

Critical transitions and the fragmenting of global forests

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Abstract

Global forests provide critical habitat for many species, essential ecosystem services, and are coupled to atmospheric dynamics through exchanges of energy, water and gases. One of the most important changes produced in the biosphere is the replacement of forest areas with human dominated landscapes. These areas contain many fewer species than the natural ecosystem they replaced, and this change is one of the main drivers of extinctions in the Anthropocene. Another effect is that habitat replacement leads to fragmentation, altering the sizes of patches, the structure and function of the forest. In different kinds of vegetation, including forests, the patch size distributions follow power laws. These have been used as a signal of critical phase transitions, where the system state changes suddenly at a critical point; in the case of forest patches, this implies an abrupt change in connectivity that causes a increased fragmentation level, posing an additional risk to forest function as an habitat and ecosystem. All these patterns have been observed only at relatively small scales, however. Here we studied the distribution of forest patch sizes at a global level—wide regions of connected forest across continents and big islands—examining their changes over the last fourteen years and different signals of a critical transition. The conditions that indicate that a region is near a critical fragmentation threshold are: a patch size distribution following a power law; temporal fluctuations of the largest patch following a power law; variance of largest patch fluctuations increasing in time; and a negative skewness of the largest patch fluctuations. We found that most regions, except the Eurasian mainland, followed a power-law distribution. Only the tropical forest of Africa and South America met the five criteria and thus seemed to be near a critical fragmentation threshold. This implies that the combined influence of human pressures and climate forcings might trigger undesired effects of fragmentation, such as species loss and degradation of ecosystems services, in these regions. The simple criteria proposed here could be used as early warning to estimate the distance to a fragmentation threshold in forest around the globe, and provide

1 a guide to direct conservation efforts at a continental level.

1 Introduction

2 Forests are one of the most important ecosystems on earth, providing habitat for a large proportion of species
3 and contributing extensively to global biodiversity (Crowther *et al.*, 2015). In the previous century human
4 activities have influenced global bio-geochemical cycles (Bonan, 2008; Canfield *et al.*, 2010), with one of
5 the most dramatic changes being the replacement of 40% of Earth’s formerly biodiverse land areas with
6 landscapes that contain only a few species of crop plants, domestic animals and humans (Foley *et al.*, 2011).
7 These local changes have accumulated over time and now constitute a global forcing (Barnosky *et al.*, 2012).

8 Another global scale forcing that is tied to habitat destruction is fragmentation, which is defined as the
9 division of a continuous habitat into separated portions that are smaller and more isolated. Fragmentation
10 produces multiple interwoven effects: reductions of biodiversity between 13% and 75%, decreasing forest
11 biomass, and changes in nutrient cycling (Haddad *et al.*, 2015). The effects of fragmentation are not only
12 important from an ecological point of view but also that of human activities, as ecosystem services are deeply
13 influenced by the level of landscape fragmentation (Mitchell *et al.*, 2015).

14 Ecosystems have complex interactions between species and present feedbacks at different levels of organi-
15 zation (Gilman *et al.*, 2010), and external forcings can produce abrupt changes from one state to another,
16 called critical transitions (Scheffer *et al.*, 2009). These abrupt state shifts cannot be linearly forecasted from
17 past changes, and are thus difficult to predict and manage (Scheffer *et al.*, 2009). Critical transitions have
18 been detected mostly at local scales (Drake & Griffen, 2010; Carpenter *et al.*, 2011), but the accumulation
19 of changes in local communities that overlap geographically can propagate and theoretically cause an abrupt
20 change of the entire system at larger scales (Barnosky *et al.*, 2012). Coupled with the existence of global
21 scale forcings, this implies the possibility that a critical transition could occur at a global scale (Rockstrom
22 *et al.*, 2009; Folke *et al.*, 2011).

23 Complex systems can experience two general classes of critical transitions (Solé, 2011). In so-called first
24 order transitions, a catastrophic regime shift that is mostly irreversible occurs because of the existence of
25 alternative stable states (Scheffer *et al.*, 2001). This class of transitions is suspected to be present in a variety
26 of ecosystems such as lakes, woodlands, coral reefs (Scheffer *et al.*, 2001), semi-arid grasslands (Bestelmeyer
27 *et al.*, 2011), and fish populations (Vasilakopoulos & Marshall, 2015). They can be the result of positive
28 feedback mechanisms (Martín *et al.*, 2015); for example, fires in some forest ecosystems were more likely to
29 occur in previously burned areas than in unburned places (Kitzberger *et al.*, 2012).

30 The other class of critical transitions are continuous or second order transitions (Solé & Bascompte, 2006).
31 In these cases, there is a narrow region where the system suddenly changes from one domain to another,

1 with the change being continuous and in theory reversible. This kind of transitions were suggested to be
2 present in tropical forest (Pueyo *et al.*, 2010), semi-arid mountain ecosystems (McKenzie & Kennedy, 2012),
3 tundra shrublands (Naito & Cairns, 2015). The transition happens at critical point where we can observe a
4 distinctive spatial pattern: scale invariant fractal structures characterized by power law patch distributions
5 (Stauffer & Aharony, 1994).

6 There are several processes that can convert a catastrophic transition to a second order transitions (Martín
7 *et al.*, 2015). These include stochasticity, such as demographic fluctuations, spatial heterogeneities, and/or
8 dispersal limitation. All these components are present in forest around the globe (Seidler & Plotkin, 2006;
9 Filotas *et al.*, 2014; Fung *et al.*, 2016), thus continuous transitions might be more probable than catastrophic
10 transitions. Moreover there is some evidence of recovery in some systems that supposedly suffered an
11 irreversible transition produced by overgrazing (Zhang *et al.*, 2005) and desertification (Allington & Valone,
12 2010).

