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CONTEST

Tips and Tricks

```
## Tips and Tricks
- [C++ tips and tricks](https://codeforces.com/blog/entry/74684)
- invokes RTE (Run Time Error) upon integer overflow
#pragma GCC optimize "trapv"
- invoke RTE for input error (e.g. reading a long long into an int)
cin.exceptions(cin.failbit);
- use pramgas for C++ speed boost
#pragma GCC optimize("03,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
### Troubleshooting
/* stuff you should look for
   * int overflow, array bounds
   * special cases (n=1?)
   * do smth instead of nothing and stay organized
   * WRITE STUFF DOWN
   * DON'T GET STUCK ON ONE APPROACH
- - -
Author: Bena
- refer to [KACTL
    🕁 Troubleshoot](https://github.com/kth-competitive-programming/kactl/blob/main/content/co|ተኮጀታኒቸቪኒያሀኮትሮቴክሲያኒት total cost to assign each worker to some distinct job
## Sources
- [[Tutorial] GCC Optimization Pragmas](https://codeforces.com/blog/entry/96344)
- [Don't use rand(): a guide to random number generators in
```

Hash codes

```
#! /bin/bash
#Hashes a file, ignoring all:
# - whitespace
# - comments
# - asserts
# - includes
# - pragmas
#Use to verify that code was correctly typed.
#usage:
# chmod +x hash.sh
# cat a.cpp | ./hash.sh
#or just copy this command:
```

```
cat a.cpp | sed -r '/(assert|include|pragma)/d' | cpp -fpreprocessed -P | tr -d
     \hookrightarrow '[:space:]' | md5sum | cut -c-6
sed -r '/(assert|include|pragma)/d' | cpp -fpreprocessed -P | tr -d '[:space:]' | md5sum | cut
```

Test on random inputs

```
#! /bin/bash
#runs 2 programs against each other on random inputs until they output different results
#source: https://github.com/Errichto/youtube/blob/master/testing/s.sh
# chmod +x test.sh
# ./test.sh
for((i = 1; ++i)); do
   echo $i
    ./test.out > in
    diff --ignore-all-space <(./a.out < in) <(./brute.out < in) || break</pre>
done
```

MAX FLOW

Hungarian

```
//cat hungarian.hpp | ./hash.sh
//935a16
#pragma once
//source: https://e-maxx.ru/algo/assignment_hungary
//input: cost[1...n][1...m] with 1 <= n <= m
//n workers, indexed 1, 2, ..., n
//m jobs, indexed 1, 2, ..., m
//it costs `cost[i][j] ` to assign worker i to job j (1<=i<=n, 1<=j<=m)</pre>
//0(n^2 * m)
//trick 1: set `cost[i][j]` to INF to say: "worker `i` cannot be assigned job `j`"
//trick 2: `cost[i][j]` can be negative, so to instead find max total cost over all matchings:
     \hookrightarrow set all `cost[i][j]` to `-cost[i][j]`.
//Now max total cost = - hungarian(cost).min_cost
const long long INF = 1e18;
struct weighted_match {
    long long min_cost;
    vector<int> matching;//worker `i` (1<=i<=n) is assigned to job `matching[i]`</pre>
         \hookrightarrow (1<=matching[i]<=m)
weighted_match hungarian(const vector<vector<long long>>& cost) {
    int n = ssize(cost) - 1, m = ssize(cost[0]) - 1;
    assert(n <= m);</pre>
    vector<int> p(m + 1), way(m + 1);
    vector<long long> u(n + 1), v(m + 1);
    for (int i = 1; i \le n; i++) {
        p[0] = i;
        int j0 = 0;
        vector<long long> minv(m + 1, INF);
        vector<bool> used(m + 1, 0);
        do {
```

```
used[j0] = 1;
        int i0 = p[j0], j1 = 0;
        long long delta = INF;
        for (int j = 1; j \le m; j++)
            if (!used[i]) {
                long long cur = cost[i0][j] - u[i0] - v[j];
                if (cur < minv[j])</pre>
                     minv[j] = cur, way[j] = j0;
                if (minv[j] < delta)</pre>
                     delta = minv[j], j1 = j;
        for (int j = 0; j \le m; j++)
            if (used[j])
                u[p[j]] += delta, v[j] -= delta;
            else
                minv[j] -= delta;
        j0 = j1;
    } while (p[j0] != 0);
    do {
        int j1 = way[j0];
        p[j0] = p[j1];
        j0 = j1;
    } while (j0);
}
vector<int> ans(n + 1);
for (int j = 1; j \le m; j++)
    ans[p[i]] = i:
return {-v[0], ans};
```

Min Cost Max Flow

```
//cat min_cost_max_flow.hpp | ./hash.sh
//9dd6b6
#pragma once
//source: https://e-maxx.ru/algo/min_cost_flow
const long long INF = 1e18;
struct mcmf {
   using ll = long long;
   struct edge {
       int a, b;
       11 cap, cost, flow;
       int back;
   };
   const int N;
   vector<edge> e;
   vector<vector<int>> g;
   mcmf(int a_n) : N(a_n), g(N) {}
   void add_edge(int a, int b, ll cap, ll cost) {
       edge e1 = \{a, b, cap, cost, 0, ssize(g[b])\};
        edge e2 = \{b, a, 0, -cost, 0, ssize(g[a])\};
       g[a].push_back(ssize(e));
       e.push_back(e1);
       g[b].push_back(ssize(e));
       e.push_back(e2);
   }
   pair<ll, ll> get_flow(int s, int t, ll total_flow) {
       11 flow = 0, cost = 0;
```

```
while (flow < total_flow) {</pre>
            vector<ll> d(N, INF);
            vector\langle int \rangle p_edge(N), id(N, 0), q(N), p(N);
            int qh = 0, qt = 0;
            q[qt++] = s;
            d[s] = 0;
            while (qh != qt) {
                int v = q[qh++];
                id[v] = 2;
                if (qh == N)
                    qh = 0;
                for (int i = 0; i < ssize(g[v]); i++) {
                    const edge& r = e[g[v][i]];
                    if (r.flow < r.cap && d[v] + r.cost < d[r.b]) {
                        d[r.b] = d[v] + r.cost;
                        if (id[r.b] == 0) {
                             q[qt++] = r.b;
                             if (qt == N)
                                 qt = 0;
                        } else if (id[r.b] == 2) {
                             if (--qh == -1)
                                 qh = N - 1;
                             q[qh] = r.b;
                        }
                        id[r.b] = 1;
                        p[r.b] = v;
                        p_edge[r.b] = i;
                    }
                }
            if (d[t] == INF)
                break;
            11 addflow = total_flow - flow;
            for (int v = t; v != s; v = p[v]) {
                int pv = p[v], pr = p_edge[v];
                addflow = min(addflow, e[g[pv][pr]].cap - e[g[pv][pr]].flow);
            }
            for (int v = t; v != s; v = p[v]) {
                int pv = p[v], pr = p_edge[v], r = e[g[pv][pr]].back;
                e[g[pv][pr]].flow += addflow;
                e[g[v][r]].flow -= addflow;
                cost += e[g[pv][pr]].cost * addflow;
            }
            flow += addflow;
        return {flow, cost};
    }
};
```

GRAPHS

Block Vertex Tree

```
//cat block_vertex_tree.hpp | ./hash.sh
//a5c2b9
#pragma once
#include "bridges_and_cuts.hpp"
```

```
//returns adjacency list of block vertex tree
// graph_info cc = bridge_and_cut(adj, m);
// vector<vector<int>> bvt = block_vertex_tree(adj, cc);
//to loop over each *unique* bcc containing a node v:
// for (int bccid : bvt[v]) {
//
       bccid -= n:
//
// }
//to loop over each *unique* node inside a bcc:
// for (int v : bvt[bccid + n]) {
//
// }
vector<vector<int>> block_vertex_tree(const vector<vector<pair<int, int>>>& adj, const

    graph_info& cc) {
    int n = ssize(adj);
    vector<vector<int>>> bvt(n + cc.num_bccs);
    vector<bool> vis(cc.num_bccs, 0);
    for (int v = 0; v < n; v++) {
        for (auto [_, e_id] : adj[v]) {
            int bccid = cc.bcc_id[e_id];
            if (!vis[bccid]) {
                vis[bccid] = 1;
                bvt[v].push_back(bccid + n);//add edge between original node, and bcc node
                bvt[bccid + n].push_back(v);
            }
        }
        for (int bccid : bvt[v])
            vis[bccid - n] = 0;
   }
    return bvt;
```

Bridge Tree

```
//cat bridge_tree.hpp | ./hash.sh
//8eb014
#pragma once
#include "bridges_and_cuts.hpp"
//never adds multiple edges as bridges_and_cuts.hpp correctly marks them as non-bridges
//usage:
// graph_info cc = bridge_and_cut(adj, m);
// vector<vector<int>> bt = bridge_tree(adj, cc);
vector<vector<int>> bridge_tree(const vector<vector<pair<int, int>>>& adj, const graph_info&
     \hookrightarrow cc) {
    vector<vector<int>> tree(cc.num_2_edge_ccs);
    for (int i = 0; i < ssize(adj); i++)</pre>
        for (auto [to, e_id] : adj[i])
            if (cc.is_bridge[e_id])
                tree[cc.two_edge_ccid[i]].push_back(cc.two_edge_ccid[to]);
    return tree;
```

