{\text{el-ph}}/dp \approx -0.2\%$ /kbar, respectively. In contrast to T_c , $\lambda^{-2}(0)$ was found to increase with $d \ln \lambda^{-2}(0)/dp = 0.29(11)\%$ /kbar. Only a small part of this effect can be explained by a pressure induced renormalization of the electron-phonon interaction and the band structure effects. The major part can be probably explained by considering the possibility of a nonadiabatic coupling of the charge carriers to the crystal lattice appearing in ZrB_{12} close to the surface.

II. EXPERIMENTAL DETAILS

Details on the sample preparation for ZrB_{12} can be found elsewhere.¹⁴ The single crystal has been grounded in mortar and then etched in nitric acid in order to remove the inclusion of impurity ZrB_2 fraction.¹⁵ After that, powder was sieved via the $10 \mu\text{m}$ sieve in order to obtain small grains needed for determination of λ from magnetization measurements. The grain size distribution was determined by analyzing scanning electron microscope (SEM) photographs. The hydrostatic pressure was generated in a copper-beryllium

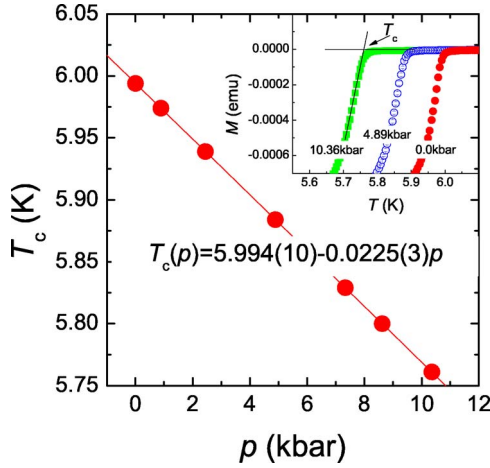


FIG. 1. (Color online) Pressure dependence of the transition temperature T_c for ZrB_{12} . The errors are smaller than the size of the symbols. The inset shows $M(T)$ curves in the vicinity of T_c (from the left to the right) 10.36, 4.89, and 0.0 kbar.

piston cylinder clamp especially designed for magnetization measurements under pressure.¹⁶ The sample was mixed with Fluorient FC77 (pressure transmitting medium) with a sample-to-liquid volume ratio of approximately 1/6. The pressure dependence of T_c was taken from a separate set of magnetization experiments where a small piece of indium [$T_c(p=0)=3.4$ K] with known $T_c(p)$ dependence was added to the sample and both T_c 's of indium and ZrB_{12} were recorded. The field-cooled (FC) magnetization measurements were performed with a SQUID magnetometer in a field of 0.5 mT at temperatures between 1.75 K and 10 K. The absence of weak links between grains was confirmed by the linear magnetic field dependence of the FC magnetization, measured at 0.25 mT, 0.5 mT, and 1.0 mT for the highest and the lowest pressures at $T=1.75$ K.

III. EXPERIMENTAL RESULTS AND DISCUSSION

Figure 1 shows the pressure dependence of the transition temperature T_c of ZrB_{12} obtained from magnetization measurements. T_c was taken from the linearly extrapolated $M(T)$ curves in the vicinity of T_c with $M=0$ line (see inset in Fig. 1). The linear fit yields $dT_c/dp = -0.0225(3)$ K/kbar. Note that this value is in good agreement with $dT_c/dp \approx -0.024$ K/kbar obtained indirectly by Lortz *et al.*⁴ from thermal expansion measurements.

The logarithmic volume derivative of T_c in the case of a strong coupled BCS superconductor can be described by the following equation:¹⁷

$$\frac{d \ln T_c}{d \ln V} = -B \frac{d \ln T_c}{dp} = (2A - 1) \gamma + A \frac{d \ln \eta}{d \ln V}, \quad (1)$$

where $A = 1.04 \lambda_{\text{el-ph}} (1 + 0.38 \mu^*) [\lambda_{\text{el-ph}} - \mu^* (1 + 0.62 \lambda_{\text{el-ph}})]^{-2}$ is a function of the electron-phonon coupling constant $\lambda_{\text{el-ph}}$ and the Coulomb pseudopotential μ^* ,¹⁷ B denotes the bulk modulus, $\gamma = -d \ln \langle \omega \rangle / d \ln V$ is the Grüneisen parameter, $\langle \omega \rangle$ is an average phonon frequency, $\eta \equiv N(E_f) \langle I^2 \rangle$ is the Hopfeld

