Linear models II

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2017-12-20

# General Linear Models in R: Part 2

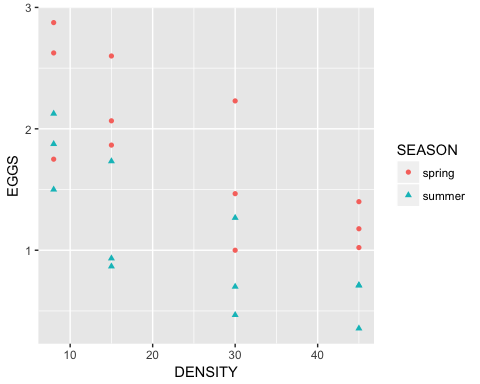
## A 2-Way Factorial Analysis of Variance of Limpets

This dataset is taken from the Quinn and Keough book. It is a study looking at density dependent fecundity in limpets in two different seasons. The null hypothesis is that there is no effect of density or season on the production of eggs. Alternatives include there being a density effect that differs between seasons (interaction between density and season) or an additive effect of season and density (no interaction – e.g. slope of density dependence is the same, but means are lower or higher between seasons). > Step 1: Import the limpet data into R and attach the data sheet. Identify the names of the columns in R and do a panel plot of eggs vs. density, split by season

require(ggplot2)

## Loading required package: ggplot2

p <- qplot(data=limp,  
 x=DENSITY,  
 y=EGGS,  
 colour=SEASON,  
 shape=SEASON)  
print(p)



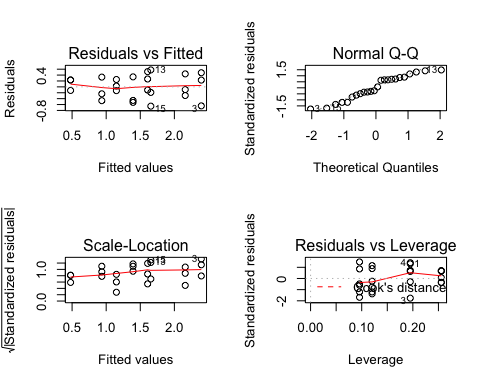
Ask yourself now – what kind of analysis are we doing? ANOVA, ANCOVA, Multiple Regression? Which variables are categorical and which are continuous? Can you find out?

str(limp)

## 'data.frame': 24 obs. of 3 variables:  
## $ DENSITY: int 8 8 8 8 8 8 15 15 15 15 ...  
## $ SEASON : Factor w/ 2 levels "spring","summer": 1 1 1 2 2 2 1 1 1 2 ...  
## $ EGGS : num 2.88 2.62 1.75 2.12 1.5 ...

Based on the graph, what do I expect my 2-way analysis to show – the null hypothesis, the alternative of an interaction, or the alternative of no interaction? To do this analysis, we use the workhorse, lm(), follow this immediately by a check of assumptions, then an examination of the anova table and the coefficients table. lm performs general linear models – these models assume normally distributed errors, but are robust to deviations in sample sizes (unbalanced designs).

m1<-lm(EGGS~DENSITY\*SEASON,  
 data=limp)  
par(mfrow=c(2,2))  
plot(m1)



anova(m1)

## Analysis of Variance Table  
##   
## Response: EGGS  
## Df Sum Sq Mean Sq F value Pr(>F)   
## DENSITY 1 5.0241 5.0241 30.1971 2.226e-05 \*\*\*  
## SEASON 1 3.2502 3.2502 19.5350 0.0002637 \*\*\*  
## DENSITY:SEASON 1 0.0118 0.0118 0.0711 0.7925333   
## Residuals 20 3.3275 0.1664   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

summary(m1)

##   
## Call:  
## lm(formula = EGGS ~ DENSITY \* SEASON, data = limp)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -0.65468 -0.25021 -0.03318 0.28335 0.57532   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) 2.664166 0.234118 11.380 3.45e-10 \*\*\*  
## DENSITY -0.033650 0.008259 -4.074 0.000591 \*\*\*  
## SEASONsummer -0.812282 0.331092 -2.453 0.023450 \*   
## DENSITY:SEASONsummer 0.003114 0.011680 0.267 0.792533   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 0.4079 on 20 degrees of freedom  
## Multiple R-squared: 0.7135, Adjusted R-squared: 0.6705   
## F-statistic: 16.6 on 3 and 20 DF, p-value: 1.186e-05

before we go over the details: \* why do we assign the model a name m1? \* What does DENSITY\*SEASON mean in the model? \* What does par(mfrow=c(2,2)) do? \* What should plot(m1) produce?

