

Analysis of critical transitions at the Global Forest

Abstract

One of the most important changes produced in the biosphere is the replacement of forest areas with human dominated landscapes. These areas contain much less species than the natural ecosystem they replaced, and are one of the main drivers of extinctions in the anthropocene. The forest cover is also coupled to atmospheric dynamics and the balance of gases in the atmosphere. The dynamics of forest fragments or patches is central to its function as ecosystem. In different kinds of vegetation including forests the patch size distributions follow power laws or approximate power law, but all these patterns have been observed at relatively small scales. Here we studied the distribution of forest patch sizes at a global level and its changes in the last fourteen years. We hypothesize that the global forest patches should follow a power law distribution. Power laws are a signal of critical phase transitions, where the system changes suddenly of state at a critical point, in the case of forest patches this change implies an abrupt change in the connectivity that poses a risk on the functioning of forest as an habitat and as an ecosystem. Thus we estimate the closeness of forest at the continental level to a possible critical transition as an early warning indicator.

Introduction

Forest is one of the most important ecosystems on earth providing habitat for a large proportion of species and contributing extensively to global biodiversity [1]. In the previous century human activities have reached the global scale changing influencing the bio-geochemical cycles [2]. One of the most dramatic human induced changes is the replacement of 40% of Earth's formerly biodiverse land areas with landscapes that contain only a few species of crop plants, domestic animals and humans [3]. These changes have been happening locally but they have been accumulated over time and have reached a global scale that constitutes a global forcing [4]. That means a force that can induce changes at the level of the whole biosphere. Another global scale forcing that is tied to habitat destruction is fragmentation. Fragmentation is defined as the division of a continuous habitat into separated portions that are smaller and more isolated, this produces multiple interwoven effects: reductions of biodiversity between 13% and 75%, decreasing forest biomass and changes in nutrient cycling [5].

Complex interaction between species and feedbacks at different levels of organization [6] can produce abrupt changes called critical transitions [7]. These abrupt state shifts can not be linearly forecasted from past changes so they are difficult to predict and manage [7]. Critical transitions had been detected mostly at local

scales [8,9], but the accumulation of changes in local communities that overlap geographically can propagate and cause an abrupt change of the entire system [4], this is coupled with the existence of global scale forcings implies the possibility that a critical transition occurs at a global scale [10,11].

There are two general classes of critical transitions: one where the sudden shift between states is mostly irreversible showing the presence of two stable states. These show hysteresis that is a catastrophic regime shift [12], also called first order transitions. This could be the result of a positive feedback mechanisms [13], for example the growth of forest in a site is more probable if it is surrounded by forest than if it is surrounded by cultivated or degraded land [14]. This is observed in semiarid regions where the transition from a vegetated state to a desertic one occurs as a result of human pressures and climatic change [15], in biological invasions [16], and biology and social sciences in general [17].

The second are continuous critical transitions [18], or second order transitions. In this case there is a narrow region where the system changes from one domain to another, besides the change is also sudden it is continuous and theoretically reversible. These transitions are linked to spatial structures: at the critical point we can observe scale invariant fractal structures characterized by power law patch distributions [19].

The spatial phenomena studied by percolation theory is related to the concept of connection, in a very general way we can find a path between the objects that belongs to a system [17], thus connectivity is a fundamental property of general systems and also, ecosystems from forests [20] to marine ecosystems [21] and the whole biosphere [22]. Percolation is characterized by two domains or phases. One dominated by short range interactions where information can not spread and another where long range interactions are possible and information can spread over the whole area. In this context information is taken in a broad sense and can represent species dispersal or movement. Thus, there is a critical point that defines a threshold boundary between the two domains and the system could be driven close or far of the critical point by an external force. Climate change and deforestation are the main forces that could be the drivers of a phase change in forests [5,23].

Percolation thresholds are important to understand forest growth dynamics: when the system is above the critical point is in a connected state and the dispersal of species inside the forest is enhanced. Dispersal strategies are influenced by percolation thresholds in three-dimensional forest structure [24]. Recently has been show that not only the patches but species distributions also have percolation thresholds [25]. If we push the system below the percolation threshold the system will be in an unconnected state, which could produce a biodiversity collapse [26,27]. In an opposite direction being in a connected state could produce the acceleration of an invasion of forest into a prairie [28,29].

One of the problems with critical transitions is that the value of the critical threshold is not known in advance, and near that point a small change can precipitate a state shift of the system, thus they are very difficult to anticipate. Several methods were developed to detect the closeness of the critical point such as a deceleration in recovery from perturbations, an increase in variance in the spatial or temporal pattern. Besides some of these methods have been experimentally tested [8,30], still there is a debate about the its reliability [31,32]. In most real systems where spatial dynamics is important we could observe processes like: demographic fluctuations, spatial heterogeneities and/or dispersal limitation. This processes that introduce stochasticity can convert a catastrophic transition to a second order transitions [13]. Forest is a system where we these three processes are ubiquitous so continuous transitions should be more probable than catastrophic transitions, moreover some evidence of a second order critical transition related to drought and fire has been found in tropical forest [33]

Our objective is to evaluate the forest patch distribution at a continental scale, using the framework of percolation theory, to detect possible signals of a critical transitions related to connectivity. The advantage of using data at a continental scale is that for very large systems the transitions are very sharp thus much easier to detect than at smaller scales, where noise can mask the signals of the transition.

Methods

Percolation theory

A more indeep introduction of percolation theory can be found elsewhere [19] and a review from an ecological point of view is available [34]. Here to explain the basic elements of percolation theory we formulate a simple model: we represent our area of interest by a square lattice and each site of the lattice can be occupied—e.g. by forest—with a probability p . The lattice will be more occupied when p is greater, but the sites are randomly distributed. We are interested in the connection between sites so we have to establish a neighborhood, for this example we define the eight sites surrounding the focal site as neighbors. The sites that are neighbors define a patch. When there is a patch that connects the lattice from side to side it is said that the system percolates. The percolating patch suddenly appears at some value of p called the critical point p_c .

Thus percolation is characterized by two well defined phases: the unconnected phase (called subcritical in physics) when $p < p_c$, a individual of a species cannot travel far away inside the forest, the forest is fragmented, or in a general sense information cannot spread. The second is the connected phase (supercritical) when $p > p_c$, species can move inside a forest patch from side to side of the area, information can spread over the whole area. Near the critical point several scaling laws arise: the structure of the patch that spans the area is

fractal, the size distribution of the patches is power-law, and other quantities also follow power-law scaling [19].