13 The spatial phenomena observed in continuous critical transitions deal with connectivity, a fundamental
14 property of general systems and ecosystems from forests (Ochoa-Quintero *et al.*, 2015) to marine ecosystems
15 (Leibold & Norberg, 2004) and the whole biosphere (Lenton & Williams, 2013). When a system goes from
16 a fragmented to a connected state we say that it percolates (Solé, 2011). Percolation implies that there is a
17 path of connections that involves the whole system. Thus we can characterize two domains or phases: one
18 dominated by short-range interactions where information cannot spread, and another in which long range
19 interactions are possible and information can spread over the whole area. (The term “information” is used
20 in a broad sense and can represent species dispersal or movement.)

21 Thus, there is a critical “percolation threshold” between the two phases, and the system could be driven
22 close to or beyond this point by an external force; climate change and deforestation are the main forces
23 that could be the drivers of such a phase change in contemporary forests (Bonan, 2008; Haddad *et al.*,
24 2015). There are several applications of this concept in ecology: species’ dispersal strategies are influenced
25 by percolation thresholds in three-dimensional forest structure (Solé *et al.*, 2005), and it has been shown
26 that species distributions also have percolation thresholds (He & Hubbell, 2003). This implies that pushing
27 the system below the percolation threshold could produce a biodiversity collapse (Bascompte *et al.*, 1996;
28 Solé *et al.*, 2004; Pardini *et al.*, 2010); conversely, being in a connected state (above the threshold) could
29 accelerate the invasion of forest into prairie (Loehle *et al.*, 1996; Naito & Cairns, 2015).

30 One of the main challenges with systems that can experience critical transitions—of any kind—is that the
31 value of the critical threshold is not known in advance. In addition, because near the critical point a small
32 change can precipitate a state shift of the system, they are difficult to predict. Several methods have been

developed to detect if a system is close to the critical point, e.g. a deceleration in recovery from perturbations, or an increase in variance in the spatial or temporal pattern (Hastings & Wysham, 2010; Carpenter *et al.*, 2011; Boettiger & Hastings, 2012; Dai *et al.*, 2012).

In this study, our objective is to look for evidence that forests around the globe are near continuous critical point that represent a fragmentation threshold. We use the framework of percolation to first evaluate if forest patch distribution at a continental scale is described by a power law distribution and then examined the fluctuations of the largest patch. The advantage of using data at a continental scale is that for very large systems the transitions are very sharp (Solé, 2011) and thus much easier to detect than at smaller scales, where noise can mask the signals of the transition.

Methods

Study areas definition

We analyzed mainland forests at a continental scale, covering the whole globe, by delimiting land areas with a near-contiguous forest cover, separated with each other by large non-forested areas. Using this criterion, we delimited the following forest regions. In America, three regions were defined: South America temperate forest (SAT), subtropical and tropical forest up to Mexico (SAST), and USA and Canada forest (NA). Europe and North Asia were treated as one region (EUAS). The rest of the delimited regions were South-east Asia (SEAS), Africa (AF), and Australia (OC). We also included in the analysis islands larger than 10^5 km². The mainland region has the number 1 e.g. OC1, and the nearby islands have consecutive numeration (Supplementary figure S1-S6).

Forest patch distribution

We studied forest patch distribution in each defined area from 2000 to 2014 using the MODerate-resolution Imaging Spectroradiometer (MODIS) Vegetation Continuous Fields (VCF) Tree Cover dataset version 051 (DiMiceli *et al.*, 2015). This dataset is produced at a global level with a 231-m resolution, from 2000 onwards on an annual basis. There are several definition of forest based on percent tree cover (Sexton *et al.*, 2015), we choose a 30% threshold to convert the percentage tree cover to a binary image of forest and non-forest pixels. This was the definition used by the United Nations' International Geosphere-Biosphere Programme (Belward, 1996), and studies of global fragmentation (Haddad *et al.*, 2015). This definition avoids the errors produced by low discrimination of MODIS VCF between forest and dense herbaceous vegetation at low forest

cover (Sexton *et al.*, 2015). Patches of contiguous forest were determined in the binary image by grouping connected forest pixels using a neighborhood of 8 forest units (Moore neighborhood).

Percolation theory

A more in-depth introduction to percolation theory can be found elsewhere (Stauffer & Aharony, 1994) and a review from an ecological point of view is available (Oborny *et al.*, 2007). Here, to explain the basic elements of percolation theory we formulate a simple model: we represent our area of interest by a square lattice and each site of the lattice can be occupied—e.g. by forest—with a probability p . The lattice will be more occupied when p is greater, but the sites are randomly distributed. We are interested in the connection between sites, so we define a neighborhood as the eight adjacent sites surrounding any particular site. The sites that are neighbors of other occupied sites define a patch. When there is a patch that connects the lattice from opposite sides, it is said that the system percolates. When p is increased from low values, a percolating patch suddenly appears at some value of p called the critical point p_c .

Thus percolation is characterized by two well defined phases: the unconnected phase when $p < p_c$ (called subcritical in physics), in which species cannot travel far inside the forest, as it is fragmented; in a general sense, information cannot spread. The second is the connected phase when $p > p_c$ (supercritical), species can move inside a forest patch from side to side of the area (lattice), i.e. information can spread over the whole area. Near the critical point several scaling laws arise: the structure of the patch that spans the area is fractal, the size distribution of the patches is power-law, and other quantities also follow power-law scaling (Stauffer & Aharony, 1994).