# Some Interpretations

The “Call” in summary() specifies your model – is this what you wanted? The Residuals gives the quartiles of the residuals – are they evenly distributed? The coefficients are as in any statistical package – the estimates for each term are the coefficients that help describe change in the dependent variable as a function of the independent variable(s).

The Residual Standard Error, Multiple R2 and Adjusted R2 tell you the standard things about variance explanation Finally, the F-test, degrees of freedom and overall significance of the model is presented Do the diagnostic plots show anything bad? The anova table shows which if any terms are significant? Is this table a sequential sums of squares? Which terms are marginal to the interaction? What does this mean? Which Hypothesis does this analysis support? Remove the interaction term (e.g. reanlyse as m2<-lm(EGGS~DENSITY+SEASON)). Are the p-values the same as the ANOVA table with the interaction term?

Let’s examine the fitted values and make a plot of our predictions. Note how we can use tapply and predict to get the fitted values (look at the help for them!). Note the “response” notation, as this predicts the fitted values of the model in terms of the response variable. This will be important later with generalized linear models, as you can predict differently (e.g. in terms of the transformed response variable).

require(broom)

## Loading required package: broom

m1\_augmented <- augment(m1)  
  
require(dplyr)

## Loading required package: dplyr

##   
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':  
##   
## filter, lag

## The following objects are masked from 'package:base':  
##   
## intersect, setdiff, setequal, union

season\_means <- m1\_augmented %>%  
 group\_by(SEASON) %>%  
 summarise(mean\_fitted=mean(.fitted))  
  
print(season\_means)

## # A tibble: 2 x 2  
## SEASON mean\_fitted  
## <fctr> <dbl>  
## 1 spring 1.83975  
## 2 summer 1.10375

density\_means <- m1\_augmented %>%  
 group\_by(DENSITY) %>%  
 summarise(mean\_fitted=mean(.fitted))  
  
print(density\_means)

## # A tibble: 4 x 2  
## DENSITY mean\_fitted  
## <int> <dbl>  
## 1 8 2.0012823  
## 2 15 1.7766322  
## 3 30 1.2952392  
## 4 45 0.8138462

density\_season\_means <- m1\_augmented %>%  
 group\_by(DENSITY,SEASON) %>%  
 summarise(mean\_fitted=mean(.fitted))  
  
print(density\_season\_means)

## # A tibble: 8 x 3  
## # Groups: DENSITY [?]  
## DENSITY SEASON mean\_fitted  
## <int> <fctr> <dbl>  
## 1 8 spring 2.3949692  
## 2 8 summer 1.6075953  
## 3 15 spring 2.1594217  
## 4 15 summer 1.3938428  
## 5 30 spring 1.6546769  
## 6 30 summer 0.9358016  
## 7 45 spring 1.1499321  
## 8 45 summer 0.4777604

require(tidyr)

## Loading required package: tidyr

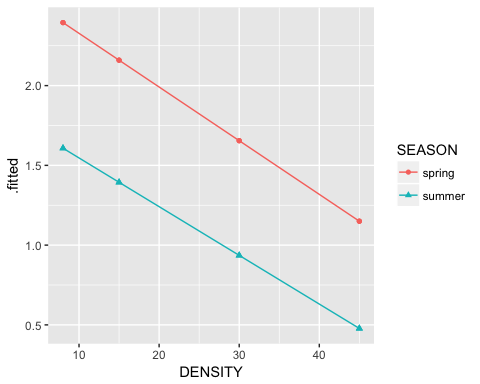
spread(density\_season\_means,   
 key=SEASON,   
 value=mean\_fitted)

## # A tibble: 4 x 3  
## # Groups: DENSITY [4]  
## DENSITY spring summer  
## \* <int> <dbl> <dbl>  
## 1 8 2.394969 1.6075953  
## 2 15 2.159422 1.3938428  
## 3 30 1.654677 0.9358016  
## 4 45 1.149932 0.4777604

What does spread do?