The value of the critical point p_c depends on the geometry of the lattice and on the definition of the neighborhood, but other power-law exponents only depend on the lattice dimension. Close to criticality is found that the distribution of patch sizes is:

$$(1) \quad n_s(p_c) \propto s^{-\tau}$$

where $n_s(p)$ is the number of patches of size s . The exponent τ does not depend on the details of the model and it is called universal [19]. All percolation theory was developed for infinite lattices thus at the critical point ξ becomes infinite, in finite systems ξ is in the order of the size of the lattice. These and other universal scaling laws can be applied for landscape structures that are approximately random, called in physics isotropic percolation universality class. These scaling laws are valid if the forest sites are correlated over short distances [35]. And they also can be applied if the patches are dynamically generated by models that have some kind of memory like that degraded forest patches recover differently than sites that never had forest [36,37].

Area definition

We choose mainland zones at a continental scale to analyze based in the possibility of connection, close patches of continuous forest must connect the region, big islands like Madagascar were included as a separate regions, smaller islands were not included, we considered big islands connected to the mainland when they are at 1 km or less distance away. With this criteria we defined three regions in America, one corresponding to South America temperate forest (SAT), another to subtropical and tropical forest up to Mexico (SAST), and the last covering USA and Canada forest (NA). Europe and north Asia were all connected and they are included in one region (EUAS), the other regions are south Asia (SEAS), Africa (AF), and Australia and islands (OC) (Supplementary figure S1-S6).

To define patches we use the MODerate-resolution Imaging Spectroradiometer (MODIS) Vegetation Continuous Fields (VCF) Tree Cover dataset. This dataset is produced at 250-meters resolution, globally from 2000 to 2014, we used the version 051 [38]. There are several definition of forest [39], but we choose a 30% threshold to convert the percentage tree cover to a binary image of forest and non-forest pixels. This was the definition used by the United Nations' International Geosphere-Biosphere Programme [40], and studies of global fragmentation [5]. Patches of contiguous forest were determined in the binary image by grouping connected pixels using a neighborhood of 8 forest units (Moore neighborhood). We set a minimal patch size (X_{min}) at nine pixels to avoid artifacts at patch edges due to discretization.

1 Patch size distributions

2 From the point of view of percolation theory, the necessary condition we need to be near a critical transition
3 is that the patch size distribution follows a power-law. But this is not a sufficient condition because power-law
4 distributions are present in a wide range of conditions in vegetation of arid ecosystems [41,42] and ant colonies
5 [43] and attached microalgae [44,45]. The origin of these power-laws is attributed to a facilitation mechanisms
6 [46,47], that is likely to be present in forest [48].

7 We fitted the empirical distribution of forest patch areas to four distributions using maximum likelihood
8 estimation [49,50]. The distributions were: power-law, power-law with exponential cut-off, log-normal, and
9 exponential distributions. We assume that the patch size distribution is a continuous variable that was
10 discretized by remote sensing data acquisition procedure.

11 Besides the hard X_{min} limit we set due to discretization, the power-law distribution needs a lower bound for its
12 scaling behaviour. This lower bound is also estimated from the data by maximizing the Kolmogorov-Smirnov
13 (KS) statistic comparing empirical to fitted cumulative distribution function [50]. We also calculate the
14 uncertainty of the parameters using a non-parametric bootstrap method [51].

15 The corrected Akaike Information Criteria (AIC_c) and the Akaike weights were computed for each model
16 [52]. Akaike weights (w_i) are the weight of evidence in favor of model i being the actual best model for the
17 situation at hand given that one of the N models must be the best model for that set of N models.

18 Additionally, we computed the goodness of fit of the power-law model following the bootstrap approach
19 described by Clauset et. al [50], where simulated data sets following the fitted model are generated, and a
20 p-value equal to the proportion of simulated data sets that has a KS statistic less extreme than empirical
21 data. The criterion to reject the power law model was $p \leq 0.1$ but as we have a very large n negligible small
22 deviations could produce a rejection [53], thus we chose a $p \leq 0.05$ to reject the power law model.

23 To test for differences between the fitted power law exponent for regions and subregions we used a weighted
24 linear regression with a residual auto-correlation structure. For this we use a generalized least squares
25 procedures: function `gls` from package `nlme` [54]. The weights were the bootstrapped 95% confidence intervals
26 and we added an auto-regressive model of order 1 to the residuals to account for temporal autocorrelation.

27 Image processing were done in MATLAB. All statistical analyses were done using the GNU R [55], using
28 code provided by Cosma R. Shalizi for power law with exponential cutoff model and the `powerlaw` package
29 [56] for fitting the other distributions.

1 Largest patch dynamics

2 The largest patch is the one that connects the highest number of sites in the area, it has been used extensively
3 to indicate fragmentation [20,57]. The relation of the size of the largest patch S_{max} with critical transitions
4 has been extensively studied in relation to percolation phenomena [19], but seldom used in ecological studies
5 (but see [35]). When we are in a connected state ($p > p_c$) the landscape is almost insensitive to removal of
6 a small fraction of forest, but close to the critical point the removal of small areas can have an important
7 effects [18,34]. At this point the largest patch will have a filamentary structure, extended forest areas will be
8 connected by thin threads, thus small losses could produce big fluctuations.

9 (Figure Showing filamentary structure of patches)

10 Thus one way to evaluate the fragmentation of the forest is to calculate the proportion of the largest patch
11 against the total area, as is very difficult to evaluate the total area that the forest could potentially occupy
12 we use the total forest area. Thus we calculate the proportion of the largest patch, dividing S_{max} by the
13 total forest area for this year: $RS_{max} = S_{max} / \sum_i S_i$. When the proportion RS_{max} is big (more than 60%)
14 the largest patch structure is more compact and the critical fragmentation threshold is probably far away.
15 When this proportion is low, 20% or less we are probably in fragmented state.

16 We calculate the fluctuations around the mean with the absolute values $\Delta S_{max} = S_{max}(t) - \langle S_{max} \rangle$, and
17 also using the proportions of RS_{max} . To characterize the fluctuations we fitted three empirical distributions:
18 power-law, log-normal, and exponential; using the same methods described previously. We expect that large
19 fluctuation near a critical point have heavy tails (log-normal or power-law) and that fluctuations far from
20 a critical point have exponential tails, corresponds to Gaussian processes. As the data set spans 15 years
21 we have do not have enough power to reliably detect which distribution is better [50]. To improve this we
22 performed the goodness of fit test described above for all the distributions.

23 A robust way to detect if the system is near a critical transition is to analyze the increase of variance of
24 the forest's density [58], the problem is that the variance increase appears when we are very close to the
25 transition [59]. An alternative is to analyze the variance of the fluctuations of the largest patch ΔS_{max} , a
26 maximum is attained at the critical point but a significant increase occurs well before the system reach the
27 threshold [59]. Also before the critical fragmentation the skewness of the distribution of ΔS_{max} should be
28 negative. We characterized the increase in the variance using quantile regression: if variance is increasing the
29 slopes of upper or/and lower quartiles should be positive or negative.