The value of the critical point p_c depends on the geometry of the lattice and on the definition of the neighborhood, but other power-law exponents only depend on the lattice dimension. Close to the critical point, the distribution of patch sizes is:

$$(1) \quad n_s(p_c) \propto s^{-\alpha}$$

where $n_s(p)$ is the number of patches of size s . The exponent α does not depend on the details of the model and it is called universal (Stauffer & Aharony, 1994). These scaling laws can be applied for landscape structures that are approximately random, or at least only correlated over short distances (Gastner *et al.*, 2009). In physics this is called “isotropic percolation universality class”, and corresponds to an exponent $\alpha = 2.05495$. If we observe that the patch size distribution has another exponent it will not belong to this universality class and some other mechanism should be invoked to explain it. Percolation thresholds can also be generated by models that have some kind of memory (Hinrichsen, 2000; Ódor, 2004): for example, a

patch that has been exploited for many years will recover differently than a recently deforested forest patch. In this case, the system could belong to a different universality class, or in some cases there is no universality, in which case the value of α will depend on the parameters and details of the model (Corrado *et al.*, 2014). To illustrate the concepts we made simulations with a simple forest model with two states: forest and non-forest. This model was called the contact process and was introduced for epidemics (Harris, 1974), but has many applications in ecology (Solé & Bascompte, 2006; Gastner *et al.*, 2009). A site with forest could become extinct with probability e , and produce another forest site in a defined neighborhood with probability c . We defined the neighborhood as an isotropic power law probability distribution. We can define a single control parameter $\lambda = c/e$ and we made simulations for the subcritical fragmentation state $\lambda < \lambda_c$, with $\lambda = 2$, near the critical point for $\lambda = 2.5$ and for the supercritical state with $\lambda = 5$ (see supplementary percolation animations).

Patch size distributions

We fitted the empirical distribution of forest patch areas, based on the MODIS-derived data described above, to four distributions using maximum likelihood estimation (Goldstein *et al.*, 2004; Clauset *et al.*, 2009). The distributions were: power-law, power-law with exponential cut-off, log-normal, and exponential. We assumed that the patch size distribution is a continuous variable that was discretized by remote sensing data acquisition procedure.

We set a minimal patch size (X_{min}) at nine pixels to fit the patch size distributions to avoid artifacts at patch edges due to discretization (Weerman *et al.*, 2012). Besides this hard X_{min} limit we set due to discretization, the power-law distribution needs a lower bound for its scaling behavior. This lower bound is also estimated from the data by maximizing the Kolmogorov-Smirnov (KS) statistic, computed by comparing the empirical and fitted cumulative distribution functions (Clauset *et al.*, 2009). We also calculated the uncertainty of the parameters using a non-parametric bootstrap method (Efron & Tibshirani, 1994), and computed corrected Akaike Information Criteria (AIC_c) and Akaike weights for each model (Burnham & Anderson, 2002). Akaike weights (w_i) are the weight of evidence in favor of model i being the actual best model given that one of the N models must be the best model for that set of N models.

Additionally, we computed the goodness of fit of the power-law model following the bootstrap approach described by Clauset *et. al* (2009), where simulated data sets following the fitted model are generated, and a p -value computed as the proportion of simulated data sets that has a KS statistic less extreme than empirical data. The criterion to reject the power law model suggested by Clauset *et. al* (2009) was $p \leq 0.1$, but as we

have a very large n , meaning that negligible small deviations could produce a rejection (Klaus *et al.*, 2011), we chose a $p \leq 0.05$ to reject the power law model.

To test for differences between the fitted power law exponent for each study area we used a generalized least squares linear model (Zuur *et al.*, 2009) with weights and a residual auto-correlation structure. Weights were the bootstrapped 95% confidence intervals and we added an auto-regressive model of order 1 to the residuals to account for temporal autocorrelation.

Largest patch dynamics

The largest patch is the one that connects the highest number of sites in the area. This has been used extensively to indicate fragmentation (Gardner & Urban, 2007; Ochoa-Quintero *et al.*, 2015). The relation of the size of the largest patch S_{max} to critical transitions has been extensively studied in relation to percolation phenomena (Stauffer & Aharony, 1994; Bazant, 2000; Botet & Ploszajczak, 2004), but seldom used in ecological studies (for an exception see Gastner *et al.* (2009)). When the system is in a connected state ($p > p_c$) the landscape is almost insensitive to the loss of a small fraction of forest, but close to the critical point a minor loss can have important effects (Solé & Bascompte, 2006; Oborny *et al.*, 2007), because at this point the largest patch will have a filamentary structure, i.e. extended forest areas will be connected by thin threads. Small losses can thus produce large fluctuations.

One way to evaluate the fragmentation of the forest is to calculate the proportion of the largest patch against the total area (Keitt *et al.*, 1997). The total area of the regions we are considering (Supplementary figure S1-S6) may not be the same than the total area that the forest could potentially occupy, thus a more accurate way to evaluate the weight of S_{max} is to use the total forest area, that can be easily calculated summing all the forest pixels. We calculate the proportion of the largest patch for each year, dividing S_{max} by the total forest area of the same year: $RS_{max} = S_{max} / \sum_i S_i$. This has the effect of reducing the S_{max} fluctuations produced due to environmental or climatic changes influences in total forest area. When the proportion RS_{max} is large (more than 60%) the largest patch contains most of the forest so there are fewer small forest patches and the system is probably in a connected phase. Conversely, when it is low (less than 20%), the system is probably in a fragmented phase (Saravia & Momo, 2015).

The RS_{max} is a useful qualitative index that does not tell us if the system is near or far from the critical transition; this can be evaluated using the temporal fluctuations. We calculate the fluctuations around the mean with the absolute values $\Delta S_{max} = S_{max}(t) - \langle S_{max} \rangle$, using the proportions of RS_{max} . To characterize fluctuations we fitted three empirical distributions: power-law, log-normal, and exponential, using the same

methods described previously. We expect that large fluctuation near a critical point have heavy tails (log-normal or power-law) and that fluctuations far from a critical point have exponential tails, corresponding to Gaussian processes (Rooij *et al.*, 2013). As the data set spans 15 years, we do not have enough power to reliably detect which distribution is better (Clauset *et al.*, 2009). To improve this we performed the goodness of fit test described above for all the distributions. We generated animated maps showing the fluctuations of the two largest patches to aid in the interpretations of the results.