Bridges and Cuts

```
//cat bridges_and_cuts.hpp | ./hash.sh
//3f21b9
```

```
#pragma once
//O(n+m) time & space
//2 edge cc and bcc stuff doesn't depend on each other, so delete whatever is not needed
//handles multiple edges
//
//example initialization of `adj`:
//for (int i = 0; i < m; i++) {
// int u, v;
// cin >> u >> v;
// u--, v--;
// adj[u].emplace_back(v, i);
// adj[v].emplace_back(u, i);
//}
struct graph_info {
    //2 edge connected component stuff (e.g. components split by bridge edges)
         → https://cp-algorithms.com/graph/bridge-searching.html
    int num_2_edge_ccs;
    vector<bool> is_bridge;//edge id -> 1 iff bridge edge
    vector<int> two_edge_ccid;//node -> id of 2 edge component (which are labeled 0, 1, ...,
         //bi connected component stuff (e.g. components split by cut/articulation nodes)

   https://cp-algorithms.com/graph/cutpoints.html

    int num_bccs;
    vector<bool> is_cut;//node -> 1 iff cut node
    vector<int> bcc_id;//edge id -> id of bcc (which are labeled 0, 1, ..., `num_bccs`-1)
graph_info bridge_and_cut(const vector<vector<pair<int/*neighbor*/, int/*edge id*/>>>&

    → adj/*undirected graph*/, int m/*number of edges*/) {

    //stuff for both (always keep)
    int n = ssize(adj), timer = 1;
    vector<int> tin(n, 0);
    //2 edge cc stuff (delete if not needed)
    int num_2_edge_ccs = 0;
    vector<bool> is_bridge(m, 0);
    vector<int> two_edge_ccid(n), node_stack;
    node_stack.reserve(n);
    //bcc stuff (delete if not needed)
    int num_bccs = 0;
    vector<bool> is_cut(n, 0);
    vector<int> bcc_id(m), edge_stack;
    edge_stack.reserve(m);
    auto dfs = [&](auto self, int v, int p_id) -> int {
        int low = tin[v] = timer++, deg = 0;
        node_stack.push_back(v);
        for (auto [to, e_id] : adj[v]) {
            if (e_id == p_id)
                continue;
            if (!tin[to]) {
                edge_stack.push_back(e_id);
                int low_ch = self(self, to, e_id);
                if (low_ch >= tin[v]) {
                    is_cut[v] = 1;
                    while (1) {
                        int edge = edge_stack.back();
                        edge_stack.pop_back();
                        bcc_id[edge] = num_bccs;
                        if (edge == e_id)
                            break:
                    }
```

```
num_bccs++;
            }
            low = min(low, low_ch);
            deg++;
        } else if (tin[to] < tin[v]) {</pre>
            edge_stack.push_back(e_id);
            low = min(low, tin[to]);
        }
    if (p_id == -1)
        is\_cut[v] = (deg > 1);
    if (tin[v] == low) {
        if (p_id != -1)
            is_bridge[p_id] = 1;
        while (1) {
            int node = node_stack.back();
            node_stack.pop_back();
            two_edge_ccid[node] = num_2_edge_ccs;
            if (node == v)
                break;
        num_2_edge_ccs++;
    }
    return low;
};
for (int i = 0; i < n; i++)
    if (!tin[i])
        dfs(dfs, i, -1);
return {num_2_edge_ccs, is_bridge, two_edge_ccid, num_bccs, is_cut, bcc_id};
```

Strongly Connected Components

```
//cat strongly_connected_components.hpp | ./hash.sh
//69acd7
#pragma once
//source: https://github.com/kth-competitive-programming/
// kactl/blob/main/content/graph/SCC.h
struct scc_info {
   int num_sccs;
   //scc's are labeled 0,1,..., `num_sccs-1`
   //scc_id[i] is the id of the scc containing node `i`
   //for each edge i -> j: scc_id[i] >= scc_id[j] (reverse topo order of scc's)
   vector<int> scc_id;
//NOLINTNEXTLINE(readability-identifier-naming)
scc_info SCC(const vector<vector<int>>& adj/*directed, unweighted graph*/) {
    int n = ssize(adj), timer = 1, num_sccs = 0;
   vector<int> tin(n, 0), scc_id(n, -1), node_stack;
   node_stack.reserve(n);
   auto dfs = [&](auto self, int v) -> int {
        int low = tin[v] = timer++;
        node_stack.push_back(v);
        for (int to : adj[v]) {
            if (scc_id[to] < 0)</pre>
                low = min(low, tin[to] ? tin[to] : self(self, to));
       if (tin[v] == low) {
```

```
while (1) {
        int node = node_stack.back();
        node_stack.pop_back();
        scc_id[node] = num_sccs;
        if (node == v)
            break;
     }
     num_sccs++;
}
return low;
};
for (int i = 0; i < n; i++) {
     if (!tin[i])
        dfs(dfs, i);
}
return {num_sccs, scc_id};
}</pre>
```

Centroid Decomposition

```
//cat centroid_decomposition.hpp | ./hash.sh
//71e2e5
#pragma once
// Time and Space complexity are given in terms of n where n is the number of nodes in the
// Time complexity O(n log n)
// Space complexity O(n)
// Given an unweighted, undirected forest and a function,
// centroid_decomp runs the function on every decomposition
// Example usage:
// centroid_decomp decomp(adj, [&](const vector<vector<int>>& adj_removed_edges, int cent) ->
     \hookrightarrow void {
//
// });
template <typename F> struct centroid_decomp {
    vector<vector<int>> adj;
    F func;
    vector<int> sub_sz;
    centroid_decomp(const vector<vector<int>>& a_adj/*undirected forest*/, const F& a_func)
        : adj(a_adj), func(a_func), sub_sz(ssize(adj), -1) {
        for (int i = 0; i < ssize(adj); i++)</pre>
            if (sub_sz[i] == -1)
                dfs(i);
    void calc_subtree_sizes(int u, int p = -1) {
        sub_sz[u] = 1;
        for (int v : adj[u]) {
            if (v == p)
                continue:
            calc_subtree_sizes(v, u);
            sub_sz[u] += sub_sz[v];
        }
    void dfs(int u) {
        calc_subtree_sizes(u);
```

```
for (int p = -1, sz_root = sub_sz[u];;) {
        auto big_ch = find_if(adj[u].begin(), adj[u].end(), [&](int v) -> bool {
            return v != p && 2 * sub_sz[v] > sz_root;
        });
        if (big_ch == adj[u].end())
            break;
        p = u, u = *big_ch;
    }
    func(adj, u);
    for (int v : adj[u]) {
        //each node is adjacent to O(logn) centroids
        adj[v].erase(find(adj[v].begin(), adj[v].end(), u));
        dfs(v);
    }
}
```

Frequency Table of Tree Distance

```
//cat count_paths_per_length.hpp | ./hash.sh
//182b70
#pragma once
#include "../../kactl/content/numerical/FastFourierTransform.h"
#include "centroid_decomposition.hpp"
//returns array `num_paths` where `num_paths[i]` = # of paths in tree with `i` edges
//0(n log^2 n)
vector<long long> count_paths_per_length(const vector<vector<int>>& adj/*unrooted, connected
     \hookrightarrow tree*/) {
    vector<long long> num_paths(ssize(adj), 0);
    centroid_decomp decomp(adj, [&](const vector<vector<int>>& adj_removed_edges, int cent) ->
        vector<vector<double>> child_depths;
        for (int to : adj_removed_edges[cent]) {
            child_depths.emplace_back(1, 0.0);
            for (queue<pair<int, int>> q({{to, cent}}); !q.empty();) {
                child_depths.back().push_back(ssize(q));
                queue<pair<int, int>> new_q;
                while (!q.empty()) {
                    auto [curr, par] = q.front();
                    q.pop();
                    for (int ch : adj_removed_edges[curr]) {
                        if (ch == par)
                            continue;
                        new_q.emplace(ch, curr);
                    }
                }
                swap(q, new_q);
            }
        sort(child_depths.begin(), child_depths.end(), [&](const auto & x, const auto & y) {
            return x.size() < y.size();</pre>
       });
        vector<double> total_depth(1, 1.0);
        for (const auto& cnt_depth : child_depths) {
            auto prod = conv(total_depth, cnt_depth);
            for (int i = 1; i < ssize(prod); i++)
                num_paths[i] += llround(prod[i]);
            total_depth.resize(ssize(cnt_depth), 0.0);
```

Count Paths Per Node

```
//cat count_paths_per_node.hpp | ./hash.sh
//2077d2
#pragma once
#include "centroid_decomposition.hpp"
//0-based nodes
//returns array `num_paths` where `num_paths[i]` = number of paths with k edges where node `i`
     \hookrightarrow is on the path
//0(n \log n)
vector<long long> count_paths_per_node(const vector<vector<int>>& adj/*unrooted tree*/, int k)
    vector<long long> num_paths(ssize(adj));
    centroid_decomp decomp(adj, [&](const vector<vector<int>>& adj_removed_edges, int cent) ->
         \hookrightarrow \mathsf{void}\ \{
        vector<int> pre_d(1, 1), cur_d(1);
        auto dfs = [&](auto self, int u, int p, int d) -> long long {
            if (d > k)
                 return 0;
            if (ssize(cur_d) <= d)</pre>
                 cur_d.push_back(0);
            cur_d[d]++;
            long long cnt = 0;
            if (k - d < ssize(pre_d))</pre>
                 cnt += pre_d[k - d];
            for (int v : adj_removed_edges[u])
                 if (v != p)
                     cnt += self(self, v, u, d + 1);
            num_paths[u] += cnt;
            return cnt;
        };
        auto dfs_child = [&](int child) -> long long {
            long long cnt = dfs(dfs, child, cent, 1);
            pre_d.resize(ssize(cur_d));
            for (int i = 1; i < ssize(cur_d) && cur_d[i]; i++)</pre>
                 pre_d[i] += cur_d[i], cur_d[i] = 0;
            return cnt;
        };
        for (int child : adj_removed_edges[cent])
            num_paths[cent] += dfs_child(child);
        pre_d = vector<int>(1);
        cur_d = vector<int>(1);
        for (auto it = adj_removed_edges[cent].rbegin(); it != adj_removed_edges[cent].rend();
             \hookrightarrow it++)
            dfs_child(*it);
    });
    return num_paths;
```

```
//cat dijkstra.hpp | ./hash.sh
//aa6eda
#pragma once
//returns array `len` where `len[i]` = shortest path from node `start` to node `i`
//For example `len[start]` will always = 0
const long long INF = 1e18;
vector<long long> dijkstra(const vector<vector<pair<int, long long>>>& adj /*directed or

    undirected, weighted graph*/, int start) {

   using node = pair<long long, int>;
   vector<long long> len(ssize(adj), INF);
   len[start] = 0;
   priority_queue<node, vector<node>, greater<node>> q;
   q.emplace(0, start);
   while (!q.empty()) {
       auto [curr_len, v] = q.top();
       q.pop();
       if (len[v] < curr_len)</pre>
            continue;//important check: O(n*m) without it
        for (auto [to, weight] : adj[v])
           if (len[to] > weight + len[v]) {
               len[to] = weight + len[v];
               q.emplace(len[to], to);
           }
   }
   return len;
```