parameter.¹⁹ $N(E_f)$ is the density of states at the Fermi level, and $\langle I^2 \rangle$ is the average squared electronic matrix element. Let us now apply Eq. (1) to an analysis of dT_c/dp data for ZrB_{12} superconductor. One should note, however, that not all the quantities needed for such analysis have been measured for ZrB_{12} . Thus we must account for “typical” values or values measured in similar compounds. The Hopfeld parameter η generally increases under pressure with $d \ln \eta / d \ln V \approx -1$ for s -, and p -metal superconductors¹⁸ and -3 to -4 for transition-metal (d -electron) superconductors.¹⁹ Since the band structure of zirconium dodecaboride near E_f (Ref. 20) as well as the pressure effect on T_c look like those of a simple metal, for the Hopfeld parameter we choose $d \ln \eta / d \ln V = -1$. In all conventional superconductors with low critical temperatures the values of μ^* range from 0.1 to 0.15 with most concentrated around 0.1 (see, e.g., Ref. 7). Assuming now $\mu^* = 0.1$, and taking $\lambda_{\text{el-ph}} \approx 0.67$ (Ref. 3) and $B = 2490$ kbar in analogy with UB_{12} ,²¹ for the Grüneisen parameter we get the value $\gamma \approx 2.83$. This value is in reasonable agreement with $\gamma \approx 3.3$ obtained at a temperature slightly above T_c by Lortz *et al.*⁴ based on thermal expansion measurements. Such an agreement also indicates that the chosen values for the volume derivative of the Hopfeld parameter and the chemical potential are reliable.

PE on the electron-phonon coupling constant $\lambda_{\text{el-ph}}$ can be determined by using the well-known McMillan equation,²²

$$\lambda_{\text{el-ph}} \propto \frac{N(E_f) \langle I^2 \rangle}{\langle \omega^2 \rangle}, \quad (2)$$

which leads to

$$\frac{d \ln \lambda_{\text{el-ph}}}{dp} = - \frac{1}{B} \frac{d \ln \eta}{d \ln V} - \frac{2\gamma}{B}. \quad (3)$$

Substitution of $\gamma = 2.83$ and $d \ln \eta / d \ln V = -1$ gives $d \ln \lambda_{\text{el-ph}} / dp = -0.19\%$ /kbar. A slightly larger value $d \ln \lambda_{\text{el-ph}} / dp = -0.22\%$ /kbar is obtained with $\gamma = 3.3$ from Ref. 4.

As a next step we studied the pressure effect on the magnetic field penetration depth λ . The temperature dependence of λ was calculated from the measured FC magnetization by using the Shoenberg formula,²³ modified for the known grain size distribution $N(R)$,²⁴

$$\chi = - \frac{3}{2} \int_0^\infty \left(1 - \frac{3\lambda}{R} \coth \frac{R}{\lambda} + \frac{3\lambda^2}{R^2} \right) g(R) dR \bigg/ \int_0^\infty g(R) dR, \quad (4)$$

where $\chi = M/HV$ is the volume susceptibility, V is the volume of the sample, R is the grain radius, and $g(R)$ is the analytical function describing the $N(R)R^3$ dependence (see inset in Fig. 2). The resulting temperature dependence $\lambda^{-2}(T)$ at ambient pressure is shown in Fig. 2. The reconstructed data were fitted with the empirical power-law $\lambda^{-2}(T) / \lambda^{-2}(0) = 1 - (T/T_c)^n$.²⁵ The fit yields $\lambda^{-2}(0) = 48.4(2) \mu\text{m}^{-2}$, $T_c = 6.078(5)$ K, and $n = 3.65(4)$. Note that the value of the power exponent n is close to “4”, which corresponds to a strong-coupled BCS superconductor.²⁶

