

10.5 Lab 2: Clustering

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10.5.1 K-Means Clustering

The function **kmeans()** performs *K*-means clustering in R. We begin with a simple simulated example in which there are truly two clusters in the data: the first 25 observations have a mean shift relative to the next 25 observations.

```
set.seed(2)
x = matrix(rnorm(50*2), ncol = 2)
x[1:25, 1] = x[1:25, 1] + 3
x[1:25, 2] = x[1:25, 2] - 4
```

We now perform *K*-means clustering with $K = 2$.

```
km.out = kmeans(x, 2, nstart = 20)
```

The cluster assignments of the 50 observations are contained in **km.out\$cluster**.

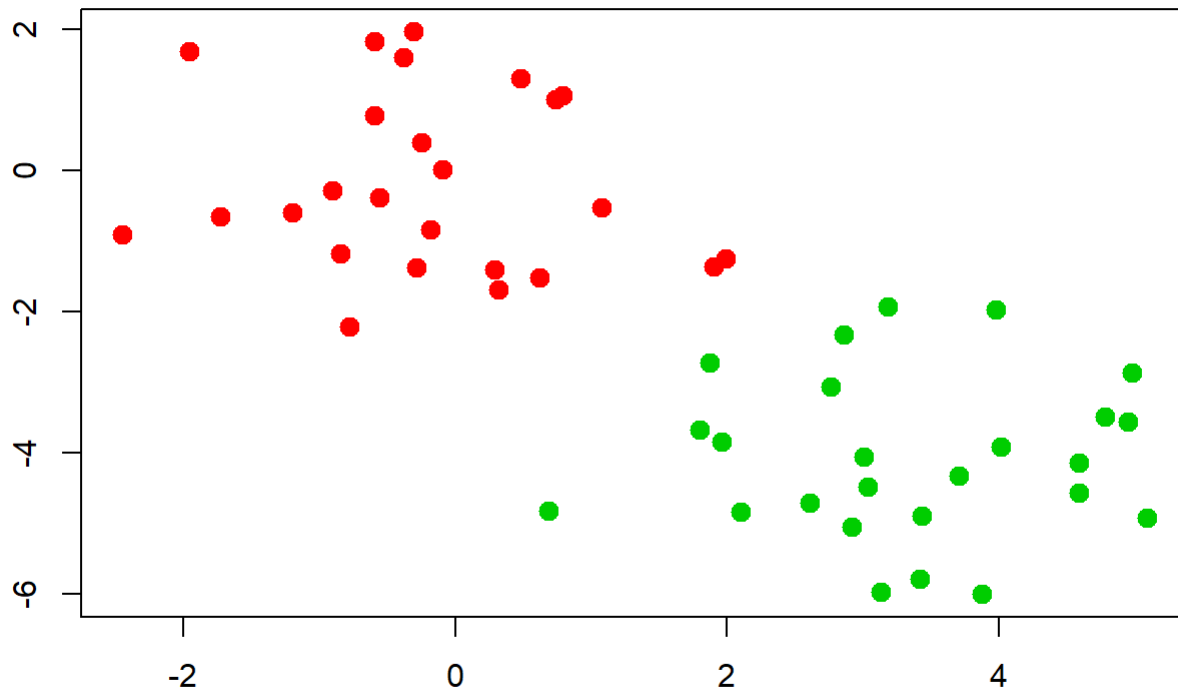
```
km.out$cluster
```

```
## [1] 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 1 1 1 1 1 1 1 1 1 1
## [36] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
```

The *K*-means clustering perfectly separated the observations into two clusters even though we did not supply any group information to **kmeans()**. We can plot the data, with each observation colored according to its cluster assignment.

```
plot(x, col = (km.out$cluster + 1), main = "K-Means Clustering Results with K=2", xlab = "", ylab = "", pch = 20, cex = 2)
```

K-Means Clustering Results with K=2



Here the observations can be easily plotted because they are two-dimensional. If there were more than two variables then we could instead perform PCA and plot the first two principal components score vectors.