HLD

```
//cat hld.hpp | ./hash.sh
//d30c4a
#pragma once
//source: https://codeforces.com/blog/entry/53170
//mnemonic: Heavy Light Decomposition
//NOLINTNEXTLINE(readability-identifier-naming)
struct HLD {
   struct node {
       int sub_sz = 1, par = -1, time_in = -1, next = -1;
   };
   vector<node> tree;
   HLD(vector<vector<int>>& adj/*forest of unrooted trees*/) : tree(ssize(adj)) {
       for (int i = 0, timer = 0; i < ssize(adj); i++) {</pre>
           if (tree[i].next == -1) {//lowest indexed node in each tree becomes root
                tree[i].next = i;
                dfs1(i, adj);
               dfs2(i, adj, timer);
           }
       }
   void dfs1(int v, vector<vector<int>>& adj) {
        auto par = find(adj[v].begin(), adj[v].end(), tree[v].par);
       if (par != adj[v].end())
            adj[v].erase(par);
       for (int& to : adj[v]) {
            tree[to].par = v;
           dfs1(to, adj);
           tree[v].sub_sz += tree[to].sub_sz;
           if (tree[to].sub_sz > tree[adj[v][0]].sub_sz)
```

```
swap(to, adj[v][0]);
        }
    }
    void dfs2(int v, const vector<vector<int>>& adj, int& timer) {
        tree[v].time_in = timer++;
        for (int to : adj[v]) {
            tree[to].next = (timer == tree[v].time_in + 1 ? tree[v].next : to);
            dfs2(to, adj, timer);
        }
    }
    // Returns inclusive-exclusive intervals (of time_in's) corresponding to the path between
         \hookrightarrow u and v, not necessarily in order
    // This can answer queries for "is some node `x` on some path" by checking if the
         \hookrightarrow tree[x].time_in is in any of these intervals
    // u, v must be in the same component
    vector<pair<int, int>> path(int u, int v) const {
        vector<pair<int, int>> res;
        for (;; v = tree[tree[v].next].par) {
            if (tree[v].time_in < tree[u].time_in)</pre>
                swap(u, v);
            if (tree[tree[v].next].time_in <= tree[u].time_in) {</pre>
                res.emplace_back(tree[u].time_in, tree[v].time_in + 1);
                return res;
            }
            res.emplace_back(tree[tree[v].next].time_in, tree[v].time_in + 1);
    }
    // Returns interval (of time_in's) corresponding to the subtree of node i
    // This can answer queries for "is some node `x` in some other node's subtree" by checking

    if tree[x].time_in is in this interval

    pair<int, int> subtree(int i) const {
        return {tree[i].time_in, tree[i].time_in + tree[i].sub_sz};
    // Returns lca of nodes u and v
    // u, v must be in the same component
    int lca(int u, int v) const {
        for (;; v = tree[tree[v].next].par) {
            if (tree[v].time_in < tree[u].time_in)</pre>
                swap(u, v);
            if (tree[tree[v].next].time_in <= tree[u].time_in)</pre>
                return u:
        }
    }
};
```

Hopcroft Karp

```
//cat hopcroft_karp.hpp | ./hash.sh
//5d1682
#pragma once
//source: https://github.com/foreverbell/acm-icpc-cheat-sheet/
// blob/master/src/graph-algorithm/hopcroft-karp.cpp
//Worst case O(E*sqrt(V)) but faster in practice
struct match {
    //# of edges in matching (which = size of min vertex cover by öKnig's theorem)
    int size_of_matching;
    //an arbitrary max matching is found. For this matching:
    //if l_to_r[node_left] == -1:
```

```
// node_left is not in matching
    // the edge `node_left` <=> l_to_r[node_left] is in the matching
    //similarly for r_to_l with edge r_to_l[node_right] <=> node_right in matching if
         \hookrightarrow r_to_l[node_right] != -1
    //matchings stored in l_to_r and r_to_l are the same matching
    //provides way to check if any node/edge is in matching
    vector<int> l_to_r, r_to_l;
    //an arbitrary min vertex cover is found. For this mvc: mvc_l[node_left] is 1 iff

→ node_left is in the min vertex cover (same for mvc_r)
    //if mvc_l[node_left] is 0, then node_left is in the corresponding maximal independent set
    vector<bool> mvc_1, mvc_r;
//Think of the bipartite graph as having a left side (with size lsz) and a right side (with
//Nodes on left side are indexed 0,1,...,lsz-1
//Nodes on right side are indexed 0,1,...,rsz-1
//`adj` is like a directed adjacency list containing edges from left side -> right side:
//To initialize `adj`: For every edge node_left <=> node_right, do:

    adj[node_left].push_back(node_right)

match hopcroft_karp(const vector<vector<int>>% adj/*bipartite graph*/, int rsz/*number of
     \hookrightarrow nodes on right side*/) {
    int size_of_matching = 0, lsz = ssize(adj);
    vector<int> l_to_r(lsz, -1), r_to_l(rsz, -1);
    while (1) {
        queue<int> q;
        vector<int> level(lsz, -1);
        for (int i = 0; i < lsz; i++)
            if (l_to_r[i] == -1)
                level[i] = 0, q.push(i);
        bool found = 0;
        vector<bool> mvc_l(lsz, 1), mvc_r(rsz, 0);
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            mvc_1[u] = 0;
            for (int x : adj[u]) {
                mvc_r[x] = 1;
                int v = r_to_1[x];
                if (v == -1)
                    found = 1;
                else if (level[v] == -1) {
                    level[v] = level[u] + 1;
                    q.push(v);
                }
            }
        }
        if (!found)
            return {size_of_matching, l_to_r, r_to_l, mvc_l, mvc_r};
        auto dfs = [&](auto self, int u) -> bool {
            for (int x : adj[u]) {
                int v = r_to_1[x];
                if (v == -1 || (level[u] + 1 == level[v] && self(self, v))) {
                    l_{to_r[u]} = x;
                    r_{to_1[x]} = u;
                    return 1;
                }
```

```
}
    level[u] = 1e9; //acts as visited array
    return 0;
};
for (int i = 0; i < lsz; i++)
    size_of_matching += (l_to_r[i] == -1 && dfs(dfs, i));
}
</pre>
```

Kth Node on Path

```
//cat kth_node_on_path.hpp | ./hash.sh
//c59307
#pragma once
#include "lca.hpp"
//consider path \{u, u's par, ..., LCA(u,v), ..., v's par, v\}. This returns the node at index k
//assumes 0 \le k \le number of edges on path from u to v
// u, v must be in the same component
//
//To loop over all nodes on a path from u to v:
//kth_node_on_path kpath(adj);
//for (int i = 0; i \le kpath.lca.dist_edges(u, v); i++) {
// int node = kpath.guery(u, v, i);
// ...
struct kth_node_on_path {
    LCA lca:
    kth_node_on_path(const vector<vector<pair<int, long long>>>& adj/*forest of weighted
         \hookrightarrow trees*/) : lca(adj) {}
    int query(int u, int v, int k) const {
        int lca_uv = lca.get_lca(u, v);
        int u_lca = lca.tree[u].depth - lca.tree[lca_uv].depth;
        int v_lca = lca.tree[v].depth - lca.tree[lca_uv].depth;
        assert(0 \le k \&\& k \le u_lca + v_lca);
        return k <= u_lca ? lca.kth_par(u, k) : lca.kth_par(v, u_lca + v_lca - k);</pre>
    }
};
```

