10.6 Lab 3: NCI60 Data Example

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Unsupervised techniques are often used in the analysis of genomic data. In particular, PCA and hierarchical clustering are populatr tools. We illustrate these techniques on the **NCI60** cancer cell line microarray data, which consists of 6,830 gene expression measurements on 64 cancer cell lines.

```
library(ISLR)

## Warning: package 'ISLR' was built under R version 3.4.4

nci.labs = NCI60$labs
nci.data = NCI60$data
```

Each cell line is labeled with a cancer type. We do not make use of the cancer types in performing PCA and clustering, as these are unsupervised techniques. But after performing PCA and clustering, we will check to see the extent to which these cancer types agree with the results of these unsupervised techniques.

The data has 64 rows and 6,830 columns.

```
dim(nci.data)

## [1] 64 6830
```

We begin by examining the cancer types for the cell lines.

```
nci.labs[1:4]

## [1] "CNS" "CNS" "RENAL"
```

```
table(nci.labs)
```

```
## nci.labs
##
        BREAST
                        CNS
                                  COLON K562A-repro K562B-repro
                                                                     LEUKEMIA
##
                                      7
                                                   1
                                               NSCLC
## MCF7A-repro MCF7D-repro
                               MELANOMA
                                                         OVARIAN
                                                                     PROSTATE
##
             1
##
         RENAL
                    UNKNOWN
##
```

10.6.1 PCA on the NCI60 Data

We first perform PCA on the data after scaling the variables (genes) to have standard deviation one, although one could reasonably argue that it is better not to scale the genes.

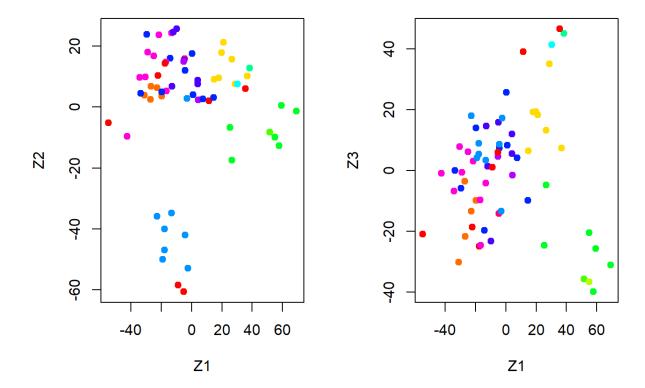
```
pr.out = prcomp(nci.data, scale = TRUE)
```

We now plot the first few principal component score vectors, in order to visualize the data. The observations (cell ines) corresponding to a given cancer type will be plotted in the same color, so that we can see to what extent the observations witthin a cancer type are similar to each other. We first create a simple function that assigns a distinct color to each element of a numeric vector. The function will be used to assign a color to each of the 64 cell lines, based on the cancer type to which it corresponds.

```
Cols = function(vec) {
  cols = rainbow(length(unique(vec)))
  return (cols[as.numeric(as.factor(vec))])
}
```

Note that the **rainbow()** function takes as its argument a positive integer and returns a vector containing that number of distinct colors. We now can plot the principal component score vectors.

```
par(mfrow = c(1,2))
plot(pr.out$x[,1:2], col = Cols(nci.labs), pch = 19, xlab = "Z1", ylab = "Z2")
plot(pr.out$x[,c(1,3)], col = Cols(nci.labs), pch = 19, xlab = "Z1", ylab = "Z3")
```



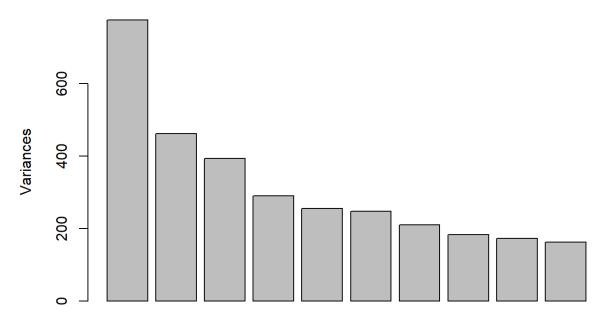
The resulting plots are shown in Figure 10.15. On the whole, cell lines corresponding to a single cancer type do tend to have similar values on the first few principal score vectors. This indicates that cell lines from the same cancer type tend to have pretty similar gene expression levels.

