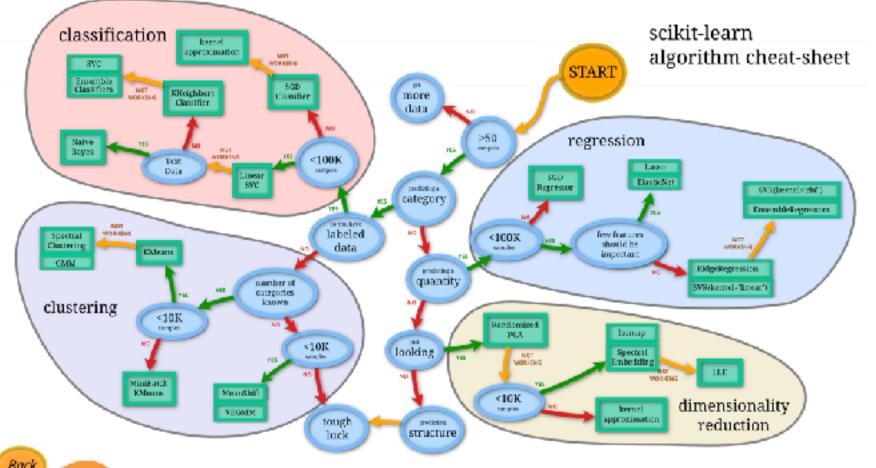
## DATA SCIENCE SYD DAT 6

Week 4 - Clustering Wednesday 2nd November

- 1. Motivation / Review
- 2. What is Clustering?
- 3. What is K-Means and how does it work?
- 4. Lab
- 5. Discussion



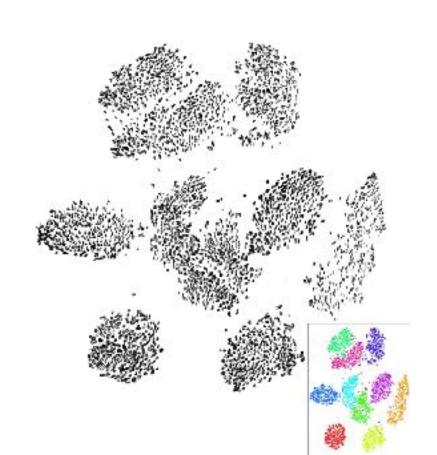
# WHAT IS CLUSTERING AND WHY DO IT?





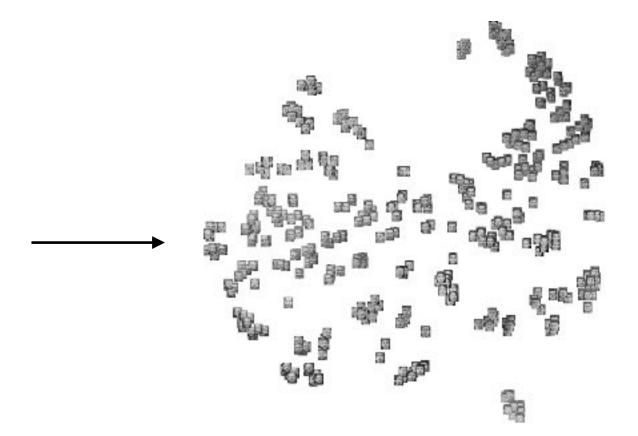
## **MNIST**

1 1 5 4 3 7 5 3 6 5 5 5 3 0 0



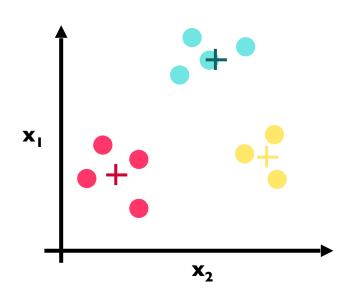
## **Olivetti Faces**





CLUSTERING 8

- What is a Cluster?
- Why would we do this?
- What is K-Means?



Recall unsupervised learning is when we are trying to find interesting patterns or groups in our data. We don't have a variable we are trying to predict (a Y value).

Clustering aims to discover subgroups in our data where the points are similar to each other. So we have a collection of groups and all points belonging to the same group are similar. Points in different groups are different to each other.

