CISC352 - Assignment 02

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1 Part 1: Pathfinding

Pre and Post Processing

Both of the following function implementations will need to read from an input file and write into an output file. This is is done through the help of the following helper functions.

```
def reader(filename):
    return_grid = []
    with open(filename) as f:
        # grid_data = [i.split() for i in f.readlines()]
        for i in f.readlines():
            a_line = i.split()
            a_list_first = a_line[0]
            the_chars = list(a_list_first)
            return_grid.append(the_chars)
        # print(the_chars)
        return return_grid
```

```
def writer(filename, grid):
    with open(filename, 'w+') as f:
    # f.write(grid_data2)
    for i in grid:
        f.write(''.join(i) + '\n')
```

In addition to this, we needed a way to find the specific locations for the *Start* cell and the *Goal* cell, this was aided through the following helper function.

1.1 Greedy

A greedy algorithm attempts to solve a problem by making the locally optimal choice at each stage in the hopes of finding the globally optimum. In pathfinding,

the algorithm will find the heuristics for all of its available options and choose the best option at that moment.

```
def greedy_a(tmp_grid, s_loc, g_loc):
    def greedy_b(tmp_grid, s_loc, g_loc):
         a_grid = copy.deepcopy(tmp_grid)
2
3
         curr_loc = copy.deepcopy(s_loc)
         prev_dir = "None"
4
         stuck = False
5
         while (not(stuck)):
6
              print("\n")
               for x in a_grid:
               print(','.join(x))
left_dist = math.inf
9
10
               right_dist = math.inf
               up_dist = math.inf
12
               down_dist = math.inf
               up\_right\_dist = math.inf
14
               up_left_dist = math.inf
15
16
               down_right_dist = math.inf
               down_left_dist = math.inf
17
18
         #Get the H values for all the directions.
19
20
         # Left distance
21
               if ((curr_loc[1] - 1) >= 0):
22
                    if (a_grid [curr_loc [0]] [curr_loc [1] - 1] == 'G'):
23
                         return a_grid
24
                    if (a_grid [curr_loc [0]] [curr_loc [1] - 1] == '_'):
25
                        # left_dist = (row_diff + col_diff)
26
         \begin{array}{c} \text{left\_dist} = \text{cheb} \left( \left[ \text{curr\_loc} \left[ 0 \right], \left( \text{curr\_loc} \left[ 1 \right] - 1 \right) \right], \\ \text{g\_loc} \right) \# \left( \text{g\_loc} \left[ 0 \right] - \text{curr\_loc} \left[ 0 \right] \right) + \left( \text{g\_loc} \left[ 1 \right] - \left( \text{curr\_loc} \left[ 1 \right] - 1 \right) \right) \\ \# \text{print} \left( \text{"left\_dist} = \text{", left\_dist} \right) \end{array}
27
              # Right distance
29
30
               if ((curr\_loc[1] + 1) < len(a\_grid[0])):
                     if (a\_grid [curr\_loc [0]] [curr\_loc [1] + 1] = 'G'): 
31
                         return a_grid
32
                    if (a_grid [curr_loc [0]] [curr_loc [1] + 1] == '-'):
33
                        # right_dist = (row_diff + col_diff)
34
                         right_dist = cheb([curr_loc[0],(curr_loc[1]+1)]
35
          \begin{array}{lll} g\_loc)\#(g\_loc\left[0\right]-curr\_loc\left[0\right])+(g\_loc\left[1\right]-(curr\_loc\left[1\right]+1))\\ \#print("right\_dist=", right\_dist) \end{array} 
36
              # Up distance
37
               if ((curr\_loc[0] - 1) >= 0):
38
                    if (a_grid [(curr_loc[0]-1)][curr_loc[1]] = 'G'):
39
                         return a_grid
40
                    if (a_grid [(curr_loc[0]+1)][curr_loc[1]] == '-'):
41
                        # up_dist = (row_diff + col_diff)
42
                         up\_dist = cheb([(curr\_loc[0]-1), curr\_loc[1]], g\_loc)
43
         44
              # Down distance
45
               if ((\operatorname{curr\_loc}[0] + 1) < \operatorname{len}(\operatorname{a\_grid})):
46
                    if (a\_grid[(curr\_loc[0]+1)][curr\_loc[1]] = 'G'):
47
                         return a_grid
48
                    if (a_grid [(curr_loc[0]+1)][curr_loc[1]] == ', '):
49
                        \# down_dist = (row_diff + col_diff)
```

```
down_dist = cheb([(curr_loc[0]+1), curr_loc[1]],
51
        g_{loc}) #(g_{loc}[0] - (curr_{loc}[0]+1)) + (g_{loc}[1] - curr_{loc}[1])
                      #print("down_dist = ", down_dist)
             #Up + Right (diagonal)
53
             if (((\operatorname{curr\_loc}[0] - 1) >= 0) and ((\operatorname{curr\_loc}[1] + 1) < \operatorname{len}(
54
        a_grid [0]))):
             #
                                          up
                  if (a_{\text{grid}} [ \text{curr-loc} [0] - 1] [ \text{curr-loc} [1] + 1] = 'G'):
56
                      return a_grid
57
58
                  if (a\_grid[curr\_loc[0]-1][curr\_loc[1]+1] = '\_'):
59
                      up\_right\_dist = cheb([(curr\_loc[0]-1),(curr\_loc
60
        [1]+1)], g_loc)
61
62
             #Up + Left (diagonal)
             if (((\operatorname{curr\_loc}[0] - 1) >= 0) and ((\operatorname{curr\_loc}[1] - 1) < \operatorname{len}(
63
        a_grid [0]))):
                                                        Left
             #
                  if (a\_grid[curr\_loc[0]-1][curr\_loc[1]-1] = 'G'):
65
66
                      return a_grid
67
                  if (a_grid [curr_loc[0]-1][curr_loc[1]-1] == '.'):
68
                       up\_left\_dist = cheb([(curr\_loc[0]-1),(curr\_loc
        [1]-1)], g_loc)
70
71
             #Down + Right (diagonal)
             if (((curr_loc[0] + 1) >= 0) and ((curr_loc[1] + 1) < len(
72
        a_grid [0]))):
                                         Down
73
             #
74
                  if (a\_grid[curr\_loc[0]+1][curr\_loc[1]+1] = 'G'):
75
                       return a_grid
             #
                                          Down
76
                                                           right
                  if (a_grid [curr_loc[0]+1][curr_loc[1]+1] == '-'):
77
                       down_right_dist = cheb([(curr_loc[0]+1),(curr_loc
78
        [1]+1)],g-loc)
79
80
             #Down + Left (diagonal)
             if (((\text{curr\_loc}[0] + 1) >= 0) and ((\text{curr\_loc}[1] - 1) < \text{len}(
81
        a_grid [0]))):
                                          Down
             #
82
                  if (a\_grid[curr\_loc[0]+1][curr\_loc[1]-1] = 'G'):
83
                       return a_grid
84
                                          Down
85
                  if (a_grid [curr_loc [0]+1][curr_loc [1]-1] == ', '):
86
87
                      down_left_dist = cheb([(curr_loc[0]+1),(curr_loc
        [1]-1)], g_loc)
88
89
             if (left_dist = math.inf and right_dist = math.inf and
90
        up_dist == math.inf and down_dist == math.inf):
                  stuck = True
91
                  return False
92
93
             if (not(stuck)):
94
                  # TODO: Improve the checking for None values before min
95
                  min_index = randomMinIndex([up_dist, down_dist,
96
        left\_dist\ ,\ right\_dist\ ,\ up\_right\_dist\ ,\ up\_left\_dist\ ,
        down_right_dist , down_left_dist])
    #print("Previous direction was %s" % prev_dir)
97
                  if (prev_dir == "Down" and min_index == 0):
98
                      return False
99
```

```
if(prev_dir == "Up" and min_index == 1):
                               return False
101
                         if(prev_dir == "Right" and min_index == 2):
103
                               return False
                         if (prev_dir == "Left" and min_index == 3):
104
                               return False
105
106
                        #Diagonal Directions
108
                         if (\min_{i=1}^{n} dex == 4):
                               curr_loc [0] -= 1
109
                               curr_loc[1] += 1
                               a\_grid\left[\,curr\_loc\left[\,0\,\right]\,\right]\left[\,curr\_loc\left[\,1\,\right]\,\right] \;=\; {}^{\backprime}P\,{}^{\backprime}
111
                              #print('up_right
                         elif (min_index = 5):
113
114
                               curr_loc[0] = 1
                               curr_loc[1] -= 1
                               a\_grid\left[\,curr\_loc\left[\,0\,\right]\,\right]\left[\,curr\_loc\left[\,1\,\right]\,\right] \;=\; {}^{\backprime}P^{\,\backprime}
116
                              #print('up_left'
117
                         elif (\min_{i=0}^{n} dex = 6):
118
                               curr_loc[0] += 1
119
                               curr_loc[1] += 1
120
                               a\_grid \left[ \, curr\_loc \left[ \, 0 \, \right] \, \right] \left[ \, curr\_loc \left[ \, 1 \, \right] \, \right] \; = \; \, {}^{\prime}P \, {}^{\prime}
121
                              #print('down_right
                         elif (\min_{i=1}^{n} \text{index} = 7):
                               curr_loc[0] += 1
curr_loc[1] -= 1
124
125
                               a_{grid}[curr_{loc}[0]][curr_{loc}[1]] = 'P'
126
127
                              #print('down_left')
128
                        #Cardinal Directions
129
                         elif (\min_{i=1}^{n} index = 2):
130
                               curr_loc[1] -= 1
131
                               a\_grid\left[\,curr\_loc\left[\,0\,\right]\,\right]\left[\,curr\_loc\left[\,1\,\right]\,\right] \;=\; {}^{\backprime}P\,{}^{\backprime}
                              #print('left')
133
                         elif (\min_{i=1}^{n} dex = 3):
135
                               curr_loc[1] += 1
136
                               a_grid[curr_loc[0]][curr_loc[1]] = 'P'
137
138
                              #print('right')
                         elif (min_index = 0)
139
                               curr_loc[0] = 1
140
                               a_grid[curr_loc[0]][curr_loc[1]] = 'P'
141
                              #print('up')
142
                         elif (\min_{i=1}^{n} index = 1):
143
144
                               curr_loc[0] += 1
                               a_grid[curr_loc[0]][curr_loc[1]] = 'P'
145
                              #print('down')
```

