Insper

Computação Gráfica

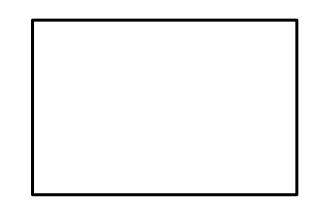
Aula 13: Revisão 3

Grafo de Cena



Criando Matriz Identidade

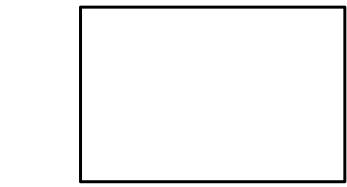
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Início
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   <TriangleSet>
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   </TriangleSet>
   <Appearance>
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   </Appearance>
  </Shape>
  <Transform scale="2 1 1">
   <Transform translation="0 -1 -1">
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     <TriangleSet>
      <Coordinate point='-1 -1 0 1 -1 0 0 1 0'/>
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   </Transform>
   <Transform translation="0 1 -2">
    <Transform rotation="0 0 1 3.14">
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 </Transform>
</Scene>
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\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}
\text{MATRIZ}
```

PILHA

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\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}
```

```
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0 2 0 0
0 0 2 0
0 0 0 1

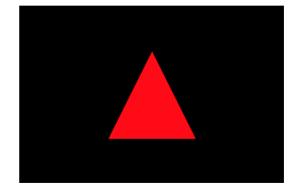
[1 0 0 0 0]
0 1 0 0
0 0 1 0
0 0 0 1

MATRIZ
```

PILHA

Desenhando Triângulo Vermelho

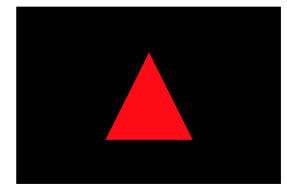
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   <Transform translation="0 -1 -1">
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     <Appearance>
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   <Transform translation="0 1 -2">
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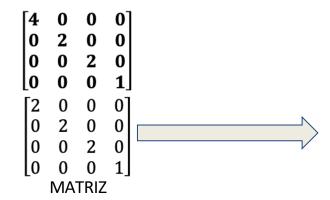
2	0	0	0]					
10	2	0	0					
0	0	2	0 0 0 1					
0	0	0	1]					
MATRIZ								

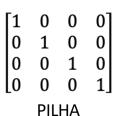
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\text{PILHA}

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   <Appearance>
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   </Appearance>
  </Shape>
  <Transform scale="2 1 1">
                                                         push
   <Transform translation="0 -1 -1">
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   </Transform>
   <Transform translation="0 1 -2">
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      <Appearance>
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```

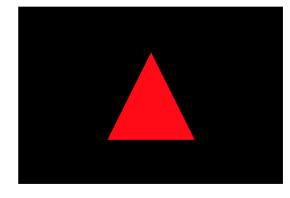


$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$





```
<Scene>
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$$\begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

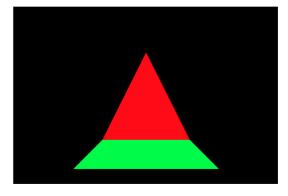
```
\[ \begin{pmatrix} 4 & 0 & 0 & 0 \\ 0 & 2 & 0 & -2 \\ 0 & 0 & 2 & -2 \\ 0 & 0 & 0 & 1 \end{pmatrix} \]
\[ \begin{pmatrix} 4 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \]
\[ MATRIZ \]
```

0 0 1 0 0 0 0 1 PILHA

Desenhando Triângulo Verde

```
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  </Shape>
  <Transform scale="2 1 1">
   <Transform translation="0 -1 -1">
    <Shape>
                                                        draw
     <TriangleSet>
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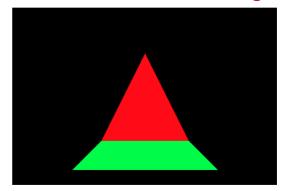
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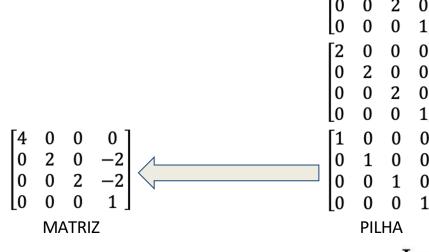


```
\begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 2 & 0 & -2 \\ 0 & 0 & 2 & -2 \\ 0 & 0 & 0 & 1 \end{bmatrix}
MATRIZ
```