We can obtain a summary of the proportion of variance explained (PVE) of the first few principal comopnenets using the **summary()** method for a **prcomp** object.

```
## Importance of components:
##
                               PC1
                                        PC2
                                                 PC3
                                                          PC4
                                                                    PC5
## Standard deviation
                          27.8535 21.48136 19.82046 17.03256 15.97181
## Proportion of Variance 0.1136 0.06756
                                             0.05752
                                                      0.04248
## Cumulative Proportion
                           0.1136
                                    0.18115
                                             0.23867
                                                      0.28115
                                                               0.31850
##
                               PC6
                                                  PC8
                                                           PC9
                                         PC7
                                                                    PC10
## Standard deviation
                           15.72108 14.47145 13.54427 13.14400 12.73860
## Proportion of Variance
                                              0.02686
                           0.03619
                                     0.03066
                                                       0.02529
                                                                0.02376
## Cumulative Proportion
                           0.35468
                                     0.38534
                                              0.41220
                                                       0.43750
                                                                0.46126
##
                              PC11
                                        PC12
                                                 PC13
                                                          PC14
                                                                    PC15
## Standard deviation
                           12.68672 12.15769 11.83019 11.62554 11.43779
## Proportion of Variance
                           0.02357
                                    0.02164
                                              0.02049
                                                       0.01979
                                                                0.01915
## Cumulative Proportion
                                                       0.54674
                           0.48482
                                    0.50646
                                              0.52695
                                                                0.56590
##
                              PC16
                                        PC17
                                                 PC18
                                                          PC19
                                                                  PC20
## Standard deviation
                          11.00051 10.65666 10.48880 10.43518 10.3219
## Proportion of Variance
                           0.01772
                                    0.01663
                                             0.01611
                                                       0.01594
                                                                0.0156
## Cumulative Proportion
                           0.58361
                                    0.60024
                                              0.61635
                                                       0.63229
                                                                0.6479
##
                              PC21
                                       PC22
                                               PC23
                                                       PC24
                                                               PC25
                                                                        PC26
## Standard deviation
                          10.14608 10.0544 9.90265 9.64766 9.50764 9.33253
## Proportion of Variance 0.01507
                                    0.0148 0.01436 0.01363 0.01324 0.01275
## Cumulative Proportion
                           0.66296
                                    0.6778 0.69212 0.70575 0.71899 0.73174
##
                              PC27
                                     PC28
                                             PC29
                                                     PC30
                                                             PC31
                                                                      PC32
## Standard deviation
                          9.27320 9.0900 8.98117 8.75003 8.59962 8.44738
## Proportion of Variance 0.01259 0.0121 0.01181 0.01121 0.01083 0.01045
## Cumulative Proportion 0.74433 0.7564 0.76824 0.77945 0.79027 0.80072
##
                              PC33
                                      PC34
                                                      PC36
                                              PC35
                                                              PC37
## Standard deviation
                          8.37305 8.21579 8.15731 7.97465 7.90446 7.82127
## Proportion of Variance 0.01026 0.00988 0.00974 0.00931 0.00915 0.00896
## Cumulative Proportion 0.81099 0.82087 0.83061 0.83992 0.84907 0.85803
##
                              PC39
                                      PC40
                                              PC41
                                                     PC42
                                                             PC43
                                                                     PC44
## Standard deviation
                          7.72156 7.58603 7.45619 7.3444 7.10449 7.0131
## Proportion of Variance 0.00873 0.00843 0.00814 0.0079 0.00739 0.0072
## Cumulative Proportion 0.86676 0.87518 0.88332 0.8912 0.89861 0.9058
##
                              PC45
                                     PC46
                                             PC47
                                                     PC48
                                                             PC49
                                                                      PC50
## Standard deviation
                          6.95839 6.8663 6.80744 6.64763 6.61607 6.40793
## Proportion of Variance 0.00709 0.0069 0.00678 0.00647 0.00641 0.00601
## Cumulative Proportion 0.91290 0.9198 0.92659 0.93306 0.93947 0.94548
##
                              PC51
                                      PC52
                                              PC53
                                                      PC54
                                                              PC55
## Standard deviation
                          6.21984 6.20326 6.06706 5.91805 5.91233 5.73539
## Proportion of Variance 0.00566 0.00563 0.00539 0.00513 0.00512 0.00482
## Cumulative Proportion 0.95114 0.95678 0.96216 0.96729 0.97241 0.97723
##
                              PC57
                                     PC58
                                             PC59
                                                     PC60
                                                             PC61
                                                                      PC62
## Standard deviation
                          5.47261 5.2921 5.02117 4.68398 4.17567 4.08212
## Proportion of Variance 0.00438 0.0041 0.00369 0.00321 0.00255 0.00244
## Cumulative Proportion 0.98161 0.9857 0.98940 0.99262 0.99517 0.99761
##
                              PC63
                                        PC64
## Standard deviation
                          4.04124 2.148e-14
## Proportion of Variance 0.00239 0.000e+00
## Cumulative Proportion 1.00000 1.000e+00
```