1.2 A*

A* is an informed-search algorithm, very similar to Dijkstra's algorithm for finding the shortest paths in graph, except for the fact that the priority isn't just sorted by the distance but by the distance of the path and the distance it has to go.

1.2.1 Standard (A*_a)

The a_star_a function takes 3 parameters; a grid, the location of the start and goal as an array in row, column format.

```
def a_star_a(tmp_grid, s_loc, g_loc):
```

Our solution for the non-diagonal movement for pathfinding starts by creating a local copy of the grid, an array to hold the visited nodes that the current node has come from as well as an array to hold the associated costs. Both of the mentioned arrays are multidimensional arrays initialized to the values *None* representing the entire grid, this is to have a 1:1 representation of costs and visited nodes to our original grid. Lastly, the initialize the needed priority queue, boolean flag to determine if a solution has been found, and variable containing the our current location.

We start the search for the goal by first pushing the root node onto the priority queue using a priority value determined by the Manhattan distance heuristic from the *Start Node* to the *Goal Node*.

```
lastlinelastline
   def manhattan(a, b):
2
        return abs(a[0] - b[0]) + abs(a[1] - b[1])
3
   #Will be used to find the h values for up down left right and
       diagonals
   def cheb(a, b):
       return max( abs( a[0] - b[0] ), abs( a[1] - b[1] ))
   def printMatrix(matrix):
9
       print("\n")
        for x in matrix:
11
12
            print(x)
   def a_star_b(tmp_grid, s_loc, g_loc):
14
15
        a_grid = copy.deepcopy(tmp_grid)
       came_from = [[None for j in range(len(a_grid[0]))] for i in
16
       range(len(a_grid))]
        cost = [[None for j in range(len(a_grid[0]))] for i in range(
       len(a_grid))]
18
        cost[s_loc[0]][s_loc[1]] = 0
19
20
21
        curr_loc = None #copy.deepcopy(s_loc)
        foundGoal = False
22
        visited = []
23
24
        heappush (visited, (cheb(s_loc, g_loc), s_loc))
25
26
       #Find the goal
27
        while (not (foundGoal)):
28
            curr_node = heappop(visited)
29
            curr_loc = curr_node[1]
30
31
            if (a\_grid[curr\_loc[0]][curr\_loc[1]] = 'G'):
                foundGoal = True
33
34
            if (not (foundGoal)):
35
                #Left
36
                \inf \left( \operatorname{curr\_loc} \left[ 1 \right] - 1 >= 0 \right) :
37
       38
                         cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
40
41
                         if(cost[curr\_loc[0])[curr\_loc[1] - 1] == None
42
       or cost\_so\_far + 1 < cost[curr\_loc[0]][curr\_loc[1] - 1]):
```

```
cost[curr\_loc[0]][curr\_loc[1] - 1] =
            cost_so_far + 1
                                              came\_from[curr\_loc[0]][curr\_loc[1] - 1] = [
44
            curr_loc[0], curr_loc[1]]
                                              heappush(visited, (cost\_so\_far + 1 + cheb([
45
            \operatorname{curr\_loc}[0], \operatorname{curr\_loc}[1] - 1, \operatorname{g\_loc}), [\operatorname{curr\_loc}[0], \operatorname{curr\_loc}
            [1] - 1]))
46
                         #Right
47
                          if(curr\_loc[1] + 1 < len(a\_grid[0])):
48
                                 if(a\_grid[curr\_loc[0]][curr\_loc[1] + 1] = '\_' or
49
            a_{grid}[curr_{loc}[0]][curr_{loc}[1] + 1] = G':
                                        cost_so_far = cost[curr_loc[0]][curr_loc[1]]
50
51
             \begin{array}{c} if\left(\operatorname{cost}\left[\operatorname{curr\_loc}\left[0\right]\right]\left[\operatorname{curr\_loc}\left[1\right]+1\right] \Longrightarrow \operatorname{None} \\ \operatorname{or} \ \operatorname{cost\_so\_far}+1 < \operatorname{cost}\left[\operatorname{curr\_loc}\left[0\right]\right]\left[\operatorname{curr\_loc}\left[1\right]+1\right]\right): \\ \operatorname{cost}\left[\operatorname{curr\_loc}\left[0\right]\right]\left[\operatorname{curr\_loc}\left[1\right]+1\right] = \end{array} 
            cost_so_far + 1
                                              came\_from[curr\_loc[0]][curr\_loc[1] + 1] = [
            curr_loc[0], curr_loc[1]]
                                              heappush (\, visited \,\, , \,\, (\, cost\_so\_far \,\, + \,\, 1 \,\, + \,\, cheb \, (\, [
56
            \operatorname{curr-loc}[0], \operatorname{curr-loc}[1] + 1, \operatorname{g-loc}), \operatorname{[curr-loc}[0], \operatorname{curr-loc}
            [1] + 1]))
57
58
                         #Up
                          if(curr_loc[0] - 1 >= 0):
59
                                 if (a\_grid[curr\_loc[0] - 1][curr\_loc[1]] = '\_' or
60
            a_{grid}[curr_{loc}[0] - 1][curr_{loc}[1]] = G'
                                        cost_so_far = cost [curr_loc [0]][curr_loc [1]]
61
62
                                        if(cost[curr\_loc[0] - 1][curr\_loc[1]] == None
64
            or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1]]):
                                              cost[curr\_loc[0] - 1][curr\_loc[1]] =
65
            cost\_so\_far + 1
                                              came\_from[curr\_loc[0] - 1][curr\_loc[1]] = [
66
            curr_loc[0], curr_loc[1]]
                                              heappush (visited, (cost_so_far + 1 + cheb([
            \operatorname{curr\_loc}[0] - 1, \operatorname{curr\_loc}[1], \operatorname{g\_loc}), [\operatorname{curr\_loc}[0] - 1,
            curr_loc[1]]))
                         #Down
69
            \begin{array}{c} \text{if} (\text{curr\_loc} \, [0] \, + \, 1 \, < \, \text{len} (\text{a\_grid})) \colon \\ \text{if} (\text{a\_grid} \, [\text{curr\_loc} \, [0] \, + \, 1] [\text{curr\_loc} \, [1]] \, = \, \, '\_' \text{ or} \\ \text{a\_grid} \, [\text{curr\_loc} \, [0] \, + \, 1] [\text{curr\_loc} \, [1]] \, = \, \, 'G') \colon \end{array}
70
71
                                        cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
72
73
74
                                        if(cost[curr\_loc[0] + 1][curr\_loc[1]] == None
75
            or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1]]):
                                              cost[curr\_loc[0] + 1][curr\_loc[1]] =
76
            cost\_so\_far + 1
                                              came\_from[curr\_loc[0] + 1][curr\_loc[1]] = [
            curr_loc[0], curr_loc[1]]
                                              heappush(visited, (cost_so_far + 1 + cheb([
             {\tt curr\_loc} \, [0] \, + \, 1 \, , \ {\tt curr\_loc} \, [1]] \, , \ {\tt g\_loc}) \, , \ [\, {\tt curr\_loc} \, [0] \, + \, 1 \, , \\
            curr_loc[1]]))
79
                         #Up Left
80
                          if (\operatorname{curr\_loc}[0] - 1 >= 0 \text{ and } \operatorname{curr\_loc}[1] - 1 >= 0):
81
                                if(a\_grid[curr\_loc[0] - 1][curr\_loc[1] - 1] = '\_'
82
```

```
or a_grid [curr_loc [0] - 1] [curr_loc [1] - 1] = 'G'):
                           cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
83
84
85
                           if(cost[curr\_loc[0] - 1][curr\_loc[1] - 1] =
86
               or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1] -
         None
         1]):
                               cost[curr\_loc[0] - 1][curr\_loc[1] - 1] =
87
         cost\_so\_far + 1
                               came\_from[curr\_loc[0] - 1][curr\_loc[1] - 1]
         = [\operatorname{curr\_loc}[0], \operatorname{curr\_loc}[1]]
                               heappush(visited, (cost_so_far + 1 + cheb([
         curr_loc[0] - 1, curr_loc[1] - 1, g_loc, [curr_loc[0] - 1, curr_loc[1] - 1))
                  #Up Right
91
                  if(curr_loc[0] - 1 \text{ and } curr_loc[1] + 1 < len(a_grid[0])
92
         ):
         93
                           cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
94
95
96
                           if(cost[curr\_loc[0] - 1][curr\_loc[1] + 1] =
97