Results

The power law distribution was selected as the best model in most of the cases (Supplementary Figure S7). In a small number of cases (4 of 300) the power law with exponential cutoff was selected but the value of the parameter α was similar by ± 0.02 to the pure power law so we use the power law parameters (See Supplementary data, region EUAS3). In finite-size systems the power law with exponential cutoff should be the favored model because the power-law is truncated to the size of the system [19], but here the size of the regions is so large that the cutoff are practically not observed .

There is only one region that does not follow a power law: Eurasia mainland, and it follows a log-normal distribution. The log-normal and power law are both heavy tailed distributions, so they are difficult to distinguish, in our case there are no doubts: Akaike weights have values near 1, this means that this is the only possible model. Additionally the goodness of fit tests clearly rejected the power law model in all cases (Supplementary table S1). In general the power law model was rejected by the goodness of fit test in less than 10% of cases. In large forest areas like Africa mainland (AF1) or South America tropical-subtropical (SAST1), larger deviations are expected and the rejections rates are higher so the proportion is 30% or less (Supplementary Table S1).

Taking into account the bootstrapped confidence intervals of each power law exponent (α) and the temporal autocorrelation, there is no significant differences between α for the regions with biggest forest areas—greater than 10^7 km² (Figure 1 and Supplementary figure S8). And also there is no differences between these regions and the ones with forest areas smaller than 10^7 km² (Supplementary Table S2 & S3). Thus we can talk about global average $\alpha = 1.908$ with a bootstrapped 95% confidence interval between 1.898 and 1.920.

We made all the analysis of the fluctuations of the largest patch relative to total forest area ΔRS_{max} and absolute fluctuations ΔS_{max} . The model selection for ΔS_{max} results in power laws distributions for all regions (Supplementary table S6). The goodness of fit test (GOF) did not reject power laws in any case, but either can not reject the other models except in a few cases, this is due to the small number of observation we have for this analysis. Analyzing the relative fluctuations there are some differences: Eurasia mainland (EUAS1), New Guinea (OC2), Malaysia (OC3), New Zealand (OC6, OC8) and Java (OC7) all follow an exponential distribution (Supplementary Table S7). We only considered that fluctuations follows a power law when this distribution is selected for both absolute and relative fluctuations.

The patch size distribution for Eurasia is log-normal and has smaller fluctuations than the other regions (Figure 2). Exponential fluctuations are compatible with a combination of independent Poisson or Gaussian processes [60]. The other regions with exponential fluctuations have all a power law patch size distribution.

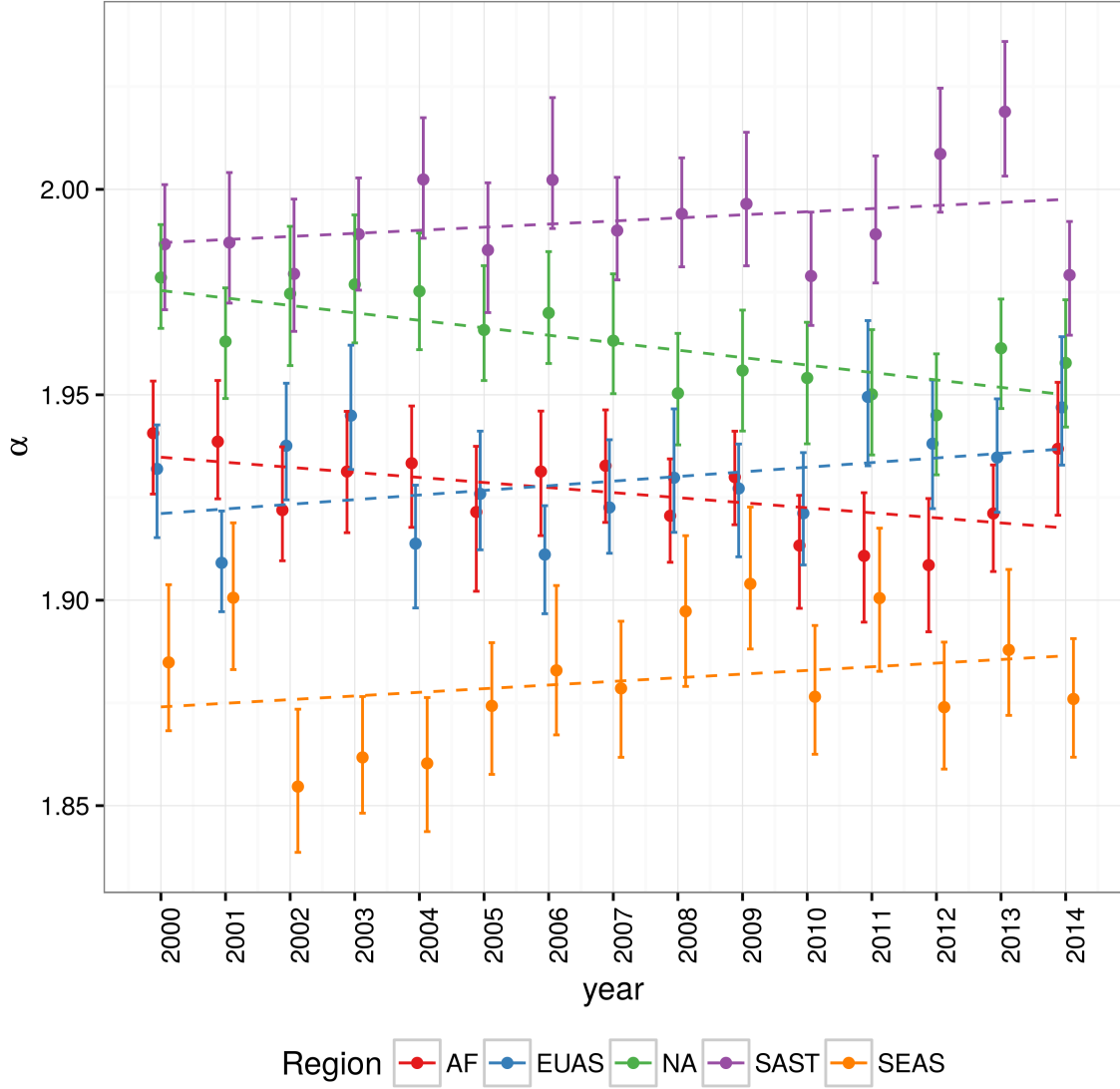


Figure 1: Power law exponents for forest patch distributions for regions with total forest area greater than 10^7 km². Dashed horizontal lines are the fitted generalized least squares linear model, error bars are 95% confidence intervals estimated by bootstrap resampling. The regions are AF: Africa, EUAS: Eurasia, NA: North America, SAST: South America Subtropical and tropical, SEAS: Southeast Asia. For EUAS the best model is log-normal but the exponents are included here for comparison.

