Superconducting gap anisotropy of LuNi$_2$B$_2$C thin films from microwave surface impedance measurements

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Surface impedance measurements of LuNi$_2$B$_2$C superconducting thin films as a function of temperature have been performed down to 1.5 K and at 20 GHz using a dielectric resonator technique. The magnetic penetration depth closely reproduces the standard BCS result, but with a reduced value of the energy gap at low temperature. These data provide evidence for an anisotropic *s*-wave character of the order parameter symmetry in LuNi$_2$B$_2$C. From the evaluation of the real part of complex conductivity, we have observed constructive (type II) coherence effects in the electromagnetic absorption below T_c.

The rare earth R borocarbides with the generic formula RNi$_2$B$_2$C are believed to be BCS-type superconductors. They have a moderately large density of states at the Fermi level, and it is generally agreed that the electron-phonon interaction is indeed the underlying mechanism for superconductivity.[1]

The members of this family are either antiferromagnetic or nonmagnetic at low temperatures. Nonmagnetic compounds with R = Y and Lu exhibit fairly high T_c values of about 15–16 K. Magnetism coexists with superconductivity for R = Dy, Ho, Er, and Tm, whereas only antiferromagnetic order occurs for R = Pr, Nd, Sm, Gd, and Tb. The antiferromagnetic ordering, and its competition (and even coexistence) with superconductivity, is conjectured to be driven by a nesting feature in the Fermi surface (FS).[2] In the Lu compound, the $4f$ band is fully occupied and therefore it is not magnetic. Since the f electrons occupy localized corelike states, the Fermi surface is expected to be similar to that of the other compounds.

A study of the Y and Lu compounds is therefore a prerequisite for the understanding of their magnetic counterparts, since they are free from the complications introduced by the presence of magnetism, and ideal for investigating the origin of superconductivity in borocarbides.

Even if, from the available experimental data, a dominating electron-phonon mediated mechanism seems to be a quite natural assumption, still there are a number of interesting properties that are not fully clarified. Among them, the unusual temperature and field dependence of the electronic specific heat[3] and the upward curvature of $H_{c2}(T)$ data close to T_c.[4] During the years, these anomalies have been interpreted by different authors as hints for unconventional (*d*-wave) superconductivity.[5] Pair-breaking effects caused by localized magnetic moments have been also invoked to explain the unusual temperature dependence of the upper critical field.[6] The presence of magnetic scattering is predicted to have an impact also on the low-temperature behavior of penetration depth λ of these compounds.

With the aim of shedding light on the origin of such anomalies, we report here on precise measurements of the microwave surface impedance of LuNi$_2$B$_2$C superconducting thin films, performed at 20 GHz by means of a sapphire dielectric resonator. The focus of this study is mainly on the temperature behavior of the magnetic penetration depth. It is well known in fact that $\lambda(T)$ at low temperatures may be used as a very sensitive probe of the symmetry of the order parameter.[7]

Very few microwave measurements have been performed since now on borocarbides, and only on the R = Y, Er, Tm, and Ho compounds of the family, leading to controversial results. Antiferromagnetic transitions at zero field were not always seen, but anomalies in the low-temperature surface impedance were clearly observed for ErNi$_2$B$_2$C, HoNi$_2$B$_2$C, and TmNi$_2$B$_2$C.[8] The temperature dependence of the penetration depth of YNi$_2$B$_2$C was found to disagree[8] or to be consistent with BCS expectations.[9] Results found for ErNi$_2$B$_2$C thin films supported a view where magnetic pair-breaking affects the superconducting density of states.[9]

LuNi$_2$B$_2$C thin films are synthesized by a dc magnetron sputtering technique in ultrahigh vacuum from a stoichiometric 5-cm-diameter target prepared by arc-melting. Samples have been deposited on different substrates, with best results obtained using single-crystal (100) MgO. In the following, however, we will report on films grown on single-crystal sapphire $10 \times 10 \times 0.5$-mm^3 substrates, because of their lowest microwave dielectric losses. Details of the procedure have been already reported elsewhere.[10] Four-point resistivity probe indicates a resistivity ρ of the order of 100 $\mu\Omega$ cm or larger, a residual resistivity ratio $r_R = \rho(300 \text{ K})/\rho(T_c) \approx 3$, a critical temperature T_c of about 15 K, ΔT_c (90–10 %) values ranging between 0.4 and 0.8 K. Inductive measurements show T_c values slightly (about 0.5 K) lower, but with similar transition widths. Structural characterization by a standard x-ray diffractometry shows a single phase growth with predominant c-axis orientation normal to the substrate plane. θ-2θ spectra evidence also the presence of a small percentage of Lu$_2$O$_3$ oxide phase. Rocking curve measurement of the (002) peak gives a FWHM$\sim 1.4°$.