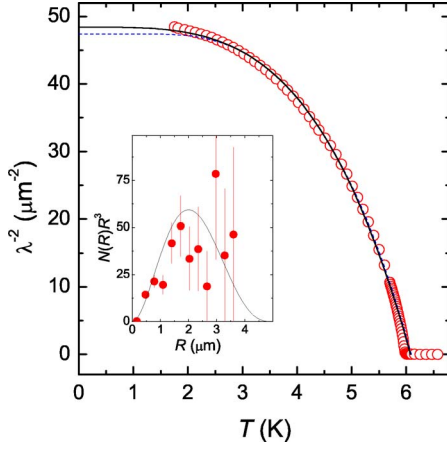


FIG. 2. (Color online) The temperature dependence of λ^{-2} calculated from the measured $\chi(T)$ by using Eq. (4). Lines represent fits with the BCS model (dashed line), and with a power law (solid line). See text for an explanation. The inset shows the volume fraction distribution $N(R)R^3$ of the ZrB_{12} powder determined from SEM photographs. The errors are statistical. The solid line represents the analytical $g(R)$ function used in Eq. (4).

In order to obtain the value of the superconducting gap Δ , the data have also been analyzed by means of the BCS model. For clean superconductor the temperature dependence of λ^{-2} can be described in the following way:²⁶

$$\frac{\lambda^{-2}(T)}{\lambda^{-2}(0)} = 1 + 2 \int_{\Delta(T)}^{\infty} \frac{\partial F}{\partial E} \frac{E}{\sqrt{E^2 - \Delta(T)^2}} dE, \quad (5)$$

where $F = [1 + \exp(E/k_B T)]^{-1}$ is the Fermi function, $\Delta(T) = \Delta_0 \cdot \tilde{\Delta}(T/T_c)$ represents the temperature dependence of the energy gap, and Δ_0 is the zero temperature value of the superconducting gap. $\tilde{\Delta}(T/T_c)$ is the normalized gap taken from Ref. 27. The best fit to the data using Eq. (5) gives $T_c = 6.09(2)$ K, $\lambda^{-2}(0) = 47.4(2)$ nm, and $\Delta_0 = 1.251(9)$ meV. The ratio $2\Delta_0/k_B T_c = 4.77(4)$ is found, suggesting that ZrB_{12} is a strong coupled BCS superconductor. Note that a rather close value $2\Delta_0/k_B T_c \approx 4.8$ has been obtained in point-contact spectroscopy³ and tunnelling⁶ experiments. On the other hand, a smaller value ≈ 3.7 has been reported by Lortz *et al.*⁴ using the heat-capacitance technique, thus suggesting a weak coupling strength. This difference has been already pointed out by Tsindlekht *et al.*⁶ It was explained by enhanced surface characteristics of the ZrB_{12} leading to rather different superconducting properties of bulk^{4,6,28} and surface.^{3,6,29,30} Our measurements were performed in the Meissner state, with the field penetrating on a distance λ from the surface and, therefore, give a value of the superconducting gap consistent with those reported in the surface sensitive experiments.^{3,6} To estimate the uncertainty in the absolute value of $\lambda(0)$ we used a procedure similar to that one described in Refs. 9 and 12. The temperature dependence of $\lambda(T)$ was calculated for $N(R) + \sqrt{N(R)}$ and $N(R) - \sqrt{N(R)}$ distributions. The fit of the resulting $\lambda(T)$ curves with the power law as well as with the BCS model gives $\lambda(0)$ in the range from 110 to 170 nm. Note that the values of the power ex-

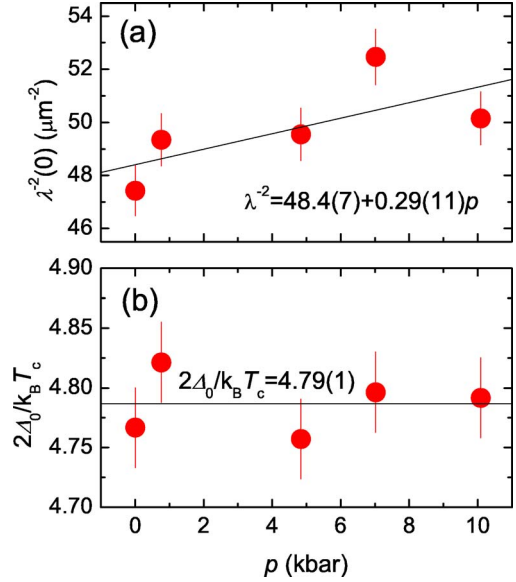


FIG. 3. (Color online) Pressure dependences of $\lambda^{-2}(0)$ (a) and $2\Delta_0/k_B T_c$ (b). The solid lines are fits with parameters shown in the figures.

ponent n (zero temperature superconducting gap Δ_0) were found to be well within error bars for each series of $\lambda(T)$ curves.