- 1 In these could be hypothesized that they are far from the fragmentation threshold thus the largest patch
- 2 have a more compact structure and small losses do not affect its size so much.

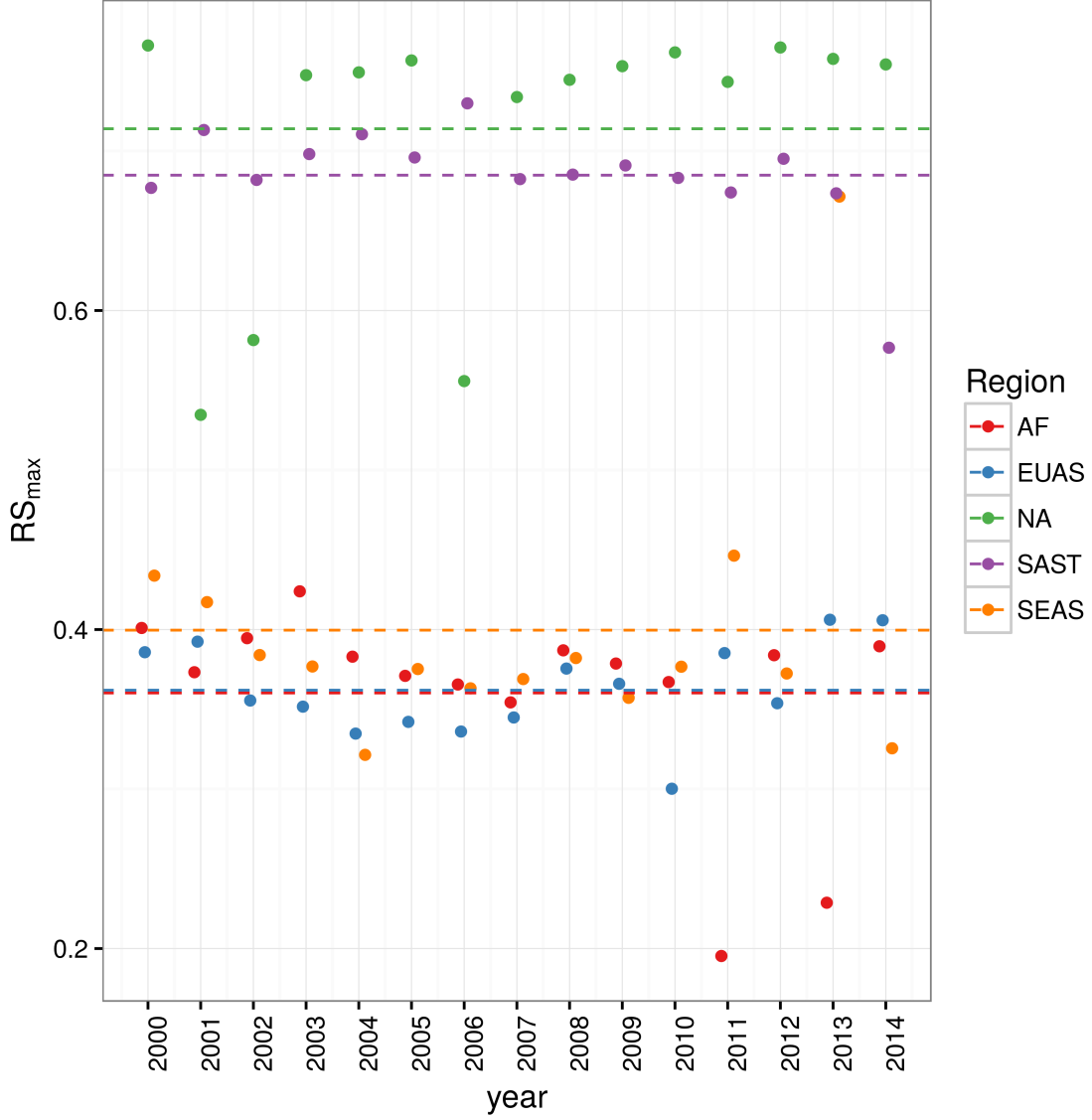


Figure 2: Largest patch proportion relative to total forest area for regions with total forest area greater than 10^7 km². The critical point for a random forest is 0.407, The regions are AF: Africa, EUAS: Eurasia, NA: North America, SAST: South America Subtropical and tropical, SEAS: Southeast Asia.

- 3 The results of quantile regressions are very similar for ΔRS_{max} fluctuations and ΔS_{max} (supplementary table
- 4 S4). In the biggest regions Africa (AF1) have the upper and lower quantiles significant with negative slopes,
- 5 but the lower quantile slope is lower so we conclude that negative fluctuations are increasing and this will
- 6 also increase variance (Figure 2). Eurasia

