

1 Statistic

1.1 Subtitle

Tuesday, April 23, 2013.

Chapter 5: Probability Densities

For continuous random variable, the outcomes are represented by intervals on the real line.

Interval $[\text{-----}]$ has infinite number of values

The probability distribution for a continuous random variable is represented by the area under a curve $f(x)$ = probability density function

Discrete $P(\bar{X} = x)$ continuous when $P(a \leq \bar{X} \leq b) = \int_a^b f(x) dx$

If you try to find $P(\bar{X} = x) = \int_x^x f(x) dx = 0$, then = the probability of a specific value = 0

However we are only looking at intervals $P(a \leq \bar{X} \leq b) = P(a < \bar{X} < b)$ with a and $b = 0$

The probability of a function from value a to b will be the area below the curve of the function from a to b

Cumulative probability functions

$F(x) = P(\bar{X} \leq x) = \int_{-\infty}^x f(t) dt$

Example: Probability density function

$f(x) = e^{-x}$ when $x \geq 0$ or 0 if $x < 0$

$P(1 \leq \bar{X} \leq 5) = \int_1^5 e^x dx = .239$

Example: Probability density function

$f(x) = 0$ when $x < 0$ | $1/2$ when $0 < x < 1$ | $2 - x$ when $1 < x < 2$ | 0 when $x > 2$

$P(.5 \leq \bar{X} \leq 1.5) = 5/8$

Mean of the Probability density weighted average

$M =$

$$\int_{big}^{big} x f(x) dx.$$

Variance of probability density

$$\sigma^2 = \int_{big}^{big} (x - \mu)^2 f(x) dx.$$

1.2 5.2 Normal Distribution

1) area under curve = 1

2) highest pt at mean

3) Symmetric about μ

4) $mean = median = mode$

5) Each unique normal distribution can be described by μ, σ

$$f(x, \mu, \sigma) = \frac{1}{\sigma\sqrt{2\pi}}$$