               or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1] +
         None
         1]):
                               cost[curr_loc[0] - 1][curr_loc[1] + 1] =
98
         cost\_so\_far \ + \ 1
                               came\_from[curr\_loc[0] - 1][curr\_loc[1] + 1]
99
         = [\operatorname{curr\_loc}[0] - 1, \operatorname{curr\_loc}[1]]
                               heappush (visited, (cost_so_far + 1 + cheb([
         curr_loc[0] - 1, curr_loc[1] + 1, g_loc, [curr_loc[0] - 1,
         curr_loc[1] + 1]))
                  #Down Left
                  if(curr_loc[0] + 1 < len(a_grid) and curr_loc[1] - 1 >=
103
          0):
                      if(a_grid[curr_loc[0] + 1][curr_loc[1] - 1] = '_-'
104
         or a_grid [curr_loc [0] + 1] [curr_loc [1] - 1] == 'G'):
                           cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
106
107
                           if(cost[curr\_loc[0] + 1][curr\_loc[1] - 1] =
108
               or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1] -
         None
         1]):
                               cost[curr_loc[0] + 1][curr_loc[1] - 1] =
         cost_so_far + 1
                               came\_from[curr\_loc[0] + 1][curr\_loc[1] - 1]
         = [\operatorname{curr\_loc}[0], \operatorname{curr\_loc}[1]]
                               heappush(visited, (cost_so_far + 1 + cheb([
         curr_loc[0] + 1, curr_loc[1] - 1, g_loc, [curr_loc[0] + 1,
         curr_loc[1] - 1]))
                  #Down Right
113
                  if(curr\_loc[0] + 1 < len(a\_grid)  and curr\_loc[1] + 1 < len(a\_grid) 
         len(a_grid[0]):
         if (a\_grid[curr\_loc[0] + 1][curr\_loc[1] + 1] = '\_'
or a\_grid[curr\_loc[0] + 1][curr\_loc[1] + 1] = 'G'):
115
                           cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
117
118
                           if(cost[curr\_loc[0] + 1][curr\_loc[1] + 1] =
119
```

```
None or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1] +
         1]):
                                  cost[curr\_loc[0] + 1][curr\_loc[1] + 1] =
120
          cost\_so\_far + 1
                                  came\_from[curr\_loc[0] + 1][curr\_loc[1] + 1]
          = [curr_loc[0], curr_loc[1]]
                                  heappush(visited, (cost\_so\_far + 1 + cheb([
         curr_loc[0] + 1, curr_loc[1] + 1, g_loc, [curr_loc[0] + 1,
         curr_loc[1] + 1]))
          while (came_from [curr_loc [0]] [curr_loc [1]] != None):
124
              curr\_loc = came\_from[curr\_loc[0]][curr\_loc[1]]
              if (a_grid [curr_loc [0]][curr_loc [1]] != 'S'):
    a_grid [curr_loc [0]][curr_loc [1]] = 'P'
126
127
128
         return a_grid
129
130
     def a_star_a(tmp_grid, s_loc, g_loc):
131
          a\_grid\ =\ copy.\, deepcopy\, (\,tmp\_grid\,)
132
         came\_from = \hbox{\tt [[None for j in range(len(a\_grid[0]))] for i in}
133
         range(len(a_grid))]
         cost = [[None for j in range(len(a_grid[0]))] for i in range(
134
         len(a_grid))]
         cost[s_{loc}[0]][s_{loc}[1]] = 0
136
137
          {\tt curr\_loc} \ = \ None \ \#{\tt copy.deepcopy} \, (\, s\_loc \, )
138
139
         foundGoal = False
          visited = []
140
141
         heappush (visited, (manhattan (s_loc, g_loc), s_loc))
143
         #Find the goal
144
          while (not (foundGoal)):
145
              curr_node = heappop(visited)
146
147
              curr\_loc = curr\_node[1]
148
              if (a\_grid[curr\_loc[0]][curr\_loc[1]] = 'G'):
149
                   foundGoal = True
              if (not (foundGoal)):
                   #Left
153
                    if(curr\_loc[1] - 1 >= 0):
                         if (a\_grid[curr\_loc[0]][curr\_loc[1] - 1] == '\_' or 
          a_{grid} [curr_{loc}[0]] [curr_{loc}[1] - 1] = 'G'):
                             cost_so_far = cost[curr_loc[0]][curr_loc[1]]
157
158
                             if(cost[curr\_loc[0])[curr\_loc[1] - 1] == None
         or cost_so_far + 1 < cost[curr_loc[0]][curr_loc[1] - 1]):
                                  cost [curr_loc [0]] [curr_loc [1] - 1] =
160
         cost_so_far + 1
                                  came\_from [curr\_loc [0]] [curr\_loc [1] - 1] = [
161
         curr_loc[0], curr_loc[1]]
                                  heappush(visited, (cost\_so\_far + 1 +
         manhattan\left(\left[\,curr\_loc\,[0]\,\,,\,\,curr\_loc\,[1]\,\,-\,\,1\right]\,,\,\,g\_loc\,\right)\,,\,\,\left[\,curr\_loc\,[0]\,\,,\,\,d
           curr_loc[1] - 1]))
                   #Right
164
165
                    if(\operatorname{curr\_loc}[1] + 1 < \operatorname{len}(\operatorname{a\_grid}[0])):
                         if(a_grid[curr_loc[0]][curr_loc[1] + 1] == '_' or
166
         a_{grid}[curr_{loc}[0]][curr_{loc}[1] + 1] = G'
```

```
167
                               cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
168
169
                               if(cost[curr\_loc[0]][curr\_loc[1] + 1] = None
          or cost\_so\_far + 1 < cost[curr\_loc[0]][curr\_loc[1] + 1]):
                                    cost [curr_loc [0]] [curr_loc [1] + 1] =
171
          cost\_so\_far + 1
                                    came\_from [curr\_loc [0]] [curr\_loc [1] + 1] = [
          curr_loc[0], curr_loc[1]]
                                     heappush(visited, (cost_so_far + 1 +
173
          manhattan \, (\, [\, curr\_loc \, [\, 0\, ]\,\, , \  \, curr\_loc \, [\, 1\, ]\,\, +\,\, 1\, ]\, , \  \, g\_loc \, )\, , \  \, [\, curr\_loc \, [\, 0\, ]\, ,
           curr_loc[1] + 1]))
174
                    #Up
176
                     if (curr\_loc[0] - 1 >= 0):
                          if (a\_grid[curr\_loc[0] - 1][curr\_loc[1]] = '\_' or
177
          a_{grid}[curr_{loc}[0] - 1][curr_{loc}[1]] \stackrel{?}{=} "G"):
                               cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
178
179
180
                               if (cost [curr\_loc [0] - 1] [curr\_loc [1]] == None
181
          or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1]]):
cost[curr\_loc[0] - 1][curr\_loc[1]] =
          cost_so_far + 1
                                    came\_from [curr\_loc [0] - 1][curr\_loc [1]] = [
183
          curr_loc[0], curr_loc[1]]
                                    heappush(visited, (cost\_so\_far + 1 +
184
          manhattan\left(\left[\,curr\_loc\,[0\,]\,-\,1\,,\;\;curr\_loc\,[1\,]\right]\,,\;\;g\_loc\,\right)\,,\;\;\left[\,curr\_loc\,[0\,]\,\right]
          - 1, curr_loc[1]]))
185
                     #Down
                     if(curr\_loc[0] + 1 < len(a\_grid)):
187
          \inf_{\substack{\text{if (a\_grid [curr\_loc [0] + 1][curr\_loc [1]] == '\_' \text{ or a\_grid [curr\_loc [0] + 1][curr\_loc [1]] == 'G'):}}
188
                               cost_so_far = cost [curr_loc [0]][curr_loc [1]]
189
190
191
          192
                                    cost[curr\_loc[0] + 1][curr\_loc[1]] =
          cost_so_far + 1
                                    came\_from [curr\_loc [0] + 1][curr\_loc [1]] = [
          \verb|curr-loc[0]|, \verb|curr-loc[1]||
                                    heappush (\, visited \,\, , \,\, (\, cost\_so\_far \,\, + \,\, 1 \,\, + \,\,
195
          manhattan ( [ \, curr\_loc \, [0] \, + \, 1 \, , \, \, curr\_loc \, [1] ] \, , \, \, g\_loc \, ) \, , \, \, [ \, curr\_loc \, [0] \,
          + 1, curr_loc[1]]))
          while (came_from [curr_loc [0]] [curr_loc [1]] != None):
197
                curr_loc = came_from [curr_loc [0]][curr_loc [1]]
198
                if (a_grid [curr_loc [0]] [curr_loc [1]] != 'S'):
199
                     a_{grid}[curr_{loc}[0]][curr_{loc}[1]] = P'
200
201
202
          return a_grid
203
     # uses manhattan distance (up down left right solution)
204
     def greedy_a(tmp_grid, s_loc, g_loc):
205
          a\_grid = copy.deepcopy(tmp\_grid)
206
          curr_loc = copy.deepcopy(s_loc)
207
          prev_dir = "None"
208
          stuck = False
209
          while (not(stuck)):
210
              print("\n")
211
```

```
for x in a_grid:
212
                                  print(''.join(x))