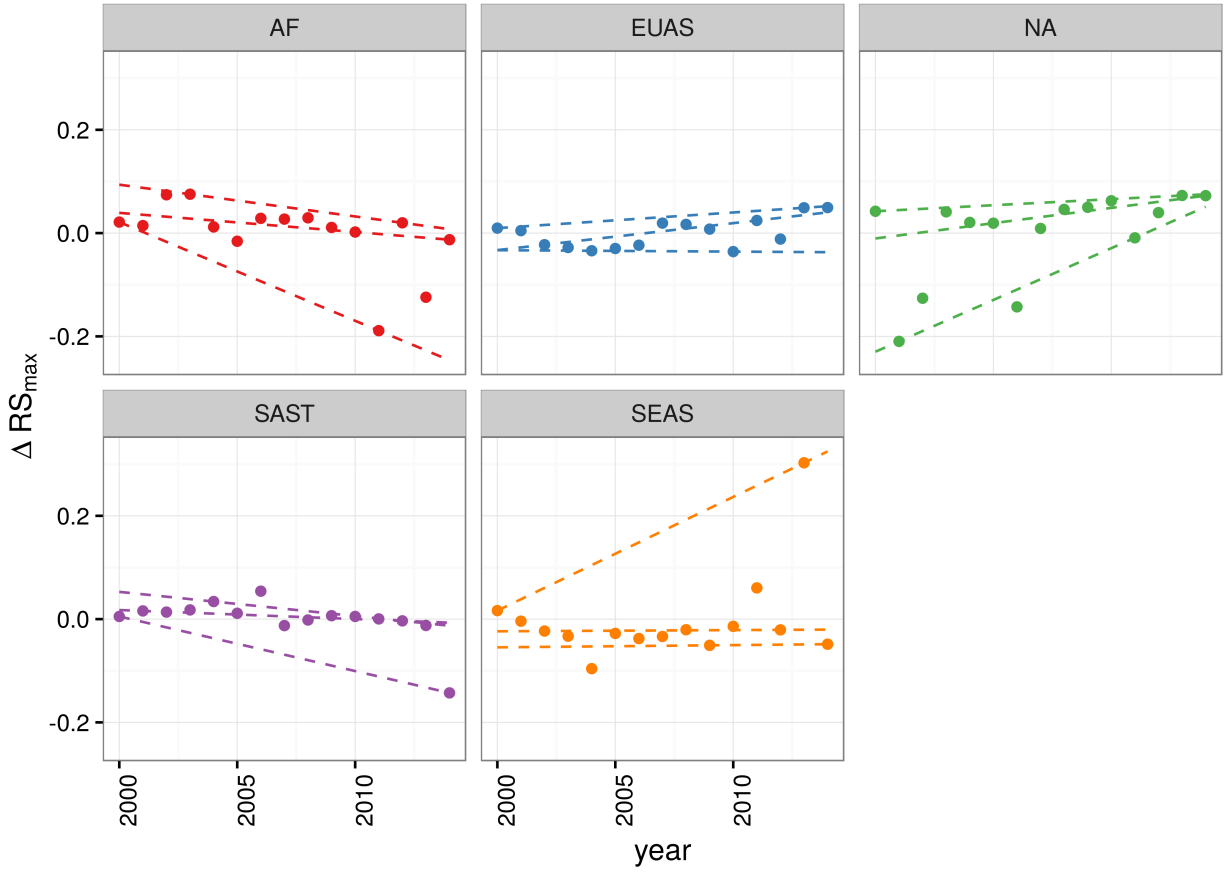


Figure 3: Largest patch fluctuations for regions with total forest area greater than 10^7km^2 . The patch sizes are relativized to the total forest area for that year. Dashed lines are 90%, 50% and 10% quantile regressions, to show if fluctuations were increasing. The regions are AF: Africa, EUAS: Eurasia, NA: North America, SAST: South America Subtropical and tropical, SEAS: Southeast Asia.

Table 1: Regions and subregions and indicators of closeness to a critical fragmentation threshold. Where, RS_{max} is the largest patch divided by the total forest area, ΔRS_{max} are the fluctuations of RS_{max} around the mean, Skewnees was calculated for RS_{max} and the increase or decrease in the variance was estimated using quantil regressions.

| Region | | | Average | Patch Size | ΔRS_{max} | Skewness | Variance |
|--------|-----|--------------------------|------------|------------|-------------------|----------|----------|
| | Sub | Description | RS_{max} | Distrib | Distrib. | | |
| AF | 1 | Africa mainland | 0.36 | Power | Power | -1.8630 | Incr. |
| | 2 | Madagascar | 0.65 | Power | Power | -0.2478 | No |
| EUAS | 1 | Eurasia, Mainland | 0.36 | LogNormal | Exp | 0.4016 | Incr. |
| | 2 | Japan | 0.94 | Power | Power | 0.0255 | No |
| | 3 | United Kingdom | 0.07 | Power | Power | 2.1330 | No |
| NA | 1 | North America | 0.71 | Power | Power | -1.5690 | Decr. |
| | 5 | Newfoundland | 0.87 | Power | Power | -0.7411 | No |
| OC | 1 | Australia, Mainland | 0.28 | Power | Power | 0.0685 | Incr. |
| | 2 | New Guinea | 0.97 | Power | Exp | 0.1321 | Decr. |
| | 3 | Malaysia/Kalimantan | 0.97 | Power | Exp | -0.9633 | No |
| | 4 | Sumatra | 0.92 | Power | Power | 1.3150 | Incr. |
| | 5 | Celebes | 0.87 | Power | Power | -0.3863 | No |
| | 6 | New Zealand south island | 0.76 | Power | Exp | -0.6683 | No |
| | 7 | Java | 0.38 | Power | Exp | -0.1948 | No |
| | 8 | New Zealand north island | 0.75 | Power | Exp | 0.2940 | No |

| Region | | | Average | Patch Size | ΔRS_{max} | Skewness | Variance |
|--------|-----|---|------------|------------|-------------------|----------|----------|
| | Sub | Description | RS_{max} | Distrib | Distrib. | | |
| SAST | 1 | South America, Tropical and subtropical forest up to Mexico | 0.68 | Power | Power | -2.7760 | Incr. |
| | 2 | Cuba | 0.21 | Power | Power | 0.2751 | No |
| SAT | 1 | South America, Temperate forest. | 0.60 | Power | Power | -1.5070 | Decr. |
| SEAS | 1 | Southeast Asia, Mainland | 0.40 | Power | Power | 3.0030 | No |
| | 2 | Philippines | 0.54 | Power | Power | 0.3113 | Incr. |

Discussion

We found that the tropical forest of Africa and the southeast Asia are near a critical fragmentation threshold, this means that the combined influence of human pressures and climate forcings can trigger all the undesired effects of fragmentation in these extended areas. An small but continuous increase in forest loss could produce a biodiversity collapse [27]. When habitat is reduced species population will decline proportionally [61]. This happens while the habitat fragments retain connectivity but as habitat reduction continues, the critical threshold is approached and as happens with the largest patch, connectivity will have large fluctuations. This could trigger several effects that act synergically: will enhance populations fluctuations and the possibility of extinctions will raise, this in turn will increase patch isolation that decrease connectivity [61]. This positive feedback mechanism will be enhanced when the fragmentation threshold is reached with the result of the loss of most habitat specialist species at a landscape scale [62]. Some authors argue that as species have heterogeneous responses to habitat loss and fragmentation and that as biotic dispersal is limited, the importance of thresholds is limited to local scales or even its existence is defied [61]. Fragmentation is by definition a local process that at some point produces an emergent phenomena that spreads over the entire landscape and this could happen even if the area considered is infinite [63]. Thus limited dispersal is no a barrier to a fragmentation threshold that extends its influence to the continental areas considered in this study. To know if these thresholds will sum up and produce a cascading effect to reach a planetary tipping point [4], we should extend the effects of these changes to know how it will feedback on global land-atmosphere that affect climate change.