In this example, we knew that there really were two clusters because we generated the data. However, for real data, in general we do not know the true number of clusters. We could instead have performed K -means clustering on this example with $K = 3$.

```
set.seed(4)
km.out = kmeans(x, 3, nstart = 20)
km.out
```

```
## K-means clustering with 3 clusters of sizes 10, 23, 17
##
## Cluster means:
##      [,1]      [,2]
## 1  2.3001545 -2.69622023
## 2 -0.3820397 -0.08740753
## 3  3.7789567 -4.56200798
##
## Clustering vector:
## [1] 3 1 3 1 3 3 3 1 3 1 3 1 3 1 3 3 3 3 3 1 3 3 3 2 2 2 2 2 2 2 2 2 2
## [36] 2 2 2 2 2 2 2 2 1 2 1 2 2 2 2
##
## Within cluster sum of squares by cluster:
## [1] 19.56137 52.67700 25.74089
## (between_SS / total_SS =  79.3 %)
##
## Available components:
##
## [1] "cluster"      "centers"      "totss"        "withinss"
## [5] "tot.withinss" "betweenss"    "size"         "iter"
## [9] "ifault"
```

When $K = 3$, K-means clustering splits up the two clusters.

To run the **kmenas()** function in R with multiple initial cluster assignments, we use the **nstart** argument. If a value of **nstart** greater than one is used, then K-means clustering will be performed using multiple random assignments in Step 1 of Algorithm 10.1, and the **kmeans()** function will only report the best results. Here we compare using **nstart=1** to **nstart=20**.

```
set.seed(3)
km.out = kmeans(x, 3, nstart = 1)
km.out$tot.withinss
```

```
## [1] 104.3319
```

```
km.out = kmeans(x, 3, nstart = 20)
km.out$tot.withinss
```

```
## [1] 97.97927
```

Note that **km.out\$tot.withinss** is the total within-cluster sum of squares, which we seek to minimize by performing K-means clustering. The individual within-cluster sum-of-squares are contained in the vector **km.out\$withinss**.

We *strongly* recommend always running K-menass clustering with a large value of **nstart**, such as 20 or 50, since otherwise an undesirable local optimum may be obtained.

When performing K-means clustering, in addition to using multiple initial assignments, it is also important to set a random seed using the **set.seed()** function. This way, the initial cluster assignments in Step 1 can be replicated, and the K-means output will be fully reproducible.

10.5.2 Hierarchical Clustering

The **hclust()** function implements hierarchical clustering in R. In the following example we use the data from Section 10.5.1 to plot the hierarchical clustering dendrogram using complete, single, and average linkage clustering, with Euclidean distance as the dissimilarity measure. We begin by clustering observations using complete linkage. The **dist()** function is used to compute the 50 x 50 inter-observation Euclidean distance matrix.