A robust way to detect if the system is near a critical transition is to analyze the increase in variance of the density (Benedetti-Cecchi *et al.*, 2015). It has been demonstrated that the variance increase in density appears when the system is very close to the transition (Corrado *et al.*, 2014), thus practically it does not constitute an early warning indicator. An alternative is to analyze the variance of the fluctuations of the largest patch ΔS_{max} : the maximum is attained at the critical point but a significant increase occurs well before the system reaches the critical point (Corrado *et al.*, 2014). In addition, before the critical fragmentation, the skewness of the distribution of ΔS_{max} should be negative, implying that fluctuations below the average are more frequent. We characterized the increase in the variance using quantile regression: if variance is increasing the slopes of upper or/and lower quartiles should be positive or negative.

All statistical analyses were performed using the GNU R version 3.3.0 (R Core Team, 2015), using code provided by Cosma R. Shalizi for fitting the power law with exponential cutoff model and the `powerlaw` package (Gillespie, 2015) for fitting the other distributions. For the generalized least squares linear model we used the R function `gls` from package `nlme` (Pinheiro *et al.*, 2016); and we fitted quantile regressions using the R package `quantreg` (Koenker, 2016). Image processing was done in MATLAB r2015b (The Mathworks Inc.). The complete source code for image processing and statistical analysis, and the patch size data files are available at figshare <http://dx.doi.org/10.6084/m9.figshare.4263905>.

Results

The power law distribution was selected as the best model in 92% of the cases (Supplementary Figure S7). In a small number of cases (1%) the power law with exponential cutoff was selected, but the value of the parameter α was similar by ± 0.02 to the pure power law. Additionally the patch size where the exponential tail begins is very large, thus we used the power law parameters for this cases (See Supplementary data, region EUAS3). In finite-size systems the favored model should be the power law with exponential cutoff, because the power-law tails are truncated to the size of the system (Stauffer & Aharony, 1994). Here the regions are so large that the cutoff is practically not observed.

There is only one region that did not follow a power law: Eurasia mainland, which showed a log-normal distribution, representing 7% of the cases. The log-normal and power law are both heavy tailed distributions and difficult to distinguish, but in this case Akaike weights have very high values for log-normal (near 1), meaning that this is the only possible model. In addition, the goodness of fit tests clearly rejected the power law model in all cases for this region (Supplementary table S1, region EUAS1). In general the goodness of fit test rejected the power law model in fewer than 10% of cases. In large forest areas like Africa mainland (AF1) or South America tropical-subtropical (SAST1), larger deviations are expected and the rejection rates are higher so the proportion is 30% or less (Supplementary Table S1).

Taking into account the bootstrapped confidence intervals of each power law exponent (α) and the temporal autocorrelation, there were no significant differences between α for the regions with the biggest (greater than 10^7 km²) forest areas (Figure 1 and Supplementary figure S8). There were also no differences between these regions and smaller ones (Supplementary Table S2 & S3), and all the slopes of α were not different from 0 (Supplementary Table S3). This implies a global average $\alpha = 1.908$, with a bootstrapped 95% confidence interval between 1.898 and 1.920.

The proportion of the largest patch relative to total forest area RS_{max} for regions with more than 10^7 km² of forest is shown in figure 2. South America tropical and subtropical (SAST1) and North America (NA1) have a higher RS_{max} of more than 60%, and other big regions 40% or less. For regions with less total forest area (Supplementary figure S9 & Table 1), the United Kingdom (EUAS3) has a very low proportion near 1%, while other regions such as New Guinea (OC2) and Malaysia/Kalimantan (OC3) have a very high proportion. SEAS2 (Philippines) is a very interesting case because it seems to be under 30% until the year 2005, fluctuates in the range 30-60%, and then stays over 60% (supplementary figure S9).

We analyzed the distributions of fluctuations of the largest patch relative to total forest area ΔRS_{max} and the fluctuations of the largest patch ΔS_{max} . The model selection for ΔS_{max} resulted in power law distributions for all regions (Supplementary table S6). For ΔRS_{max} instead some regions showed exponential distributions: Eurasia mainland (EUAS1), New Guinea (OC2), Malaysia (OC3), New Zealand (OC6, OC8) and Java (OC7), all others were power laws (Supplementary Table S7). The goodness of fit test (GOF) did not reject power laws in any case, but neither did it reject the other models except in a few cases; this was due to the small number of observations. We only considered fluctuations to follow a power law when this distribution was selected for both absolute and relative fluctuations.

The animations of the two largest patches (Supplementary largest patch animations) qualitatively shows the nature of fluctuations and if the state of the forest is connected or not. If the largest patch is always the same patch over time, the forest is probably not fragmented; this happens for regions with RS_{max} of