We can use predict to make a final plot of the predicted values from the generalised linear models. Sometimes useful for presenting the data

p <- qplot(data=m1\_augmented,  
 x=DENSITY,  
 y=.fitted,  
 colour=SEASON,  
 shape=SEASON,  
 geom=c("point", "line"))  
print(p)



How about data + fits? EXAMINE THIS CLOSELY

WHICH IS THE BEST FIT ?

## Soay Sheep Data Exploration

Import the file soay2.csv. Call it sheep.

These data are described as follows.

str(sheep)

## 'data.frame': 501 obs. of 9 variables:  
## $ NAME : Factor w/ 466 levels "NG020","NG039",..: 1 2 3 4 5 6 6 7 8 9 ...  
## $ YEARf : int 93 93 93 93 93 93 93 93 93 93 ...  
## $ AGE : int 1 1 1 1 1 1 1 1 1 1 ...  
## $ SEX : Factor w/ 2 levels "F","M": 1 1 2 2 2 2 2 1 1 1 ...  
## $ WEIGHT : num 19 15 22 18.4 18.8 25.4 25.4 15.6 20.4 17.2 ...  
## $ Testosterone: num NA NA NA NA NA NA NA NA NA NA ...  
## $ ODIN : num 1.715 0.594 1.75 1.054 1.957 ...  
## $ STR : int 0 100 300 300 1200 1000 1000 0 0 300 ...  
## $ SURV1 : int 1 1 1 1 1 1 1 1 1 1 ...

Produce a histogram of WEIGHT, Testosterone, ODIN, STR and SURV1 in a graph with 6 panels.

Part of the a plot produced by ggpairs is a density plot akin to a histogram.

require(GGally)

## Loading required package: GGally

##   
## Attaching package: 'GGally'

## The following object is masked from 'package:dplyr':  
##   
## nasa

ggpairs(sheep[,names(sheep) %in% c("WEIGHT", "Testosterone", "ODIN", "STR" ,"SURV1")])

## Warning: Removed 1 rows containing non-finite values (stat\_density).

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 230 rows containing missing values

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 22 rows containing missing values

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removing 1 row that contained a missing value

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 81 rows containing missing values

## Warning: Removed 230 rows containing missing values (geom\_point).

## Warning: Removed 230 rows containing non-finite values (stat\_density).

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 250 rows containing missing values

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 230 rows containing missing values

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 263 rows containing missing values

## Warning: Removed 22 rows containing missing values (geom\_point).

## Warning: Removed 250 rows containing missing values (geom\_point).

## Warning: Removed 21 rows containing non-finite values (stat\_density).

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 21 rows containing missing values

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 98 rows containing missing values

## Warning: Removed 1 rows containing missing values (geom\_point).

## Warning: Removed 230 rows containing missing values (geom\_point).

## Warning: Removed 21 rows containing missing values (geom\_point).

## Warning in (function (data, mapping, alignPercent = 0.6, method =  
## "pearson", : Removed 80 rows containing missing values

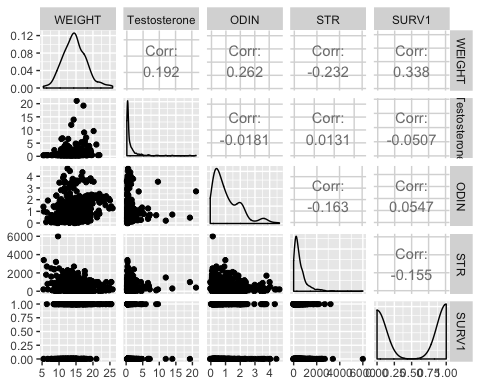
## Warning: Removed 81 rows containing missing values (geom\_point).

## Warning: Removed 263 rows containing missing values (geom\_point).

## Warning: Removed 98 rows containing missing values (geom\_point).

## Warning: Removed 80 rows containing missing values (geom\_point).

## Warning: Removed 80 rows containing non-finite values (stat\_density).

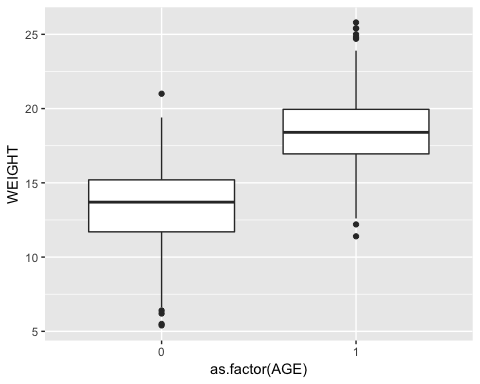


Is WEIGHT approximately normally distributed?