Figure 3(a) shows the pressure dependence of $\lambda^{-2}(0)$ obtained by fitting the reconstructed $\lambda(T)$ data at different pressures with the BCS model [Eq. (5)]. In these experiments we studied relative effects measured on the same sample in the same pressure cell. The main systematic error of these measurements comes from misalignments of the experimental setup occurring when the cell is removed from the SQUID magnetometer, to change the pressure, and put back again. This procedure was checked with a set of measurements at constant pressure. The systematic scattering of the magnetization data is about 0.3%, giving a relative error in $\lambda^{-2}(T)$ of about 3%. The reducing of the grain size with pressure was taken into account in $\lambda(T)$ calculation [Eq. (4)], by using the bulk modulus reported above. The linear fit yields $\lambda^{-2}(0) = 48.4(7) + 0.29(11)p$, implying that λ^{-2} increases under pressure with $d \ln \lambda^{-2}(0)/dp = 0.60(23) \% / \text{kbar}$ [see Fig. 3(a)].

To analyze the observed effect we used a procedure similar to the one described by Di Castro *et al.*¹⁰ There it was suggested that λ^{-2} increases under pressure because of two reasons, (i) band structure effects and (ii) renormalization of the electron-phonon coupling.¹⁰ Under the assumption of ellipsoidal or cylindrical Fermi surface the first one can be obtained as¹⁰

$$\frac{d \ln \lambda^{-2}(0)}{dp} = \frac{1}{3B} - \frac{d \ln N(E_F)}{dp} \approx \frac{1}{3B} - \frac{1}{B} \frac{d \ln \eta}{d \ln V}. \quad (6)$$

Here we used the fact that the pressure dependence of the electronic matrix element $\langle I^2 \rangle$ entering the Hopfield parameter η can usually be neglected.³¹ Hence, by setting $d \ln \eta / d \ln V \approx -1$, and $B = 2490$ kbar (see above) we obtain $d \ln \lambda^{-2}(0)/dp = 0.05 \% / \text{kbar}$.

The electron-phonon renormalized penetration depth reduces to $\lambda^{*-2}(0) = \lambda^{-2}(0)/(1 + \lambda_{\text{el-ph}})$,⁷ where $\lambda(0)$ is the bare quantity we have considered before. We have then

$$\frac{d \ln \lambda^{*-2}(0)}{dp} = - \frac{\lambda_{\text{el-ph}}}{1 + \lambda_{\text{el-ph}}} \frac{d \ln \lambda_{\text{el-ph}}}{dp}. \quad (7)$$

By substituting $\lambda_{\text{el-ph}} \approx 0.67$ (Ref. 3) and $d \ln \lambda_{\text{el-ph}}/dp \approx -0.2\%/kbar$ obtained above we get $d \ln \lambda^{*-2}(0)/dp \approx 0.08\%/kbar$.³² Thus the total pressure shift of $\lambda^{-2}(0)$ expected assuming conventional (adiabatic) coupling of the charge carriers to the lattice in ZrB_{12} is of the order of $0.13\%/kbar$. This value is more than three times smaller than the experimentally observed one $0.60(23)\%/kbar$. This implies that in addition to band structure effects and renormalization of the electron-phonon coupling there are other effects responsible for the increasing of $\lambda^{-2}(0)$ under pressure. Bearing in mind that λ measurements have been performed in a Meissner state, the observed dependence of λ on p can be explained suggesting that in ZrB_{12} close to the surface the coupling of the charge carriers to the lattice has a nonadiabatic character. Note that similar effects have been observed in $\text{YBa}_2\text{Cu}_3\text{O}_8$ that appears to be a highly nonadiabatic superconductor.¹²

The results on the zero temperature superconducting gap Δ_0 are summarized in Fig. 3(b), where the ratio $2\Delta_0/k_B T_c$ is plotted as a function of the pressure p . Δ_0 and T_c were obtained from the fit of $\lambda^{-2}(T, p)$ data by using Eq. (5). The solid line represents a fit by the relation $2\Delta_0/k_B T_c = \text{const}$ to the data. Bearing in mind that T_c scales linearly with pressure (see Fig. 1) the constant ratio can be understood in the frame

of the BCS theory, which predicts $2\Delta_0/k_B T_c = 3.52$. In the present study this ratio was found to be pressure independent within experimental errors, with mean value $4.79(1)$.