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   </Transform>
                                                       gog
   <Transform translation="0 1 -2">
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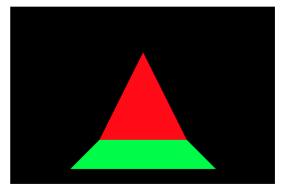
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push

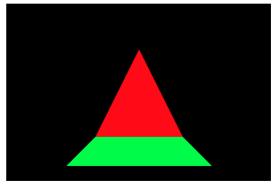
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<Scene>
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  </Shape>
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     </TriangleSet>
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      <Appearance>
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```

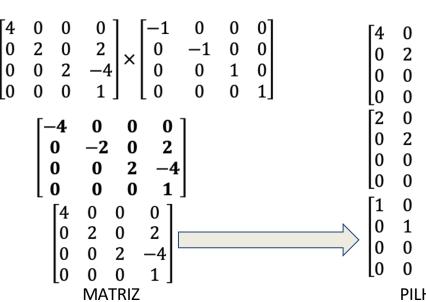


$$\begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & -2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

push

```
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</Scene>
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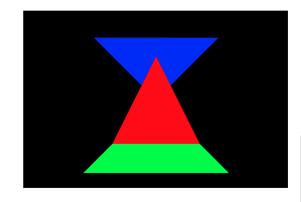
0 **PILHA**

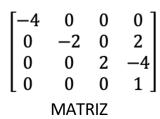
0

Desenhando Triângulo Azul

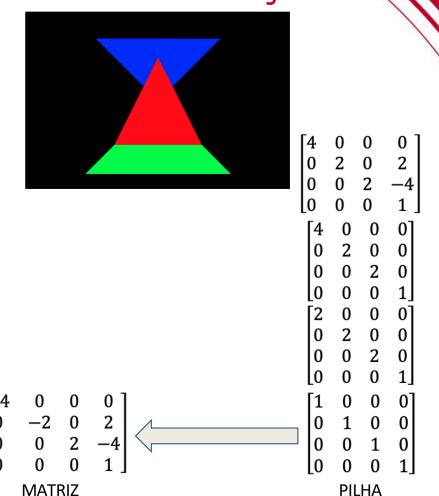
draw

```
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  </Transform>
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</Scene>
```



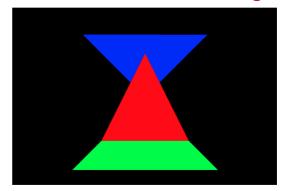


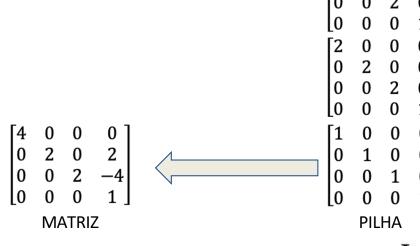




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```

</Scene>

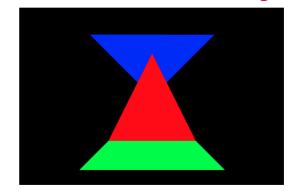


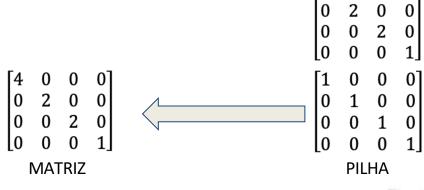


Insper

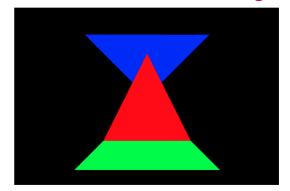
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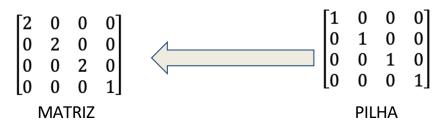
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 </Transform>
</Scene>
```





```
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  </Transform>
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                          aoa
</Scene>
```

