Numerical Methods Course Assignment Report

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Abstract

In this work we present the analysis of the linear advection equation modelled in one dimension, x, without sources or sinks of the advected variable ϕ . The exact expression of the equation is:

$$\phi_t + u\phi_x = 0 \tag{1}$$

We consider the case of constant and uniform wind, u, and with given initial condition $\phi(x,0) = \phi_0$. It can be shown that the analytic solution of (1) is:

$$\phi(x,t) = \phi_0(x - ut) \tag{2}$$

We have modelled equation (1) using several numerical schemes, currently:

- FTBS
- CTCS

The FTBS scheme has been chosen for its "naivety", being first order accurate in time and space, to show how a "basic" method works. The CTCS method has been chosen because, among the explicit ones, it's the method that guarantees the highest order of accuracy, namely two. A comparison of the two methods has been carried out. This report contains the preliminary results, the full analysis will be presented in the final version of the submission which will contain further developements.

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Chapter 1

FTBS

The first method to be explored is FTBS. Characteristics of the method can be found in [1]. FTBS has been chosen as "naive" method to be compared to a more "sophisticathed" method and show the quantitative and qualitative differences.

1.1 General characteristics

We will explore the characteristics of the FTBS method, in terms of

1.2 Phyton code

The function used for the method is in the file advectionSchemes.py, and the function in the code is the following, with comments included on the meaning of inputs:

Bibliography

[1] J. Bröcker, B. Calderhead, D. Cheraghi, C. Cotter, D. Holm, T. Kuna, B. Pelloni, T. Shepherd, H. Weller. M α thematics of Planet Earth World Scientific, 2017