213
                          left_dist = math.inf
214
                          right_dist = math.inf
216
                          up_dist = math.inf
                          down_dist = math.inf
217
218
                          # Left distance
                          if ((curr_loc[1] - 1) >= 0):
219
                                   220
221
                                           return a_grid
                                   if(a_grid[curr_loc[0]][curr_loc[1] - 1] == ', '):
222
                  \begin{array}{lll} & \text{left\_dist} = \text{manhattan} ([\text{curr\_loc}[0], (\text{curr\_loc}[1]-1)], \text{g\_loc}) \# (\text{g\_loc}[0] - \text{curr\_loc}[0]) + (\text{g\_loc}[1] - (\text{curr\_loc}[0]) \end{array}
223
                  [1]-1))
                          # Right distance
                          if ((curr_loc[1] + 1) < len(a_grid[0]):
225
                                   226
                                           return a_grid
227
                                   if (a_grid [curr_loc [0]] [curr_loc [1] + 1] == '-'):
228
                                          # right_dist = (row_diff + col_diff)
229
                                           right_dist = manhattan([curr_loc[0], (curr_loc[1]+1)
230
                 [g_{loc}] = (g_{loc}) = (g_{loc}[0] - curr_{loc}[0]) + (g_{loc}[1] - (curr_{loc}[1] + 1))
                                          #print("right_dist = ", right_dist)
231
                          # Up distance
                          if ((curr_loc[0] - 1) >= 0):
                                   if (a\_grid[(curr\_loc[0]-1)][curr\_loc[1]] = 'G'):
234
235
                                           return a_grid
                                   if (a_grid [(curr_loc[0]-1)][curr_loc[1]] == '-'):
236
                                           # up_dist = (row_diff + col_diff)
237
                                           up\_dist = manhattan([(curr\_loc[0]-1), curr\_loc[1]],
                 g_loc)#(g_loc[0] - (curr_loc[0]-1)) + (g_loc[1] - curr_loc[1])
#print("up_dist = ", up_dist)
                          # Down distance
240
                          if ((\operatorname{curr-loc}[0] + 1) < \operatorname{len}(\operatorname{a-grid})):
241
                                   242
243
                                           return a_grid
                                   if (a_grid [(curr_loc[0]+1)][curr_loc[1]] == '_'):
244
245
                                          \# down_dist = (row_diff + col_diff)
                                           down\_dist = manhattan([(curr\_loc[0]+1), curr\_loc
246
                  [1]], g_{loc}) \#(g_{loc}[0] - (curr_{loc}[0]+1)) + (g_{loc}[1] - (curr_{loc}[1]+1)) + (g_{loc}[1]+1)) + (g_{loc}[1] - (curr_{loc}[1]+1)) + (g_{loc}[1]+1)) + (g_{loc}[1]+1)) + (g_{loc}[1]+1) + (g_{loc}[1]+1)) + (g_{loc}[1]+1) + (g_{loc}[1]
                  curr_loc[1])
                                          #print("down_dist = ", down_dist)
247
248
249
                          if (left_dist = math.inf and right_dist = math.inf and
250
                 up_dist == math.inf and down_dist == math.inf):
                                  stuck = True
251
                                   return False
252
253
                          if (not(stuck)):
254
                                  # TODO: Improve the checking for None values before min
                    check
                                   min_index = randomMinIndex([up_dist, down_dist,
256
                  left_dist , right_dist])#min(up_dist , down_dist , left_dist ,
                  right_dist)
                                  257
                                           return False
259
                                   if (prev_dir == "Up" and min_index == 1):
260
                                           return False
261
                                   if(prev_dir == "Right" and min_index == 2):
262
```

```
return False
263
                                              if(prev_dir == "Left" and min_index == 3):
264
                                                         return False
265
266
                                              if (\min_{i=1}^{n} 
267
                                                         if (prev_dir = "Right"):
268
269
                                                                   return False
                                                         prev_dir = "Left"
270
                                                         curr_loc[1] -= 1
271
                                                         a_{grid} [curr_{loc}[0]] [curr_{loc}[1]] = 'P'
272
                                                        #print('left')
273
                                              elif (\min_{i=1}^{n} dex = 3):
274
275
                                                         if (prev_dir == "Left"):
                                                                   return False
276
                                                         prev_dir = "Right"
277
                                                         curr_loc[1] += 1
a_grid[curr_loc[0]][curr_loc[1]] = 'P'
278
                                                        #print('right')
280
                                              elif (min_index == 0):
    if (prev_dir == "Down"):
281
282
                                                                   return False
283
                                                         prev_dir = "Up"
284
                                                         curr_loc[0] -= 1
                                                         a\_grid \left[ \, curr\_loc \, [\, 0\, ] \, \right] \left[ \, curr\_loc \, [\, 1\, ] \, \right] \; = \; {}^{\prime}P \, {}^{\prime}
286
                                                        #print('up')
287
288
                                                         (\min_{i} \text{index} = 1):
                                                         if (prev_dir = "Up"):
289
290
                                                                    return False
                                                         prev_dir = "Down"
291
                                                         curr_loc[0] += 1
292
                                                         a_grid[curr_loc[0]][curr_loc[1]] = P
293
                                                        #print('down')
294
295
           # uses cheb distance (up down left right diagonal solution)
296
            def greedy_b(tmp_grid, s_loc, g_loc):
297
298
                       a_grid = copy.deepcopy(tmp_grid)
                       curr_loc = copy.deepcopy(s_loc)
299
                       prev_dir = "None"
300
301
                       stuck = False
                       while (not(stuck)):
302
                                   print("\n")
303
304
                                   for x in a_grid:
                                             print(',', join(x))
305
                                   left_dist = math.inf
306
307
                                   right_dist = math.inf
                                   up_dist = math.inf
308
309
                                   down_dist = math.inf
                                   up\_right\_dist = math.inf
310
                                   up\_left\_dist = math.inf
311
                                   down\_right\_dist = math.inf
312
                                   down_left_dist = math.inf
313
314
                      #Get the H values for all the directions.
315
316
                      # Left distance
317
                                   if ((curr\_loc[1] - 1) >= 0):
318
                                              if (a\_grid[curr\_loc[0]][curr\_loc[1] - 1] = 'G'):
319
                                                       return a_grid
320
```

```
if (a_grid [curr_loc [0]] [curr_loc [1] - 1] == '_'):
321
                          # left_dist = (row_diff + col_diff)
322
                           left_dist = cheb([curr_loc[0], (curr_loc[1]-1)],
323