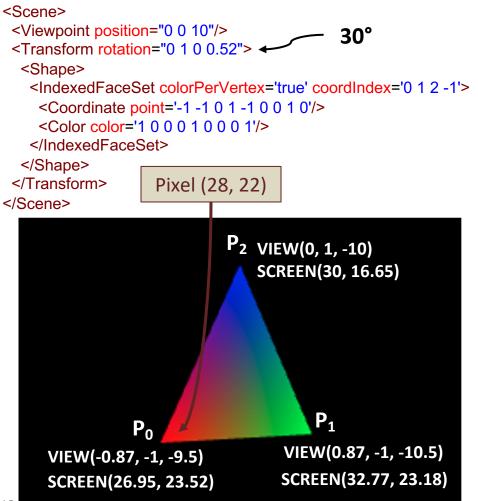




Interpolação em Triângulos



Triângulo com vértices de cores diferentes



Distâncias do ponto(28, 22) as arestas L(x, y) = (x - x0)(y1 - y0) - (y - y0)(x1 - x0)

 $L_0 = (28.5 - 32.77)(16.65 - 23.18) - (22.5 - 23.18)(30 - 32.77)$ $L_0 = (-4.27)(-6.53) - (-0.68)(-2.77)$ $L_0 = 27.8831 - 1.8836$

 $L_0 = 25.9995$

 $L_1 = (28.5 - 30)(23.52 - 16.65) - (22.5 - 16.65)(26.95 - 30)$ $L_1 = (-1.5)(6.87) - (5.85)(-3.05)$ $L_1 = -10.305 + 17.8425$

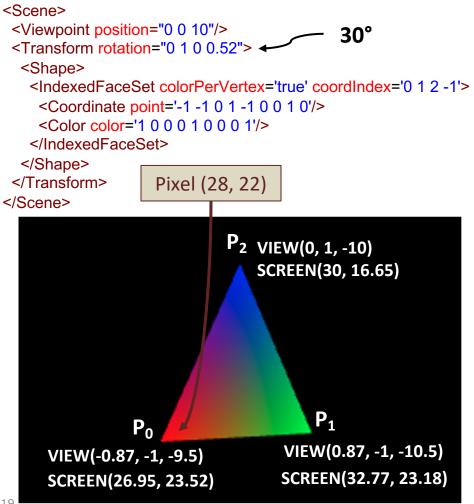
 $L_1 = 7.5375$

 $L_2 = (28.5 - 26.95)(23.18 - 23.52) - (22.5 - 23.52)(32.77 - 26.95)$ $L_2 = (1.55)(-0.34) - (-1.02)(5.82)$ $L_2 = -0.527 + 5.9364$

 $L_2 = 5.4094$

Todos positivos: Dentro !!!

Triângulo com vértices de cores diferentes



Área dos triângulos:

Area =
$$|x_0(y_1-y_2) + x_1(y_2-y_0) + x_2(y_0-y_1)| / 2$$

A = |26.95(23.18-16.65)+32.77(16.65-23.52)+30(23.52-23.18)|/2

A = |26.95(6.53)+32.77(-6.87)+30(0.34)|/2

A = |175.9835-225.1299+10.2|/2

A = 19.4732

 $A_0 = |28.5(23.18-16.65)+32.77(16.65-22.5)+30(22.5-23.18)|/2$

 $A_0 = |28.5(6.53)+32.77(-5.85)+30(-0.68)|/2$

 $A_0 = |186.105-191.7045-20.4|/2$

 $A_0 = 12.99975$

 $A_1 = |28.5(16.65-23.52)+30(23.52-22.5)+26.95(22.5-16.65)|/2$

 $A_1 = |28.5(-6.87)+30(1.02)+26.95(5.85)|/2$

 $A_1 = |-195.795+30.6+157.6575|/2$

 $A_1 = 3.76875$

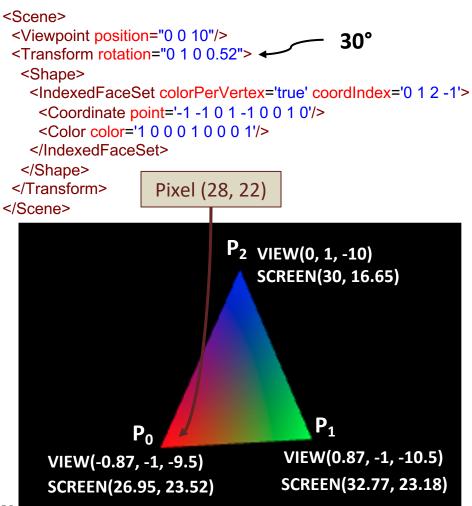
 $A_2 = |28.5(23.52-23.18)+26.95(23.18-22.5)+32.77(22.5-23.52)|/2$