1 Why exponential cut-off are not observed?

2 End discussing why fragmentation thresholds matters for the application of management efforts.

3 **References**

4 1. Crowther TW, Glick HB, Covey KR, Bettigole C, Maynard DS, et al. (2015) Mapping tree density at
5 a global scale. *Nature* 525: 201–205. Available: [http://www.nature.com/nature/journal/v525/n7568/full/](http://www.nature.com/nature/journal/v525/n7568/full/nature14967.html)
6 [nature14967.html](http://www.nature.com/nature/journal/v525/n7568/full/nature14967.html).

7 2. Canfield DE, Glazer AN, Falkowski PG (2010) The Evolution and Future of Earth’s Nitrogen Cycle.
8 *Science* 330: 192–196. Available: <http://www.sciencemag.org/cgi/doi/10.1126/science.1186120>.

9 3. Foley JA, Ramankutty N, Brauman KA, Cassidy ES, Gerber JS, et al. (2011) Solutions for a cultivated
10 planet. *Nature* 478: 337–342. Available: <http://www.nature.com/doi/10.1038/nature10452>.

11 4. Barnosky AD, Hadly EA, Bascompte J, Berlow EL, Brown JH, et al. (2012) Approaching a state shift in
12 Earth’s biosphere. *Nature* 486: 52–58. Available: <http://www.nature.com/nature/journal/v486/n7401/full/nature11018.html>
13 <http://dx.doi.org/10.1038/nature11018>.

14 5. Haddad NM, Brudvig LA, Clobert J, Davies KF, Gonzalez A, et al. (2015) Habitat fragmentation and its
15 lasting impact on Earth’s ecosystems. *Science Advances* 1: e1500052. Available: [http://advances.sciencemag.](http://advances.sciencemag.org/cgi/doi/10.1126/sciadv.1500052)
16 [org/cgi/doi/10.1126/sciadv.1500052](http://advances.sciencemag.org/cgi/doi/10.1126/sciadv.1500052).

17 6. Gilman SE, Urban MC, Tewksbury J, Gilchrist GW, Holt RD (2010) A framework for community
18 interactions under climate change. *Trends in Ecology & Evolution* 25: 325–331. Available: [http://www.](http://www.sciencedirect.com/science/article/pii/S0169534710000613)
19 [sciencedirect.com/science/article/pii/S0169534710000613](http://www.sciencedirect.com/science/article/pii/S0169534710000613).

20 7. Scheffer M, Bascompte J, Brock WA, Brovkin V, Carpenter SR, et al. (2009) Early-warning signals for
21 critical transitions. *Nature* 461: 53–59. Available: <http://dx.doi.org/10.1038/nature08227>.

22 8. Carpenter SR, Cole JJ, Pace ML, Batt R, Brock WA, et al. (2011) Early Warnings of Regime Shifts: A
23 Whole-Ecosystem Experiment. *Science* 332: 1079–1082. Available: [http://www.sciencemag.org/content/332/](http://www.sciencemag.org/content/332/6033/1079.abstract)
24 [6033/1079.abstract](http://www.sciencemag.org/content/332/6033/1079.abstract).

25 9. Drake JM, Griffen BD (2010) Early warning signals of extinction in deteriorating environments. *Nature* 467:
26 456–459. Available: <http://dx.doi.org/10.1038/nature09389> [http://www.nature.com/nature/journal/v467/n7314/abs/nature09](http://www.nature.com/nature/journal/v467/n7314/abs/nature09389)
27 [information](http://www.nature.com/nature/journal/v467/n7314/abs/nature09389).

28 10. Rockstrom J, Steffen W, Noone K, Persson A, Chapin FS, et al. (2009) A safe operating space for

- 1 humanity. *Nature* 461: 472–475. Available: <http://dx.doi.org/10.1038/461472a>.
- 2 11. Folke C, Jansson Å, Rockström J, Olsson P, Carpenter SR, et al. (2011) Reconnecting to the Biosphere.
- 3 *AMBIO* 40: 719–738. Available: <http://link.springer.com/article/10.1007/s13280-011-0184-y>.
- 4 12. Scheffer M, Walkerk B, Carpenter S, Foley J a, Folke C, et al. (2001) Catastrophic shifts in ecosystems.
- 5 *Nature* 413: 591–596. doi:10.1038/35098000.
- 6 13. Martín PV, Bonachela JA, Levin SA, Muñoz MA (2015) Eluding catastrophic shifts. *Proceedings of the*
- 7 *National Academy of Sciences* 112: E1828–E1836. Available: [http://www.pnas.org/content/early/2015/03/](http://www.pnas.org/content/early/2015/03/27/1414708112)
- 8 [27/1414708112](http://www.pnas.org/content/early/2015/03/27/1414708112).
- 9 14. Xu C, Van Nes EH, Holmgren M, Kéfi S, Scheffer M (2015) Local Facilitation May Cause Tipping Points
- 10 on a Landscape Level Preceded by Early-Warning Indicators. *The American Naturalist* 186: E000–E000.
- 11 Available: <http://www.jstor.org/stable/info/10.1086/682674>.
- 12 15. Kéfi S, Rietkerk M, Baalen M van, Loreau M (2007) Local facilitation, bistability and transitions in arid
- 13 ecosystems. *Theoretical Population Biology* 71: 367–379. Available: [http://www.sciencedirect.com/science/](http://www.sciencedirect.com/science/article/pii/S0040580906001250)
- 14 [article/pii/S0040580906001250](http://www.sciencedirect.com/science/article/pii/S0040580906001250).
- 15 16. Taylor CM, Hastings A (2005) Allee effects in biological invasions. *Ecology Letters* 8: 895–908. Available:
- 16 <http://dx.doi.org/10.1111/j.1461-0248.2005.00787.x>.
- 17 17. Solé RV (2011) *Phase Transitions*. Princeton University Press. Available: [https://books.google.com.ar/](https://books.google.com.ar/books?id=8RcLuv-Ll2kC)
- 18 [books?id=8RcLuv-Ll2kC](https://books.google.com.ar/books?id=8RcLuv-Ll2kC).
- 19 18. Solé RV, Bascompte J (2006) *Self-organization in complex ecosystems*. New Jersey, USA.: Princeton
- 20 University Press. Available: <http://books.google.com.ar/books?id=v4gpGH6Gv68C>.
- 21 19. Stauffer D, Aharony A (1994) *Introduction To Percolation Theory*. London: Taylor & Francis.
- 22 20. Ochoa-Quintero JM, Gardner TA, Rosa I, de Barros Ferraz SF, Sutherland WJ (2015) Thresholds of
- 23 species loss in Amazonian deforestation frontier landscapes. *Conservation Biology* 29: 440–451. Available:
- 24 <http://onlinelibrary.wiley.com/doi/10.1111/cobi.12446/abstract>.
- 25 21. Leibold MA, Norberg J (2004) Biodiversity in metacommunities: Plankton as complex adaptive systems?
- 26 *Limnology and Oceanography* 49: 1278–1289. Available: <http://www.aslo.org/lo/pdf/vol{ }49/issue{ }4{ }part{ }2/12>
- 27 22. Lenton TM, Williams HTP (2013) On the origin of planetary-scale tipping points. *Trends in Ecology &*
- 28 *Evolution* 28: 380–382. Available: <http://www.sciencedirect.com/science/article/pii/S0169534713001456>.
- 29 23. Bonan GB (2008) *Forests and Climate Change: Forcings, Feedbacks, and the Climate Benefits of Forests*.