LCA

```
//cat lca.hpp | ./hash.sh
//b28532
#pragma once
//https://codeforces.com/blog/entry/74847
//mnemonic: Least/Lowest Common Ancestor
//NOLINTNEXTLINE(readability-identifier-naming)
struct LCA {
    struct node {
        int jmp = -1, jmp\_edges = 0, par = -1, depth = 0;
        long long dist = 0LL;
    };
    vector<node> tree:
    LCA(const vector<vector<pair<int, long long>>>& adj/*forest of weighted trees*/) :
         \hookrightarrow tree(ssize(adj)) {
        for (int i = 0; i < ssize(adj); i++) {</pre>
            if (tree[i].jmp == -1) {//lowest indexed node in each tree becomes root
                 tree[i].jmp = i;
                 dfs(i, adj);
```

```
}
        }
   }
   void dfs(int v, const vector<vector<pair<int, long long>>>& adj) {
        int imp, imp_edges;
        if (tree[v].jmp != v && tree[v].jmp_edges == tree[tree[v].jmp].jmp_edges)
            jmp = tree[tree[v].jmp].jmp, jmp_edges = 2 * tree[v].jmp_edges + 1;
        else
            jmp = v, jmp_edges = 1;
        for (auto [ch, w] : adj[v]) {
            if (ch == tree[v].par)
                continue;
            tree[ch] = {
                jmp,
                jmp_edges,
                1 + tree[v].depth,
                w + tree[v].dist
            };
            dfs(ch, adj);
   }
    //traverse up k edges in O(\log(k)). So with k=1 this returns `v`'s parent
    int kth_par(int v, int k) const {
        k = min(k, tree[v].depth);
        while (k > 0) {
            if (tree[v].jmp_edges <= k) {</pre>
                k -= tree[v].jmp_edges;
                v = tree[v].jmp;
            } else {
                k--;
                v = tree[v].par;
            }
        }
        return v;
   }
    // x, y must be in the same component
    int get_lca(int x, int y) const {
        if (tree[x].depth < tree[y].depth)</pre>
            swap(x, y);
        x = kth_par(x, tree[x].depth - tree[y].depth);
        while (x != y) {
            if (tree[x].jmp != tree[y].jmp)
                x = tree[x].jmp, y = tree[y].jmp;
                x = tree[x].par, y = tree[y].par;
        return x;
   }
   int dist_edges(int x, int y) const {
        return tree[x].depth + tree[y].depth - 2 * tree[get_lca(x, y)].depth;
   }
   long long dist_weight(int x, int y) const {
        return tree[x].dist + tree[y].dist - 2 * tree[get_lca(x, y)].dist;
   }
};
```

Rooted Tree Isomorphism

```
//cat subtree_isomorphism.hpp | ./hash.sh
//455aef
#pragma once
// Complexity given in terms of n where n is the number of nodes in the forest
// Time complexity O(n log n)
// Space complexity O(n)
// Given an undirected or directed rooted forest
// subtree_iso classifies each rooted subtree
// minimum label of each tree becomes root
struct iso_info {
    int num_distinct_subtrees; //0 <= id[i] < num_distinct_subtrees for all i</pre>
    vector<int> id; //id[u] == id[v] iff subtree u is isomorphic to subtree v
};
iso_info subtree_iso(const vector<vector<int>>& adj) {
    vector<int> id(ssize(adj), -1);
    map<vector<int>, int> hashes;
    auto dfs = [&](auto self, int u, int p) -> int {
        vector<int> ch_ids;
        ch_ids.reserve(ssize(adj[u]));
        for (int v : adj[u]) {
            if (v != p)
                ch_ids.push_back(self(self, v, u));
        sort(ch_ids.begin(), ch_ids.end());
        auto it = hashes.find(ch_ids);
        if (it == hashes.end())
            return id[u] = hashes[ch_ids] = ssize(hashes);
        return id[u] = it->second;
    for (int i = 0; i < ssize(adj); i++)
        if (id[i] == -1)
            dfs(dfs, i, i);
    return {ssize(hashes), id};
```

MATH

Derangements

```
dp[i] = (i - 1) * (dp[i - 1] + dp[i - 2]) % mod;
return dp;
}
```

Binary Exponentiation MOD

```
//cat binary_exponentiation_mod.hpp | ./hash.sh
//92a3ef
#pragma once
//returns (base^pw)%mod in O(log(pw)), but returns 1 for 0^0
//What if base doesn't fit in long long?
//Since (base^pw)\mod == ((base\mod)^pw)\mod we can calculate base under mod of `mod`
//What if pw doesn't fit in long long?
//assuming mod is prime:
//(base^pw)%mod == (base^(pw%(mod-1)))%mod (from Fermat's little theorem)
//so calculate pw under mod of `mod-1`
//note `mod-1` is not prime, so you need to be able to calculate `pw%(mod-1)` without division
long long bin_exp(long long base, long long pw, long long mod) {
   assert(0 <= pw && 0 <= base && 1 <= mod);
   long long res = 1;
   base %= mod;
   while (pw > 0) {
       if (pw & 1)
           res = res * base % mod;
       base = base * base % mod;
       pw >>= 1;
   }
   return res;
```

Fibonacci

Matrix Multiplication

```
//cat matrix_mult.hpp | ./hash.sh
//910018
#pragma once
```

Mobius Inversion

```
//cat mobius_inversion.hpp | ./hash.sh
//811515
#pragma once
//mobius[i] = 0 iff there exists a prime p s.t. i%(p^2)=0
//mobius[i] = -1 iff i has an odd number of distinct prime factors
//mobius[i] = 1 iff i has an even number of distinct prime factors
const int N = 1e6 + 10;
int mobius[N];
void calc_mobius() {
    mobius[1] = 1;
    for (int i = 1; i < N; i++)
        for (int j = i + i; j < N; j += i)
            mobius[j] -= mobius[i];
}</pre>
```

N Choose K MOD

```
//cat n_choose_k_mod.hpp | ./hash.sh
//c7fb35
#pragma once
//for mod inverse
#include "binary_exponentiation_mod.hpp"
// usage:
//
       n_{choose} k nk(n, 1e9+7) to use `choose`, `inv` with inputs strictly < n
// or:
//
       n_choose_k nk(mod, mod) to use `choose_lucas` with arbitrarily large inputs
struct n_choose_k {
    n_choose_k(int n, long long a_mod) : mod(a_mod), fact(n, 1), inv_fact(n, 1) {
        //this implementation doesn't work if n > mod because n! % mod = 0 when n >= mod. So

→ `inv_fact` array will be all 0's

        assert(max(n, 2) <= mod);</pre>
        //assert mod is prime. mod is intended to fit inside an int so that
        //multiplications fit in a longlong before being modded down. So this
        //will take sqrt(2^31) time
        for (int i = 2; i * i \le mod; i++)
            assert(mod % i);
```

```
for (int i = 2; i < n; i++)
        fact[i] = fact[i - 1] * i % mod;
    inv_fact.back() = bin_exp(fact.back(), mod - 2, mod);
    for (int i = n - 2; i \ge 2; i--)
        inv_fact[i] = inv_fact[i + 1] * (i + 1) % mod;
//classic n choose k
//fails when n >= mod
long long choose(int n, int k) const {
    if (k < 0 | | k > n)
       return 0;
    //now we know 0 <= k <= n so 0 <= n
    return fact[n] * inv_fact[k] % mod * inv_fact[n - k] % mod;
}
//lucas theorem to calculate n choose k in O(log(k))
//need to calculate all factorials in range [0,mod), so 0(mod) time&space, so need
     //handles n >= mod correctly
long long choose_lucas(long long n, long long k) const {
    if (k < 0 | | k > n)
       return 0;
    if (k == 0 || k == n)
       return 1;
    return choose_lucas(n / mod, k / mod) * choose(int(n % mod), int(k % mod)) % mod;
//returns x such that x * n % mod == 1
long long inv(int n) const {
    assert(1 <= n); //don't divide by 0 :)</pre>
    return fact[n - 1] * inv_fact[n] % mod;
}
long long mod;
vector<long long> fact, inv_fact;
```

Partitions

```
//cat partitions.hpp | ./hash.sh
//e7ae42
#pragma once
//https://oeis.org/A000041
//O(n sgrt n) time, but small-ish constant factor (there does exist a O(n log n) solution as
    \hookrightarrow well)
vector<long long> partitions(int n, long long mod) {
   vector<long long> dp(n, 1);
   for (int i = 1; i < n; i++) {
       long long sum = 0;
       for (int j = 1, pent = 1, sign = 1; pent <= i; j++, pent += 3 * j - 2, sign = -sign) {
           if (pent + j <= i)
               sum += dp[i - pent - j] * sign + mod;
           sum += dp[i - pent] * sign + mod;
       dp[i] = sum \% mod;
   }
   return dp;
```

Prime Sieve

```
//cat prime_sieve.hpp | ./hash.sh
//25a877
#pragma once
bool is_prime(int val, const vector<int>& sieve) {
    assert(val < ssize(sieve));</pre>
    return val >= 2 && sieve[val] == val;
vector<int> get_prime_factors(int val, const vector<int>& sieve) {
    assert(val < ssize(sieve));</pre>
    vector<int> factors;
    while (val > 1) {
        int p = sieve[val]:
        factors.push_back(p);
        val /= p;
    }
    return factors;
//returns array `sieve` where `sieve[i]` = some prime factor of `i`
vector<int> get_sieve(int n) {
    vector<int> sieve(n);
    iota(sieve.begin(), sieve.end(), 0);
    for (int i = 2; i * i < n; i++)
        if (sieve[i] == i)
            for (int j = i * i; j < n; j += i)
                sieve[j] = i;
    return sieve;
```

