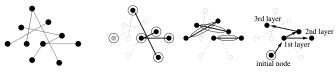
network sampling

introduction to network analysis (ina)

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sampling overview

- snowball sampling and contact tracing in sociology network-based methods for sampling hidden populations
- fractality and self-similarity of real networks [SHM05] fractality is property of object that it is similar to part of itself self-similarity demands power-law size scaling under renormalization
- any real network is just sample of true network [BŠWB15]



original network

node/link selection and snowball sampling

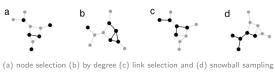
sampling populations

- snowball sampling similar to breadth-first search nodes sampled proportional to their eigenvector centrality
- contact tracing similar to biased best-first search nodes sampled according to some hidden variable
- respondent-driven sampling similar to random walk nodes sampled proportional to their degree

estimate
$$\langle x \rangle = \frac{\sum_{i} x_{i}}{\sum_{i} 1}$$
 corrected $\langle x \rangle = \frac{\sum_{i} x_{i}/k_{i}}{\sum_{i} 1/k_{i}}$

sampling *methods*

- random selection methods for global network sparsification random node/link selection w/ or w/o induction etc.
- network exploration methods for local network sampling random walks, snowball and expansion sampling etc.
- merging/aggregation methods for network simplification box covering, cluster growing, community aggregation etc.

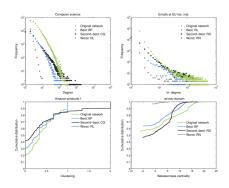




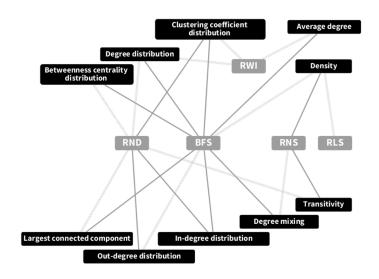
(a) community aggregation and (b) cluster growing

sampling *networks*

- similar sampled networks for $\gtrsim 15\%$ network [LF06]
- methods indistinguishable for $\ll 1\%$ network [BŠB17]
- selection/exploration ≫ aggregation methods [BŠB14] independent of network type or size but not sample size

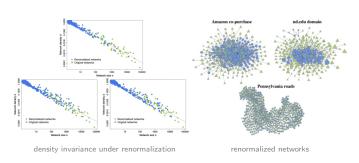


sampling scheme



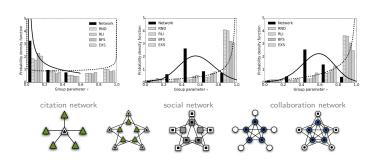
sampling *density*

- self-similar network density of real networks [LJT+11] most real networks are sparse with $\rho \approx 7.89 n^{-0.99}$
- network density invariant under any renormalization [BŠB12]
 box covering, cluster growing, community aggregation etc.



sampling communities

- pronounced community structure in real networks [GN02] many real networks contain communities with $\tau\gg 0$
- community structure enhanced under any sampling [BŠWB15]
 random selection, snowball and expansion sampling etc.



sampling references



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