

Large network structure and random graph models

You are given a selection of **networks of various size and origin**.

- [Zachary's karate club network](#) (34 nodes)
- [Davis's southern women network](#) (32 nodes)
- [Lusseau's bottlenose dolphins network](#) (62 nodes)
- [Ingredients network by common compounds](#) (1,525 nodes)
- [Map of Darknet from Tor network](#) (7,178 nodes)
- [Human protein-protein interaction network](#) (19,634 nodes)
- [Internet map of autonomous systems](#) (75,885 nodes)
- [Amazon product copurchase network](#) (262,111 nodes)
- [Paper citation network of APS](#) (438,943 nodes)
- [Small part of Google web graph](#) (875,713 nodes)
- [Road/highway network of Texas](#) (1,379,917 nodes)

All networks are available in Pajek format.



I. Toy network construction and Pajek format

1. Using your library, **construct small toy network** with a few nodes and edges. Print out its name, and the number of nodes and edges.
2. Using the methods provided by your library, **read in all networks** above and print out their size. What

is the size of the largest network you are able to read in say half a minute?

II. Network statistics, connectivity, distances and clustering

1. Compute **basic statistics of networks** above. These are the number of nodes n , the number of isolated nodes n_0 , the number of edges m , the number of self-edges or loops m_0 , the average node degree $\langle k \rangle = 2m/n$ and the undirected density $\rho = \langle k \rangle / (n - 1)$. Are the results expected?

Computational complexity is \leq linear $\mathcal{O}(m)$ and applicable to any network that fits in your memory.

2. Using depth-first search methods provided by your library, compute **connected components of networks** above. Print out the fraction of nodes in the largest connected component S and the number of all connected components s . Are the results expected?

Computational complexity is linear $\mathcal{O}(m)$ and applicable to any network that fits in your memory.

3. Using breadth-first search methods provided by your library, compute **distances between the nodes of networks** above. Print out the average distance between the nodes $\langle d \rangle$ and the maximum distance or diameter d_{max} . Are the results expected?

Computational complexity is inevitably quadratic $\mathcal{O}(nm)$ and applicable only to smaller networks.

4. Using triad counting methods provided by your library, compute **clustering coefficient of networks** above. Print out the average clustering coefficient $\langle C \rangle$. Are the results expected?

Computational complexity is superlinear $\mathcal{O}(m\langle k \rangle)$ and applicable to all but the largest networks.

5. (homework) Using plotting functionality provided by your library, compute **degree distribution of networks** above. Plot degree distribution p_k on a doubly logarithmic plot. Are the results expected?

Computational complexity is linear $\mathcal{O}(n)$ and applicable to any network that fits in your memory.

6. What is the **size of the largest network** you are able to analyze in say half a minute?

III. Random graphs, scale-free and small-world network models

1. Using the methods provided by your library, construct **Erdős-Rényi random graphs** $G(n, m)$ with the same number of nodes n and edges m as networks above. Print out their basic statistics. Are the results expected?
2. (homework) Using the methods provided by your library, construct **Barabási-Albert scale-free networks** $G(n, \langle k \rangle / 2)$ with the same number of nodes n and the average degree $\langle k \rangle$ as networks above. Print out their basic statistics. Are the results expected?