Linear regression Now let’s do an exploratory linear regression analysis. The question we are asking is “What factors influence body weight in Soay sheep?” Our goal is to explore, using linear regression, whether sex age and parasite load influence body weight. Start with plots of the data again Is AGE a factor or a Covariate?

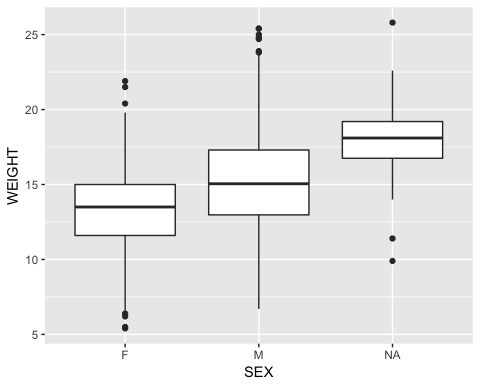
p <- qplot(data=sheep,  
 y=WEIGHT,  
 x=as.factor(AGE),  
 geom="boxplot")  
print(p)

## Warning: Removed 1 rows containing non-finite values (stat\_boxplot).



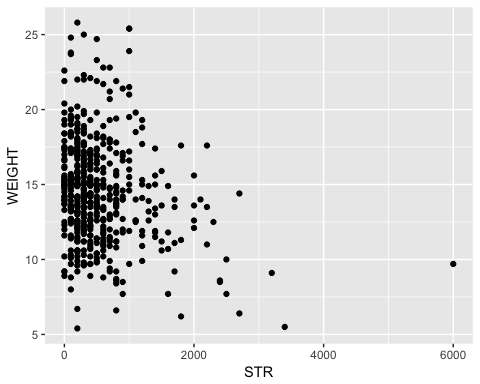
p <- qplot(data=sheep,  
 y=WEIGHT,  
 x=SEX,  
 geom="boxplot")  
print(p)

## Warning: Removed 1 rows containing non-finite values (stat\_boxplot).



p <- qplot(data=sheep,  
 y=WEIGHT,  
 x=STR)  
print(p)

## Warning: Removed 1 rows containing missing values (geom\_point).



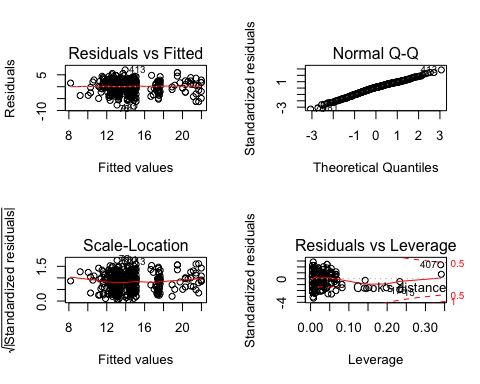
m1 <- lm(WEIGHT~factor(AGE)\*SEX\*STR,  
 data=sheep)

Note how names(m1) produced a list of component pieces to the object, defined my lm. We can use these objects to reproduce some of the diagnostic plots.

names(m1)

## [1] "coefficients" "residuals" "effects" "rank"   
## [5] "fitted.values" "assign" "qr" "df.residual"   
## [9] "na.action" "contrasts" "xlevels" "call"   
## [13] "terms" "model"

par(mfrow=c(2,2))  
plot(m1)

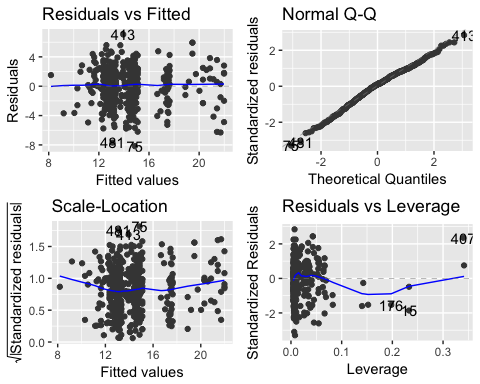


require(ggfortify)