- 1 Science 320: 1444–1449. Available: <http://www.sciencemag.org/content/320/5882/1444.abstract>.
- 2 24. Solé RV, Bartumeus F, Gamarra JGP (2005) Gap percolation in rainforests. *Oikos* 110: 177–185.
- 3 Available: <http://onlinelibrary.wiley.com/doi/10.1111/j.0030-1299.2005.13843.x/abstract>.
- 4 25. He F, Hubbell S (2003) Percolation Theory for the Distribution and Abundance of Species. *Physical*
- 5 *Review Letters* 91: 198103. Available: <http://link.aps.org/doi/10.1103/PhysRevLett.91.198103>.
- 6 26. Bascompte J, Solé RV, Sole RV (1996) Habitat fragmentation and extinction thresholds in spatially explicit
- 7 models. *Journal of Animal Ecology* 65: 465–473. Available: <http://www.jstor.org/discover/10.2307/5781?uid=3737512{\&}uid=>
- 8 27. Solé RV, Alonso D, Saldaña J (2004) Habitat fragmentation and biodiversity collapse in neutral
- 9 communities. *Ecological Complexity* 1: 65–75. Available: [http://www.sciencedirect.com/science/article/pii/](http://www.sciencedirect.com/science/article/pii/S1476945X03000084)
- 10 [S1476945X03000084](http://www.sciencedirect.com/science/article/pii/S1476945X03000084).
- 11 28. Loehle C, Li B-L, Sundell RC (1996) Forest spread and phase transitions at forest-prairie ecotones in
- 12 Kansas, U.S.A. *Landscape Ecology* 11: 225–235.
- 13 29. Naito AT, Cairns DM (2015) Patterns of shrub expansion in Alaskan arctic river corridors suggest phase
- 14 transition. *Ecology and Evolution* 5: 87–101. Available: <http://dx.doi.org/10.1002/ece3.1341>.
- 15 30. Dai L, Vorselen D, Korolev KS, Gore J (2012) Generic Indicators for Loss of Resilience Before a Tipping
- 16 Point Leading to Population Collapse. *Science* 336: 1175–1177. Available: [http://www.sciencemag.org/](http://www.sciencemag.org/content/336/6085/1175.abstract)
- 17 [content/336/6085/1175.abstract](http://www.sciencemag.org/content/336/6085/1175.abstract).
- 18 31. Hastings A, Wysham DB (2010) Regime shifts in ecological systems can occur with no warning.
- 19 *Ecology Letters* 13: 464–472. Available: [http://onlinelibrary.wiley.com/doi/10.1111/j.1461-0248.2010.01439.](http://onlinelibrary.wiley.com/doi/10.1111/j.1461-0248.2010.01439.x/abstract)
- 20 [x/abstract](http://onlinelibrary.wiley.com/doi/10.1111/j.1461-0248.2010.01439.x/abstract).
- 21 32. Boettiger C, Hastings A (2012) Quantifying limits to detection of early warning for critical transitions.
- 22 *Journal of The Royal Society Interface* 9: 2527–2539. doi:10.1098/rsif.2012.0125.
- 23 33. Pueyo S, Graça PML de A, Barbosa RI, Cots R, Cardona E, et al. (2010) Testing for criticality in
- 24 ecosystem dynamics: the case of Amazonian rainforest and savanna fire. *Ecology Letters* 13: 793–802.
- 25 Available: <http://dx.doi.org/10.1111/j.1461-0248.2010.01497.x>.
- 26 34. Oborny B, Szabó G, Meszéna G (2007) Survival of species in patchy landscapes: percolation in
- 27 space and time. In: *Scaling biodiversity*. Cambridge University Press. pp. 409–440. Available: <http://dx.doi.org/10.1017/CBO9780511814938.022>.
- 28
- 29 35. Gastner MT, Oborny B, Zimmermann DK, Pruessner G (2009) Transition from Connected to Fragmented

- 1 Vegetation across an Environmental Gradient: Scaling Laws in Ecotone Geometry. *The American Naturalist*
2 174: E23–E39. Available: <http://www.jstor.org/stable/10.1086/599292>.
- 3 36. Ódor G (2004) Universality classes in nonequilibrium lattice systems. *Reviews of Modern Physics* 76:
4 663–724. Available: <http://link.aps.org/doi/10.1103/RevModPhys.76.663>.
- 5 37. Hinrichsen H (2000) Non-equilibrium critical phenomena and phase transitions into absorbing states.
6 *Advances in Physics* 49: 815–958. Available: <http://dx.doi.org/10.1080/00018730050198152>.
- 7 38. DiMiceli C, Carroll M, Sohlberg R, Huang C, Hansen M, et al. (2015) Annual Global Automated MODIS
8 Vegetation Continuous Fields (MOD44B) at 250 m Spatial Resolution for Data Years Beginning Day 65,
9 2000 - 2014, Collection 051 Percent Tree Cover, University of Maryland, College Park, MD, USA. Available:
10 https://lpdaac.usgs.gov/dataset{_}discovery/modis/modis{_}products{_}table/mod44b.
- 11 39. Sexton JO, Noojipady P, Song X-P, Feng M, Song D-X, et al. (2015) Conservation pol-
12 icy and the measurement of forests. *Nature Climate Change* advance on: 192–196. Available:
13 <http://www.nature.com/nclimate/journal/vaop/ncurrent/full/nclimate2816.html> <http://dx.doi.org/10.1038/nclimate2816>
14 <http://10.1038/nclimate2816> [http://www.nature.com/nclimate/journal/v6/n2/abs/nclimate2816.html{_}supplementary-](http://www.nature.com/nclimate/journal/v6/n2/abs/nclimate2816.html{_}supplementary-information)
15 [information](http://www.nature.com/nclimate/journal/v6/n2/abs/nclimate2816.html{_}supplementary-information).
- 16 40. Belward AS (1996) The IGBP-DIS Global 1 Km Land Cover Data Set “DISCover”: Proposal and
17 Implementation Plans : Report of the Land Recover Working Group of IGBP-DIS. IGBP-DIS Office.
18 Available: <https://books.google.com.ar/books?id=qixsNAAACAAJ>.
- 19 41. Kéfi S, Rietkerk M, Alados CL, Pueyo Y, Papanastasis VP, et al. (2007) Spatial vegetation
20 patterns and imminent desertification in Mediterranean arid ecosystems. *Nature* 449: 213–217. Available:
21 <http://dx.doi.org/10.1038/nature06111> <http://www.nature.com/nature/journal/v449/n7159/abs/nature06111.html>.
- 22 42. Scanlon TM, Caylor KK, Levin SA, Rodriguez-iturbe I (2007) Positive feedbacks promote power-law
23 clustering of Kalahari vegetation. *Nature* 449: 209–212. doi:10.1038/nature06060.
- 24 43. Vandermeer J, Perfecto I, Philpott SM (2008) Clusters of ant colonies and robust criticality in a tropical
25 agroecosystem. *Nature* 451: 457–460. doi:10.1038/nature06477.
- 26 44. Saravia LA, Giorgi A, Momo F (2012) Multifractal growth in periphyton communities. *Oikos* 121:
27 1810–1820. Available: <http://doi.wiley.com/10.1111/j.1600-0706.2011.20423.x>.
- 28 45. Dal Bello M, Maggi E, Rindi L, Capocchi A, Fontanini D, et al. (2014) Multifractal spatial distribution
29 of epilithic microphytobenthos on a Mediterranean rocky shore. *Oikos* 124: 477–485. Available: <http://doi.wiley.com/10.1111/oikos.12477>.