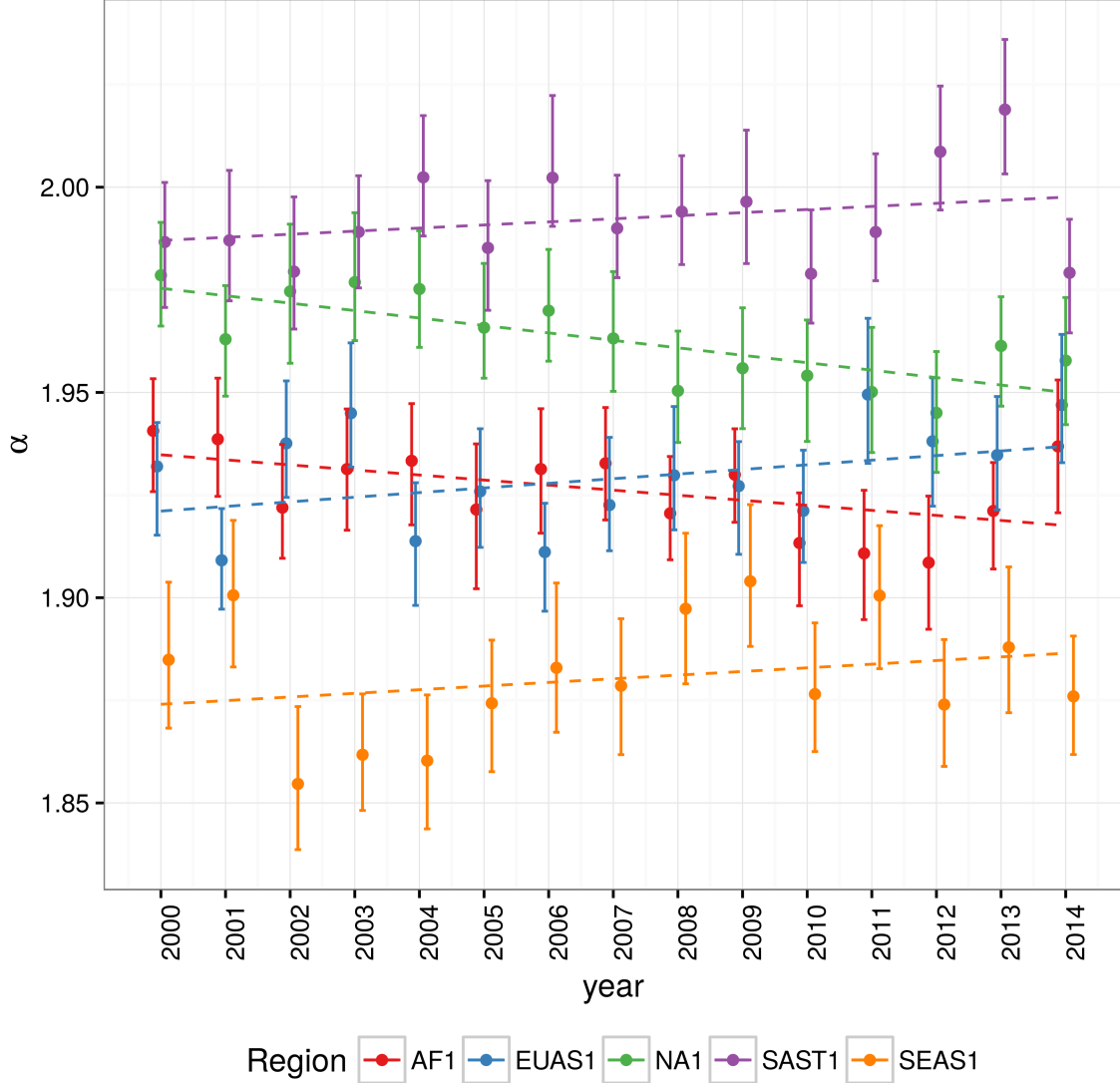


Figure 1: Power law exponents (α) of forest patch distributions for regions with total forest area $> 10^7$ km². Dashed horizontal lines are the fitted generalized least squares linear model, with 95% confidence interval error bars estimated by bootstrap resampling. The regions are AF1: Africa mainland, EUAS1: Eurasia mainland, NA1: North America mainland, SAST1: South America subtropical and tropical, SEAS1: Southeast Asia mainland. For EUAS1 the best model is log-normal but the exponents are included here for comparison.