           g_loc) #(g_loc[0] - curr_loc[0]) + (g_loc[1] - (curr_loc[1]-1))
#print("left_dist = ", left_dist)
324
                # Right distance
325
                if ((curr_loc[1] + 1) < len(a_grid[0]):
                      if(a\_grid[curr\_loc[0]][curr\_loc[1]' + 1] = 'G'):
327
328
                           return a_grid
                      if (a_grid [curr_loc [0]] [curr_loc [1] + 1] == '_'):
329
                          # right_dist = (row_diff + col_diff)
330
                           \label{eq:right_dist} \mbox{right\_dist} \ = \ \mbox{cheb} \left( \left[ \mbox{curr\_loc} \left[ 0 \right], \left( \mbox{curr\_loc} \left[ 1 \right] + 1 \right) \right],
331
            \begin{array}{lll} g\_loc \,)\#(\,g\_loc\,[\,0\,] \,-\, \, curr\_loc\,[\,0\,] \,) \,+\, (\,g\_loc\,[\,1\,] \,-\, (\,curr\_loc\,[\,1\,] \,+\, 1) \,) \\ \#print\,(\,"\,right\_dist\,\,=\,\,",\,\,right\_dist\,\,) \end{array} 
332
333
                # Up distance
                if ((curr_loc[0] - 1) >= 0):
334
                      if (a\_grid[(curr\_loc[0]-1)][curr\_loc[1]] = 'G'):
335
336
                           return a_grid
                      337
338
                          \# \text{ up\_dist} = (\text{row\_diff} + \text{col\_diff})
                           up\_dist = cheb([(curr\_loc[0]-1), curr\_loc[1]], g\_loc)
339
          #(g_loc[0] - (curr_loc[0]-1)) + (g_loc[1] - curr_loc[1])
#print("up_dist = ", up_dist)
                # Down distance
341
                if ((curr_loc[0] + 1) < len(a_grid)):
342
                      if (a_grid[(curr_loc[0]+1)][curr_loc[1]] = 'G'):
                           return a_grid
344
                      if(a_grid[(curr_loc[0]+1)][curr_loc[1]] == '-'):
345
                          # down_dist = (row_diff + col_diff)
346
                           down_dist = cheb([(curr_loc[0]+1), curr_loc[1]],
347
           g_{-loc}) #(g_{-loc}[0] - (curr_{-loc}[0]+1)) + (g_{-loc}[1] - curr_{-loc}[1])
                          #print("down_dist = ", down_dist)
348
                #Up + Right (diagonal)
349
                if (((\operatorname{curr\_loc}[0] - 1) >= 0) and ((\operatorname{curr\_loc}[1] + 1) < \operatorname{len}(
350
           a_grid [0]))):
351
                #
                                                                right
                                                up
352
                      if (a\_grid[curr\_loc[0]-1][curr\_loc[1]+1] = 'G'):
                           return a_grid
353
354
                                                up
                      if (a\_grid [curr\_loc [0] - 1] [curr\_loc [1] + 1] = '\_'):
355
356
                           up\_right\_dist = cheb([(curr\_loc[0]-1),(curr\_loc
           [1]+1)], g_loc)
357
                #Up + Left (diagonal)
358
359
                 if (((\operatorname{curr\_loc}[0] - 1) >= 0) and ((\operatorname{curr\_loc}[1] - 1) < \operatorname{len}(
           a_grid [0]))):
                #
                                                                Left
360
                      if (a\_grid[curr\_loc[0]-1][curr\_loc[1]-1] = 'G'):
361
362
                           return a_grid
                                                                Left
363
                      if (a\_grid[curr\_loc[0]-1][curr\_loc[1]-1] = '\_'):
364
                          up\_left\_dist = cheb([(curr\_loc[0]-1),(curr\_loc
365
           [1]-1)], g_loc)
366
                #Down + Right (diagonal)
367
                if (((\operatorname{curr\_loc}[0] + 1) >= 0) and ((\operatorname{curr\_loc}[1] + 1) < \operatorname{len}(
368
           a_grid [0]))):
                #
                                                \operatorname{Down}
                      if (a_grid[curr_loc[0]+1][curr_loc[1]+1] = 'G'):
370
371
                           return a_grid
                                                Down
372
                      if (a_{grid} [curr_{loc}[0]+1] [curr_{loc}[1]+1] = '_{'}):
373
```

```
down_right_dist = cheb([(curr_loc[0]+1),(curr_loc
          [1]+1)], g_loc)
375
               #Down + Left (diagonal)
376
               if (((curr_loc[0] + 1) >= 0) and ((curr_loc[1] - 1) < len(
377
          a_grid [0]))):
              #
                                            Down
                    if (a\_grid[curr\_loc[0]+1][curr\_loc[1]-1] = 'G'):
379
380
                        return a_grid
381
                    \frac{if(a\_grid[curr\_loc[0]+1][curr\_loc[1]-1] == , \_,):}{}
382
                        down_left_dist = cheb([(curr_loc[0]+1),(curr_loc
383
          [1]-1)],g-loc)
384
               if (left_dist = math.inf and right_dist = math.inf and
386
          up_dist = math.inf and down_dist = math.inf):
                   stuck = True
                    return False
388
389
               if (not(stuck)):
390
                   # TODO: Improve the checking for None values before min
391
           check
                   min_index = randomMinIndex([up_dist, down_dist,
392
          left_dist , right_dist , up_right_dist , up_left_dist ,
          down_right_dist , down_left_dist])
    #print("Previous direction was %s" % prev_dir)
393
                    \inf (\text{prev\_dir} = \text{"Down"} \text{ and } \min_{\text{index}} = 0):
394
                        return False
395
                    if(prev_dir = "Up" and min_index = 1):
396
                        return False
397
                    if (prev_dir = "Right" and min_index = 2):
398
                        return False
399
                    if (prev_dir == "Left" and min_index == 3):
                        return False
401
402
403
                   #Diagonal Directions
                    if (\min_{i=1}^{n} dex = 4):
404
                        curr_loc[0] -= 1
405
                        curr_loc[1] += 1
406
                        a\_grid \, [\, curr\_loc \, [\, 0\, ]\, ] \, [\, curr\_loc \, [\, 1\, ]\, ] \,\, = \,\, {}^{\backprime}P\,{}^{\backprime}
407
                        #print('up_right')
408
                    elif (\min_{i=1}^{n} dex = 5):
409
                        curr\_loc[0] = 1
410
411
                        curr_loc[1] -= 1
                        a_grid [curr_loc [0]] [curr_loc [1]] = 'P'
412
413
                        #print('up_left'
                    elif (\min_{i=0}^{\infty} dex = 6):
414
                        curr_loc[0] += 1
415
                        curr_loc[1] += 1
416
                        a_grid[curr_loc[0]][curr_loc[1]] = 'P'
#print('down_right')
417
418
                    elif (min_index == 7):
419
                        curr\_loc[0] += 1
420
421
                        curr_loc[1] -= 1
                        a_{grid} [curr_{loc}[0]] [curr_{loc}[1]] = 'P'
422
                        #print('down_left')
423
424
                   #Cardinal Directions
425
426
                    elif (\min_{i=1}^{n} dex = 2):
                        curr_loc[1] -= 1
427
                        a_grid[curr_loc[0]][curr_loc[1]] = P
428
```

```
#print('left')
429
430
                     elif (\min_{i=1}^{n} index == 3):
431
432
                           curr_loc[1] += 1
                           a_grid [curr_loc [0]] [curr_loc [1]] = 'P'
433
                          #print('right')
434
435
                     elif (min_index = 0)
                          curr_loc [0] -= 1
436
                           a\_grid\left[\,curr\_loc\left[\,0\,\right]\,\right]\left[\,curr\_loc\left[\,1\,\right]\,\right] \;=\; {}^{\backprime}P\,{}^{\backprime}
437
                          #print('up')
438
                     elif (min_index == 1):
439
440
                          curr\_loc[0] += 1
                           a_{grid} [curr_{loc}[0]] [curr_{loc}[1]] = 'P'
441
                          #print('down')
442
444
445
     def randomMinIndex(array):
446
          minValue = min(array)
447
448
          minIndices = []
449
           for i in range(len(array)):
450
                if (array[i] == minValue):
451
                     minIndices.append(i)
452
453
454
          return minIndices [random.randint(0, len(minIndices) - 1)]
455
     main()
456
```