 $A_2 = |28.5(0.34) + 26.95(0.68) + 32.77(-1.02)|/2$

 $A_2 = |9.69+18.326-33.4254|/2$

 $A_2 = 2.7047$

Triângulo com vértices de cores diferentes



Área dos triângulos:

$$A = 19.4732$$

$$A_0 = 12.99975$$

$$A_1 = 3.76875$$

$$A_2 = 2.7047$$

Pesos

$$\alpha = 12.99975 / 19.4732 \approx 0.668$$

$$\beta$$
 = 3.76875 / 19. 4732 ~= 0.194

$$\gamma = 2.7047 / 19.4732 \approx 0.139$$

ou

$$\gamma = 1 - \alpha - \beta \approx 0.138$$

Cor do pixel:

$$R = \alpha R_0 + \beta R_1 + \gamma R_2 = 0.668$$

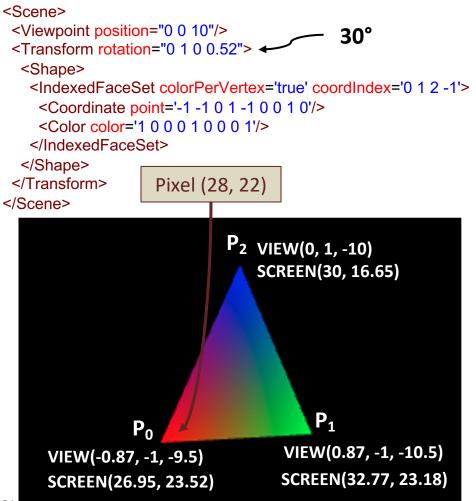
$$G = \alpha G_0 + \beta G_1 + \gamma G_2 = 0.194$$

$$B = \alpha B_0 + \beta B_1 + \gamma B_2 = 0.139$$

$$C = (0.668, 0.194, 0.139)$$



Cores do Triângulo com Correção Perspectiva



Pesos

$$\alpha = 0.668$$

$$Z_0 = |-9.5| = 9.5$$

$$\beta = 0.194$$

$$\beta = 0.194$$
 $Z_1 = |-10.5| = 10.5$

$$y = 0.139$$

$$\gamma = 0.139$$
 $Z_2 = |-10.0| = 10$

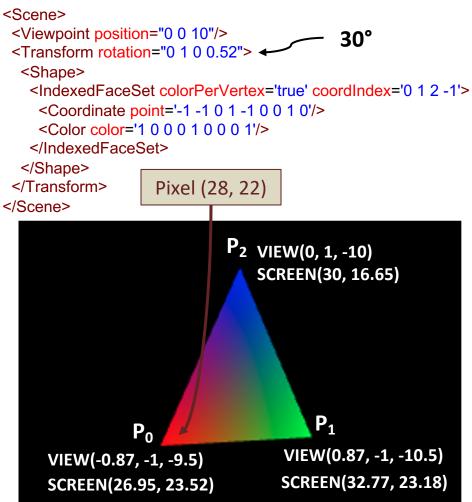
$$Z = rac{1}{lpha rac{1}{Z_0} + eta rac{1}{Z_1} + \gamma rac{1}{Z_2}}$$

$$Z = \frac{1}{0.668 \frac{1}{9.5} + 0.194 \frac{1}{10.5} + 0.139 \frac{1}{10}}$$

$$Z = \frac{1}{0.0703 + 0.0185 + 0.0139}$$

$$Z = 9.74$$

Cores do Triângulo com Correção Perspectiva



Pesos
$$Z_0 = |-9.5| = 9.5$$

 $\alpha = 0.668$ $Z_1 = |-10.5| = 10.5$
 $\beta = 0.194$ $Z_2 = |-10.0| = 10$
 $Z = 9.74$