Row Reduce

```
//cat row_reduce.hpp | ./hash.sh
//c812f1
#pragma once
//for mod inverse
#include "binary_exponentiation_mod.hpp"
//First `cols` columns of mat represents a matrix to be left in reduced row echelon form
//Row operations will be performed to all later columns
//
//example usage:
// auto [rank, det] = row_reduce(mat, ssize(mat[0]), mod) //row reduce matrix with no extra
     \hookrightarrow columns
pair<int/*rank*/, long long/*determinant*/> row_reduce(vector<vector<long long>>& mat, int
     \hookrightarrow cols, long long mod) {
    int n = ssize(mat), m = ssize(mat[0]), rank = 0;
    long long det = 1;
    assert(cols <= m);</pre>
    for (int col = 0; col < cols && rank < n; col++) {</pre>
        //find arbitrary pivot and swap pivot to current row
        for (int i = rank; i < n; i++)
            if (mat[i][col] != 0) {
                if (rank != i)
                    det = det == 0 ? 0 : mod - det;
                swap(mat[i], mat[rank]);
                break;
        if (mat[rank][col] == 0) {
            det = 0;
            continue:
```

```
}
    det = det * mat[rank][col] % mod;
    //make pivot 1 by dividing row by inverse of pivot
    long long a_inv = bin_exp(mat[rank][col], mod - 2, mod);
    for (int j = 0; j < m; j++)
        mat[rank][j] = mat[rank][j] * a_inv % mod;
    //zero-out all numbers above & below pivot
    for (int i = 0; i < n; i++)
        if (i != rank && mat[i][col] != 0) {
            long long val = mat[i][col];
            for (int j = 0; j < m; j++) {
                mat[i][j] -= mat[rank][j] * val % mod;
                if (mat[i][j] < 0)</pre>
                    mat[i][j] += mod;
        }
    rank++;
}
assert(rank <= min(n, cols));</pre>
return {rank, det};
```

Solve Linear Equations MOD

```
//cat solve_linear_mod.hpp | ./hash.sh
//0a302e
#pragma once
#include "row_reduce.hpp"
struct matrix_info {
   int rank;
   long long det;
   vector<long long> x;
//Solves mat * x = b under prime mod.
//mat is a n (rows) by m (cols) matrix, b is a length n column vector, x is a length m vector.
//assumes n,m >= 1, else RTE
//Returns rank of mat, determinant of mat, and x (solution vector to mat * x = b).
//x is empty if no solution. If rank < m, there are multiple solutions and an arbitrary one is
     \hookrightarrow returned.
//Leaves mat in reduced row echelon form (unlike kactl) with b appended.
//Trick: Number of unique solutions = (size of domain) ^ (# of free variables).
//# of free variables is generally equivalent to n - rank.
//0(n * m * min(n,m))
matrix_info solve_linear_mod(vector<vector<long long>>& mat, const vector<long long>& b, long
     \hookrightarrow long mod) {
   assert(ssize(mat) == ssize(b));
   int n = ssize(mat), m = ssize(mat[0]);
   for (int i = 0; i < n; i++)
        mat[i].push_back(b[i]);
   auto [rank, det] = row_reduce(mat, m, mod);//row reduce not including the last column
   //check if solution exists
   for (int i = rank; i < n; i++) {
        if (mat[i].back() != 0)
           return {rank, det, {} }; //no solution exists
   }
   //initialize solution vector (`x`) from row-reduced matrix
   vector<long long> x(m, 0);
    for (int i = 0, j = 0; i < rank; i++) {
```

Euler's Totient Phi Function

```
//cat totient.hpp | ./hash.sh
//36bd41
#pragma once
//Euler's totient function counts the positive integers
//up to a given integer n that are relatively prime to n.
//To improve, pre-calc prime factors or use Pollard-rho to find prime factors.
int totient(int n) {
    int res = n;
    for (int i = 2; i * i <= n; i++) {
        if (n % i == 0) {
            while (n \% i == 0)
                n /= i;
            res -= res / i;
    }
    if (n > 1)
        res -= res / n;
    return res;
```

Tetration MOD

```
//cat tetration_mod.hpp | ./hash.sh
//e2153e
#pragma once
#include "binary_exponentiation_mod.hpp"
#include "totient.hpp"
//to calculate (base^pw)%mod with huge pw and non-prime mod:
//let t = totient(mod)
//if log2(mod) \le pw then (base^pw)^mod == (base^(t+(pw%t)))^mod
//source: https://cp-algorithms.com/algebra/phi-function.html#generalization
//returns base ^ (base ^ (base ^ ... )) % mod, where the height of the tower is pw
long long tetration(long long base, long long pw, long long mod) {
    if (mod == 1)
        return 0:
    if (base == 0)
        return (pw + 1) % 2 % mod;
    if (base == 1 || pw == 0)
        return 1;
    if (pw == 1)
        return base % mod;
    if (base == 2 && pw == 2)
        return 4 % mod;
    if (base == 2 && pw == 3)
        return 16 % mod;
    if (base == 3 \&\& pw == 2)
```

```
return 27 % mod;
//need enough base cases such that the following is true
//log2(mod) <= tetration(base, pw - 1) (before modding)
int t = totient(int(mod));
long long exp = tetration(base, pw - 1, t);
return bin_exp(base, exp + t, mod);
}</pre>
```

MISC

Cartesian Tree

```
//cat cartesian_tree.hpp | ./hash.sh
//204c45
#pragma once
#include "monotonic_stack.hpp"
//min cartesian tree
vector<int> cartesian_tree(const vector<int>& arr) {
   int n = ssize(arr);
   auto rv /*reverse*/ = [&](int i) -> int {
       return n - 1 - i;
   };
   vector<int> left = monotonic_stack<int>(arr, greater());
   vector<int> right = monotonic_stack<int>(vector<int>(arr.rbegin(), arr.rend()), greater());
   vector<int> par(n);
   for (int i = 0; i < n; i++) {
       int le = left[i], ri = rv(right[rv(i)]);
       if (le >= 0 && ri < n)
           par[i] = arr[le] > arr[ri] ? le : ri;
       else if (le >= 0)
           par[i] = le;
       else if (ri < n)
           par[i] = ri;
       else
           par[i] = i;
   }
   return par;
```

Count Rectangles

```
};
for (int i = 0; i < n; i++) {
    for (int j = 0; j < m; j++)
        arr[j] = grid[i][j] * (arr[j] + 1);
    vector<int> left = monotonic_stack<int>(arr, greater());
    vector<int> right = monotonic_stack<int>(vector<int>(arr.rbegin(), arr.rend()),
         \hookrightarrow greater_equal());
    for (int j = 0; j < m; j++) {
        int le = j - left[j] - 1, ri = rv(right[rv(j)]) - j - 1;
        cnt[arr[j]][le + ri + 1]++;
        cnt[arr[i]][le]--;
        cnt[arr[j]][ri]--;
}
for (int i = 1; i \le n; i++)
    for (int k = 0; k < 2; k++)
        for (int j = m - 1; j >= 1; j--)
            cnt[i][j] += cnt[i][j + 1];
for (int j = 1; j \le m; j++)
    for (int i = n - 1; i >= 1; i --)
        cnt[i][j] += cnt[i + 1][j];
return cnt:
```

Max Rectangle in Histogram

```
//cat max_rect_histogram.hpp | ./hash.sh
//95288f
#pragma once
#include "monotonic_stack.hpp"
long long max_rect_histogram(const vector<int>& arr) {
    auto rv /*reverse*/ = [&](int i) -> int {
        return ssize(arr) - 1 - i;
    };
    vector<int> left = monotonic_stack<int>(arr, greater_equal());
    vector<int> right = monotonic_stack<int>(vector<int>(arr.rbegin(), arr.rend()),
         \hookrightarrow greater_equal());
    long long max_area = 0;
    for (int i = 0; i < ssize(arr); i++) {</pre>
        int le = left[i], ri = rv(right[rv(i)]);//arr[i] is the max of range (le, ri)
        max_area = max(max_area, 1LL * arr[i] * (ri - le - 1));
    }
    return max_area;
```

Monotonic Stack

GCD Convolution

```
//cat gcd_convolution.hpp | ./hash.sh
//d92c44
#pragma once
// c[k] = the sum for all pairs where gcd(i,j) == k of a[i] * b[j]
template<int MOD> vector<int> gcd_convolution(const vector<int>& a, const vector<int>& b) {
   assert(ssize(a) == ssize(b));
   int n = ssize(a);
   vector<int> c(n);
   for (int gcd = n - 1; gcd >= 1; gcd--) {
       int sum_a = 0, sum_b = 0;
       for (int i = gcd; i < n; i += gcd) {
           sum_a = (sum_a + a[i]) \% MOD, sum_b = (sum_b + b[i]) \% MOD;
           c[gcd] = (c[gcd] - c[i] + MOD) % MOD;
       c[gcd] = int((c[gcd] + 1LL * sum_a * sum_b) % MOD);
   }
   return c;
```

Iterate Chooses

```
//cat iterate_chooses.hpp | ./hash.sh
//c79083
#pragma once

// source: https://github.com/kth-competitive-programming/
// kactl/blob/main/content/various/chapter.tex
// iterates all bitmasks of size n with k bits set
// Time Complexity: O(n choose k)
// Space Complexity: O(1)

int next_subset(int mask) {
   int c = mask & -mask, r = mask + c;
   return r | (((r ^ mask) >> 2) / c);
}

void iterate_chooses(int n, int k, const function<void(int)>& func) {
   for (int mask = (1 << k) - 1; mask < (1 << n); mask = next_subset(mask))
      func(mask);
}</pre>
```

Iterate Submasks

```
//cat iterate_submasks.hpp | ./hash.sh
//084c05
#pragma once

// iterates all submasks of mask
// Time Complexity: 0(3^n) to iterate every submask of every mask of size n
// Space Complexity: 0(1)

void iterate_submasks(int mask, const function<void(int)>& func) {
    for (int submask = mask; submask; submask = (submask - 1) & mask)
        func(submask);
}
```

Iterate Supermasks

```
//cat iterate_supermasks.hpp | ./hash.sh
//76b38f
#pragma once

// iterates all supermasks of mask
// Time Complexity: 0(3^n) to iterate every supermask of every mask of size n
// Space Complexity: 0(1)

void iterate_supermasks(int mask, int n, const function<void(int)>& func) {
    for (int supermask = mask; supermask < (1 << n); supermask = (supermask + 1) | mask)
        func(supermask);
}</pre>
```