We have performed measurements of the magnetic penetration depth λ and surface resistance R_s as a function of temperature on two optimized samples. Each sample consists of two films, 300 nm thick, produced in the same deposition run, having therefore nominally the same structural, trans-
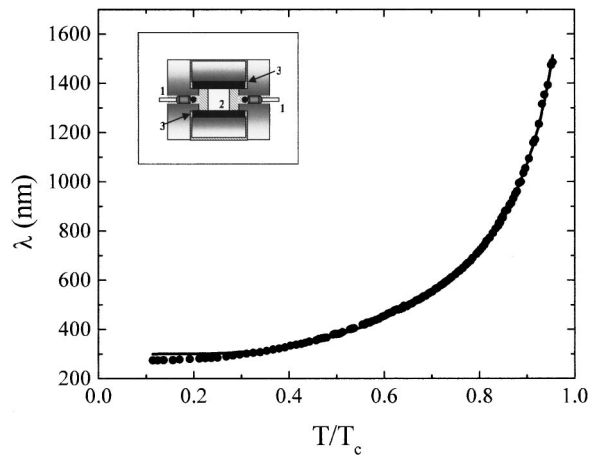
FIG. 1. Temperature dependence of the penetration depth λ and fit to the BCS theory (continuous line). In the inset, a schematic drawing of the dielectric resonator operating at 20 GHz: coupling ports (1), sapphire puck (2), superconducting films (3).

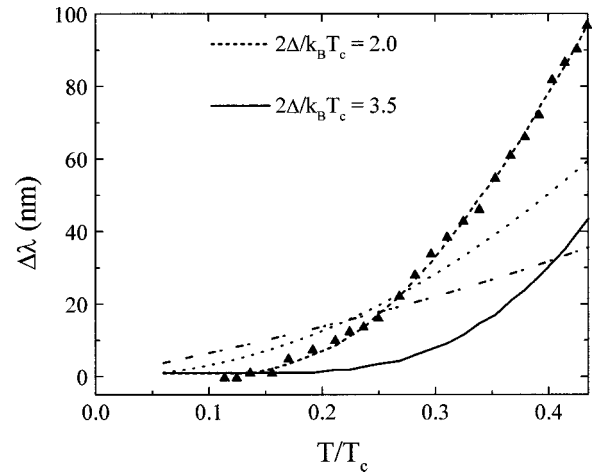

FIG. 2. $\lambda(T) - \lambda(0)$ as a function of the reduced temperature for $T < T_c/2$. Continuous and dashed lines represent the fit using the BCS theory and $\Delta(0) = 2.1$ and 1.2 meV, respectively, the dot-dashed line is the result assuming the presence of correlated magnetic impurities (see text), the dotted curve expresses the quadratic dependence expected from a dirty *d*-wave model.

port, and superconducting properties. In the following, we will show the results of measurements undertaken on the best of the two samples from T_c down to 1.5 K. Data for the second sample follow a similar behavior.

The surface impedance $Z_s = R_s + jX_s = R_s + j\mu_0\omega\lambda$, where ω is the angular frequency, is investigated by means of a dielectrically loaded cylindrical resonator[11] operating at 20 GHz. The TE_{011} field is excited and detected by two semi-rigid coaxial cables, each having a small loop at the end, and the resonant frequency f and Q factor are measured in the transmission mode and in unloaded condition. In the inset of Fig. 1, a schematic drawing of the experimental setup is presented.

In Fig. 1 the penetration depth data, extracted from the resonant frequency measurements, are displayed as a function of temperature. The data are fitted to the BCS theory, using the Halbritter code,[12] shown as a continuous curve in the graph. The coherence length ξ_0, the critical temperature T_c, and the mean free path l are set as input values, taken either from literature (ξ_0) or from transport measurements (T_c and resistivity ρ), and the London penetration depth at zero temperature $\lambda_L(0)$ is extracted from the numerical fit. The strong coupling ratio $2\Delta(0)/k_BT_c$ is taken to be the BCS value 3.5, consistent with previous findings.[13] All the parameters are reported in Table I. Data agree well with expectations for a weak-coupled *s*-wave superconductor, but at the lowest temperatures they show a significant discrepancy. This is more clearly displayed in Fig. 2, where the quantity $\Delta\lambda(T) = \lambda(T) - \lambda(0)$ is plotted as a function of temperature for $T/T_c < 0.5$. The BCS curve using parameters taken from