Next, we continuously loop through the main pathfinding part until a goal is found. Within this main block we start off by popping off the first item in the priority queue and perform a check to see if the newly popped node is the *Goal Node*. If it is not we check for an open spots or the *Goal* in the four available directions; up, down, left and right, and on those spots we then perform checks to main sure that they are within the grid. We then update the costs for the open spots and the *came_from grid* and push the results onto our priority queue.

Lastly, we look through the *came_from* grid and write into our local grid instance, the path we took from the *Start Node* to the *Goal Node*, and return the grid.

Here is the entire main function for this version of A*.

```
def a_star_a(tmp_grid, s_loc, g_loc):
        a_grid = copy.deepcopy(tmp_grid)
       came\_from = [[None for j in range(len(a\_grid[0]))] for i in
3
       range(len(a_grid))]
        cost = [[None for j in range(len(a_grid[0]))] for i in range(
       len(a_grid))]
        cost[s_loc[0]][s_loc[1]] = 0
6
8
        curr_loc = None #copy.deepcopy(s_loc)
        foundGoal = False
9
        visited = []
11
        heappush (visited, (manhattan(s_loc, g_loc), s_loc))
12
13
14
       #Find the goal
        while (not (foundGoal)):
            curr_node = heappop(visited)
16
            curr_loc = curr_node[1]
17
18
```

```
if (a\_grid[curr\_loc[0]][curr\_loc[1]] = 'G'):
19
                       foundGoal = True
20
21
                 if (not (foundGoal)):
22
23
                       #Left
                       if(curr\_loc[1] - 1 >= 0):
24
25
                              if(a\_grid[curr\_loc[0]][curr\_loc[1] - 1] == '\_' or
           a_{grid}[curr_{loc}[0]][curr_{loc}[1] - 1] = G':
                                   cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
26
27
28
           \begin{array}{c} if\left(\cos t\left[\operatorname{curr\_loc}\left[0\right]\right]\left[\operatorname{curr\_loc}\left[1\right]-1\right] \Longrightarrow \operatorname{None} \\ or \ \operatorname{cost\_so\_far} \ +\ 1 < \operatorname{cost}\left[\operatorname{curr\_loc}\left[0\right]\right]\left[\operatorname{curr\_loc}\left[1\right]-1\right]\right): \end{array} 
29
                                         cost [curr_loc [0]] [curr_loc [1] - 1] =
30
           cost_so_far + 1
                                         came\_from [curr\_loc [0]] [curr\_loc [1] - 1] = [
31
           curr_loc[0], curr_loc[1]]
                                         heappush(visited, (cost_so_far + 1 +
           manhattan\left(\left[\,curr\_loc\,[0]\,\,,\,\,curr\_loc\,[1]\,\,-\,\,1\right]\,,\,\,g\_loc\,\right)\,,\,\,\left[\,curr\_loc\,[0]\,\,,\,\,d
            curr_loc[1] - 1]))
33
                       #Right
34
                       if(curr\_loc[1] + 1 < len(a\_grid[0])):
35
                             if(a\_grid[curr\_loc[0]][curr\_loc[1] + 1] = '\_' or
36
           a_{grid} [curr_{loc}[0]] [curr_{loc}[1] + 1] = 'G'):
37
                                   cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
38
39
                                    if(cost[curr\_loc[0]][curr\_loc[1] + 1] == None
40
           or cost\_so\_far + 1 < cost[curr\_loc[0]][curr\_loc[1] + 1]):
                                         cost[curr\_loc[0]][curr\_loc[1] + 1] =
           cost_so_far + 1
                                         came\_from[curr\_loc[0]][curr\_loc[1] + 1] = [
42
           curr_loc[0], curr_loc[1]]
                                         heappush (\, visited \,\, , \,\, (\, cost\_so\_far \,\, + \,\, 1 \,\, + \,\,
43
           manhattan\left(\left[\,curr\_loc\,[0]\,,\;\;curr\_loc\,[1]\,\,+\,\,1\right],\;\;g\_loc\,\right),\;\;\left[\,curr\_loc\,[0]\,,\;\;
            curr_loc[1] + 1]))
44
45
                       if(curr\_loc[0] - 1 >= 0):
46
                             if (a\_grid[curr\_loc[0] - 1][curr\_loc[1]] = '\_' or
47
           a_{\text{grid}}[\text{curr\_loc}[0] - 1][\text{curr\_loc}[1]] = \text{'G'}):
                                   cost_so_far = cost [curr_loc[0]][curr_loc[1]]
48
49
50
                                   if (cost[curr\_loc[0] - 1][curr\_loc[1]] == None
          or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1]]):
cost[curr\_loc[0] - 1][curr\_loc[1]] =
           cost_so_far + 1
                                         came\_from[curr\_loc[0] - 1][curr\_loc[1]] = [
           \operatorname{curr\_loc}[0], \operatorname{curr\_loc}[1]
                                         heappush(visited, (cost\_so\_far + 1 +
          \operatorname{manhattan}([\operatorname{curr\_loc}[0] - 1, \operatorname{curr\_loc}[1]], \operatorname{g\_loc}), [\operatorname{curr\_loc}[0]]
          - 1, curr_loc[1]]))
                       #Down
56
                       if(curr_loc[0] + 1 < len(a_grid)):
    if(a_grid[curr_loc[0] + 1][curr_loc[1]] == '_' or
57
58
           a_{\text{grid}}[\text{curr\_loc}[0] + 1][\text{curr\_loc}[1]] \stackrel{?}{=} \text{'G'}):
59
                                   cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
60
61
```

```
if(cost[curr\_loc[0] + 1][curr\_loc[1]] == None
          or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1]]):
                                       cost[curr\_loc[0] + 1][curr\_loc[1]] =
63
          cost_so_far + 1
                                       came\_from[curr\_loc[0] + 1][curr\_loc[1]] = [
64
          curr_loc[0], curr_loc[1]]
                                       heappush(visited, (cost\_so\_far + 1 +
          manhattan\left(\left[\,curr\_loc\,[0]\right.\right. + 1, \ curr\_loc\,[1]\right], \ g\_loc\,\right), \ \left[\,curr\_loc\,[0]\right]
          + 1, curr_loc[1]]))
66
          while (came_from [curr_loc [0]] [curr_loc [1]] != None):
67
                curr_loc = came_from[curr_loc[0]][curr_loc[1]]
if (a_grid[curr_loc[0]][curr_loc[1]] != 'S'):
    a_grid[curr_loc[0]][curr_loc[1]] = 'P'
68
69
70
71
          return a_grid
```

