

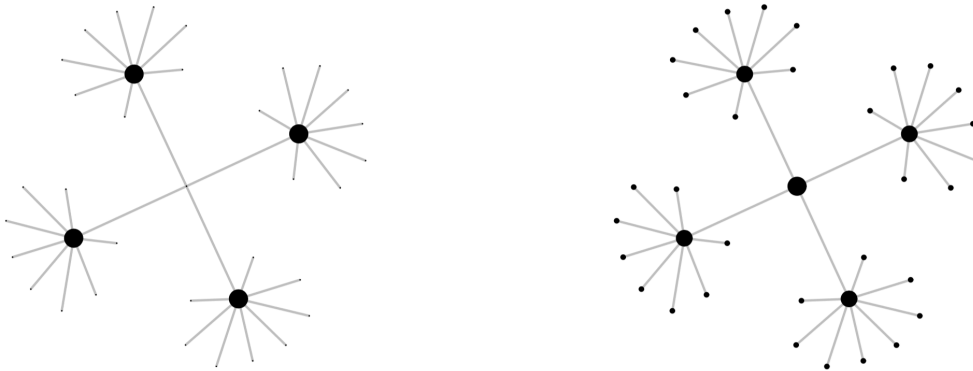
## ÷-vector centrality challenge

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Classical spectral centrality measures define important nodes as those that are connected to important others. For example, in the case of *eigenvector centrality*  $e$  defined as

$$\lambda e = Ae,$$

where  $A$  is network adjacency matrix and  $\lambda$  is its leading eigenvalue, the importance of a node is **proportional** to the number **and** importance of its neighbors (see right side of figure below).



Recently proposed ÷-vector centrality  $x$  defines the importance of nodes as

$$x = Ax^{\div},$$

where  $x^{\div}$  is a vector whose entries are the reciprocal of values of  $x$ ,  $x_i^{\div} = x_i^{-1}$ . Thus, in contrast to before, the importance of a node is **proportional** to the number of its neighbors, but **inversely proportional** to their importance (see left side of figure above).

Give an example of a particular network and scenario where ÷-vector centrality would be **meaningful**.  
(State what are network nodes and links, and what  $x$  measures.)