Number of Distinct Subsequences DP

```
//cat num_distinct_subsequences.hpp | ./hash.sh
//d94bdc
#pragma once
//returns number of distinct subsequences
//the empty subsequence is counted
int num_subsequences(const vector<int>& arr, int mod) {
    vector<int> dp(ssize(arr) + 1, 1);
    map<int, int> last;
    for (int i = 0; i < ssize(arr); i++) {</pre>
        int& curr = dp[i + 1] = 2 * dp[i];
        if (curr >= mod)
            curr -= mod:
        auto it = last.find(arr[i]);
        if (it != last.end()) {
            curr -= dp[it->second];
            if (curr < 0)
                curr += mod;
            it->second = i;
        } else
            last[arr[i]] = i;
    return dp.back();
```

```
//cat policy_based_data_structures.hpp | ./hash.sh
//a777d7
#pragma once
//place these includes *before* the `#define int long long` else compile error
//not using <bits/extc++.h> as it compile errors on codeforces c++20 compiler
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
//BST with extra functions https://codeforces.com/blog/entry/11080
//order_of_key - # of elements *strictly* less than given element
//find_by_order - find kth largest element, k is 0 based so find_by_order(0) returns min
     \hookrightarrow element
template <typename T> using indexed_set = tree<T, null_type, less<T>, rb_tree_tag,

    tree_order_statistics_node_update>;
//example initialization:
indexed_set<pair<long long, int>> is;
//hash table (apparently faster than unordered_map): https://codeforces.com/blog/entry/60737
//example initialization:
gp_hash_table<string, long long> ht;
```

Random

```
//cat random.hpp | ./hash.sh
//ab9111
#pragma once

//source: https://codeforces.com/blog/entry/61675

mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());

//intended types: int, unsigned, long long
//returns a random number in range [le, ri)
template <typename T> inline T get_rand(T le, T ri) {
    assert(le < ri);
    return uniform_int_distribution<T>(le, ri - 1)(rng);
}

//vector<int> a;
//shuffle(a.begin(), a.end(), rng);
```

Safe Hash

```
return splitmix64(x + FIXED_RANDOM);
};
};
//usage:
unordered_map<long long, int, custom_hash> safe_map;
#include "policy_based_data_structures.hpp"
gp_hash_table<long long, int, custom_hash> safe_hash_table;
```

RANGE DATA STRUCTURES

Number Distinct Elements

```
//cat distinct_query.hpp | ./hash.sh
//79534f
#pragma once
//source: https://cp-algorithms.com/data_structures/segment_tree.html
// #preserving-the-history-of-its-values-persistent-segment-tree
//works with negatives
//O(n log n) time and space
struct distinct_query {
   struct node {
       int sum;
       int lch, rch;//children, indexes into `tree`
       node(int a_sum, int a_lch, int a_rch) : sum(a_sum), lch(a_lch), rch(a_rch) {}
   const int N;
   vector<int> roots;
   deque<node> tree;
   distinct_query(const vector<int>& arr) : N(ssize(arr)), roots(N + 1, 0) {
       tree.emplace_back(0, 0, 0); //acts as null
       map<int, int> last_idx;
       for (int i = 0; i < N; i++) {
           roots[i + 1] = update(roots[i], 0, N, last_idx[arr[i]]);
           last_idx[arr[i]] = i + 1;
   int update(int v, int tl, int tr, int idx) {
       if (tr - tl == 1) {
           tree.emplace_back(tree[v].sum + 1, 0, 0);
           return ssize(tree) - 1;
       int tm = tl + (tr - tl) / 2;
       int lch = tree[v].lch;
       int rch = tree[v].rch;
       if (idx < tm)
           lch = update(lch, tl, tm, idx);
       else
           rch = update(rch, tm, tr, idx);
       tree.emplace_back(tree[lch].sum + tree[rch].sum, lch, rch);
       return ssize(tree) - 1;
   //returns number of distinct elements in range [le,ri)
   int query(int le, int ri) const {
       assert(0 <= le && le <= ri && ri <= N);
       return query(roots[le], roots[ri], 0, N, le + 1);
   int query(int vl, int vr, int tl, int tr, int idx) const {
```

Implicit Lazy Segment Tree

```
//cat implicit_seg_tree.hpp | ./hash.sh
//ab5eb9
#pragma once
//example initialization:
// implicit_seg_tree<10'000'000> ist(le, ri);
template <int N> struct implicit_seg_tree {
   using dt = array<long long, 2>;//min, number of mins
   using ch = long long;
   static dt combine(const dt& le, const dt& ri) {
       if (le[0] == ri[0])
           return {le[0], le[1] + ri[1]};
       return min(le, ri);
   static constexpr dt UNIT{(long long)1e18, 0LL);
   struct node {
       dt val;
       ch lazy = 0;
       int lch = -1, rch = -1; // children, indexes into `tree`, -1 for null
   int ptr = 0, root_l, root_r;//[root_l, root_r) defines range of root node; handles
   implicit_seg_tree(int le, int ri) : root_l(le), root_r(ri) {
       tree[ptr++].val = {0, ri - le};
   }
   void apply(int v, ch add) {
       tree[v].val[0] += add;
       tree[v].lazy += add;
   }
   void push(int v, int tl, int tr) {
       if (tr - tl > 1 && tree[v].lch == -1) {
           int tm = tl + (tr - tl) / 2;
           assert(ptr + 1 < N);
           tree[v].lch = ptr;
           tree[ptr++].val = {0, tm - tl};
           tree[v].rch = ptr;
           tree[ptr++].val = {0, tr - tm};
       if (tree[v].lazy) {
           apply(tree[v].lch, tree[v].lazy);
           apply(tree[v].rch, tree[v].lazy);
           tree[v].lazy = 0;
       }
   }
   //update range [le,ri)
   void update(int le, int ri, ch add) {
       update(0, root_l, root_r, le, ri, add);
```

```
void update(int v, int tl, int tr, int le, int ri, ch add) {
        if (ri <= tl || tr <= le)</pre>
            return:
        if (le <= tl && tr <= ri)
            return apply(v, add);
        push(v, tl, tr);
        int tm = tl + (tr - tl) / 2;
        update(tree[v].lch, tl, tm, le, ri, add);
        update(tree[v].rch, tm, tr, le, ri, add);
        tree[v].val = combine(tree[tree[v].lch].val,
                               tree[tree[v].rch].val);
    //query range [le,ri)
    dt query(int le, int ri) {
        return query(0, root_l, root_r, le, ri);
    dt query(int v, int tl, int tr, int le, int ri) {
        if (ri <= tl || tr <= le)
            return UNIT;
        if (le <= tl && tr <= ri)</pre>
            return tree[v].val;
        push(v, tl, tr);
        int tm = tl + (tr - tl) / 2;
        return combine(query(tree[v].lch, tl, tm, le, ri),
                       query(tree[v].rch, tm, tr, le, ri));
    }
};
```

Kth Smallest

```
//cat kth_smallest.hpp | ./hash.sh
//b86dd0
#pragma once
//source: https://cp-algorithms.com/data_structures/segment_tree.html
// #preserving-the-history-of-its-values-persistent-segment-tree
struct kth_smallest {
    struct node {
        int sum;
        int lch, rch;//children, indexes into `tree`
        node(int a_sum, int a_lch, int a_rch) : sum(a_sum), lch(a_lch), rch(a_rch) {}
    int mn = INT_MAX, mx = INT_MIN;
    vector<int> roots:
    deque<node> tree;
    kth_smallest(const vector<int>& arr) : roots(ssize(arr) + 1, 0) {
        tree.emplace_back(0, 0, 0); //acts as null
        for (int val : arr)
            mn = min(mn, val), mx = max(mx, val + 1);
        for (int i = 0; i < ssize(arr); i++)
            roots[i + 1] = update(roots[i], mn, mx, arr[i]);
    int update(int v, int tl, int tr, int idx) {
        if (tr - tl == 1) {
            tree.emplace_back(tree[v].sum + 1, 0, 0);
            return ssize(tree) - 1;
        int tm = tl + (tr - tl) / 2;
```

```
int lch = tree[v].lch;
        int rch = tree[v].rch;
        if (idx < tm)</pre>
            lch = update(lch, tl, tm, idx);
            rch = update(rch, tm, tr, idx);
        tree.emplace_back(tree[lch].sum + tree[rch].sum, lch, rch);
        return ssize(tree) - 1;
    }
    /* find (k+1)th smallest number in range [le, ri)
     * k is 0-based, so query(le,ri,0) returns the min
    int query(int le, int ri, int k) const {
        assert(0 <= k && k < ri - le); //note this condition implies le < ri</pre>
        assert(0 <= le && ri < ssize(roots));</pre>
        return query(roots[le], roots[ri], mn, mx, k);
    }
    int query(int vl, int vr, int tl, int tr, int k) const {
        assert(tree[vr].sum > tree[vl].sum);
        if (tr - tl == 1)
            return tl:
        int tm = tl + (tr - tl) / 2;
        int left_count = tree[tree[vr].lch].sum - tree[tree[vl].lch].sum;
        if (left_count > k)
            return query(tree[v1].lch, tree[vr].lch, tl, tm, k);
        return query(tree[v1].rch, tree[vr].rch, tm, tr, k - left_count);
   }
};
```

