

# ECE 411 - HW3 & HW4 Exam Cheat Sheet (Lipo-Novotny Conventions)

## 1) Frames & Conventions

- q-axis  $\parallel \alpha$  at  $\theta=0$ ; d is  $-90^\circ$  from q (clockwise).
- $\theta_e$ : electrical angle ( $\alpha \rightarrow q$ , CCW);  $\omega_e = d\theta_e/dt$ .
- $q = \text{Real}\{\cdot\}$ ,  $d = -\text{Imag}\{\cdot\}$ ;  $\beta = -\text{Imag}\{\alpha\beta\}$  for plotting.

## 2) Clarke & Park Transforms

Clarke:  $\alpha = (2/3)[V_a - 0.5V_b - 0.5V_c]$

$$\beta = (2/3)(\sqrt{3}/2)(V_c - V_b)$$

Park:  $q = \alpha \cos\theta - \beta \sin\theta$

$$d = \alpha \sin\theta + \beta \cos\theta$$

Inverse:  $\alpha = q \cos\theta + d \sin\theta$ ;  $\beta = -q \sin\theta + d \cos\theta$

## 3) Phasor Definitions

$$a = e^{j2\pi/3}; \quad x_{\{\alpha\beta\}} = (2/3)(x_a + a x_b + a^2 x_c)$$

Park:  $x_{\{qd\}} = x_{\{\alpha\beta\}} e^{-j\theta_e}$ ;  $q = \text{Re}\{x_{\{qd\}}\}$ ,  $d = -\text{Im}\{x_{\{qd\}}\}$

$$E_0 = \omega_e \Lambda_0; \quad \Lambda_0 = E_0 / \omega_e$$

## 4) Base Quantities (per-unit)

$$V_B = V_{\{dc\}}/\sqrt{3}, \quad I_B = I_{\{\max\}}, \quad Z_B = V_B/I_B$$

$$P_B = 1.5 V_B I_B, \quad \omega_B = 2\pi f_B, \quad T_B = P_B/\omega_{\{mB\}}$$

## 5) Voltage Equations

Round-rotor:  $V_q = R_s I_q + \omega_e L_s I_d + E_q$

$$V_d = R_s I_d - \omega_e L_s I_q + E_d$$

Salient-pole:  $V_q = R_s I_q + \omega_e L_d I_d + E_q$

$$V_d = R_s I_d - \omega_e L_q I_q + E_d$$

## 6) Torque & Power

$$P = 1.5(V_q I_q + V_d I_d)$$

$$T_e = P / \omega_e$$

$$T_e = (E_q I_q)/\omega_e + ((L_d - L_q) I_d I_q)/\omega_e$$

Salient-pole:

$$T_{\text{field}} = -(E_0 V_0)/(\omega_e L_d) \sin\delta$$

$$T_{\text{rel}} = -(V_0^2(L_d - L_q))/(2\omega_e L_d L_q) \sin(2\delta)$$

One-page review — HW3 & HW4 core equations under Lipo-Novotny convention.

$$T_e = T_{\text{field}} + T_{\text{rel}}$$

## 7) Field Weakening

Voltage limit ( $R_s=0$ ):  $V_0^2 = (\omega_e \Lambda_0)^2 - (\omega_e L_s I_0)^2$

$$\Lambda_0 = \sqrt{[(V_0/\omega_e)^2 + (L_s I_0)^2]}$$

$$T_{\max} = V_0 I_0 / \omega_e; \quad P_{\max} = V_0 I_0$$

$$\text{Flux ratio} = \Lambda_{\text{new}} / \Lambda_{\text{rated}}$$

## 8) $R_s \neq 0$ Effects

$$Z_s = \sqrt{(R_s^2 + (\omega_e L_s)^2)}$$

$$T_{\max} = (V_0 E_0)/(\omega_e Z_s) - (E_0^2 R_s)/(\omega_e Z_s^2)$$

$$\delta_{\max} = \sin^{-1}(R_s/Z_s) - \pi/2$$

## 9) Saliency & Ratios

$$\text{Saliency ratio } \xi = L_d / L_q$$

$$T_{\text{rel,max}} = T_{\text{field,max}} \rightarrow L_q = (V_0 L_d)/(2E_0 + V_0 R_s)$$

## 10) Quick Reference (exam tips)

- Open-circuit:  $v_q \approx \omega_e \Lambda_0$ ,  $v_d \approx 0$  (confirm q- $\alpha$  alignment).
- Generator:  $P_{\text{mech}} = -P_{\text{elec}}$ ; motoring  $\rightarrow +T_e$ .
- $\delta$  increases with load torque; small  $\delta \approx$  linear region.
- Keep per-unit bases consistent ( $V_B$ ,  $I_B$ ,  $L$  in pu).
- $q$  = torque-producing axis;  $d$  = flux (field) axis.