



Multi-criteria decisionmaking

Reginald Dewil







Multi-criteria decision making

MCDM methods are a set of tools to support decision making in multiple criteria problems concerning different stakeholders with conflicting values.

Also known as Multi-criteria decision analysis (MCDA)

Has a different focus than the related field of Multi-Objective Optimization







Multi-objective optimization

Consider a problem with 2 conflicting objectives



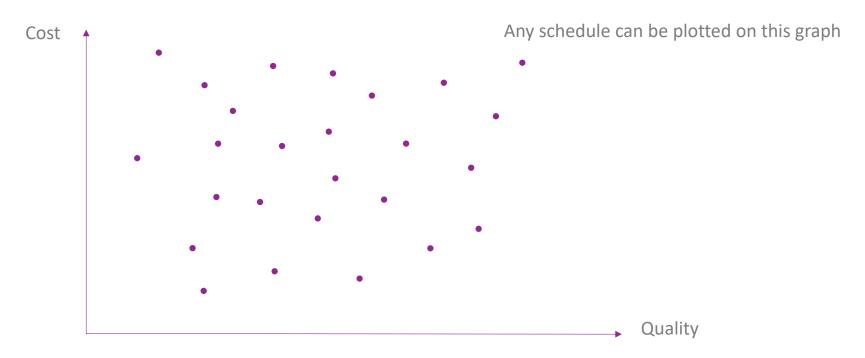






Multi-objective optimization

Consider a scheduling problem with 2 conflicting objectives



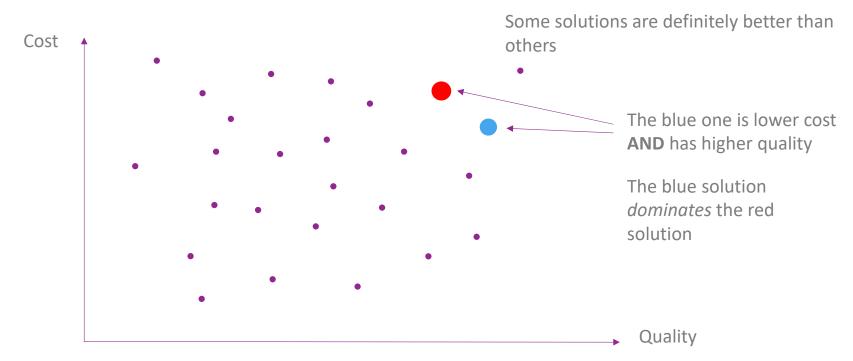






Multi-objective optimization

Consider a scheduling problem with 2 conflicting objectives







Cost

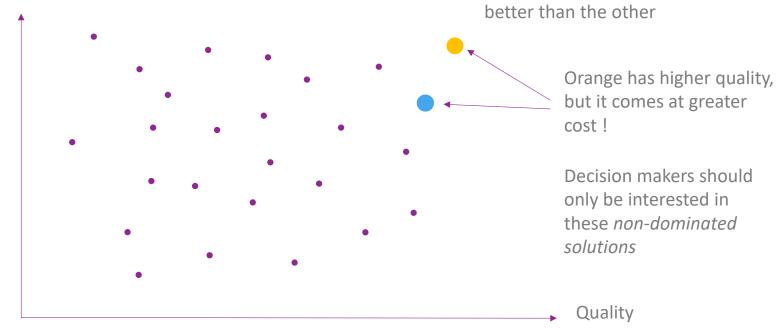
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Multi-objective optimization

Consider a scheduling problem with 2 conflicting objectives

For some other combinations: we cannot make a statement on whether one is better than the other





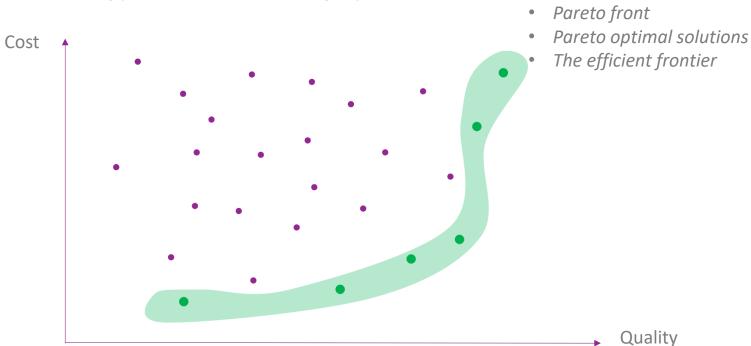




These solutions are called:

Multi-objective optimization

Consider a scheduling problem with 2 conflicting objectives





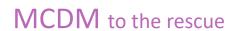


Multi-objective optimization



- Finding this efficient frontier is not easy for many problem settings
 - Employ Mathematical Programming, Heuristics, and Meta heuristics
- MODM optimization can limit the number of options to choose from
 - Only Pareto-optimal solutions
 - In many applications, the number of pareto-optimal solutions is limited when dealing only with 2 objectives
 - Many multi-disciplinary problems involve 3,4,5, ... 10+ criteria
- Still:
 - A trade-off needs to be made
 - 2. Decision-makers can value different criteria differently
 - 3. Transparancy sometimes required on how a decision was

Intuition does not always cut it





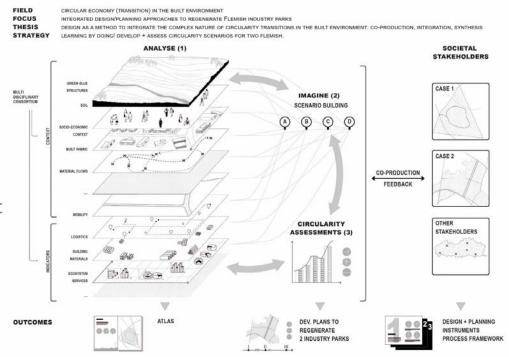




Future planning of industry parks

- Economic
 - Operating cost of industry park
 - Cash requirements for investment
 - Congestion (#hours lost)
 - Impact on modal split
- Environmental
 - CO2 emmissions
 - NOx emmissions
 - Circularity of materials ot the built environment
 - Energy use of the industry park
- Social
 - Integration of industry park with neighborhood
 - Employment options for different social groups

....







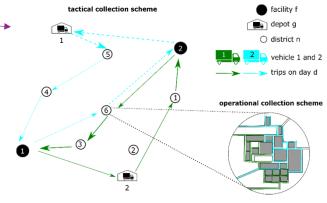


Waste Processing Facility Location Problem

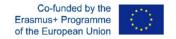
- Location & Processing Type decision affects:
 - operational cost of waste collection
 - investment cost
 - regulatory risk
 - community resistance risk
 - pollution
 - noise
 - smell
 - jobs
 - •

Each criterion has a different value for each type of stakeholder:

- Manager at the company
- Neighbor of potential location
- Citizen that is not a neighbor
- Politican



Solve integrated facility location and waste collection routing problems to get reliable estimates







MCDM Methods => many techniques

MCDM methods [edit]

The following MCDM methods are available, many of which are implemented by specialized decision-making software: [3][4]

- · Aggregated Indices Randomization Method (AIRM)
- · Analytic hierarchy process (AHP)
- · Analytic network process (ANP)
- · Balance Beam process
- Base-criterion method (BCM)^[44]
- Best worst method (BWM)^{[45][48]}
- · Brown-Gibson model
- Characteristic Objects METhod (COMET)[47][48]
- Choosing By Advantages (CBA)
- · Data envelopment analysis
- Decision EXpert (DEX)
- Disaggregation Aggregation Approaches (UTA*, UTAII, UTA
- · Rough set (Rough set approach)
- · Dominance-based rough set approach (DRSA)
- · ELECTRE (Outranking)
- Evaluation Based on Distance from Average Solution (EDAS)
- · Evidential reasoning approach (ER)
- Goal programming (GP)
- Grey relational analysis (GRA)