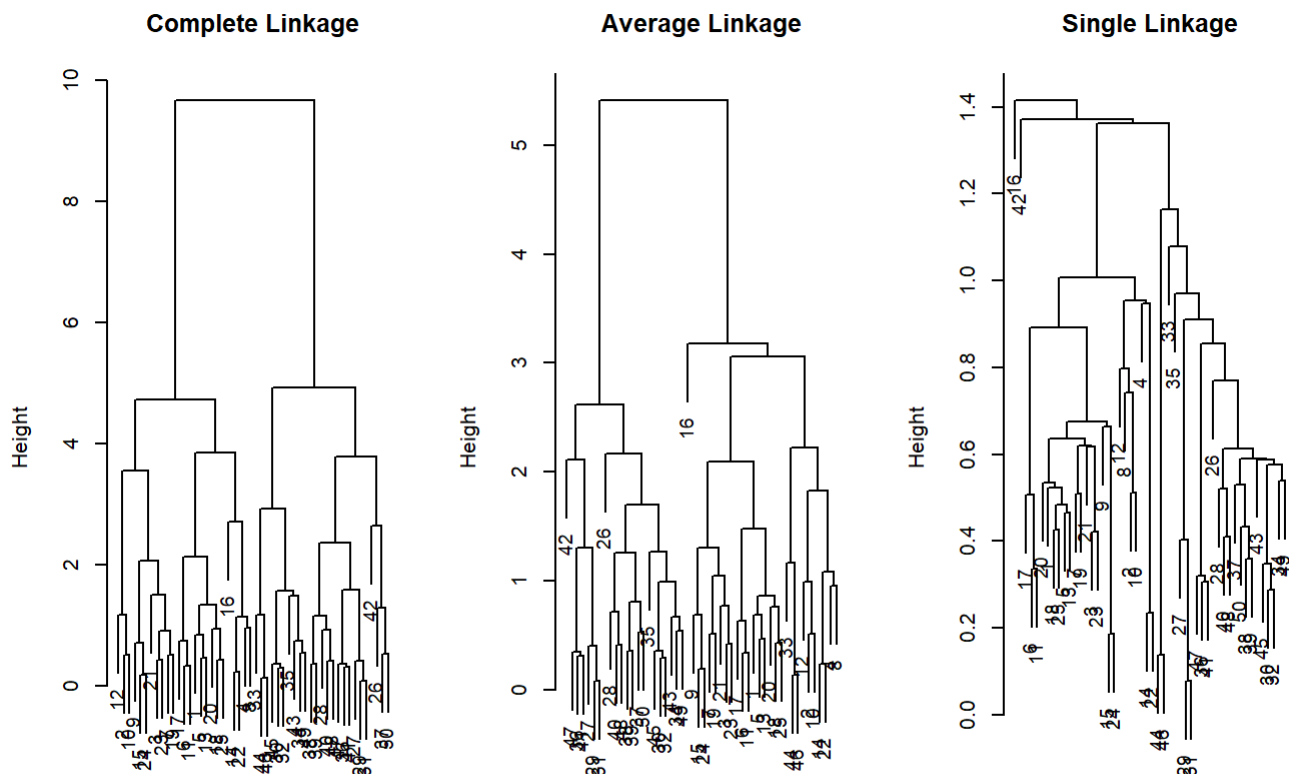
```
hc.complete = hclust(dist(x), method = "complete")
```

We could just as easily perform hierarchical clustering with average or single linkage instead:

```
hc.average = hclust(dist(x), method = "average")  
hc.single = hclust(dist(x), method = "single")
```

We can now plot the dendrograms obtained using the usual **plot()** function. The numbers at the bottom of the plot identify each observation.

```
par(mfrow = c(1, 3))  
plot(hc.complete, main = "Complete Linkage", xlab = "", sub = "", cex = 0.9)  
plot(hc.average, main = "Average Linkage", xlab = "", sub = "", cex = 0.9)  
plot(hc.single, main = "Single Linkage", xlab = "", sub = "", cex = 0.9)
```



To determine the cluster labels for each observation associated with a given cut of the dendrogram, we can use the **cutree()** function:

```
cutree(hc.complete, 2)
```

```
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 2 2 2 2 2 2 2 2 2  
## [36] 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
```

```
cutree(hc.average, 2)
```

```
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 2 2 2 2 2 2 1 2 2  
## [36] 2 2 2 2 2 2 2 2 1 2 1 2 2 2 2
```

```
cutree(hc.single, 2)
```

```
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1  
## [36] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
```

For this data, complete and average linkage generally separate the observations into their correct groups. However, single linkage identifies one point as belonging to its own cluster. A more sensible answer is obtained when four clusters are selected, although there are still two singletons.