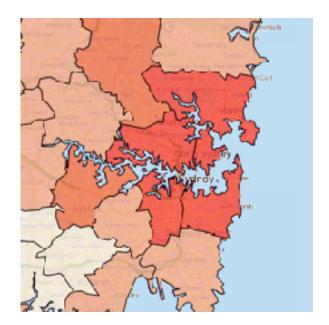
We have to decide what variables we will construct the groups on. What makes them different (or similar)?

To enhance our understanding of a dataset by dividing the data into groups.

Clustering provides a layer of abstraction from individual data points.

The goal is to extract and enhance the natural structure of the data

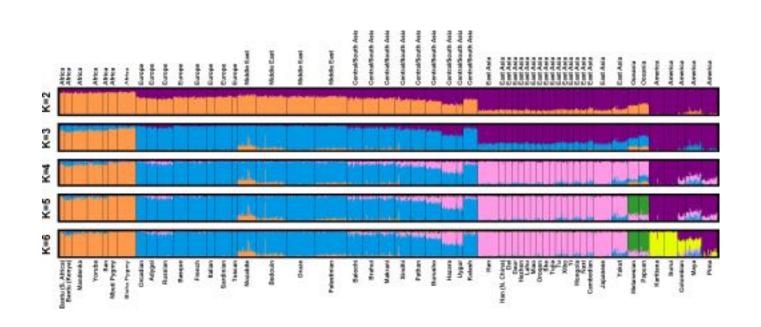
Marketing teams might want to group customers into like groups as a way of summarising the data



Financial groups may want to group transactions into like groups as a way to find unusual payments



## Genetics data can be clustered to identify ancestry



## HOW DO WE CLUSTER DATA?

1) Choose k initial centroids (note that k is an input)

- 2) For each point:
  - find distance to each centroid
  - assign point to nearest centroid
- 3) Recalculate centroid positions
- 4) Repeat steps 2-3 until stopping criteria met

## STEP 1 - CHOOSE CENTROIDS

## There are several options:

- randomly (but may yield divergent behavior)
- perform alternative clustering task, use resulting centroids as initial k-means centroids
- start with global centroid, choose point at max distance, repeat (but might select outlier)

The similarity criterion is determined by the measure we choose.

In the case of k-means clustering, the similarity metric is the **Euclidian distance**:

$$d(x_1, x_2) = \sqrt{\sum_{i=1}^{N} (x_{1i} - x_{2i})^2}$$

## **STEP 3 - RECALCULATE CENTROID POSITIONS**

Q: How do we re-compute the positions of the centres at each iteration of the algorithm?

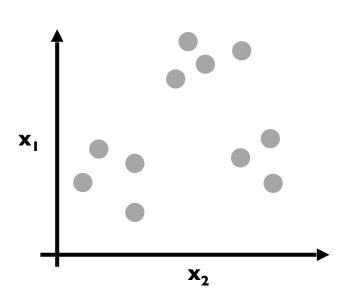
A: By calculating the centroid (i.e., the geometric centre)

We iterate until some stopping criteria are met; in general, suitable convergence is achieved in a small number of steps.

Stopping criteria can be based on the centroids (eg, if positions change by no more than  $\epsilon$ ) or on the points (eg, if no more than x% change clusters between iterations).

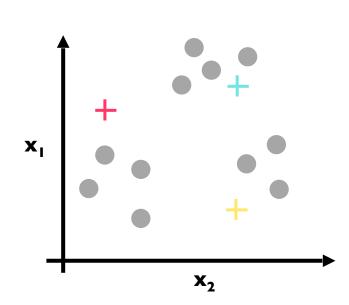
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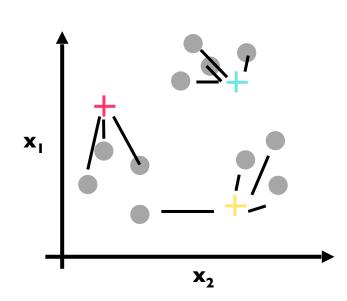


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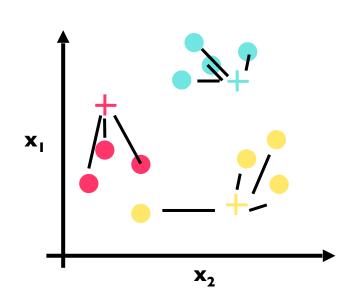


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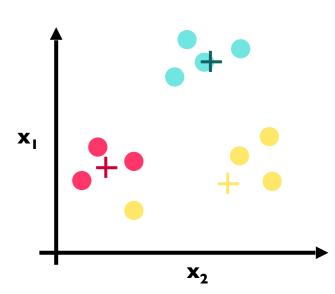
3) Recalculate centroid positions