1.2.2 Standard and Diagonals (A*_b)

The second version of this solution, one in which we are able to move in diagonal directions in addition to the standard directions, is very similar to the first version. The function the same inputs, a grid, and the location of the *Start* and *Goal* cell.

```
def a_star_b(tmp_grid, s_loc, g_loc):
```

We then create a local copy of the grid, initialize our *came_from* and *cost* grid, setup the cost of the *Start* cell as 0, set our current location and lastly setup our looping boolean flags. Afterwards, we initialize our priority queue. This time we use the Chebyshev distance metric as our heuristic value to allow for the diagonal movement as it works as a radial distance measure.

```
def cheb(a, b):

return max( abs( a[0] - b[0] ), abs( a[1] - b[1] ))
```

The same looping as the first solution then occurs, looking for a completion flag. Next, we pop the next available node from the queue and look for empty spaces or the *Goal* cell in a radial sense while running grid validation checks, and then update the *cost* grid and *came_from* grid. This is then followed by the pushing of the available spots into the priority queue. This looping then repeats until the *Goal* cell is found. Lastly, the local grid instance is then written with the path based on the *came_from* grid. The local grid instance is then returned from the function to be written to the text output file by the writer function.

Here is the code for the section version of the A* pathfinder.

```
a_star_b(tmp_grid, s_loc, g_loc):
        a_grid = copy.deepcopy(tmp_grid)
2
       came\_from = [[None for j in range(len(a\_grid[0]))] for i in
3
       range(len(a_grid))]
       cost = [[None for j in range(len(a_grid[0]))] for i in range(
       len(a_grid))]
       cost[s_loc[0]][s_loc[1]] = 0
6
       curr_loc = None #copy.deepcopy(s_loc)
       foundGoal = False
9
       visited = []
11
       heappush (visited, (cheb(s_loc, g_loc), s_loc))
```

```
#Find the goal
14
           while ( not ( foundGoal ) ) :
                  curr_node = heappop(visited)
16
                  curr_loc = curr_node[1]
17
18
19
                  if (a\_grid[curr\_loc[0]][curr\_loc[1]] = 'G'):
                        foundGoal = True
20
21
                  if (not (foundGoal)):
22
                        #Left
                        if(curr_loc[1] - 1 >= 0):
24
                               if (a\_grid[curr\_loc[0]][curr\_loc[1] - 1] = '\_' or
25
           a_{grid}[curr_{loc}[0]][curr_{loc}[1] - 1] = G':
                                     cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
27
28
                                     if(cost[curr\_loc[0]][curr\_loc[1] - 1] == None
29
           or cost\_so\_far + 1 < cost[curr\_loc[0]][curr\_loc[1] - 1]): cost[curr\_loc[0]][curr\_loc[1] - 1] =
30
           cost\_so\_far + 1
                                           came\_from [curr\_loc[0]] [curr\_loc[1] - 1] = [
31
           curr_loc[0], curr_loc[1]]
                                           heappush(visited, (cost_so_far + 1 + cheb([
           \texttt{curr\_loc}\left[0\right], \ \texttt{curr\_loc}\left[1\right] \ - \ 1\right], \ \texttt{g\_loc}\left), \ \left[\,\texttt{curr\_loc}\left[0\right], \ \texttt{curr\_loc}\right]
           [1] - 1])
                        #Right
34
                        if(curr\_loc[1] + 1 < len(a\_grid[0])):
35
                                if (a\_grid[curr\_loc[0]][curr\_loc[1] + 1] = '\_' or 
36
           a_{grid}[curr_{loc}[0]][curr_{loc}[1] + 1] = G'):
                                     cost_so_far = cost [curr_loc [0]][curr_loc [1]]
38
39
            \begin{array}{c} \text{if} \left( \operatorname{cost} \left[ \operatorname{curr\_loc} \left[ 0 \right] \right] \left[ \operatorname{curr\_loc} \left[ 1 \right] + 1 \right] = \operatorname{None} \\ \text{or} \ \operatorname{cost\_so\_far} + 1 < \operatorname{cost} \left[ \operatorname{curr\_loc} \left[ 0 \right] \right] \left[ \operatorname{curr\_loc} \left[ 1 \right] + 1 \right] ) : \\ \operatorname{cost} \left[ \operatorname{curr\_loc} \left[ 0 \right] \right] \left[ \operatorname{curr\_loc} \left[ 1 \right] + 1 \right] = \end{array} 
40
41
           cost_so_far + 1
                                           came\_from [curr\_loc [0]] [curr\_loc [1] + 1] = [
           curr_loc[0], curr_loc[1]]
                                          heappush(visited, (cost\_so\_far + 1 + cheb([
43
           \operatorname{curr\_loc}[0], \operatorname{curr\_loc}[1] + 1, \operatorname{g\_loc}), [\operatorname{curr\_loc}[0], \operatorname{curr\_loc}
           [1] + 1]))
44
45
                        if(curr_loc[0] - 1 >= 0):
46
                               if(a\_grid[curr\_loc[0] - 1][curr\_loc[1]] == '\_' or
47
           a_{grid}[curr_{loc}[0] - 1][curr_{loc}[1]] = G':
                                     cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
48
49
50
                                     if (cost [curr\_loc [0] - 1] [curr\_loc [1]] == None
51
           or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1]]):
                                           cost[curr\_loc[0] - 1][curr\_loc[1]] =
           cost_so_far + 1
                                           came\_from[curr\_loc[0] - 1][curr\_loc[1]] = [
           curr_loc[0], curr_loc[1]]
                                           heappush(visited, (cost_so_far + 1 + cheb([
           {\tt curr\_loc}\,[0] \; - \; 1, \; {\tt curr\_loc}\,[1]] \; , \; \; {\tt g\_loc}) \; , \; [\; {\tt curr\_loc}\,[0] \; - \; 1, \;
           curr_loc[1]]))
                       #Down
56
```

```
if(curr\_loc[0] + 1 < len(a\_grid)):
57
                       if(a\_grid[curr\_loc[0] + 1][curr\_loc[1]] == '\_' or
58
         a_{grid}[curr_{loc}[0] + 1][curr_{loc}[1]] = 'G'):
                            cost_so_far = cost [curr_loc [0]] [curr_loc [1]]
59
60
61
                            if(cost[curr\_loc[0] + 1][curr\_loc[1]] == None
62
        or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1]]):
                                cost[curr\_loc[0] + 1][curr\_loc[1]] =
63
         cost_so_far + 1
                                came\_from \, [\, curr\_loc \, [\, 0\, ] \,\, + \,\, 1\, ] \, [\, curr\_loc \, [\, 1\, ]\, ] \,\, = \,\, [\,
64
        curr_loc[0], curr_loc[1]]
                                heappush(visited, (cost_so_far + 1 + cheb([
65
        curr_loc[0] + 1, curr_loc[1], g_loc, [curr_loc[0] + 1,
        curr_loc[1]]))
66
                  #Up Left
67
                  if (\operatorname{curr\_loc}[0] - 1 >= 0 and \operatorname{curr\_loc}[1] - 1 >= 0):
68
        69
                            cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
70
71
72
                            if(cost[curr\_loc[0] - 1][curr\_loc[1] - 1] =
               or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1] -
        None
         1]):
                                cost[curr\_loc[0] - 1][curr\_loc[1] - 1] =
74
        cost\_so\_far \ + \ 1
                                came\_from[curr\_loc[0] - 1][curr\_loc[1] - 1]
75
         = [\operatorname{curr\_loc}[0], \operatorname{curr\_loc}[1]]
                                heappush (visited, (cost_so_far + 1 + cheb([
        curr_loc[0] - 1, curr_loc[1] - 1, g_loc, [curr_loc[0] - 1, curr_loc[1] - 1))
                  #Up Right
78
                  if(curr\_loc[0] - 1 \text{ and } curr\_loc[1] + 1 < len(a\_grid[0])
79
        ):
                       if(a_grid[curr_loc[0] - 1][curr_loc[1] + 1] == '_-'
80
        or a_grid [curr_loc [0] - 1] [curr_loc [1] + 1] = 'G'):
                            cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
81
82
83
                            if(cost[curr\_loc[0] - 1][curr\_loc[1] + 1] =
84
               or cost\_so\_far + 1 < cost[curr\_loc[0] - 1][curr\_loc[1] +
        None
        1]):
                                cost[curr\_loc[0] - 1][curr\_loc[1] + 1] =
85
        cost_so_far + 1
                                 came\_from \left[ \, curr\_loc \left[ \, 0 \, \right] \, - \, 1 \, \right] \left[ \, curr\_loc \left[ \, 1 \, \right] \, + \, 1 \right] 
86
         = [\operatorname{curr\_loc}[0] - 1, \operatorname{curr\_loc}[1]]
                                heappush(visited, (cost_so_far + 1 + cheb([
        {\tt curr\_loc}\,[0]\,-\,1,\,\,{\tt curr\_loc}\,[1]\,+\,1]\,,\,\,{\tt g\_loc}\,)\,,\,\,[\,{\tt curr\_loc}\,[0]\,-\,1,
         curr_loc[1] + 1]))
88
                  #Down Left
89
                  if(curr\_loc[0] + 1 < len(a\_grid) and curr\_loc[1] - 1 >=
          0):
        91
                            cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
92
93
94
                            if(cost[curr\_loc[0] + 1][curr\_loc[1] - 1] =
95
```

```
None or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1] -
          1]):
                                    cost[curr\_loc[0] + 1][curr\_loc[1] - 1] =
96
          cost\_so\_far + 1
                                    came\_from[curr\_loc[0] + 1][curr\_loc[1] - 1]
97
           = [curr_loc[0], curr_loc[1]]
                                    heappush (visited, (cost_so_far + 1 + cheb([
          curr_loc[0] + 1, curr_loc[1] - 1, g_loc, [curr_loc[0] + 1,
          curr_loc[1] - 1]))
                    #Down Right
100
                     if (\operatorname{curr-loc}[0] + 1 < \operatorname{len}(\operatorname{a-grid}) and \operatorname{curr-loc}[1] + 1 <
          len (a_grid [0])):
                          \inf(a_{\text{grid}}[\text{curr\_loc}[0] + 1][\text{curr\_loc}[1] + 1] = '_{\text{-}}'
          or a_grid [curr_loc [0] + 1][curr_loc [1] + 1] = 'G'):
                               cost\_so\_far = cost[curr\_loc[0]][curr\_loc[1]]
104
                               if(cost[curr\_loc[0] + 1][curr\_loc[1] + 1] =
106
                 or cost\_so\_far + 1 < cost[curr\_loc[0] + 1][curr\_loc[1] +
          None
          1]):
                                    cost[curr\_loc[0] + 1][curr\_loc[1] + 1] =
          cost_so_far + 1
                                    came\_from[curr\_loc[0] + 1][curr\_loc[1] + 1]
108
           = [curr_loc[0], curr_loc[1]]
                                    heappush (\, visited \,\, , \,\, (\, cost\_so\_far \,\, + \,\, 1 \,\, + \,\, cheb \, (\, [
109
          curr_loc[0] + 1, curr_loc[1] + 1, g_loc, [curr_loc[0] + 1,
          curr_loc[1] + 1]))
          while (came_from [curr_loc [0]] [curr_loc [1]] != None):
111
               curr_loc = came_from[curr_loc[0]][curr_loc[1]]
if (a_grid[curr_loc[0]][curr_loc[1]] != 'S'):
    a_grid[curr_loc[0]][curr_loc[1]] = 'P'
114
116
          return a_grid
```