- · Inner product of vectors (IPV)
- . Measuring Attractiveness by a categorical Based Evaluation Technique (MACBETH)
- Simple Multi-Attribute Rating Technique (SMART) [50]
- · Stratified Multi Criteria Decision Making (SMCDM)
- · Multi-Attribute Global Inference of Quality (MAGIQ)
- . Multi-attribute utility theory (MAUT)
- · Multi-attribute value theory (MAVT)
- · Markovian Multi Criteria Decision Making
- New Approach to Appraisal (NATA)
- Nonstructural Fuzzy Decision Support System (NSFDSS)
- · Potentially All Pairwise RanKings of all possible Alternatives (PAPRIKA)
- PROMETHEE (Outranking)
- Ranking based on optimal points (RBOP)^[51]
- Stochastic Multicriteria Acceptability Analysis (SMAA)
- · Superiority and inferiority ranking method (SIR method)
- . Technique for the Order of Prioritisation by Similarity to Ideal Solution (TOPSIS)
- · Value analysis (VA)
- Value engineering (VE)
- VIKOR method^[52]
- Weighted product model (WPM)
- Weighted sum model (WSM)
- Modelo Integrado de Valor para Estructuras Sostenibles (MIVES)^{[53][54]}

Wikipedia, the one and only







MCDM

Feasible alternatives

Preferably Pareto Optimal – but not always known after e.g. brainstorming solutions or candidates

• Evalution criteria?





MCDM - criteria

- Avoid overlap
- Be clear and exhaustive
- Some criteria may be divided up into several subcriteria





MCDM Methods

Linear Additional Methods

Define weights for each criterion

Evaluate each alternative on all its criteria

Total value of an alternative is the weighted sum of criterion scores

Select highest valued alternative

Absolute Methods

In comparison with the ideal situation

- > Appreciation specifications
- > Concepts to synthesize
- > Utility scores (distances)

Relative Methods

In comparison with each other (2 by 2)

- > Outranking methods
- > Analytical Hierarchy Process (AHP)







MCDM Methods

Linear Additional Methods

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Relative Methods

In comparison with each other (2 by 2)

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MCDM – Linear Additional Method

Determine criteria weights

Criterion	Description	Weight
C1	Risk	70
C2	Ergonomic Load	50
C3	Cost	30
C4	Service Deliverd	100
C5	Service Experienced	60





MCDM – Linear Additional Method

Evaluate Alternatives

Criterion	Description	Weight	Alternative 1	Alternative 2	Alternative 3	Alternative 4
C1	Risk	70	10	4	8	7
C2	Ergonomic Load	50	6	8	7	8
C3	Cost	30	5	8	10	8
C4	Service Deliverd	100	7	10	9	8
C5	Service Experienced	60	10	10	6	7
			2450	2520	2470	2350





MCDM – alternative evalution

Evaluate Alternatives

Criterion	Description	Weight	Alternative 1	Alternative 2	Alternative 3	Alternative 4
C1	Risk	70	10	4	8	7
C2	Ergonomic Load	50	6	8	7	8
C3	Cost	30	5	8	10	8
C4	Service Deliverd	100	7	10	9	8
C5	Service Experienced	60	10	10	6	7
		I	2450	2520	2470	2350

Getting consensus on the weights by different stakeholders can be a lengthy process Some criteria are sometimes hard to objectively score.
Leads to additional possibilities for arguments







MCDM – relative methods

Analytic Hierarchy Process

T.L. Saaty, How to make a decision: The Analytic Hierarchy Process, EJOR 48, pp9-26, 1990

- Outranking
 - E.g. ELECTRE [Roy]
 - E.g. PROMETHEE [Brans]



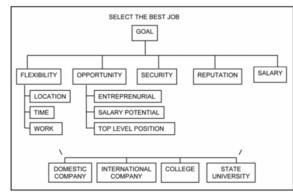




Analytic Hierarchy Process (AHP)

 Weights of criteria are determined through pairwise comparison by the stakeholders

- Steps:
 - 1. Define objective
 - 2. Structure the decision hierarchy:
 - Goal of the decision on top
 - 2. Then intermediate levels (criteria and sub criteria)
 - 3. Down to the alternatives
 - 3. Construct a set of pairwise comparison matrices. Each element in an upper level is used to compare the elements in the level immediately below with respect to it
 - 4. Calculate weights/priorities. Use the priorities of a given level to weight the priorities of the level below for every element









Analytic Hierarchy Process (AHP)

• We need a scale to indicate how many times more important one element is over the other