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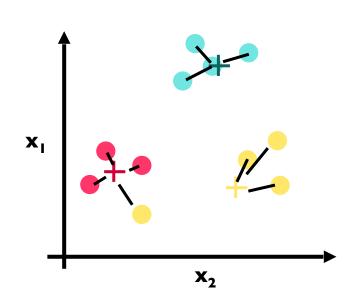
3) Recalculate centroid positions





1) Choose k initial centroids

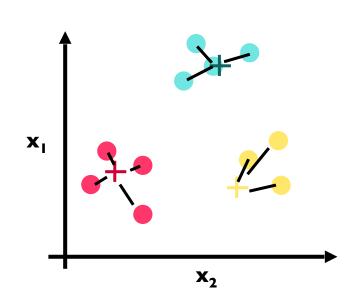
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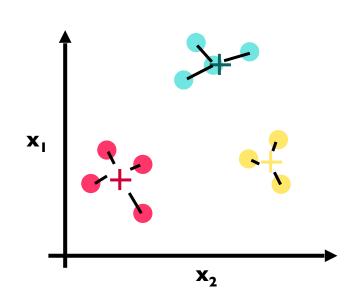
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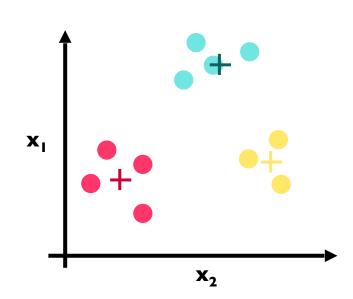
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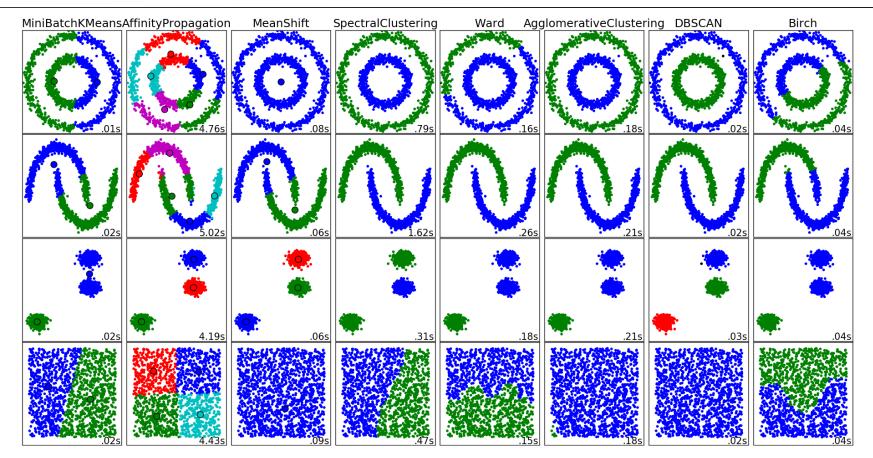


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## HOW DO WE KNOW OUR CLUSTERS ARE ANY GMM2

In general, k-means will converge to a solution and return a partition of k clusters, even if no natural clusters exist in the data.

We will look at two validation metrics useful for partitional clustering, **cohesion** and **separation**.

Cohesion measures clustering effectiveness within a cluster.

$$\hat{C}(C_i) = \sum_{x \in C_i} d(x, c_i)$$

Separation measures clustering effectiveness between clusters.

$$\hat{S}(C_i, C_j) = d(c_i, c_j)$$

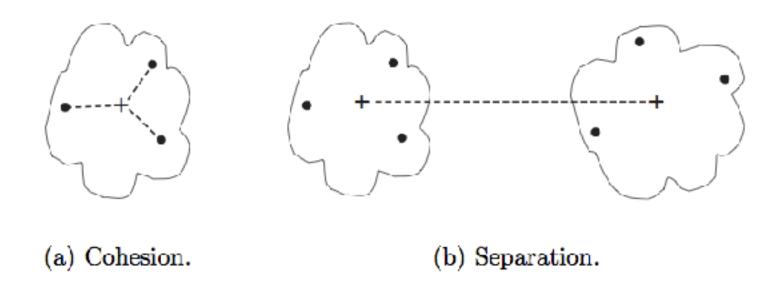


Figure 8.28. Prototype-based view of cluster cohesion and separation.