2 Part 2: Alpha-Beta Pruning

Our alpha-beta pruning solution first reads in a line from its input file and builds a dictionary of Node objects using the information it finds about each node. It then adds references to other nodes by finding the child node in the dictionary and adding a reference to it in the parent. For nodes which only have leaf nodes as children, we append the value of each leaf node to a list of child values. The Node class is implemented in Python as such:

```
class Node:
       node\_count = 0
2
       def __init__(self, letter, minmax, value=-1):
            self.letter = letter
5
6
            self.min = minmax
            self.values = []
            self.children = []
9
            Node.node\_count += 1
       def valueSetter(self, value):
11
            self.values.append(value)
12
       def childrenSetter(self, value):
```

```
self.children.append(value)
16
        def alpha_beta(self, a, b):
    print("\nNode %s" % self.letter)
    print("Min: %s" % self.min)
17
18
19
             print("Alpha: %s" % a + "\nBeta: %s" % b)
20
21
             examined = 0
             if(len(self.children) == 0):
22
                 if self.min:
                     for x in self.values:
24
                          examined += 1
25
26
                          b = \min(b, x)
27
                          if b \le a:
                              print("\nNode: %s" % self.letter + "\nBeta
28
       %s" %b + " is better than alpha %s" %a)
                               return (b, examined)
29
                     return (b, examined)
30
                 else:
31
                      for x in self.values:
32
33
                          examined += 1
                          a = \max(a, x)
34
                          if a >= b:
35
                               print("\nNode: %s" % self.letter + "\nAlpha
         %s" %a + " is better than beta %s" %b)
                              return (a, examined)
37
38
                     return (a, examined)
             else:
39
                 if self.min:
40
                      for child in self.children:
41
                          childValue = child.alpha_beta(a, b)
42
                          best = childValue[0]
43
                          examined += childValue[1]
44
                          b = \min(b, best)
45
                          if b \le a:
46
                              print("\nNode: %s" % self.letter + "\nBeta
47
       %s" % b + " is better than alpha %s" % a)
                               return (b, examined)
48
                     return (b, examined)
49
50
                 else:
                      print("Max node")
51
                      for child in self.children:
52
53
                          childValue = child.alpha_beta(a, b)
                          best = childValue[0]
54
                          examined += childValue[1]
55
56
                          a = \max(a, best)
                          if a >= b:
                               print("\nNode: %s" % self.letter + "\nAlpha
58
         %s" %a + " is better than beta %s" %b)
                               return (a, examined)
59
                      return (a, examined)
```

In order to determine the max, or min, value of the game tree, the alpha_beta function of the root node can be called with the arguments negative infinity, for alpha, and positive infinity, for beta. The root node will then call the same function in its children, as will they on their children. Once a node which only has leaf nodes as children has its alpha_beta function invoked, if it is a min node then it will look for the leaf with the smallest value less than beta, stopping the search and returning its minimum value if it ever encounters a value less than alpha. For max nodes, the same process is followed, trying to find a new

maximum value which is greater than alpha while still less than beta, returning its maximum value encountered if it finds such a value.

Nodes employ the same strategy all the way back up the tree, using the values returned by its children as its potential max or min values instead of the static evaluation of leaf nodes. Once the search of all children has completed, although not all children have necessarily been examined, the root node returns the best value it has encountered, alpha if it is a max node and beta if it is a min node

Our solution also keeps track of the number of examined leaf nodes. A node whose children are all leaf nodes counts how many it examines and returns that value once it is done. Nodes with non-leaf children sum the number of leaf nodes examined by its children. Since nodes stop their search if they encounter a value which is better for their opponent than their current best, not all leaf nodes need to be examined. Therefore, the total number of leaf nodes examined may be fewer than the number of leaf nodes in the game tree.

Once the tree has been solved, and the solution values written to the output file, successive lines are read in and solved until no trees remain.