 Table 1
 The fundamental scale of absolute numbers

Intensity of Importance	Definition	Explanation				
1	Equal Importance	Two activities contribute equally to the objective				
2	Weak or slight					
3	Moderate importance	Experience and judgement slightly favour one activity over another				
4	Moderate plus					
5	Strong importance	Experience and judgement strongly favour one activity over another				
6	Strong plus					
7	Very strong or demonstrated importance	An activity is favoured very strongly over another; its dominance demonstrated in practice				
8	Very, very strong					
9	Extreme importance	The evidence favouring one activity over another is of the highest possible order of affirmation				
Reciprocals of above	If activity <i>i</i> has one of the above non-zero numbers assigned to it when compared with activity <i>j</i> , then <i>j</i> has the reciprocal value when compared with <i>i</i>	A reasonable assumption				
1.1–1.9	If the activities are very close	May be difficult to assign the best value but when compared with other contrasting activities the size of the small numbers would not be too noticeable, yet they can still indicate the relative importance of the activities.				

Anexamin	e	examination	MALIE INC	venienis
The country	-	examination	Control Juice	Semente

Drink consumption in US	Coffee	Wine	Tea	Beer	Sodas	Milk	Water
Coffee		9	5	2	1	1	1/2
Wine	1/9	1	1/3	1/9	1/9	1/9	1/9
Tea	1/5	2	1	1/3	1/4	1/3	1/9
Beer	1/2	9	3	1	1/2	1	1/3
Soda	1	9	4	2	1	2	1/2
Milk	1	9	3	1	1/2	1	1/3
Water	2	9	9	3	2	3	1 _





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Analytic Hierarchy Process (AHP)

• Decision-maker executes a pair-wise comparison for a set of elements

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 The fundamental scale of absolute numbers

Intensity of Importance	Definition	Explanation				
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2	Weak or slight					
3	Moderate importance	Experience and judgement slightly favour one activity over another				
4	Moderate plus	(2)				
5	Strong importance	Experience and judgement strongly favour one activity over another				
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7	Very strong or demonstrated importance	An activity is favoured very strongly over another; its dominance demonstrated in practice				
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Reciprocals of above	If activity <i>i</i> has one of the above non-zero numbers	A reasonable assumption				
	assigned to it when compared with activity <i>j</i> , then <i>j</i> has the reciprocal value when compared with <i>i</i>					
1.1–1.9	If the activities are very close	May be difficult to assign the best value but when compared with other contrasting activities the size of the small numbers would not be too noticeable, yet they can still indicate the relative importance of the activities.				

An example of examination using judgements

Drink consumption in US	Coffee	Wine	Tea	Beer	Sodas	Milk	Water
Coffee		9	5	2	1	1	1/2
Wine	1/9	1	1/3	1/9	1/9	1/9	1/9
Tea	1/5	3	1	1/3	1/4	1/3	1/9
Beer	1/2	9	3	1	1/2	1	1/3
Soda	1	9	4	2	1	2	1/2
Milk	1	9	3	1	1/2	1	1/3
Water	2	9	9	3	2	3	1 ノ

Notice the value for i-j is the inverse for j-i







Analytic Hierarchy Process (AHP)

Normalized pair-wise matrix is calculated

(Here, an approximation approach is used. Exact through eigenfactor maxtrix calculations)

Normalized matrix

	Coffee	Wine	Tea	Beer	Sodas	Milk	Water
Coffee	1/5,81	9/49	5/25,33				
Wine	0,11/5,81	1/49					
Tea	0,2/5,81						
Beer				• •			
Soda							
Milk							



An example of examination using judgements

	Coffee	Wine	Tea	Beer	Sodas	Milk	Water
Coffee		9	5	2	1	1	1/2
Wine	1/9	1	1/3	1/9	1/9	1/9	1/9
Tea	1/5	2	1	1/3	1/4	1/3	1/9
Beer	1/2	9	3	1	1/2	1	1/3
Soda	1	9	4	2	1	2	1/2
Milk	1	9	3	1	1/2	1	1/3
Water	2	9	9	3	2	3	1 _

5,81 49 25,33 9,44 5,36 21,11 2,89



Water





Analytic Hierarchy Process (AHP)