One useful measure than combines the ideas of cohesion and separation is the silhouette coefficient. For point  $x_i$ , this is given by:

$$SC_i = \frac{b_i - a_i}{max(a_i, b_i)}$$

such that:

 $a_i$  = average in-cluster distance to  $x_i$ 

 $b_{ij}$  = average between-cluster distance to  $x_i$ 

 $b_i = \min_j(b_{ij})$ 

The silhouette coefficient can take values between -1 and 1.

In general, we want separation to be high and cohesion to be low. This corresponds to a value of SC close to +1.

A negative silhouette coefficient means the cluster radius is larger than the space between clusters, and thus clusters overlap The silhouette coefficient for the cluster  $C_i$  is given by the average silhouette coefficient across all points in  $C_i$ :

$$SC(C_i) = \frac{1}{m_i} \sum_{x \in C_i} SC_i$$

The overall silhouette coefficient is given by the average silhouette coefficient across all clusters:

$$SC_{total} = \frac{1}{k} \sum_{1}^{k} SC(C_i)$$

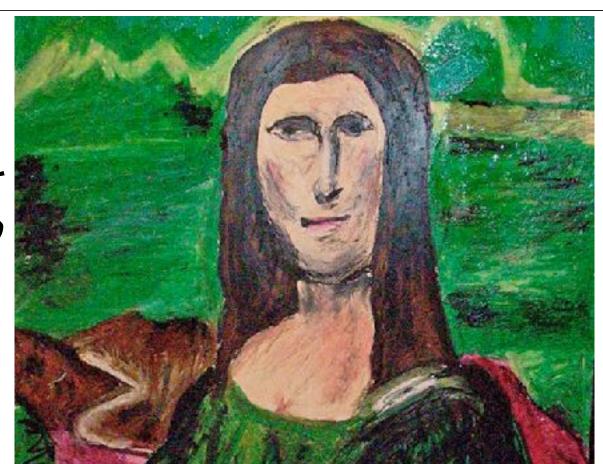
One useful application of cluster validation is to determine the best number of clusters for your dataset.

Q: How would you do this?

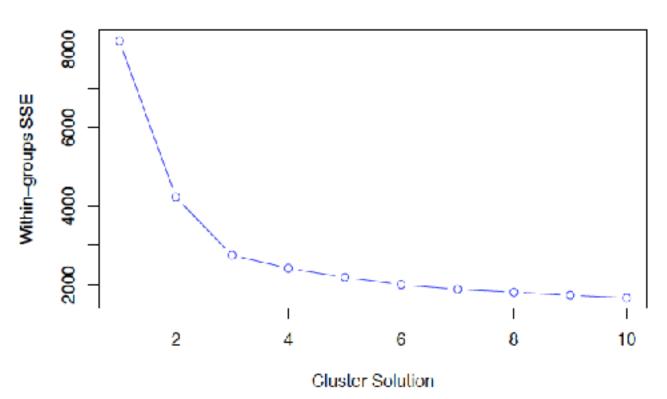
A: By computing the SSE or SC for different values of k.

Ultimately, cluster validation and clustering in general are suggestive techniques that rely on human interpretation to be meaningful.









## **Strengths:**

K-means is a popular algorithm because of its computational efficiency and simple and intuitive nature.

### Weaknesses:

However, K-means is highly scale dependent, and is not suitable for data with widely varying shapes and densities.

## DATA SCIENCE PART TIME COURSE

## LAB

## **SYNCHING YOUR FORK WITH THE COURSE REPO**

- 1. re-name your labs with lab\_name.<yourname>.ipynb (to prevent a conflict)
- 2. cd <path to the root of your SYD\_DAT\_6 local repo>
- 3. commit your changes ahead of sync
  - git status
  - git add.
  - git commit -m "descriptive label for the commit"
  - git status
- 4. download new material from official course repo (upstream) and merge it
  - git checkout master (ensures you are in the master branch)
  - git fetch upstream
  - git merge upstream/master



## DATA SCIENCE

## HOMEWORK

### Homework

→ Homework 2 – Due Monday 14th of November

### Read the following

- Chapter 10.3 of Introduction to Statistical Learning Clustering Methods in Introduction to Statistical Learning (15 pages)
- Chapter 8.1 of Introduction to Statistical Learning The Basics of Decision Trees