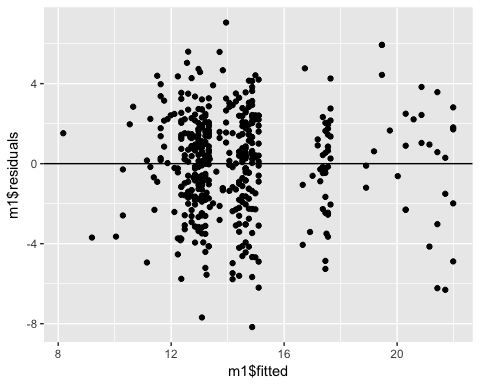
## Loading required package: ggfortify

## Warning: namespace 'DBI' is not available and has been replaced  
## by .GlobalEnv when processing object 'collapse'  
  
## Warning: namespace 'DBI' is not available and has been replaced  
## by .GlobalEnv when processing object 'collapse'

autoplot(m1)



p <- qplot(y=m1$residuals,  
 x=m1$fitted)+  
 geom\_hline(yintercept = 0)  
print(p)

 As above, we use anova and summary to explore this model

anova(m1)

## Analysis of Variance Table  
##   
## Response: WEIGHT  
## Df Sum Sq Mean Sq F value Pr(>F)   
## factor(AGE) 1 1719.05 1719.05 277.2729 < 2.2e-16 \*\*\*  
## SEX 1 391.41 391.41 63.1326 1.565e-14 \*\*\*  
## STR 1 236.49 236.49 38.1447 1.470e-09 \*\*\*  
## factor(AGE):SEX 1 43.57 43.57 7.0279 0.008308 \*\*   
## factor(AGE):STR 1 16.61 16.61 2.6793 0.102356   
## SEX:STR 1 0.01 0.01 0.0018 0.965796   
## factor(AGE):SEX:STR 1 5.71 5.71 0.9215 0.337588   
## Residuals 450 2789.93 6.20   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

summary(m1)

##   
## Call:  
## lm(formula = WEIGHT ~ factor(AGE) \* SEX \* STR, data = sheep)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -8.1674 -1.6051 0.2602 1.7329 7.0551   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) 13.3321950 0.2370810 56.235 < 2e-16 \*\*\*  
## factor(AGE)1 4.3106971 0.6249103 6.898 1.79e-11 \*\*\*  
## SEXM 1.7658136 0.3477047 5.078 5.58e-07 \*\*\*  
## STR -0.0012170 0.0003170 -3.839 0.000141 \*\*\*  
## factor(AGE)1:SEXM 2.8583150 0.9761075 2.928 0.003581 \*\*   
## factor(AGE)1:STR 0.0003090 0.0018420 0.168 0.866867   
## SEXM:STR 0.0000639 0.0004160 0.154 0.877998   
## factor(AGE)1:SEXM:STR -0.0019600 0.0020417 -0.960 0.337588   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 2.49 on 450 degrees of freedom  
## (43 observations deleted due to missingness)  
## Multiple R-squared: 0.4638, Adjusted R-squared: 0.4554   
## F-statistic: 55.6 on 7 and 450 DF, p-value: < 2.2e-16

Now, we are faced with some interesting decisions. As we are exploring this data, one might argue that we are not necessarily looking for the best predictive model (adding terms to the model will invariably increase the R2 and make it better at predicting). Instead, we use the philosophy of the minimum adequate model to seek out the variables that explain significant amounts of variance.

To do this, we begin by looking at the highest order terms in the model – in this case the 3-way interaction. Because 1) our anova table is sequential and we can only trust the p-values on the highest order terms, and 2) because everything above this is marginal, we ask the very simple question – is the 3way significant? If the answer is no, than removing it from the model makes no significant change in our explanation of variance. Remember this principle. We can use a trick in R to update our model and make sure that our interpretation is correct.

m2 <- update(m1, ~.-factor(AGE):SEX:STR)  
anova(m2)