$$C = Z \cdot \left(lpha rac{C_0}{Z_0} + eta rac{C_1}{Z_1} + \gamma rac{C_2}{Z_2}
ight)$$

$$C_R = 9.74 \left(0.668 \frac{1}{9.5} + 0.194 \frac{0}{10.5} + 0.139 \frac{0}{10} \right) = 0.685$$

$$C_G = 9.74 \left(0.668 \frac{0}{9.5} + 0.194 \frac{1}{10.5} + 0.139 \frac{0}{10} \right) = 0.180$$

$$C_B = 9.74 \left(0.668 \frac{0}{9.5} + 0.194 \frac{0}{10.5} + 0.139 \frac{1}{10} \right) = 0.135$$

$$C = (0.685, 0.180, 0.135)$$



Aplicando Texturas

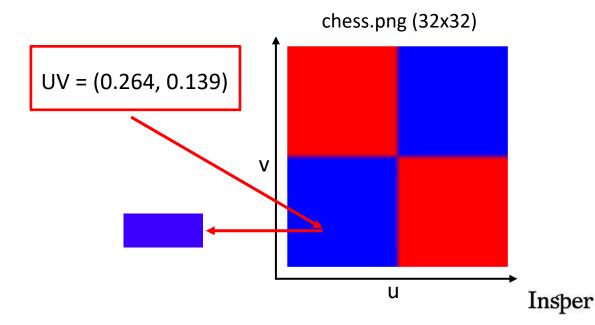


Triângulo com Texturas

```
<Scene>
 <Viewpoint position="0 0 10"/>
 <Transform rotation="0 1 0 0.52">
  <Shape>
   <IndexedFaceSet coordIndex='0 1 2 -1'>
     <Coordinate point='-1 -1 0 1 -1 0 0 1 0'/>
      <TextureCoordinate point='0.0 0.0 1.0 0.0 0.5 1.0'/>
   IndexedFaceSet>
   <Appearance>
     <lmageTexture url=' "chess.png" '/>
   </Appearance>
  </Shape>
 </Transform>
</Scene>
                       P<sub>2</sub> uv(0.5, 1.0)
  Pixel (28, 22)
                                P_1
                              uv(1.0, 0.0)
     uv(0.0, 0.0)
```

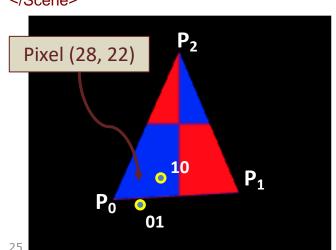
Pesos $U = \alpha U_0 + \beta U_1 + \gamma U_2$ $\alpha = 0.668$ U = 0.668*0.0 + 0.194*1.0 + 0.139*0.5 $\beta = 0.194$ U = 0.2635 $\gamma = 0.139$

 $V = \alpha V_0 + \beta V_1 + \gamma V_2$ V = 0.668*0.0 + 0.194*0.0 + 0.139*1.0 V = 0.139



Triângulo com Texturas MipMap

```
<Scene>
<Viewpoint position="0 0 10"/>
<Transform rotation="0 1 0 0.52">
<Shape>
<IndexedFaceSet coordIndex='0 1 2 -1'>
<Coordinate point='-1 -1 0 1 -1 0 0 1 0'/>
<TextureCoordinate point='0.0 0.0 1.0 0.0 0.5 1.0'/>
</IndexedFaceSet>
<Appearance>
<ImageTexture url=' "chess.png" '/>
</Appearance>
</Shape>
</Transform>
</Scene>
```



$$UV = (0.264, 0.139)$$

Coordenadas (u,v) pixel₁₀(29, 22) => UV(0.414, 0.129) pixel₀₁(28, 23) => UV(0.248, -0.010)

$$rac{\partial u}{\partial x} = rac{\mathrm{u}_{10} - \mathrm{u}_{00}}{1} \quad rac{\partial v}{\partial x} = rac{\mathrm{v}_{10} - \mathrm{v}_{00}}{1}$$

$$rac{\partial u}{\partial y} = rac{\mathrm{u}_{01} - \mathrm{u}_{00}}{1} \quad rac{\partial v}{\partial y} = rac{\mathrm{v}_{01} - \mathrm{v}_{00}}{1}$$