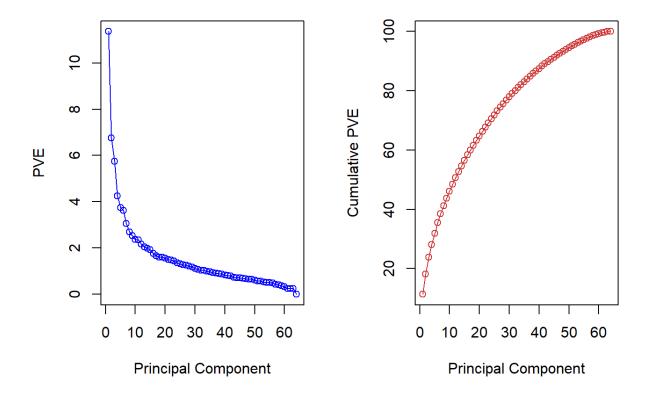
Using the plot() function, we can also plot the variance explained by the first few principal components.





Note that the height of each bar in the bar plot is given by squaring the corresponding element of **pr.out\$sdev**. However, it is more informative to plot the PVE of each principal component (i.e. a scree plot) and the cumulative PVE of each principal component. This can be done with just a little work.

```
pve = 100 * pr.out$sdev^2 / sum(pr.out$sdev^2)
par(mfrow = c(1,2))
plot(pve, type = "o", ylab = "PVE", xlab = "Principal Component", col = "blue")
plot(cumsum(pve), type = "o", ylab = "Cumulative PVE", xlab = "Principal Component", col = "br own3")
```



Note that the elements of **pve** can also be computed directly from the summary, summary(pr.out) importance[2,]**, and the elements of <math>**cumsum(pve)**aregiven by**summary(pr.out) **importance[3,]**. We see that together, the first seven principal components explain around 40% of the variance in the data. This is not a huge amount of the variance. However, looking at the scree plot, we see that while each of the first seven principal components explain a substantial amount of the variance, there is a marked decrease in the variance explained by further principal components. That is, there is an *elbow* in the plot after approximately the seventh principal component. This elbow suggests that there may be littel benefit to examining more than seven or so principal components, though even examining seven principal components may be difficult.