IV. CONCLUSIONS

In conclusion, we performed magnetization measurements in ZrB_{12} under hydrostatic pressure. A negative pressure effect on T_c with $dT_c/dp = -0.0225(3)$ K/kbar is observed. The electron-phonon coupling constant $\lambda_{\text{el-ph}}$ decreases with pressure with $d \ln \lambda_{\text{el-ph}}/dp \approx -0.20\%/kbar$. The magnetic field penetration depth λ measured in the Meissner state is largely determined by the surface characteristics.³³ λ was found to increase with pressure, with the pressure effect coefficient $d \ln \lambda^{-2}(0)/dp = 0.60(23)\%/kbar$. This coefficient is much larger than that one estimated theoretically within the adiabatic approximation. This can be explained suggesting that in ZrB_{12} , close to the surface, the coupling of the charge carriers to the lattice has a nonadiabatic character. The ratio $2\Delta_0/k_B T_c = 4.79(1)$ is found to be pressure independent and close to the strong coupling BCS value $4.8(1)$ reported in Refs. 3 and 6. The value of λ extrapolated to zero temperature and at $p=0$ was estimated to be $140(30)$ nm.

ACKNOWLEDGMENTS

The authors are grateful to S. Strässle for help during the preparation of this paper. This work was supported by the Swiss National Science Foundation and by the NCCR program Materials with Novel Electronic Properties (MaNEP) sponsored by the Swiss National Science Foundation.

¹A. B. Migdal, Sov. Phys. JETP **7**, 996 (1958); G. M. Eliashberg, *ibid.* **11**, 696 (1960).

²E. Cappelluti and L. Pietronero, Phys. Status Solidi B **242**, 133 (2005).

³D. Daghero, R. S. Gonnelli, G. A. Umbarino, A. Calzolari, V. Dellarocca, V. A. Stepanov, V. B. Filippov, and Y. B. Paderno, Supercond. Sci. Technol. **17**, S250 (2004).

⁴R. Lortz, Y. Wang, S. Abe, C. Meingast, Yu. B. Paderno, V. Filippov, and A. Junod, Phys. Rev. B **72**, 024547 (2005).

⁵B. T. Matthias, T. H. Geballe, K. Andres, E. Corenzwit, G. W. Hull, and J. P. Maita, Science **159**, 530 (1968).

⁶M. I. Tsindlekht, G. I. Leviev, I. Asulin, A. Sharoni, O. Millo, I. Felner, Y. B. Paderno, V. B. Filippov, and M. A. Belogolovskii, Phys. Rev. B **69**, 212508 (2004).

⁷J. P. Carbotte, Rev. Mod. Phys. **62**, 1027 (1990).

⁸P. Paci, M. Capone, E. Cappelluti, S. Ciuchi, C. Grimaldi, and L. Pietronero, Phys. Rev. Lett. **94**, 036406 (2005).

⁹R. Khasanov, D. G. Eshchenko, J. Karpinski, S. M. Kazakov, N. D. Zhigadlo, R. Brütsch, D. Gavillet, D. Di Castro, A. Shengelaya, F. La Mattina, A. Maisuradze, C. Baines, and H. Keller, Phys. Rev. Lett. **93**, 157004 (2004).

¹⁰D. Di Castro, R. Khasanov, C. Grimaldi, J. Karpinski, S. M. Kazakov, R. Brütsch, and H. Keller, Phys. Rev. B **72**, 094504 (2005).

¹¹D. Di Castro, M. Angst, D. G. Eshchenko, R. Khasanov, J. Roos, I. M. Savić, A. Shengelaya, S. L. Budko, P. C. Canfield, K. Conder, J. Karpinski, S. M. Kazakov, R. A. Ribeiro, and H. Keller, Phys. Rev. B **70**, 014519 (2004).

¹²R. Khasanov, J. Karpinski, and H. Keller, J. Phys.: Condens. Matter **17**, 2453 (2005).

