

$$F(x) = \sqrt{\frac{x-5}{x+6}}$$

Let $f(x) = \sqrt{x}$, $g(x) = \frac{x-5}{x+6}$

$$\therefore F(x) = f \circ g(x)$$

g is a rational function
 \therefore it is continuous at every point in its domain
 by Theorem 25

f is of the form $\sqrt[n]{x}$ where $n=2$
 \therefore it is continuous for all $x > 0$
 by Theorem 26 (2)

$\therefore F$ is continuous for all x such that $g(x) > 0$

Investigate intervals with 5 and -6 as critical values :

	$x - 5$	$x + 6$	$g(x) = \frac{x-5}{x+6}$
$x < -6$	-	-	+
$x = -6$	-	0	UNDEFINED
$-6 < x < 5$	-	+	-
$x = 5$	0	+	+
$x > 5$	+	+	+

Investigate $x = -6$:

$f(-6)$ does not exist

$\therefore F$ is discontinuous at $x = -6$

Investigate $x = 5$:

$$f(5) = 0$$

$$\lim_{x \rightarrow 5^+} f(x) = 0 = f(5)$$

$\therefore F$ is right-continuous at $x = 5$

$\therefore F$ is continuous at
 $(-\infty, -6) \cup [5, +\infty)$

$\therefore F$ is continuous at the open interval $(-\infty, -6)$
 and the half-open interval $[5, +\infty)$