

Grand graph challenge

Consider an **Erdős–Rényi random graph** with n nodes and $\frac{n \ln n}{8}$ links. Implement an **efficient algorithm** that constructs such a graph and computes the fraction of nodes in the giant connected component S . The algorithm can use any graph representation and any method for computing connected components. It should merely **compute S for a given n** . What is the size of the **largest graph** you are able to analyze in roughly **one minute**?

| Nodes n | Links $\frac{n \ln n}{8}$ | Giant S | Graph T_G | Search T_S | Time T_{G+S} |
|-------------------|---------------------------|---------------|------------------|------------------|------------------|
| 1000 | 863 | 70.32% | 0.00 sec | 0.00 sec | 0.00 sec |
| 10000 | 11 513 | 86.46% | 0.00 sec | 0.00 sec | 0.01 sec |
| 100 000 | 143 912 | 93.14% | 0.03 sec | 0.03 sec | 0.06 sec |
| 1 000 000 | 1 726 939 | 96.42% | 0.63 sec | 0.53 sec | 1.16 sec |
| 5 000 000 | 9 640 593 | 97.69% | 10.18 sec | 3.70 sec | 13.88 sec |
| 10 000 000 | 20 147 620 | 98.08% | 15.19 sec | 10.43 sec | 25.62 sec |
| 15 000 000 | 30 981 676 | 98.28% | 21.79 sec | 13.59 sec | 35.38 sec |
| 20 000 000 | 42 028 107 | 98.40% | 31.37 sec | 19.94 sec | 51.31 sec |
| 25 000 000 | 53 232 457 | 98.49% | 42.00 sec | 30.32 sec | 72.32 sec |
| 30 000 000 | 64 562 655 | 98.56% | 66.23 sec | 44.30 sec | 110.53 sec |
| 50 000 000 | 110 797 085 | 98.74% | 232.47 sec | 113.79 sec | 346.26 sec |

Table shows performance of a Java implementation run on 2.3 GHz Intel Core i7 with 16 GB memory.