

# 1 Statistic

## 1.1 Subtitle

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### Chapter 5: Probability Densities

For continuous random variable, the outcomes are represented by intervals on the real line.

Interval  $[\text{-----}]$  has infinite number of values

The probability distribution for a continuous random variable is represented by the area under a curve  $f(x)$  = probability density function

Discrete  $P(\bar{X} = x)$  continuous when  $P(a \leq \bar{X} \leq b) = \text{"Integration from a to b"} \int_a^b f(x) dx$

If you try to find  $P(\bar{X} = x) = \text{"integration x to x"} \int_x^x f(x) dx = 0$ , then = the probability of a specific value = 0

However we are only looking at intervals  $P(a \leq \bar{X} \leq b) = P(a < \bar{X} < b)$  with  $a$  and  $b = 0$

The probability of a function from value  $a$  to  $b$  will be the area below the curve of the function from  $a$  to  $b$

Cumulative probability functions

$F(x) = P(\bar{X} \leq x) = \text{"integral from -infinity to x"} \int_{-\infty}^x f(t) dt$

Example: Probability density function

$f(x) = e^{-x}$  when  $x \geq 0$  or  $0$  if  $x < 0$

$P(1 \leq \bar{X} \leq 5) = \text{"integral 5 to 1"} \int_1^5 e^x dx = .239$

Example: Probability density function

$f(x) = 0$  when  $x < 0$  |  $1/2$  when  $0 < x < 1$  |  $2 - x$  when  $1 < x < 2$  |  $0$  when  $x > 2$

$P(.5 \leq \bar{X} \leq 1.5) = 5/8$

Mean of the Probability density weighted average

$M =$

$$\int_{big}^{big} x f(x) dx.$$

Variance of probability density

$$\sigma^2 = \int_{big}^{big} (x - \mu)^2 f(x) dx.$$

## 1.2 5.2 Normal Distribution

1) area under curve = 1

2) highest pt at mean

3) Symmetric about  $\mu$

4)  $mean = median = mode$

5) Each unique normal distribution can be described by  $\mu, \sigma$

$$f(x, \mu, \sigma) = \frac{1}{\sigma\sqrt{2\pi}}$$