Table I is represented by the continuous line; in this graph, experimental points start to depart from the zero temperature value, and from the BCS expectations, already at $T/T_c \approx 0.15$. One can see that a good agreement between theory and data can be achieved only using a reduced value of the energy gap, $2\Delta(0)/k_BT_c = 2.0 \pm 0.2$ (dashed line). This is, to our understanding, striking evidence for the existence of a strongly anisotropic *s*-wave gap in the LuNi$_2$B$_2$C borocarbide. Indeed, in a band structure study Dugdale *et al.*[14] showed experimentally a rather complicated Fermi surface for this compound, revealing the presence of a sheet capable of nesting. The observed anisotropy was consistent with the observation of a square flux-line lattice and the unusual upper critical field behavior reported in previous experiments. Recent photoemission experiments[15] in the parent compound YNi$_2$B$_2$C provided also spectroscopic evidence for an anisotropic *s*-wave gap. It is worthwhile to mention, however, that in our case the gap anisotropy, $\Delta(0)_{max}/\Delta(0)_{min} \approx 1.75$, is more pronounced than results from other measurements: electronic Raman spectroscopy,[16] for example, shows a maximum anisotropy of 10%.

Of course, the presence of low-lying energy states at very low temperatures can be also related to other effects, like to somehow depressed superconductivity on the sample surface. However, since $t \lesssim \lambda(0)$, what the surface impedance is probing here is actually the "bulk" electrodynamic response of the LuNi$_2$B$_2$C films.

For completeness, we have also analyzed the penetration depth data taking into account the effect of correlation between magnetic impurities at low temperature, which gives rise to a spin-flip scattering frustration as T goes to zero.[6] This is accomplished introducing a temperature-dependent magnetic scattering amplitude $\Gamma(T) = \Gamma_0(1 + \beta T/\theta)/(1 + T/\theta)$, where $\Gamma_0 = \Gamma(0)$, θ is a characteristic temperature describing the effects of correlation, β is a parameter describing the relative change in Γ caused by correlation. In this model Δ strongly depends on T even in the low-

TABLE I. BCS fitting parameters for the experimental $\lambda(T)$ data of a LuNi$_2$B$_2$C sample.

T_c (K)	$\Delta(0)$ (meV)	$\lambda_L(O)$ (nm)	ξ_0 (nm)	l^a (nm)
14.2	2.1	275 ± 20	7	2

[a]From Ref. 24.

temperature region, since the decrease in the effectiveness of pair breaking translates in an increase of the pairing amplitude ("recovery" effect). The combined effect of $\Delta(T)$ and $\Gamma(T)$ gives rise to an almost linear dependence of the magnetic penetration depth near $T=0$ K, displayed as a dot-dashed line in Fig. 2. Using the specific values of parameters β, θ, and Γ_0 taken from Ref. 6, one can see that the model prediction can be hardly reconciled with the experimental data.

It has been recently proposed an interpretation of a number of unusual features presented by borocarbides in terms of a three-dimensional version of $d_{x^2-y^2}$ superconductivity. The experimentally observed saturation of the penetration depth at the lowest temperature however argues strongly against the possibility of nodes in the gap function of LuNi$_2$B$_2$C. For the sake of comparison, in Fig. 2 we have also plotted the quadratic dependence expected for a dirty $d_{x^2-y^2}$ superconductor (dotted line).[17]

From quality factor measurements we have also obtained the surface resistance value as a function of temperature. Assuming the usual f^2 scaling, the comparison of the measured R_s with previous results on both single crystals and thin films of parent compounds evidences values that are between one and two orders of magnitude lower. Owing also to the good structural and surface quality of our samples, this makes us confident that the observed microwave dissipation is mainly intrinsic in origin. In spite of this, data cannot be consistently fitted in the overall temperature range within a BCS framework using the same parameters shown in Table I, since the level of losses is still too high. Surface impurities and other structural imperfections may of course affect the surface resistance in various ways. We speculate however that the observed losses may be an evidence of an unusual number of "unpaired" charge carriers arising from the same sheet in the FS that is responsible for the anisotropy. Indeed, for T less than $T_c/2$ the surface resistance behavior can be described using the standard BCS exponential dependence

$$R_s - R_{res} \approx A \sqrt{\Delta/k_B T} e^{-\Delta/k_B T}. \qquad (1)$$

where R_{res} is the residual surface resistance and A is a phenomenological parameter. The value found for the ratio $2\Delta(0)/k_B T_c$ lies between 1.5 and 1.8, depending mainly on the value chosen for the constant term R_{res}, in fair agreement therefore with penetration depth results at low temperatures. In Fig. 3 the quantity $R_s - R_{res}$ is displayed, together with the low-temperature BCS fit $[2\Delta(0)/k_B T_c = 1.6]$. In this picture, losses can be ascribed to the existence of remnant scattering states due to the anisotropy in the energy gap or to the presence of strong electron-electron scattering in the nested regions of the FS.[18]