Normalized matrix

	Coffee	Wine	Tea	Beer	Sodas	Milk	Water	AVERAGE
Coffee	0,17	0,18	0,20	0,21	0,19	0,05	0,17	0,167
Wine	0,02	0,02	0,01	0,01	0,02	0,01	0,04	0,018
Tea	0,03	0,06	0,04	0,03	0,05	0,62	0,04	0,124
Beer	0,09	0,18	0,12	0,11	0,09	0,05	0,12	0,107
Soda	0,17	0,18	0,16	0,21	0,19	0,09	0,17	0,169
Milk	0,17	0,18	0,12	0,11	0,09	0,05	0,12	0,119
Water	0,34	0,18	0,36	0,32	0,37	0,14	0,35	0,295

Criteria weights

Additional calculations can be made to test whether the weights are consistent and hence can be used for decision making

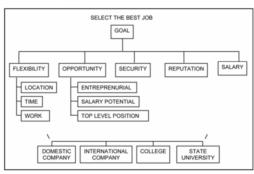






Analytic Hierarchy Process (AHP)

- Applying AHP to larger problem
 - 1. Define objective
 - 2. Structure the decision hierarchy:
 - 3. Construct a set of pairwise comparison matrices. Each element in an upper level is used to compare the elements in the level immediately below with respect to it
 - 4. Calculate weights/priorities. Use the priorities of a given level to weight the priorities of the level below for every element





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Analytic Hierarchy Process (AHP)

3. Construct a set of pairwise comparison matrices. Each element in an upper level is used to compare the elements in the level immediately below with respect to it

GOAL								
	flex	opport	security	reputation	salary			
flex								
opport								
security								
reputation								
calany					7			

Flexibility							
location time work							
location							
time							
work							

	Opportunity								
entrepr sal. Pot top. Lvl po									
entrepr									
sal. Pot									
top. Lvl pos									

Location								
	domestic comp international comp college state univ							
domestic comp								
international comp								
college								
state university								

Work
|
| Omestic international comp | college

domestic comp international comp college state university

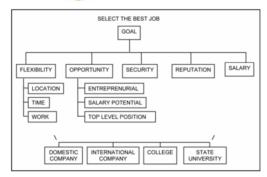
	state univers
state university	
	domestic co
	internation

Time							
	domestic comp	international comp	college	state university			
domestic comp							
international comp							
college							
state university							

Top Level Position							
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domestic comp							
international comp							
college							
state university							

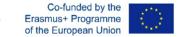
Salary Potential								
domestic comp international comp college state universi								
domestic comp								
international comp								
college								
state university								





	Ent	repreneurial						
domestic comp international comp college state university								
domestic comp								
international comp								
college								
state university								
		Salary						
	domestic comp	international comp	college	state university				
domestic comp								
international comp								
college								
state university								

Reputation								
	domestic	international comp	college	state university				
domestic comp								
international comp								
college								
state university								







Analytic Hierarchy Process (AHP)

4. Calculate weights/priorities. Use the priorities of a given level to weight the priorities of the level below for every element

Criteria Subcriteria	Flexibility 0.036			Future opportunity 0.122			Security 0.262	Reputation 0.075	Salary 0.506	Overall Priority
Global weights (criteria × subcriteria)	Location 0.091	Time 0.218	Work 0.691	Entrepreneurial 0.105	Salary increases 0.637	Top level position 0.258	0.262	0.075	0.506	
Domestic Company	0.003	0.008	0.025	0.013	0.078	0.032	0.225	0.064	0.124	• 0,134 ←
Internatn'l Company	0.295	0.084	0.062	0.090	0.555	0.591	0.054	0.101	0.547	0,365
College	0.496	0.055	0.115	0.061	0.258	0.274	0.095	0.247	0.289	0,224
State University	0.131	0.285	0.249	0.239	0.124	0.083	0.626	0.588	0.039	0,252

$$0,036*(0,003*0,091+0,008*0,218+0,025*0,691)$$

+ $0,122*(0,105*0,013+0,637*0,078+0,258*0,032)$
+ $0,262*0,225+0,075*0,64+0,506*0,124$

Co-funded by the Erasmus+ Programme of the European Union





Conclusions

- Four difficulties in MCDM
 - 1. Generating (non-dominated) alternatives
 - 2. Agreeing on the evaluation criteria
 - 3. Agreeing on the criteria weights
 - 4. Evaluating the alternatives objectively
- Many different tools exist
- Discussion will always take place in setting up the framework
- Tools are transparent