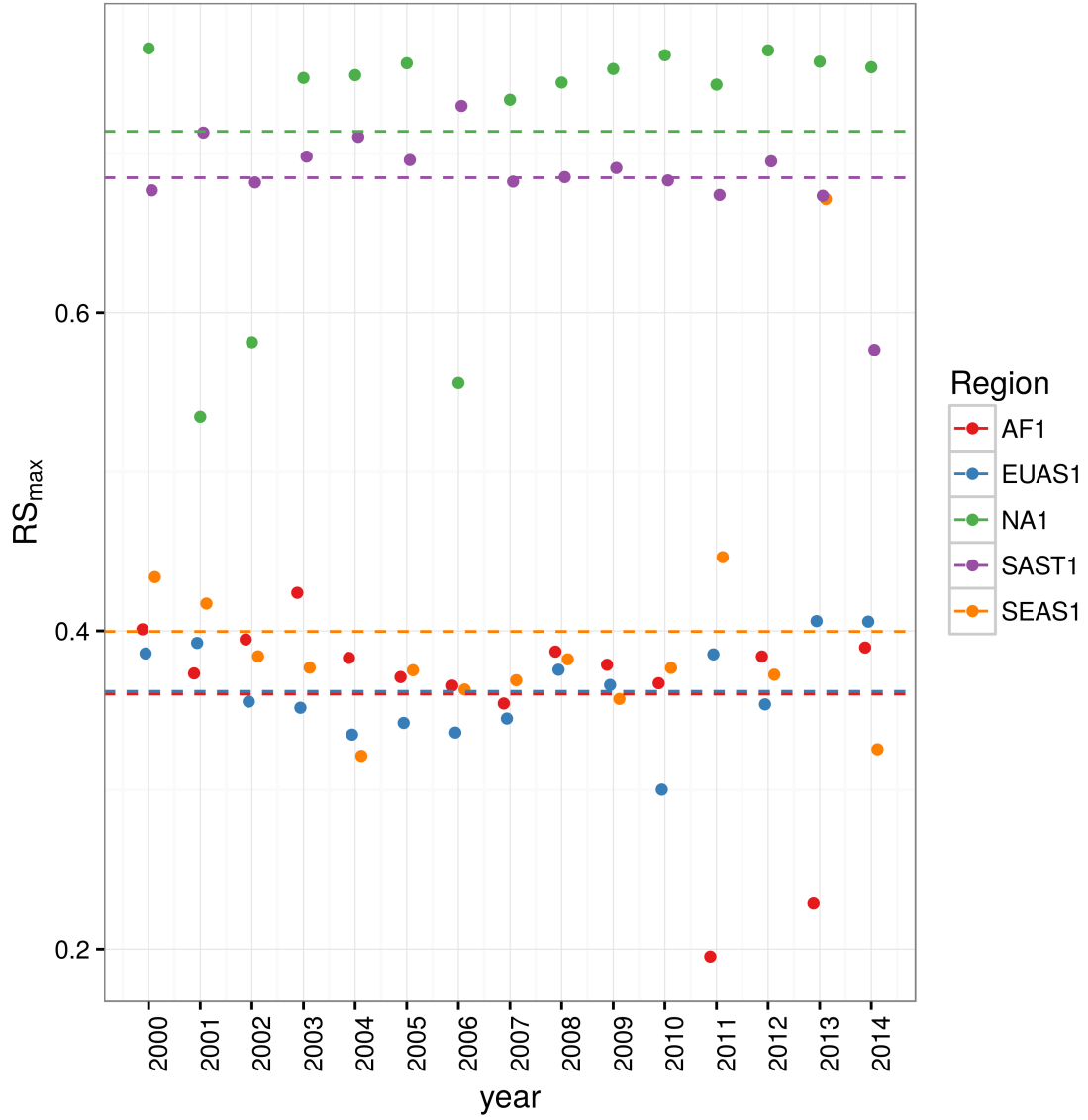


Figure 2: Largest patch proportion relative to total forest area RS_{max} , for regions with total forest area $> 10^7$ km². Dashed lines are averages across time. The regions are AF1: Africa mainland, EUAS1: Eurasia mainland, NA1: North America mainland, SAST1: South America tropical and subtropical, SEAS1: Southeast Asia mainland.

more than 40% such as AF2 (Madagascar), NA1 (North America), and OC3 (Malaysia). In the regions with RS_{max} between 40% and 30% the identity of the largest patch could change or stay the same in time. For OC7 (Java) the largest patch changes and for AF1 (Africa mainland) it stays the same. Only for EUAS1 (Eurasia mainland) we observed that the two largest patches are always the same, implying that this region is probably composed of two independent domains and should be divided in further studies. The regions with RS_{max} less than 25%: SAST2 (Cuba) and EUAS3 (United Kingdom), the largest patch always changes reflecting their fragmented state. In the case of SEAS2 (Philippines) a transition is observed, with the identity of the largest patch first variable, and then constant after 2010.

The results of quantile regressions are identical for ΔRS_{max} and ΔS_{max} (supplementary table S4). Among the biggest regions, Africa (AF1) has upper and lower quantiles with significantly negative slopes, but the lower quantile slope is lower, implying that negative fluctuations and variance are increasing (Figure 3). Eurasia mainland (EUAS1) has only the upper quantile significant with a positive slope, suggesting an increase in the variance. North America mainland (NA1) exhibits a significant lower quantile with positive slope, implying decreasing variance. Finally, for mainland Australia, all quantiles are significant, and the slope of the lower quantiles is greater than the upper ones, showing that variance is decreasing (Supplementary figure S10). These results are summarized in Table 1.

The conditions that indicate that a region is near a critical fragmentation threshold are that patch size distributions follow a power law; temporal ΔRS_{max} fluctuations follow a power law; variance of ΔRS_{max} is increasing in time; and skewness is negative. All these conditions were true only for Africa mainland (AF1) and South America tropical & subtropical (SAST1).

Table 1: Regions and indicators of closeness to a critical fragmentation threshold. Where, RS_{max} is the largest patch divided by the total forest area, ΔRS_{max} are the fluctuations of RS_{max} around the mean, skewness was calculated for RS_{max} and the increase or decrease in the variance was estimated using quantile regressions, NS means the results were non-significant.

Region			Average	Patch Size	ΔRS_{max}	Skewness	Variance
Description			RS_{max}	Distrib	Distrib.		
AF	1	Africa mainland	0.36	Power	Power	-1.8630	Increase
	2	Madagascar	0.65	Power	Power	-0.2478	NS
EUAS	1	Eurasia, mainland	0.36	LogNormal	Exp	0.4016	Increase

Region			Average	Patch Size	ΔRS_{max}	Skewness	Variance
		Description	RS_{max}	Distrib	Distrib.		
NA	2	Japan	0.94	Power	Power	0.0255	NS
	3	United Kingdom	0.07	Power	Power	2.1330	NS
	1	North America, mainland		0.71 Pow	er Power		-1.5690
							De-crease
	5	Newfoundland	0.87	Power	Power	-0.7411	NS
OC	1	Australia, Mainland	0.28	Power	Power	0.0685	Decrease
	2	New Guinea	0.97	Power	Exp	0.1321	Decrease
	3	Malaysia/Kalimantan	0.97	Power	Exp	-0.9633	NS
	4	Sumatra	0.92	Power	Power	1.3150	Increase
	5	Sulawesi	0.87	Power	Power	-0.3863	NS
	6	New Zealand South Island	0.76	Power	Exp	-0.6683	NS
	7	Java	0.38	Power	Exp	-0.1948	NS
	8	New Zealand North Island	0.75	Power	Exp	0.2940	NS
SAST	1	South America, Tropical and subtropical forest up to Mexico	0.68	Power	Power	-2.7760	Increase
	2	Cuba	0.21	Power	Power	0.2751	NS
SAT	1	South America, Temperate forest	0.60	Power	Power	-1.5070	Decrease

Region			Average	Patch Size	ΔRS_{max}	Skewness	Variance
Description			RS_{max}	Distrib	Distrib.		
SEAS	1	Southeast Asia, Mainland	0.40	Power	Power	3.0030	NS
	2	Philippines	0.54	Power	Power	0.3113	Increase

Discussion

We found that the forest patch distribution of most regions of the world followed power laws spanning seven orders of magnitude. These include tropical rainforest, boreal and temperate forest. Power laws have previously been found for several kinds of vegetation, but never at global scales as in this study. Interestingly, Eurasia does not follow a power law, but it is a geographically extended region, consisting of different domains (as we observed in the Supplementary Information animations). It is known that the union of two independent power law distributions produces a lognormal distribution (Rooij *et al.*, 2013). Future studies should split this region into two or more new regions, and test if the underlying distributions are power laws.