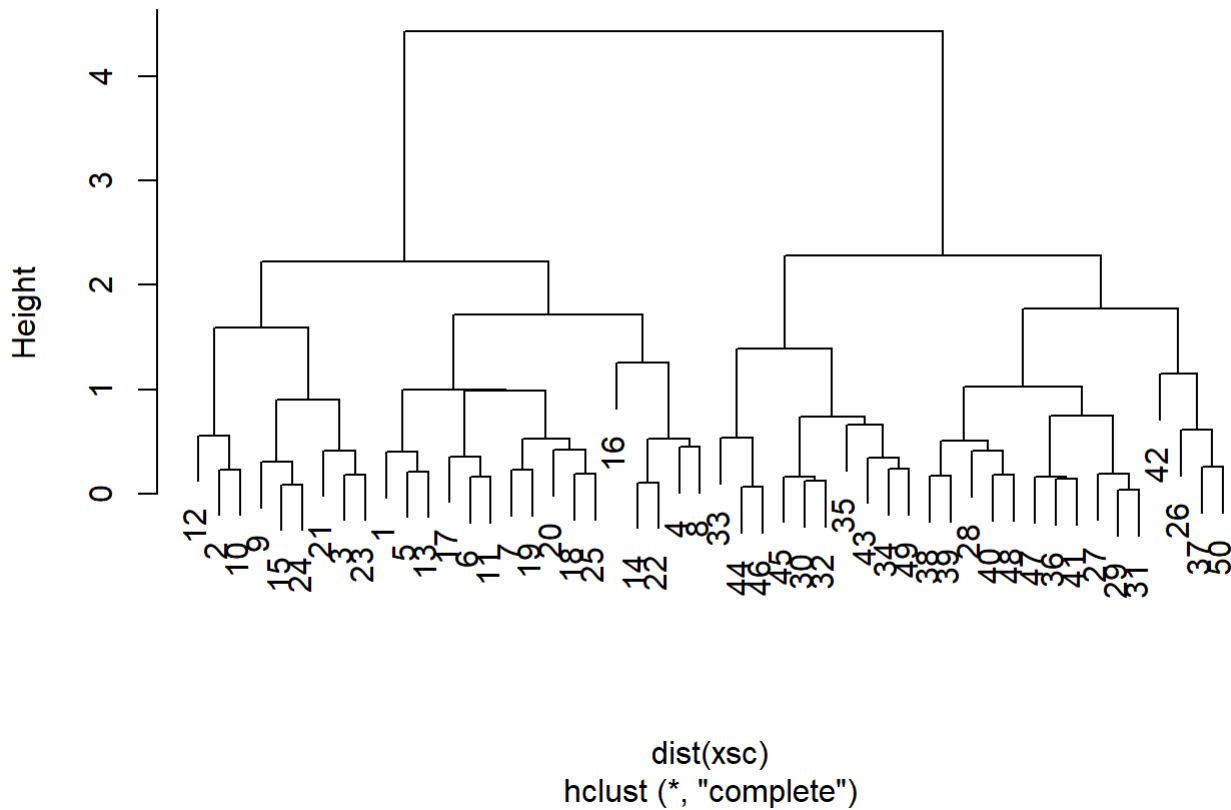
```
cutree(hc.single, 4)
```

```
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 1 1 1 1 1 1 1 1 1 3 3 3 3 3 3 3 3  
## [36] 3 3 3 3 3 3 4 3 3 3 3 3 3 3 3
```

To scale the variables before performing hierarchical clustering of the observations, we use the **scale()** function:

```
xsc = scale(x)  
plot(hclust(dist(xsc), method = "complete"), main = "Hierarchical Clustering with Scaled  
Features")
```

Hierarchical Clustering with Scaled Features



Correlation-based distance can be computed using the **as.dist()** function, which converts an arbitrary square symmetric matrix into a form that the **hclust()** function recognizes as a distance matrix. However, this only makes sense for data with at least three features since the absolute correlation between any two observations with measurements on two features is always 1. Hence, we will cluster a three-dimensional data set.

```
x = matrix(rnorm(30 * 3), ncol = 3)
dd = as.dist(1 - cor(t(x)))
plot(hclust(dd, method = "complete"), main = "Complete Linkage with Correlation-Based Distance", xlab = "", sub = "")
```

Complete Linkage with Correlation-Based Distance