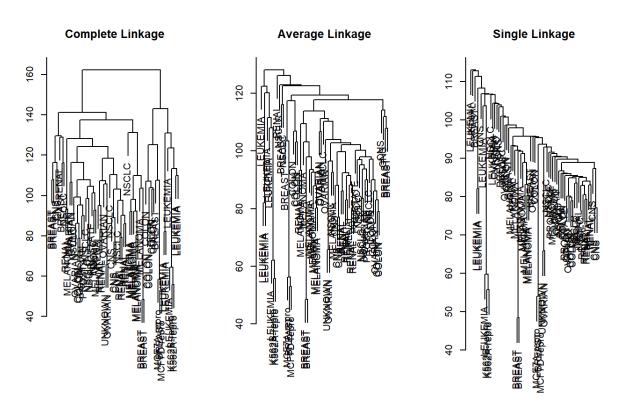
10.6.2 Clustering the Observations of the NCI60 Data

We now proceed to hierarchically cluster the cell lines in the **NCI60** data, with the goal of finding out whether or not the observations cluster into distinct types of cancer. To begin, we standardize the variables to have mean zero and standard deviation one. As mentioned earlier, this step is optional and should be performed only if we want each gene to be on the same scale.

```
sd.data = scale(nci.data)
```

We now perform hierarchical clustering of the observations using complete, single, and average linkage. Euclidean distance is used as the dissimilarity measure.

```
par(mfrow = c(1, 3))
data.dist = dist(sd.data)
plot(hclust(data.dist), labels = nci.labs, main = "Complete Linkage", xlab = "", sub = "", yla
b = "")
plot(hclust(data.dist, method = "average"), labels = nci.labs, main = "Average Linkage", xlab
= "", sub = "", ylab = "")
plot(hclust(data.dist, method = "single"), labels = nci.labs, main = "Single Linkage", xlab =
"", sub = "", ylab = "")
```



We see that the choice of linkage certainly affects the results. Typically, single linkage will tend to yield *trailing* clusters: very large clusters onto which individual observations attach one-by-one. On the other hand, complete and average linkage tend to yield more balanced, attractive clusters. For this reason, complete and average linkage are generally preferred to single linkage. Clearly cell lines within a single cancer type do tend to cluster together, although the clustering is not perfect. We will use complete linkage hierarchical clustering for the analysis that follows.

We can cut the dendrogram at the height that will yield a particular number of clusters, say four:

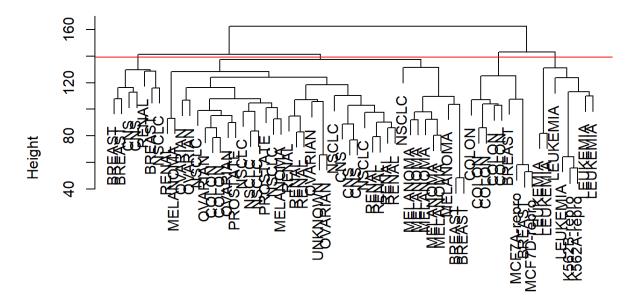
```
hc.out = hclust(dist(sd.data))
hc.clusters = cutree(hc.out, 4)
table(hc.clusters, nci.labs)
```

```
##
                nci.labs
## hc.clusters BREAST CNS COLON K562A-repro K562B-repro LEUKEMIA MCF7A-repro
##
                       2
                           3
                                  2
               1
                           2
               2
                       3
                                  0
                                                0
                                                              0
                                                                        0
                                                                                      0
##
               3
                           0
                                  0
                                                1
                                                                        6
##
                       0
                                                              1
                                                                                      0
                                  5
                                                0
                                                              0
                                                                        0
##
               4
                       2
                                                                                      1
                nci.labs
##
   hc.clusters MCF7D-repro MELANOMA NSCLC OVARIAN PROSTATE RENAL UNKNOWN
##
                            0
                                       8
                                              8
                                                       6
                                                                  2
               1
##
               2
                            0
                                              1
                                                       0
                                                                  0
                                                                        1
                                                                                  0
               3
                            0
                                              0
                                                                                  0
##
                                       0
                                                       0
                                                                 0
                                                                        0
               4
                             1
                                                       0
                                                                  0
                                                                                  0
##
                                              0
                                                                        0
```

There are some clear patterns. All the leukemia cell lines fall in cluster 3, while the breast cancer cell lines are spread out over three different clusters. We can plot the cut on the dendrogram that produces these four clusters:

```
par(mfrow = c(1, 1))
plot(hc.out, labels = nci.labs)
abline(h = 139, col = "red")
```

Cluster Dendrogram



dist(sd.data) hclust (*, "complete")

The **abline()** function draws a straight line on top of any existing plot in R. The argument **h=139** plots a horizontal line at height 139 on the dendrogram; this is the height that results in four distinct clusters. It is easy to verify that the resulting clusters are the same as the ones we obtained using **cutree(hc.out, 4)**.