Merge Sort Tree

```
//cat merge_sort_tree.hpp | ./hash.sh
//e110ed
#pragma once
//For point updates: either switch to policy based BST, or use sqrt decomposition
struct merge_sort_tree {
   const int N, S/*smallest power of 2 >= N*/;
   vector<vector<int>> tree;
   merge_sort_tree(const vector<int>& arr) : N(ssize(arr)), S(N ? 1 << __lg(2 * N - 1) : 0),
        \hookrightarrow tree(2 * N) {
       for (int i = 0; i < N; i++)
            tree[i + N] = {arr[i]};
       rotate(tree.rbegin(), tree.rbegin() + S - N, tree.rbegin() + N);
        for (int i = N - 1; i >= 1; i--) {
           const auto& le = tree[2 * i];
           const auto& ri = tree[2 * i + 1];
           tree[i].reserve(ssize(le) + ssize(ri));
           merge(le.begin(), le.end(), ri.begin(), ri.end(), back_inserter(tree[i]));
       }
   }
   int value(int v, int x) const {
       return int(lower_bound(tree[v].begin(), tree[v].end(), x) - tree[v].begin());
   }
   int to_leaf(int i) const {
       i += S;
       return i < 2 * N ? i : 2 * (i - N);
   //How many values in range [le, ri) are < x?
```

```
//0(log^2(n))
int query(int le, int ri, int x) const {
   int res = 0;
   for (le = to_leaf(le), ri = to_leaf(ri); le < ri; le >>= 1, ri >>= 1) {
      if (le & 1)
            res += value(le++, x);
      if (ri & 1)
            res += value(--ri, x);
   }
   return res;
}
```

BIT

```
//cat bit.hpp | ./hash.sh
//ab7995
#pragma once
//mnemonic: Binary Indexed Tree
//NOLINTNEXTLINE(readability-identifier-naming)
template <typename T> struct BIT {
    vector<T> bit;
    BIT(int n) : bit(n, 0) {}
    BIT(const vector<T>& a) : bit(a) {
        for (int i = 0; i < ssize(a); i++) {
            int j = i | (i + 1);
            if (j < ssize(a))</pre>
                bit[j] += bit[i];
        }
    }
    void update(int i, const T& d) {
        assert(0 <= i && i < ssize(bit));</pre>
        for (; i < ssize(bit); i |= i + 1)
            bit[i] += d;
    T sum(int ri) const {//sum of range [0, ri)
        assert(0 <= ri && ri <= ssize(bit));</pre>
        T ret = 0;
        for (; ri > 0; ri &= ri - 1)
            ret += bit[ri - 1];
        return ret;
    T sum(int le, int ri) const {//sum of range [le, ri)
        assert(0 <= le && le <= ri && ri <= ssize(bit));
        return sum(ri) - sum(le);
    }
    //Returns min pos (0<=pos<=ssize(bit)+1) such that sum of [0, pos) >= sum
    //Returns ssize(bit) + 1 if no sum is >= sum, or 0 if empty sum is.
    //Doesn't work with negatives
    int lower_bound(T sum) const {
        if (sum <= 0)
            return 0:
        int pos = 0;
        for (int pw = 1 << __lg(ssize(bit) | 1); pw; pw >>= 1)
            if (pos + pw <= ssize(bit) && bit[pos + pw - 1] < sum)</pre>
                pos += pw, sum -= bit[pos - 1];
        return pos + 1;
```

|};

RMQ

```
//cat rmq.hpp | ./hash.sh
//a7bca5
#pragma once
//source: https://github.com/kth-competitive-programming/
// kactl/blob/main/content/data-structures/RMO.h
// vector<long long> arr;
// RMQ<long long> rmq(arr, [&](auto x, auto y) { return min(x,y); });
//to also get index of min element, do:
// RMQ<pair<T, int>> rmq(arr, [&](auto x, auto y) { return min(x,y); });
//and initialize arr[i].second = i (0<=i<n)</pre>
//If there are multiple indexes of min element, it'll return the smallest
//(left-most) one
//mnemonic: Range Min/Max Query
//NOLINTNEXTLINE(readability-identifier-naming)
template <typename T> struct RMQ {
    vector<vector<T>> dp;
    function<T(const T&, const T&)> op;
    RMQ(const vector<T>& arr, const function<T(const T&, const T&)>& a_op) : dp(1, arr),
         \hookrightarrow op(a_op) {
        for (int pw = 1, k = 1; 2 * pw <= ssize(arr); pw *= 2, k++) {
            dp.emplace_back(ssize(arr) - 2 * pw + 1);
            for (int j = 0; j < ssize(dp.back()); j++)
                dp[k][j] = op(dp[k - 1][j], dp[k - 1][j + pw]);
        }
    }
    //inclusive-exclusive range [le, ri)
    T query(int le, int ri) const {
        assert(0 <= le && le < ri && ri <= ssize(dp[0]));
        int lg = __lg(ri - le);
        return op(dp[lg][le], dp[lg][ri - (1 << lg)]);</pre>
   }
};
```

Disjoint RMQ

Lazy Segment Tree

```
//cat lazy_segment_tree.hpp | ./hash.sh
//96535f
#pragma once
//source: https://codeforces.com/blog/entry/18051,

→ https://github.com/ecnerwala/cp-book/blob/master/src/seg_tree.hpp,

→ https://github.com/yosupo06/Algorithm/blob/master/src/datastructure/segtree.hpp

//rotating leaves makes it a single complete binary tree (instead of a set of perfect binary
     \hookrightarrow trees)
//so standard implementations of
// - recursive seg tree
// - tree walks AKA binary search
//still work
struct seg_tree {
    using dt = long long;
    using ch = long long;
    static dt combine(const dt& le, const dt& ri) {
        return min(le, ri);
    static const dt UNIT = 1e18;
    struct node {
        dt val:
        ch lazy:
        int le, ri;//[le, ri)
    const int N, S/*smallest power of 2 >= N*/;
    vector<node> tree;
    seg\_tree(const\ vector< dt>\&\ arr) : N(ssize(arr)), S(N ? 1 << __lg(2 * N - 1) : 0), tree(2 * N - 1)
         \hookrightarrow N) {
        for (int i = 0; i < N; i++)
            tree[i + N] = {arr[i], 0, i, i + 1};
        rotate(tree.rbegin(), tree.rbegin() + S - N, tree.rbegin() + N);
        for (int i = N - 1; i >= 1; i--) {
            tree[i] = {
                combine(tree[2 * i].val, tree[2 * i + 1].val),
                tree[2 * i].le,
                tree[2 * i + 1].ri
            };
        }
    void apply(int v, ch change) {
        tree[v].val += change;
```

```
tree[v].lazy += change;
}
void push(int v) {
    if (tree[v].lazy) {
        apply(2 * v, tree[v].lazy);
        apply(2 * v + 1, tree[v].lazy);
        tree[v].lazy = 0;
    }
}
void build(int v) {
    tree[v].val = combine(tree[2 * v].val, tree[2 * v + 1].val);
}
int to_leaf(int i) const {
    i += S;
    return i < 2 * N ? i : 2 * (i - N);
}
//update range [le, ri)
void update(int le, int ri, ch change) {
    assert(0 <= le && le <= ri && ri <= N);
    le = to_leaf(le), ri = to_leaf(ri);
    int lca_l_r = __lg((le - 1) ^ ri);
    for (int lg = __lg(le); lg > __builtin_ctz(le); lg--)
        push(le >> lg);
    for (int lg = lca_l_r; lg > __builtin_ctz(ri); lg--)
        push(ri >> lg);
    for (int x = le, y = ri; x < y; x >>= 1, y >>= 1) {
        if (x & 1)
            apply(x++, change);
        if (y & 1)
            apply(--y, change);
    for (int lg = __builtin_ctz(ri) + 1; lg <= lca_l_r; lg++)</pre>
        build(ri >> lg);
    for (int lg = __builtin_ctz(le) + 1; lg <= __lg(le); lg++)</pre>
        build(le >> lg);
void update(int v/* = 1*/, int le, int ri, ch change) {
    if (ri <= tree[v].le || tree[v].ri <= le)</pre>
        return:
    if (le <= tree[v].le && tree[v].ri <= ri)</pre>
        return apply(v, change);
    push(v);
    update(2 * v, le, ri, change);
    update(2 * v + 1, le, ri, change);
    build(v);
}
//query range [le, ri)
dt query(int le, int ri) {
    assert(0 <= le && le <= ri && ri <= N);
    le = to_leaf(le), ri = to_leaf(ri);
    int lca_l_r = __lg((le - 1) ^ ri);
    for (int lg = __lg(le); lg > __builtin_ctz(le); lg--)
        push(le >> lg);
    for (int lg = lca_l_r; lg > __builtin_ctz(ri); lg--)
        push(ri >> lg);
    dt resl = UNIT, resr = UNIT;
    for (; le < ri; le >>= 1, ri >>= 1) {
        if (le & 1)
            resl = combine(resl, tree[le++].val);
```

STRINGS

Binary Trie

```
//cat binary_trie.hpp | ./hash.sh
//88fa9c
#pragma once
struct binary_trie {
    const int MX_BIT = 62;
    struct node {
        long long val = -1;
        int sub_sz = 0;//number of inserted values in subtree
        array<int, 2> next = {-1, -1};
    };
    vector<node> t;
    binary_trie() : t(1) {}
    //delta = 1 to insert val, -1 to remove val, 0 to get the # of val's in this data structure
    int update(long long val, int delta) {
        int c = 0;
        t[0].sub_sz += delta;
        for (int bit = MX_BIT; bit >= 0; bit--) {
            bool v = (val >> bit) & 1;
            if (t[c].next[v] == -1) {
                t[c].next[v] = ssize(t);
                t.emplace_back();
            c = t[c].next[v];
            t[c].sub_sz += delta;
        t[c].val = val;
        return t[c].sub_sz;
    int size() const {
        return t[0].sub_sz;
    //returns x such that:
    // x is in this data structure
    // value of (x ^ val) is minimum
    long long min_xor(long long val) const {
        assert(size() > 0);
        int c = 0;
        for (int bit = MX_BIT; bit >= 0; bit--) {
```

```
bool v = (val >> bit) & 1;
    int ch = t[c].next[v];
    if (ch != -1 && t[ch].sub_sz > 0)
        c = ch;
    else
        c = t[c].next[!v];
    }
    return t[c].val;
}
```

