Homework Project 2

Given 10/21/2015, Due 11/04/2015

Implement the randomized incremental algorithm to compute the maximum of a linear objective function of four variables under a set of linear inequalities.

You should write a function

which has as parameters the number of inequalities n, the coefficient matrix A and right-hand side b, the coefficients of the objective function c, as well as the result vector result, which contains the optimum values for the four variables x_0, \ldots, x_3 . It returns an integer, which is the number of recomputations at the top level taken by the algorithm to reach the optimum.

Your function should solve the LP problem

$$\begin{aligned} \max \mathbf{c} [\mathbf{0}] x_0 + \mathbf{c} [\mathbf{1}] x_1 + \mathbf{c} [\mathbf{2}] x_2 + \mathbf{c} [\mathbf{3}] x_3 \\ & \mathbf{A} [\mathbf{0}] [\mathbf{0}] x_0 + \dots + \mathbf{A} [\mathbf{0}] [\mathbf{3}] x_3 \leq \mathbf{b} [\mathbf{0}] \\ & \mathbf{A} [\mathbf{1}] [\mathbf{0}] x_0 + \dots + \mathbf{A} [\mathbf{1}] [\mathbf{3}] x_3 \leq \mathbf{b} [\mathbf{1}] \\ & \vdots \\ & \mathbf{A} [\mathbf{n} - \mathbf{1}] [\mathbf{0}] x_0 + \dots + \mathbf{A} [\mathbf{n} - \mathbf{1}] [\mathbf{3}] x_3 \leq \mathbf{b} [\mathbf{n} - \mathbf{1}] \\ & x_0 \geq 0, x_1 \geq 0, \dots, x_3 \geq 0 \end{aligned}$$

The matrix is a 4 by n matrix with n fairly large, so do not make any assumptions on the size of the matrix; any additional storage you need should be allocated dynamically. The programming language is C or C++; test your code before submission using the gcc or g++ compiler. Submit your source code (the function) by mail to peter@cs.ccny.cuny.edu.