## Analysis of Variance Table  
##   
## Response: WEIGHT  
## Df Sum Sq Mean Sq F value Pr(>F)   
## factor(AGE) 1 1719.05 1719.05 277.3212 < 2.2e-16 \*\*\*  
## SEX 1 391.41 391.41 63.1436 1.551e-14 \*\*\*  
## STR 1 236.49 236.49 38.1513 1.463e-09 \*\*\*  
## factor(AGE):SEX 1 43.57 43.57 7.0291 0.008302 \*\*   
## factor(AGE):STR 1 16.61 16.61 2.6798 0.102325   
## SEX:STR 1 0.01 0.01 0.0018 0.965793   
## Residuals 451 2795.65 6.20   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

anova(m1,m2)

## Analysis of Variance Table  
##   
## Model 1: WEIGHT ~ factor(AGE) \* SEX \* STR  
## Model 2: WEIGHT ~ factor(AGE) + SEX + STR + factor(AGE):SEX + factor(AGE):STR +   
## SEX:STR  
## Res.Df RSS Df Sum of Sq F Pr(>F)  
## 1 450 2789.9   
## 2 451 2795.7 -1 -5.7134 0.9215 0.3376

m2 is now a model formed, using the command update(), without the 3 way interaction. We look at the new anova table to confirm we lost it. We can then use anova(m1,m2) to compare the model, using an F-test, to determine whether one explains more variation than the other. It tests the change in the sums of squares against the F-distribution. Compare this p-value to the one in the anova table for model 1 above. Is it the same? Now, we are stuck with a rather difficult prospect. Model 2 has three 2-way interactions in it. Each of these is in the highest order category now (2-way). Moreover, as the table is sequential, the only p-value that we can trust is the last one, for SEX:STR. How do we cope?

We could, if we had the time and inclination, rewrite our model three times, each time, placing one of the 2-way terms at the end of our model description. Or, as we saw above, we could create 3 models, each missing one of the 2-way variables, and use anova() to compare the two. A significant p-value on any of the comparisons would indicate that indeed, the term is significant and important. These are called single-term-deletion tests. Not surprisingly there is an easier way: dropterm() from the MASS library. This function implements the single-term-deletions. You therefore need to load MASS.

require(MASS)

## Loading required package: MASS

##   
## Attaching package: 'MASS'

## The following object is masked from 'package:dplyr':  
##   
## select

dropterm(m2, test="F")

## Single term deletions  
##   
## Model:  
## WEIGHT ~ factor(AGE) + SEX + STR + factor(AGE):SEX + factor(AGE):STR +   
## SEX:STR  
## Df Sum of Sq RSS AIC F Value Pr(F)   
## <none> 2795.7 842.50   
## factor(AGE):SEX 1 58.250 2853.9 849.94 9.3970 0.002304 \*\*  
## factor(AGE):STR 1 16.246 2811.9 843.15 2.6208 0.106171   
## SEX:STR 1 0.011 2795.7 840.50 0.0018 0.965793   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Q:Why does dropterm() only report on the higher order interactions? Q: Which terms can we consider dropping?

Let’s begin with the insignificant term, and work our way down the chain of significance and order of interactions

m3 <- update(m2, ~.-SEX:STR)  
dropterm(m3,test="F")

## Single term deletions  
##   
## Model:  
## WEIGHT ~ factor(AGE) + SEX + STR + factor(AGE):SEX + factor(AGE):STR  
## Df Sum of Sq RSS AIC F Value Pr(F)   
## <none> 2795.7 840.50   
## factor(AGE):SEX 1 59.743 2855.4 848.18 9.6592 0.002003 \*\*  
## factor(AGE):STR 1 16.612 2812.3 841.21 2.6857 0.101946   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

m4 <- update(m3, ~.-factor(AGE):SEX)  
dropterm(m4,test="F")

## Single term deletions  
##   
## Model:  
## WEIGHT ~ factor(AGE) + SEX + STR + factor(AGE):STR  
## Df Sum of Sq RSS AIC F Value Pr(F)   
## <none> 2855.4 848.18   
## SEX 1 470.87 3326.3 916.09 74.702 <2e-16 \*\*\*  
## factor(AGE):STR 1 0.44 2855.8 846.26 0.070 0.7917   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Notice now that we have the minimum explanatory model. Our deletions of the 2-way terms left us with only one significant higher order term: age\*sex. This left parasite load behind, and as it is not involved in an interaction, the main effect is the highest order term for parasite load. We have detected significant effects of parasite load on Weight and of age and sex on weight. Using summary(m4) we can identify that increasing parasite load, controlling for sex and age, causes decreases in weight.