¹³G. M. Zhao, M. B. Hunt, H. Keller, and K. A. Müller, Nature (London) **385**, 236 (1997); J. Hofer, K. Conder, T. Sasagawa, G.-M. Zhao, M. Willemin, H. Keller, and K. Kishio, Phys. Rev. Lett. **84**, 4192 (2000); R. Khasanov, D. G. Eshchenko, H. Luetkens, E. Morenzoni, T. Prokscha, A. Suter, N. Garifanov, M. Mali, J. Roos, K. Conder, and H. Keller, *ibid.* **92**, 057602 (2004); R. Khasanov, A. Shengelaya, E. Morenzoni, K. Conder, I. M. Savić, and H. Keller, J. Phys.: Condens. Matter **16**, S4439 (2004).

¹⁴Y. B. Paderno, A. B. Liashchenko, V. B. Filippov, and A. V. Dukhnenko, *Proceedings of the International Conference on Science for Materials in the Frontier of the Centuries: Advantages and Challenges* (IPMS NASU, Kiev, 2002), p. 347).

¹⁵V. A. Gasparov, N. S. Sidorov, and I. I. Zver'kova, cond-mat/0508151 (unpublished).

¹⁶T. Straessle, Ph.D. thesis, ETH, Zurich, 2001.

¹⁷T. Tomita, J. J. Hamlin, J. S. Schilling, D. G. Hinks, and J. D. Jorgensen, Phys. Rev. B **64**, 092505 (2001).

- ¹⁸J. S. Schilling and S. Klotz, *Physical Properties of High Temperature Superconductors, Vol. III* (World Scientific, Singapore, 1992), p. 59.
- ¹⁹J. J. Hopfeld, *Physica (Utrecht)* **55**, 41 (1971).
- ²⁰I. R. Shein and A. L. Ivanovskii, *Phys. Solid State* **45**, 1429 (2003).
- ²¹J.-P. Dancausse, E. Gering, S. Heathman, U. Benedict, L. Gerward, S. S. Olsen, and F. Hulliger, *J. Alloys Compd.* **189**, 205 (1992).
- ²²W. L. McMillan, *Phys. Rev.* **167**, 331 (1968).
- ²³D. Shoenberg, *Proc. R. Soc. London, Ser. A* **175**, 49 (1940).
- ²⁴A. Porch, J. R. Cooper, D. N. Zheng, J. R. Waldram, A. M. Campbell, and P. A. Freeman, *Physica C* **214**, 350 (1993).
- ²⁵P. Zimmermann, H. Keller, S. L. Lee, I. M. Savić, M. Warden, D. Zech, R. Cubitt, E. M. Forgan, E. Kaldis, J. Karpinski, and C. Krüger, *Phys. Rev. B* **52**, 541 (1995).
- ²⁶M. Tinkham, *Introduction to Superconductivity* (Krieger, Malabar, FL, 1975).
- ²⁷B. Mühlshlegel, *Z. Phys.* **155**, 313 (1959).
- ²⁸Y. Wang, R. Lortz, Yu. Paderno, V. Filippov, S. Abe, U. Tutsch, and A. Junod, *Phys. Rev. B* **72**, 024548 (2005).
- ²⁹G. I. Leviev, V. M. Genkin, M. I. Tsindlekht, I. Felner, Y. B. Paderno, and V. B. Filippov, *Phys. Rev. B* **71**, 064506 (2005).
- ³⁰V. A. Gasparov, N. S. Sidorov, I. I. Zver'kova, S. S. Khassanov, and M. P. Kulakov, *JETP* **101**, 98 (2005).
- ³¹B. Lorenz and C. W. Chu, in *Frontiers in Superconducting Materials*, edited by A. V. Narlikar (Springer, Berlin, Heidelberg, 2005), p. 459.
- ³²Assuming for $\lambda_{\text{el-ph}}$ the surface enhanced value 1.9 (see introduction) we obtain a slightly larger value $d \ln \lambda_{\text{el-ph}} / dp \approx 0.13\% / \text{kbar}$.
- ³³Generally properties within 140 nm from the surface are assumed to be bulk. However, difference between “bulk” and “surface” notations depends strongly on the physical phenomenon studied. The length where superconducting properties are changed is the coherence length. It follows from direct magnetization measurements by Tsindlekht *et al.* (Ref. 6) and Wang *et al.* (Ref. 28) that in the case of ZrB_{12} the coherence length is of the order of the magnetic penetration depth. That is why we consider the properties within the depth of 140 nm as superconducting surface ones.