Printing the output of **hclust** gives a useful brief summary of the object:

```
hc.out
```

```
##
## Call:
## hclust(d = dist(sd.data))
##
## Cluster method : complete
## Distance : euclidean
## Number of objects: 64
```

We claimed earlier in Section 10.3.2 that K-means clustering and hierarchical clustering with the dendrogram cut to obtain the same number of clusters can yield very different results. How do these **NCI60** hierarchical clustering results compare to what we get ifw e perform K-means clustering with K=4?

```
set.seed(2)
km.out = kmeans(sd.data, 4, nstart = 2)
km.clusters = km.out$cluster
table(km.clusters, hc.clusters)
```

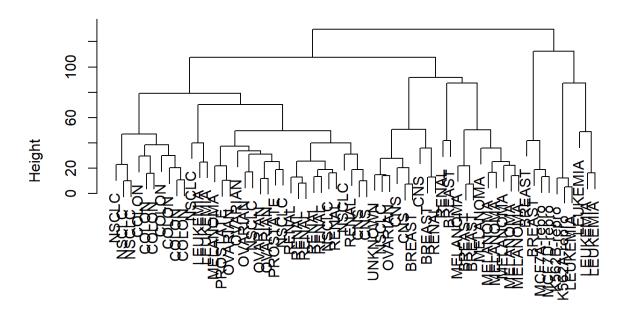
```
##
            hc.clusters
## km.clusters 1 2 3
##
           1 9 0
                   0
##
           2 3
                0
                   0
                      9
##
           3 0 0 8 0
##
           4 28 7 0
                     0
```

We see that the four clusters obtained using hierarchical clustering and *K*-means clustering are somewhat different. Cluster 2 in *K*-means clustering is identical to cluster 3 in hierarchical clustering. However, the other clusters differ: for instance, cluster 4 in *K*-means clustering contains a portion of the observations assigned to clsuter 1 by hierarchical clustering, as well as all of the observatiosn assigned to lcuster 2 by hierarchical clustering.

Rather than performing hierarchical clustering on the entire data matrix, we can simply perform hierarchical clustering on the first few principal component score vectors, as follows:

```
hc.out = hclust(dist(pr.out$x[,1:5]))
plot(hc.out, labels = nci.labs, main = "Hier. Clust. on First Five Score Vectors")
```

Hier. Clust. on First Five Score Vectors



dist(pr.out\$x[, 1:5])
hclust (*, "complete")

```
table(cutree(hc.out, 4), nci.labs)
```

```
##
       nci.labs
        BREAST CNS COLON K562A-repro K562B-repro LEUKEMIA MCF7A-repro
##
##
     1
              0
                  2
                         7
                                       0
                                                      0
                                                                2
     2
              5
                  3
                         0
                                       0
                                                      0
                                                                0
                                                                              0
##
     3
##
              0
                  0
                         0
                                       1
                                                      1
                                                                4
                                                                              0
##
              2
       nci.labs
##
        MCF7D-repro MELANOMA NSCLC OVARIAN PROSTATE RENAL UNKNOWN
##
##
     1
                   0
                              1
                                     8
                                              5
                                                         2
                                                                         0
     2
                   0
                              7
                                     1
                                              1
                                                         0
                                                                2
                                                                         1
##
##
     3
                   0
                              0
                                     0
                                              0
                                                         0
                                                                0
                                                                         0
                                              0
                                                                0
                                                                         0
##
                    1
                                                         0
```

Not suprisingly, these results are different from the ones that we obtained when we performed hierarchical clustering on the full data set. Sometimes performing clustering on the first few principal component score vectors can give better results that clustering the full data. In this situation, we might view the principal component step as one of denoising the data. We could also perform *K*-means clustering on the first few principal component score vectors rather than the full data set.