Triângulo com Texturas MipMap

Coordenadas (u,v)

x 32

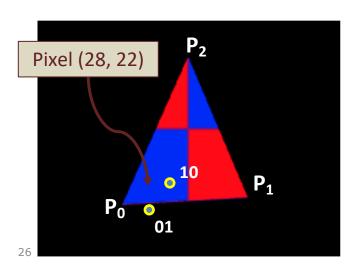
$$\frac{\partial u}{\partial x} = \frac{\mathbf{u}_{10} - \mathbf{u}_{00}}{1} = 32 \left(\frac{0.414 - 0.264}{1} \right) = 4.8$$

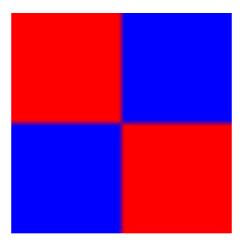
$$\frac{\partial u}{\partial y} = \frac{\mathbf{u}_{01} - \mathbf{u}_{00}}{1} = 32 \left(\frac{0.248 - 0.264}{1} \right) = -0.56$$

$$\frac{\partial v}{\partial x} = \frac{\mathbf{v}_{10} - \mathbf{v}_{00}}{1} = 32 \left(\frac{0.129 - 0.139}{1} \right) = -0.32$$

$$\frac{\partial v}{\partial y} = \frac{\mathbf{v}_{01} - \mathbf{v}_{00}}{1} = 32 \left(\frac{-0.010 - 0.139}{1} \right) = -4.8$$

chess.png (32x32)





Triângulo com Texturas MipMap

Coordenadas (u,v)

$$U = 0.264$$
 pixel (29 22) => 1

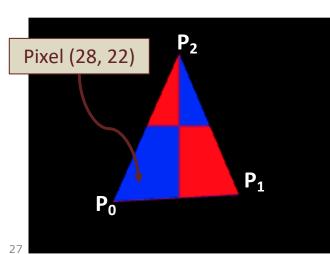
V = 0.139

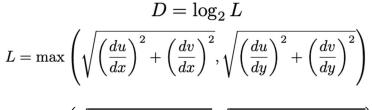
 $pixel_{10}(29, 22) => UV(0.414, 0.129)$

$$pixel_{01}(28, 23) => UV(0.248, -0.010)$$

$$\frac{du}{dx} = 4.8 \qquad \qquad \frac{dv}{dx} = -0.32$$

$$\frac{du}{dy} = -0.56 \qquad \frac{dv}{dy} = -4.8$$





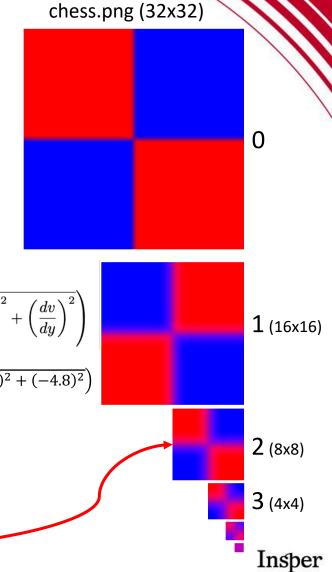
$$L = \max\left(\sqrt{(4.8)^2 + (-0.32)^2}, \sqrt{(-0.56)^2 + (-4.8)^2}\right)$$

$$L = \max(4.81,4,83)$$

L = 4.83

D = 2.27

D = 2



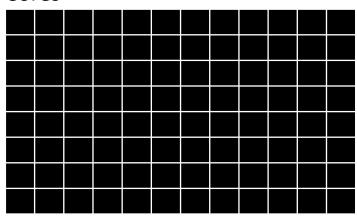
Z-Buffer



Desenhando com Z-Buffer

```
<Scene>
 <Transform translation="1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 0 2 -2 0 0 2 0'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='1 0 0'/>
   </Appearance>
  </Shape>
 </Transform>
 <Transform translation="-1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 -1 2 -2 -1 0 2 -1'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='0 0 1'/>
   </Appearance>
  </Shape>
 </Transform>
</Scene>
```