summary(m4)

##   
## Call:  
## lm(formula = WEIGHT ~ factor(AGE) + SEX + STR + factor(AGE):STR,   
## data = sheep)  
##   
## Residuals:  
## Min 1Q Median 3Q Max   
## -8.3389 -1.5452 0.2213 1.7626 6.9243   
##   
## Coefficients:  
## Estimate Std. Error t value Pr(>|t|)   
## (Intercept) 13.1966615 0.2005226 65.811 < 2e-16 \*\*\*  
## factor(AGE)1 5.2416294 0.4500662 11.646 < 2e-16 \*\*\*  
## SEXM 2.0830365 0.2410078 8.643 < 2e-16 \*\*\*  
## STR -0.0012040 0.0002068 -5.821 1.11e-08 \*\*\*  
## factor(AGE)1:STR -0.0001875 0.0007097 -0.264 0.792   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1  
##   
## Residual standard error: 2.511 on 453 degrees of freedom  
## (43 observations deleted due to missingness)  
## Multiple R-squared: 0.4512, Adjusted R-squared: 0.4463   
## F-statistic: 93.1 on 4 and 453 DF, p-value: < 2.2e-16

Finally we can use predicted values from the model to explore the interaction! First, we must declare a parasite load at which to make the prediction. Then we build a data frame for prediction. Then we use this data frame.

newdat <- with(sheep,  
 expand.grid(AGE=levels(factor(AGE)),  
 SEX=levels(SEX),  
 STR=mean(STR)))

Note how expand.grid makes a minimal dataset of values on which to predict.

pd <- predict(m4, newdat, se.fit=T)  
pd

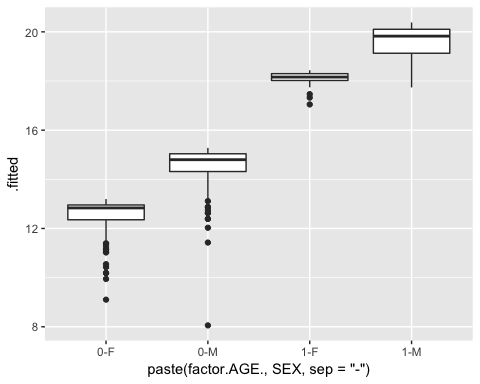
## $fit  
## 1 2 3 4   
## 12.55022 17.69116 14.63326 19.77420   
##   
## $se.fit  
## 1 2 3 4   
## 0.1694433 0.3291238 0.1824225 0.3259881   
##   
## $df  
## [1] 453  
##   
## $residual.scale  
## [1] 2.510639

Now we make a dataset for plotting. This can be done with values from predict or using augment in broom.

require(broom)  
augment\_m4 <- augment(m4)

We then plot this augmented data

p <- qplot(data=augment\_m4,  
 x=paste(factor.AGE.,SEX, sep="-"),  
 y=.fitted,  
 geom="boxplot")  
print(p)

 Some people like the idea of Type III sums of squares (as you’d get in Minitab) – so that you can look at the terms’ significance without doing the dropterm() or drop1(). See <http://www.stats.ox.ac.uk/pub/MASS3/Exegeses.pdf> for a discussion why Type IIIs are often not used. If you insist, you can use the command:

require(car)

## Loading required package: car

## Warning: package 'car' was built under R version 3.4.3

##   
## Attaching package: 'car'

## The following object is masked from 'package:dplyr':  
##   
## recode

Anova(m1,type="III")

## Anova Table (Type III tests)  
##   
## Response: WEIGHT  
## Sum Sq Df F value Pr(>F)   
## (Intercept) 19606.1 1 3162.3487 < 2.2e-16 \*\*\*  
## factor(AGE) 295.0 1 47.5839 1.795e-11 \*\*\*  
## SEX 159.9 1 25.7910 5.583e-07 \*\*\*  
## STR 91.4 1 14.7372 0.0001413 \*\*\*  
## factor(AGE):SEX 53.2 1 8.5748 0.0035814 \*\*   
## factor(AGE):STR 0.2 1 0.0281 0.8668668   
## SEX:STR 0.1 1 0.0236 0.8779976   
## factor(AGE):SEX:STR 5.7 1 0.9215 0.3375885   
## Residuals 2789.9 450   
## ---  
## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1