

Complexity for genData():

In this function, the loop runs n times and everytime it inserts a random value in a vector. So, complexity of loop is $O(n)$ and complexity of random number generating is constant. So, the overall complexity of this function is $O(n)$.

Complexity for makeBST():

The for loop runs until the list is not empty which is n times. The complexity of this loop is $O(n)$. Inside the for loop, it inserts the list in binary search tree by calling the insert function. Complexity for insert in BST is $\log(n)$ because half the node every time and insert value in the tree in the best case. So, total complexity for best case is $O(n \log n)$.

Complexity for print()

This function calls two functions, inorder and preorder. The complexity of inorder is $O(n)$ because it goes through every node in a BST and prints the data. The complexity for preorder is also same. So, the total complexity for this function is $O(n) + O(n) = O(n)$.

Complexity for height()

This function calls getHeight function in bst. The complexity of this function is

$$\begin{aligned} T(n) &= 2T(n/2) + c && [c \text{ is constant}] \\ &= 2(2T(n/4) + c) + c \\ &\dots\dots \\ &= 2^k T(n/2^k) + n(c) && [T(n/2^k) = T(1) = 1] \\ &= \log(n) + n(c) \\ &= n \end{aligned}$$

So, complexity for this function is $O(n)$