Cores



Profundidade

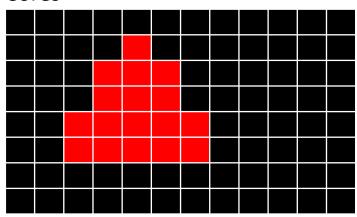
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1



Desenhando com Z-Buffer

```
<Scene>
 <Transform translation="1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 0 2 -2 0 0 2 0'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='1 0 0'/>
   </Appearance>
  </Shape>
 </Transform>
 <Transform translation="-1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 -1 2 -2 -1 0 2 -1'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='0 0 1'/>
   </Appearance>
  </Shape>
 </Transform>
</Scene>
```

Cores



Profundidade

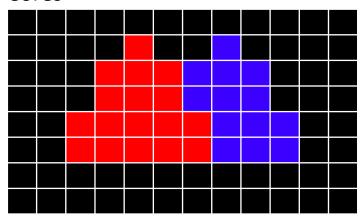
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	0.8	1	1	1	1	1	1	1
1	1	1	0.8	0.8	0.8	1	1	1	1	1	1
1	1	1	0.8	0.8	0.8	1	1	1	1	1	1
1	1	0.8	0.8	0.8	0.8	0.8	1	1	1	1	1
1	1	0.8	0.8	0.8	0.8	0.8	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1



Desenhando com Z-Buffer

```
<Scene>
 <Transform translation="1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 0 2 -2 0 0 2 0'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='1 0 0'/>
   </Appearance>
  </Shape>
 </Transform>
 <Transform translation="-1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 -1 2 -2 -1 0 2 -1'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='0 0 1'/>
   </Appearance>
  </Shape>
 </Transform>
</Scene>
```

Cores



Profundidade

1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	0.8	1	1	0.9	1	1	1	1
1	1	1	0.8	0.8	0.8	0.9	0.9	0.9	1	1	1
1	1	1	0.8	0.8	0.8	0.9	0.9	0.9	1	1	1
1	1	0.8	0.8	0.8	0.8	0.8	0.9	0.9	0.9	1	1
1	1	0.8	0.8	0.8	0.8	0.8	0.9	0.9	0.9	1	1
1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	1	1	1	1	1	1	1



Transparência



Transparência

```
<Scene>
 <Transform translation="-1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 -1 2 -2 -1 0 2 -1'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor ='0 0 1'/>
   </Appearance>
  </Shape>
 </Transform>
 <Transform translation="1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 0 2 -2 0 0 2 0'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='1 1 0'
              transparency='0.2'/>
   </Appearance>
  </Shape>
 </Transform>
</Scene>
```

Cores

											1
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,1)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)

```
cor_anterior = framebuffer[x,y] * transparência
cor_nova = rbg * (1 - transparência)
framebuffer[x,y] = cor_anterior + cor_nova
```



Transparência

```
<Scene>
 <Transform translation="-1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 -1 2 -2 -1 0 2 -1'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor ='0 0 1'/>
   </Appearance>
  </Shape>
 </Transform>
 <Transform translation="1 0 0">
  <Shape>
   <TriangleSet>
    <Coordinate point='-2 -2 0 2 -2 0 0 2 0'/>
   </TriangleSet>
   <Appearance>
    <Material emissiveColor='0 1 0'
              transparency='0.4'/>
   </Appearance>
  </Shape>
 </Transform>
</Scene>
```

Cores

(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0.6,0)	(0,0,0)	(0,0,0)	(0,0,1)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0.6,0)	(0,0.6,0)	(0,0.6,0)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0.6,0)	(0,0.6,0)	(0,0.6,0)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0.6,0)	(0,0.6,0)	(0,0.6,0)	(0,0.6,0.4)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0.6,0)	(0,0.6,0)	(0,0.6,0)	(0,0.6,0.4)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,1)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)
(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)	(0,0,0)

```
cor_anterior = framebuffer[x,y] * transparência
cor_nova = rbg * (1 - transparência)
framebuffer[x,y] = cor_anterior + cor_nova
```



Insper

Computação Gráfica

Luciano Soares lpsoares@insper.edu.br