Prefix Function

```
// You can also pass in 0 for "all" and KMP::find will only
// return the first match: {1}. Useful for checking if there exists
// some match:
//
// ssize(KMP::find(<haystack>,0)) > 0
//NOLINTNEXTLINE(readability-identifier-naming)
template <typename T> struct KMP {
    T needle;
    vector<int> pi:
    KMP(const T& a_needle) : needle(a_needle), pi(prefix_function(needle)) {}
    vector<int> find(const T& haystack, bool all = 1) const {
        vector<int> matches;
        for (int i = 0, j = 0; i < ssize(haystack); i++) {
            while (j > 0 && needle[j] != haystack[i])
                j = pi[j - 1];
            if (needle[j] == haystack[i])
                j++;
            if (j == ssize(needle)) {
                matches.push_back(i - ssize(needle) + 1);
                if (!all)
                    return matches;
                j = pi[j - 1];
            }
        return matches:
    }
};
```

KMP String Matching

```
//cat kmp.hpp | ./hash.sh
//ab4dba
#pragma once
//mnemonic: Knuth Morris Pratt
#include "prefix_function.hpp"
//usage:
// string needle;
// ...
// KMP kmp(needle);
//or
// vector<int> needle;
// ...
// KMP kmp(needle):
//kmp doubling trick: to check if 2 arrays are rotationally equivalent: run kmp
//with one array as the needle and the other array doubled (excluding the first
//& last characters) as the haystack or just use kactl's min rotation code
//
// if havstack = "bananas"
// needle = "ana"
// then we find 2 matches:
// bananas
// _ana___
// ___ana_
// 0123456 (indexes)
// and KMP::find returns {1,3} - the indexes in haystack where
// each match starts.
```

Suffix Array

```
//cat suffix_array.hpp | ./hash.sh
//da54ac
#pragma once
//source: https://judge.yosupo.jp/submission/63467
//time: O(n + max val)
//note O(n) is impossible because of O(nlogn) lower bound for comparison sorts
//assumes 0 \le s[i] \le max_val
template <typename T> vector<int> suffix_array(const T& s, int max_val) {
    int n = ssize(s);
    if (n == 0)
        return {};
    if (n == 1)
        return {0};
    if (n == 2)
        return \{(s[0] \ge s[1]), (s[0] < s[1])\};
    vector<int> sa(n, 0), is_s(n, 0);
    for (int i = n - 2; i >= 0; i--)
        is_s[i] = (s[i] < s[i + 1] || (s[i] == s[i + 1] && is_s[i + 1]));
    vector<int> head(max_val + 1, 0), tail(max_val + 1, 0);
    for (int i = 0; i < n; i++)
        head[s[i] + 1]++, tail[s[i]] += !is_s[i];
    partial_sum(head.begin(), head.end(), head.begin());
    for (int i = 0; i <= max_val; i++)</pre>
        tail[i] += head[i];
    vector<int> tmp(max_val + 1, 0);
    auto induce = [&](const vector<int>& lms) {
        fill(sa.begin(), sa.end(), -1);
```

```
copy(tail.begin(), tail.end(), tmp.begin());
              for (int i : lms)
                         sa[tmp[s[i]]++] = i;
             copy(head.begin(), head.end(), tmp.begin());
             sa[tmp[s[n-1]]++] = n-1;
             for (int i = 0; i < n; i++)
                         if (int j = sa[i]; j > 0 && !is_s[j - 1])
                                     sa[tmp[s[j-1]]++] = j-1;
             copy(head.begin(), head.end(), tmp.begin());
             for (int i = n - 1; i >= 0; i--)
                         if (int j = sa[i]; j > 0 && is_s[j-1])
                                     sa[--tmp[s[j-1]+1]] = j-1;
};
vector<int> lms_idx(n, -1), lms(0, 0);
for (int i = 1; i < n; i++)
             if (is_s[i] && !is_s[i - 1])
                         lms_idx[i] = ssize(lms), lms.push_back(i);
induce(lms);
if (ssize(lms)) {
             vector<int> s2(ssize(lms), 0), sorted_lms;
             copy_if(sa.begin(), sa.end(), back_inserter(sorted_lms), [&](int i) -> bool {
                         return lms_idx[i] != -1;
             });
             int max_val2 = 0;
             for (int i = 1; i < ssize(lms); i++) {</pre>
                         int a = sorted_lms[i - 1], b = sorted_lms[i];
                         \max_{a} = \max_{a} + 1 = \min_{a} + 
                                         \hookrightarrow lms[lms_idx[a] + 1]),
                                                                                    s.begin() + b, s.begin() + (lms_idx[b] + 1 == ssize(lms) ? n :
                                                                                                    \hookrightarrow lms[lms_idx[b] + 1]));
                          s2[lms_idx[b]] = max_val2;
             auto sa2 = suffix_array(s2, max_val2 + 1);
             for (int i = 0; i < ssize(lms); i++)
                          sorted_lms[i] = lms[sa2[i]];
             induce(sorted_lms);
}
return sa;
```

LCP Array

```
//cat longest_common_prefix.hpp | ./hash.sh
//0c613c
#pragma once
//source: https://cp-algorithms.com/string/suffix-array.html
template <typename T> vector<int> calc_lcp(const T& s, const vector<int>& sa) {
    int n = ssize(s);
    vector<int> inv_sa(n), lcp(n - 1, 0);
    for (int i = 0; i < n; i++)
        inv_sa[sa[i]] = i;
    for (int i = 0, k = 0; i < n; i++) {
        if (inv_sa[i] == n - 1) {
            k = 0;
            continue;
        }
        int j = sa[inv_sa[i] + 1];
        while (i + k < n && j + k < n && s[i + k] == s[j + k])</pre>
```

```
k++;
    lcp[inv_sa[i]] = k;
    if (k)
        k--;
    }
    return lcp;
}
```

Longest Common Prefix Query

```
//cat longest_common_prefix_query.hpp | ./hash.sh
//f53119
#pragma once
#include "suffix_array.hpp"
#include "longest_common_prefix.hpp"
#include "../range_data_structures/rmq.hpp"
//computes suffix array, lcp array, and then sparse table over lcp array
//0(n \log n)
template <typename T> struct lcp_query {
    const int N;
    vector<int> sa, inv_sa, lcp;
    RMQ<int> rmq;
    lcp_query(const T& s, int max_val) : N(ssize(s)), sa(suffix_array(s, max_val)), inv_sa(N),
        for (int i = 0; i < N; i++)
           inv_sa[sa[i]] = i;
    //length of longest common prefix of suffixes s[idx1 ... N), s[idx2 ... N), 0-based
         \hookrightarrow indexing
    //You can check if two substrings s[l1..r1), s[l2..r2) are equal in O(1) by:
    //r1-l1 == r2-l2 \&\& longest_common_prefix(l1, l2) >= r1-l1
    int get_lcp(int idx1, int idx2) const {
       if (idx1 == idx2)
           return N - idx1;
       auto [le, ri] = minmax(inv_sa[idx1], inv_sa[idx2]);
       return rmq.query(le, ri);
   //returns 1 if suffix s[idx1 ... N) < s[idx2 ... N)</pre>
    //(so 0 if idx1 == idx2)
    bool less(int idx1, int idx2) const {
       return inv_sa[idx1] < inv_sa[idx2];</pre>
    }
};
```

Palindrome Query

```
//cat palindrome_query.hpp | ./hash.sh
//68c8e1
#pragma once
#include "../../kactl/content/strings/Manacher.h"
struct pal_query {
    const int N;
    array<vi, 2> pal_len;
    pal_query(const string& s) : N(ssize(s)), pal_len(manacher(s)) {}
    //returns 1 if substring s[le...ri) is a palindrome
    //(returns 1 when le == ri)
```

```
bool is_pal(int le, int ri) const {
    assert(0 <= le && le <= ri && ri <= N);
    int len = ri - le;
    return pal_len[len & 1][le + len / 2] >= len / 2;
};
```

Trie

```
//cat trie.hpp | ./hash.sh
//2aa8c6
#pragma once
//source: https://cp-algorithms.com/string/aho_corasick.html#construction-of-the-trie
const int K = 26;//alphabet size
struct trie {
   const char MIN_CH = 'A';//'a' for lowercase, '0' for digits
   struct node {
       int next[K], cnt_words = 0, par = -1;
        char ch;
       node(int a_par = -1, char a_ch = '#') : par(a_par), ch(a_ch) {
            fill(next, next + K, -1);
        }
   };
   vector<node> t;
   trie() : t(1) {}
   void insert(const string& s) {
       int v = 0;
        for (char ch : s) {
            int let = ch - MIN_CH;
           if (t[v].next[let] == -1) {
                t[v].next[let] = ssize(t);
                t.emplace_back(v, ch);
           }
           v = t[v].next[let];
        t[v].cnt_words++;
   }
   int find(const string& s) const {
        int v = 0;
        for (char ch : s) {
           int let = ch - MIN_CH;
           if (t[v].next[let] == -1)
               return 0;
           v = t[v].next[let];
        return t[v].cnt_words;
};
```