Several mechanisms have been proposed for the emergence of power laws in forest: the first is related self organized criticality (SOC), when the system is driven by its internal dynamics to a critical state; this has been suggested mainly for fire-driven forests (Zinck & Grimm, 2009; Hantson *et al.*, 2015). Real ecosystems do not seem to meet the requirements of SOC dynamics: their dynamics are influenced by external forces, and interactions are non-homogeneous (i.e. vary from place to place) (Sole *et al.*, 2002). Moreover, SOC requires a memory effect: fire scars in a site should accumulate and interfere with the propagation of a new fire. Pueyo *et al.* (2010) did not find such effect for tropical forests, and suggest that other mechanisms might produce the observed power laws. Other studies have also found that SOC models do not reproduce the patterns of observed fires (McKenzie & Kennedy, 2012). Thus a mechanism which resembles SOC, i.e. with a double separation of scales, does not seem a plausible explanation for the global forest dynamics.

The mechanism suggested by Pueyo *et al.* (2010) is isotropic percolation, when a system is near the critical point power law structures arise. This is equivalent to the random forest model that we explained previously, and requires the tuning of an external environmental condition to carry the system to this point. We did not expect forest growth to be a random process at local scales, but it is possible that combinations of factors cancel out to produce seemingly random forest dynamics at large scales. If this is the case the power law

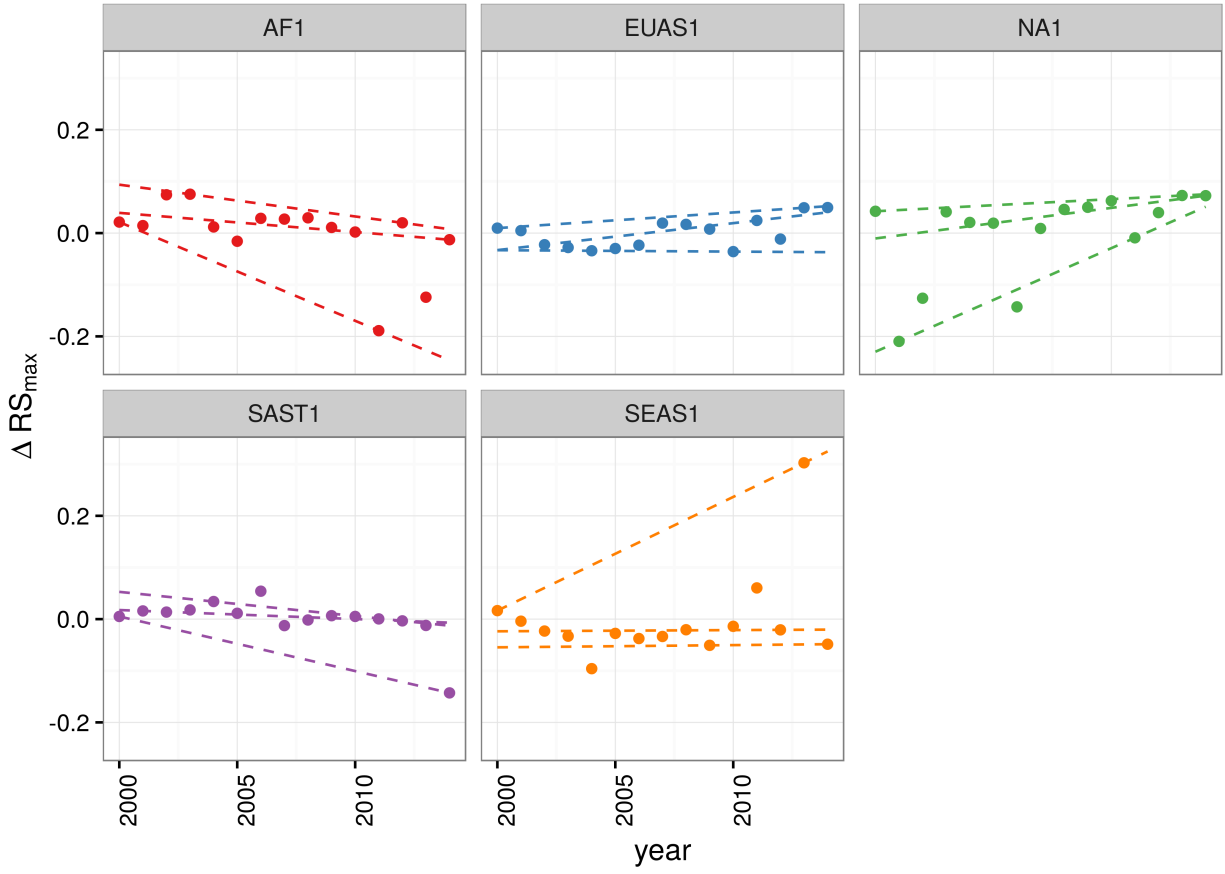


Figure 3: Largest patch fluctuations for regions with total forest area $> 10^7 \text{km}^2$. The patch sizes are relative to the total forest area of the same year. Dashed lines are 90%, 50% and 10% quantile regressions, to show if fluctuations were increasing. The regions are AF1: Africa mainland, EUAS1: Eurasia mainland, NA1: North America mainland, SAST1: South America tropical and subtropical, SEAS1: Southeast Asia mainland.

exponent should be theoretically near $\alpha = 2.055$, but this value is outside the confidence interval we observed, and thus other explanations are needed.

The third mechanism suggested as the cause of pervasive power laws in patch size distribution is facilitation (Manor & Shnerb, 2008; Irvine *et al.*, 2016): a patch surrounded by forest will have a smaller probability of been deforested or degraded than an isolated patch. We hypothesize that models that include facilitation could explain the patterns observed here. The model of Scanlon *et al.* (2007) represented the dynamics of savanna trees includes a global constraint (mean rainfall), a local facilitation mechanism, and two states (tree/non-tree), producing power laws across a rainfall gradient without the need for tuning an external parameter. The results for this model showed an $\alpha = 1.34$ which is also different from our results. Another model but with three states (tree/non-tree/degraded), including local facilitation and grazing, was also used to obtain power laws patch distributions without external tuning, and exhibited deviations from power laws at high grazing pressures (Kéfi *et al.*, 2007). The values of the power law exponent α obtained for this model are dependent on the intensity of facilitation, when facilitation is more intense the exponent is higher, but the maximal values they obtained are still lower than the ones we observed. The interesting point is that the value of the exponent is dependent on the parameters, and thus the observed α might be obtained with some parameter combination. Kéfi *et al.* (2007) proposed that a deviation in power law behavior with the form of an exponential decay or cut-off could be a signal of a critical transition. At the continental scales studied here, we did not observe exponential cut-offs, but did observe other signals of a transition. This confirms previous results (Weerman *et al.*, 2012; Kéfi *et al.*, 2014) showing that different mechanisms can produce seemingly different spatial patterns near the transition, and that early warnings based only on spatial patterns are not universal for all systems.