1 //onlinelibrary.wiley.com/doi/10.1111/oik.01503/abstract.

2 46. Manor A, Shnerb NM (2008) Origin of pareto-like spatial distributions in ecosystems. *Physical Review*
3 *Letters* 101: 268104. Available: <http://link.aps.org/doi/10.1103/PhysRevLett.101.268104>.

4 47. Irvine MA, Bull JC, Keeling MJ (2016) Aggregation dynamics explain vegetation patch-size distributions.
5 *Theoretical Population Biology* 108: 70–74. Available: [http://www.sciencedirect.com/science/article/pii/](http://www.sciencedirect.com/science/article/pii/S0040580915001239)
6 [S0040580915001239](http://www.sciencedirect.com/science/article/pii/S0040580915001239).

7 48. Bulleri F, Bruno JF, Benedetti-cccchi L (2008) Beyond Competition: Incorporating Posi-
8 tive Interactions between Species to Predict Ecosystem Invasibility. *PLoS Biology* 6: 1136–1140.
9 doi:10.1371/journal.pbio.0060162.

10 49. Goldstein ML, Morris SA, Yen GG (2004) Problems with fitting to the power-law distribution. *The*
11 *European Physical Journal B - Condensed Matter and Complex Systems* 41: 255–258. Available: [http:](http://link.springer.com/article/10.1140/epjb/e2004-00316-5)
12 [//link.springer.com/article/10.1140/epjb/e2004-00316-5](http://link.springer.com/article/10.1140/epjb/e2004-00316-5).

13 50. Clauset A, Shalizi C, Newman M (2009) Power-Law Distributions in Empirical Data. *SIAM Review* 51:
14 661–703. Available: <http://epubs.siam.org/doi/abs/10.1137/070710111>.

15 51. Efron B, Tibshirani RJ (1994) *An Introduction to the Bootstrap*. New York: Taylor & Francis. Available:
16 <https://books.google.es/books?id=gLlpIUxRntoC>.

17 52. Burnham K, Anderson DR (2002) *Model selection and multi-model inference: A practical information-*
18 *theoretic approach*. 2nd. New York: Springer-Verlag.

19 53. Klaus A, Yu S, Plenz D (2011) Statistical analyses support power law distributions found in neuronal
20 avalanches. *PloS one* 6: e19779. Available: <http://dx.plos.org/10.1371/journal.pone.0019779>.

21 54. Pinheiro J, Bates D, DebRoy S, Sarkar D, R Core Team (2016) *nlme: Linear and Nonlinear Mixed Effects*
22 *Models*. Available: <http://cran.r-project.org/package=nlme>.

23 55. R Core Team (2015) *R: A Language and Environment for Statistical Computing*. Available: [http:](http://www.r-project.org/)
24 [//www.r-project.org/](http://www.r-project.org/).

25 56. Gillespie CS (2015) Fitting Heavy Tailed Distributions: The *powerLaw* Package. *Journal of Statistical*
26 *Software* 64: 1–16. Available: <http://www.jstatsoft.org/v64/i02/>.

27 57. Gardner RH, Urban DL (2007) Neutral models for testing landscape hypotheses. *Landscape Ecology* 22: 15–
28 29. Available: <http://dx.doi.org/10.1007/s10980-006-9011-4> <http://www.springerlink.com/content/2vq21v4v78461506/>.

29 58. Benedetti-Cecchi L, Tamburello L, Maggi E, Bulleri F (2015) *Experimental Perturbations Mod-*

ify the Performance of Early Warning Indicators of Regime Shift. *Current biology* 25: 1867–1872.
doi:10.1016/j.cub.2015.05.035.

59. Corrado R, Cherubini AM, Pennetta C (2014) Early warning signals of desertification transitions in
semiarid ecosystems. *Physical Review E* 90: 62705. Available: [http://link.aps.org/doi/10.1103/PhysRevE.90.](http://link.aps.org/doi/10.1103/PhysRevE.90.062705)
062705.

60. Rooij MMJW van, Nash B, Rajaraman S, Holden JG (2013) A Fractal Approach to Dynamic Inference and
Distribution Analysis. *Frontiers in Physiology* 4. Available: [http://www.frontiersin.org/fractal/physiology/10.3389/fphys.20](http://www.frontiersin.org/fractal/physiology/10.3389/fphys.2013.00044)

61. Brook BW, Ellis EC, Perring MP, Mackay AW, Blomqvist L (2013) Does the terrestrial biosphere have
planetary tipping points? *Trends in Ecology & Evolution*. Available: [http://www.sciencedirect.com/science/](http://www.sciencedirect.com/science/article/pii/S0169534713000335)
article/pii/S0169534713000335.

62. Pardini R, Bueno A de A, Gardner TA, Prado PI, Metzger JP (2010) Beyond the Fragmentation Threshold
Hypothesis: Regime Shifts in Biodiversity Across Fragmented Landscapes. *PLoS ONE* 5: e13666. Available:
<http://dx.doi.org/10.1371/journal.pone.0013666>.

63. Oborny B, Meszéna G, Szabó G (2005) Dynamics of Populations on the Verge of Extinction. *Oikos* 109:
291–296. Available: <http://www.jstor.org/stable/3548746>.