From the surface resistance and magnetic penetration depth data, it is then possible to extract the temperature dependence of the complex conductivity $\sigma = \sigma_1 - j\sigma_2$.[19] Since $X_s \gg R_s$ in almost all the temperature range, $\sigma_2 \approx (\mu_0 \omega \lambda^2)^{-1}$ retaining of course the BCS functional dependence observed for the magnetic penetration depth. σ_1 first starts to increase below the critical temperature, reaching a broad maximum at about $0.8T_c$, and then decreases to a
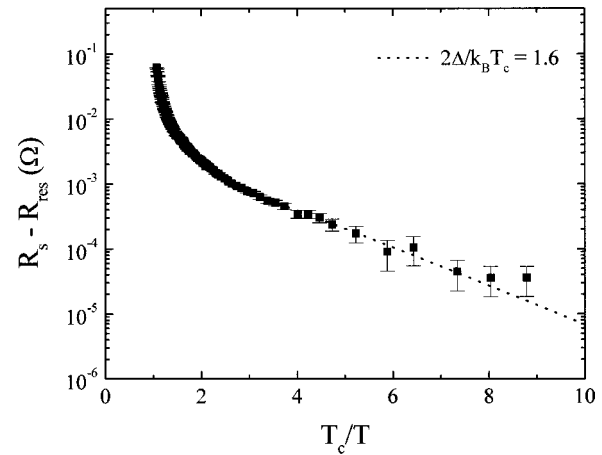

FIG. 3. Temperature dependence of the BCS contribution to the surface resistance $R_s - R_{res}$ at 20 GHz, and fit to the BCS theory (dotted line) at low temperature with a reduced gap value $[\Delta(0) = 1.0 \text{ meV}]$.

constant value at low temperatures. Subtracting in the analysis of the data the residual value R_{res} found from the fit of surface resistance, one can force the real part of conductivity to reach a zero value at $T=0$ K, which is equivalent to forcing the quasiparticle contribution to approach zero with decreasing temperature (Fig. 4). This procedure, however, does not change the nonmonotonous dependence displayed by the $\sigma_1(T)$ data. The increase in the real part of conductivity below T_c has to be related to the development of a singularity in the density of states at the gap edge, which leads therefore to the observation of a type-II coherence (Hebel-Slichter) peak.

The experimental results are in good agreement with the dirty limit ($l \ll \xi_0$) BCS weak-coupling theory. Indeed, in Fig. 4 we have compared the conductivity data with the BCS expectation (dotted line) computed using a modified two-fluid model[20] and the standard $2\Delta(0)/k_B T_c = 3.5$ ratio. In spite of the observed discrepancy at very high and very low
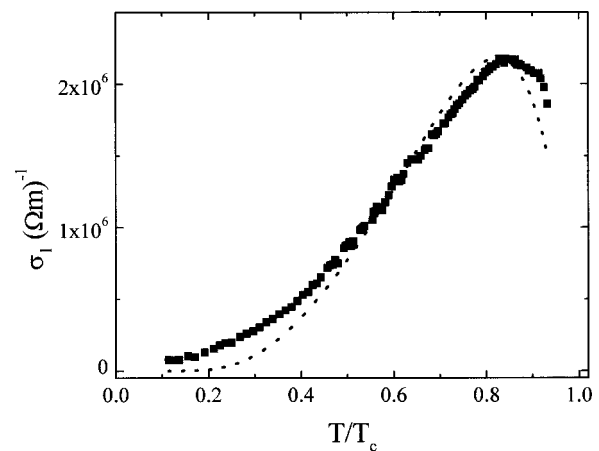

FIG. 4. Real part of the complex conductivity σ_1 as a function of temperature and fit to the BCS weak-coupling dependence (dotted line).

temperature (the model loses accuracy close to T_c, and as T goes to zero in our data the energy gap is reduced), the agreement between the curve and measurements, in terms of position and intensity of the coherence peak, is remarkable.

Most NMR studies till now reported the absence of the Hebel-Slichter peak.[21] To our knowledge, to date there is only one report from a ^{13}C NMR study of YNi_2B_2C poly-crystalline samples where a small enhancement in the spin-lattice relaxation time temperature dependence just below T_c has been observed.[22]

In conclusion, data taken from surface impedance measurements of $LuNi_2B_2C$ superconducting thin films show the following:

• The full consistency with a conventional *s*-wave phonon mediated framework. No evidence of *d*-wave symmetry has been found, nor magnetic impurity correlation effects have been proved to describe our experimental findings.

• The existence of a strong anisotropy in the energy gap, revealing itself in the low-temperature dependence of both the real and imaginary part of Z_s. This is a strong support to a common view[14,15,23] that most unusual features observed in borocarbides may be related to the presence of deep minima in the gap function.

• The evidence of a clear peak in the $\sigma_1(T)$ dependence below T_c to be associated with type-II coherence effects in the electromagnetic absorption. This is a further direct confirmation that $LuNi_2B_2C$ behaves as a conventional BCS *s*-wave superconductor.

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