It has been suggested that a combination of spatial and temporal indicators could more reliably detect critical transitions (Kéfi *et al.*, 2014). In this study, we combined five criteria to detect the closeness to a fragmentation threshold. Two of them were spatial: the forest patch size distribution, and the proportion of the largest patch relative to total forest area (RS_{max}). The other three were the distribution of temporal fluctuations in the largest patch size, the trend in the variance, and the skewness of the fluctuations. Each one of these is not a strong individual predictor, but their combination gives us an increased degree of confidence about the system being close to a critical transition.

We found that only the tropical forest of Africa and South America met all five criteria, and thus seem to be near a critical fragmentation threshold. This means that the combined influence of human pressures and climate forcings might trigger all the undesired effects of fragmentation in these extended areas. A small but continuous increase in forest loss could produce a biodiversity collapse (Solé *et al.*, 2004). This threshold

effect has been observed in different kind of models, experimental microcosms (Starzomski & Srivastava, 2007), field studies (Pardini *et al.*, 2010; Martensen *et al.*, 2012) and food webs (Martinson *et al.*, 2012). Of these two areas, Africa seems to be more affected, because the proportion of the largest patch relative to total forest area (RS_{max}) is near 30%, which could indicate that the transition is already started. Moreover, this region was estimated to be potentially bistable, with the possibility to completely transform into a savanna (Staver *et al.*, 2011). The region of South America tropical forest has a RS_{max} of more than 60% suggesting that the fragmentation transition is approaching but not yet started. The island of Philippines (SEAS2) seems to be an example of a critical transition from an unconnected to a connected state, the early warning signals can be qualitatively observed: a big fluctuation in a negative direction precedes the transition and then RS_{max} stabilizes over 60%. This confirms that the early warning indicators proposed here work in the correct direction.

At low levels of habitat reduction, species population will decline proportionally; this can happen even when the habitat fragments retain connectivity. As habitat reduction continues, the critical threshold is approached and connectivity will have large fluctuations (Brook *et al.*, 2013). This could trigger several synergistic effects: populations fluctuations and the possibility of extinctions will rise, increasing patch isolation and decreasing connectivity (Brook *et al.*, 2013). This positive feedback mechanism will be enhanced when the fragmentation threshold is reached, resulting in the loss of most habitat specialist species at a landscape scale (Pardini *et al.*, 2010). Some authors argue that since species have heterogeneous responses to habitat loss and fragmentation, and biotic dispersal is limited, the importance of thresholds is restricted to local scales or even that its existence is questionable (Brook *et al.*, 2013). Fragmentation is by definition a local process that at some point produces emergent phenomena over the entire landscape, even if the area considered is infinite (Oborny *et al.*, 2005). In addition, after a region's fragmentation threshold connectivity decreases, there is still a large and internally well connected patch that can maintain sensitive species (Martensen *et al.*, 2012). What is the time needed for these large patches to become fragmented, and pose a real danger of extinction to a myriad of sensitive species? If a forest is already in a fragmented state, a second critical transition from forest to non-forest could happen, this was called the desertification transition (Corrado *et al.*, 2014). Considering the actual trends of habitat loss, and studying the dynamics of non-forest patches—instead of the forest patches as we did here—the risk of this kind of transition could be estimated. To improve the estimation of non-forest patches other data set as the MODIS cropland probability should be incorporated (Sexton *et al.*, 2015). The simple models proposed previously could also be used to estimate if these thresholds are likely to be continuous and reversible or discontinuous and irreversible, and the degree of protection (e.g. using the set-asides strategy Banks-Leite *et al.* (2014)) than would be necessary to stop

1 this trend.

2 The effectiveness of landscape management is related to the degree of fragmentation, and the criteria to
3 direct reforestation efforts could be focused on regions near a transition (Oborny *et al.*, 2007). Regions that
4 are in an unconnected state require large efforts to recover a connected state, but regions that are near a
5 transition could be easily pushed to a connected state; feedbacks due to facilitation mechanisms might help
6 to maintain this state. If the largest patch is always the same patch over time, the forest is probably not
7 fragmented. This patch could represent a core area for conservation, because it maintains the connectivity
8 of the whole region.

9 Crossing the fragmentation critical point in forests could have negative effects on biodiversity and ecosystem
10 services (Haddad *et al.*, 2015), but it could also produce feedback loops at different levels of the biological
11 hierarchy. This means that a critical transition produced at a continental scale could have effects at the level
12 of communities, food webs, populations, phenotypes and genotypes (Barnosky *et al.*, 2012). All these effects
13 interact with climate change, thus there is a potential production of cascading effects that could lead to a
14 global collapse. Therefore, even if critical thresholds are reached only in some forest regions at a continental
15 scale, a cascading effect with global consequences could still be produced, and may contribute to reach a
16 planetary tipping point (Reyer *et al.*, 2015). The risk of such event will be higher if the dynamics of separate
17 continental regions are coupled (Lenton & Williams, 2013). Using the time series obtained in this work the
18 coupling of the continental could be further investigated. It has been proposed that to assess the probability
19 of a global scale shift, different small scale ecosystems should be studied in parallel (Barnosky *et al.*, 2012).
20 As forest comprises a major proportion of such ecosystems, we think that the transition of forests could be
21 used as a proxy for all the underling changes and as a successful predictor of a planetary tipping point.

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