

UCLA Department of Statistics

Spatial Models for Bird Origin Assignment Using Genetic and Isotopic Data

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Project Background

Ongoing research at the Center for Tropical Research (CTR) at UCLA seeks to identify patterns of continental scale migratory connections

- Current methods are too coarse for most applications
- Large amounts of data are available (>150,000 feather samples from >500 species)
 - Genetic data - microsatellites, mitochondrial haplotypes, SNPs (soon)
 - Isotopic data - $\delta^2\text{H}$

Species of interest

Hermit Thrush *Catharus guttatus*



138 Individuals
14 Locations
6 Loci
9-27 Alleles

Wilson's Warbler *Wilsonia pusilla*



163 Individuals
8 Locations
9 Loci
15-31 Alleles

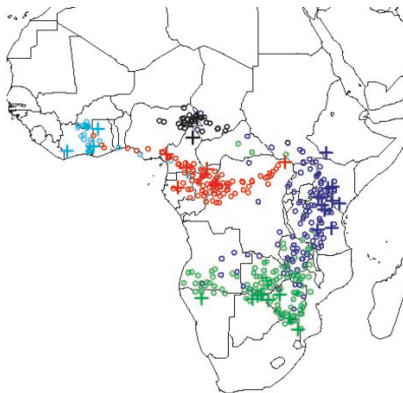
Model Framework

Assuming that the genetic (G) and isotopic (I) models are conditionally independent, then for a sample S and location k :

$$\begin{aligned} P(k|S, G, I) &\propto P(S|k, G, I) \pi(k) \\ &= P(S_G, S_I|k, G, I) \pi(k) \\ &= P(S_G|k, G, I) P(S_I|k, G, I) \pi(k) \\ &= P(S_G|k, G) P(S_I|k, I) \pi(k) \end{aligned}$$

Previous work

Wasser, et. al [2004] developed an approach for assigning genetic samples from illegal ivory shipments to geographic locations.



Model Basics

Using a multinomial error structure

$$p(y_{l \cdot k} | f_{l \cdot k}) = \frac{s_{lk}!}{\prod_i y_{lik}!} \prod_i (f_{lik})^{y_{lik}}$$

where:

- f_{lik} is the allele frequency of allele i from locus l at location k .
- y_{lik} is the count of allele i from locus l at location k .
- $s_{lk} = \sum_i y_{lik}$ is the total count of alleles from locus l at location k .

Modeling allele frequency

Allele frequencies are modeled using normalized values:

$$f_{lik} = \frac{\exp(\theta_{lik})}{\sum_j \exp(\theta_{ljk})}$$

where θ_{li} is a gaussian process:

$$\underset{[r \times 1]}{\theta_{li}} \sim \text{MVN}(\underset{[r \times 1]}{\mathbf{M}_{li}}, \underset{[r \times r]}{\Sigma})$$

Model Parameters

Mean

$$\mathbf{M}_{li} = \xi_I \eta_{li} \mathbf{1}_{[r,1]}$$

$$\xi_I \sim \text{Unif}(-\infty, \infty)$$

$$\eta_{li} \sim \text{N}(0, \beta_I)$$

$$\beta_I \sim \text{Unif}(0, 10^6)$$

Variance

$$\{\Sigma\}_{k_1, k_2} = \sigma(d_{k_1, k_2} | \alpha)$$

Assumes process is stationary and isotropic

Covariance Functions

Powered Exponential Covariance:

$$\sigma(d|\alpha) = \alpha_0 \exp \left[- \left(\frac{d}{\alpha_1} \right)^{\alpha_2} \right] + \alpha_3 I_{d=0}$$

Matérn Covariance:

$$\sigma(d|\alpha) = \alpha_0 \frac{1}{\Gamma(\alpha_2) 2^{(\alpha_2-1)}} \left(\frac{d}{\alpha_1} \right)^{\alpha_2} K_{\alpha_2} \left(\frac{d}{\alpha_1} \right) + \alpha_3 I_{d=0}$$

with the following priors on α :

$$\alpha_0, \log(\alpha_1), \log(\alpha_2), \alpha_3 \sim \text{Unif}$$

Model Fitting via MCMC

All parameters are updated by random walk Metropolis Hasting with normal jump proposals.

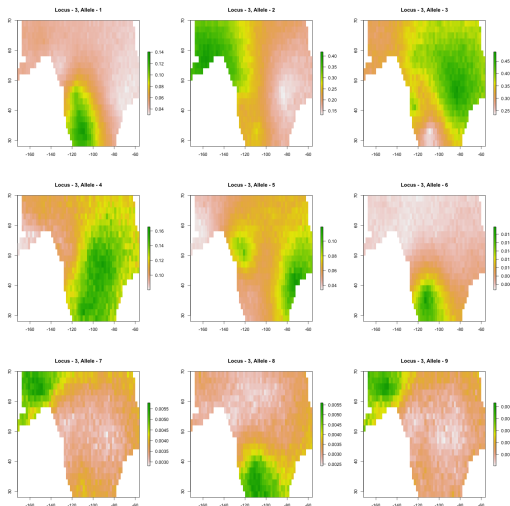
However, we first reparameterize as follows:

$$\begin{aligned} \mathbf{V}_{li} &\sim \text{MVN}(0, \Sigma) \\ [r \times 1] &\quad [r \times r] \\ \mathbf{V}_{li} &= \text{Chol}(\Sigma) \cdot \mathbf{X}_{li} \\ [r \times 1] &\quad [r \times r] \quad [r \times 1] \end{aligned}$$

where

$$\{\mathbf{X}_{li}\}_k \sim N(0, 1)$$

Allele Frequency - Hermit Thrush - Locus 3



Probability of a Sample

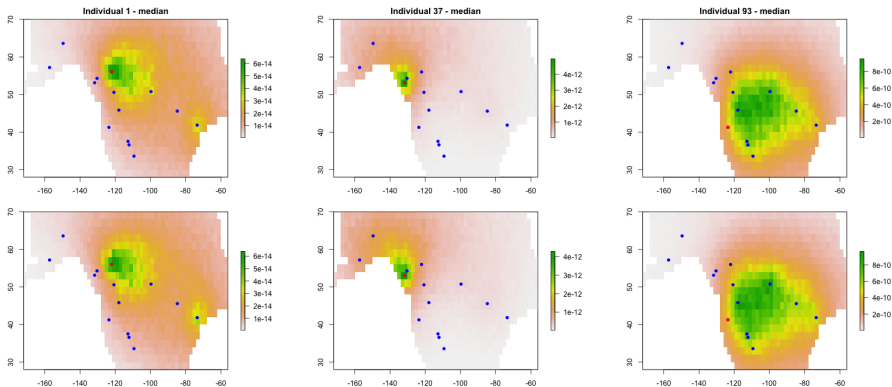
For a sample S with alleles i_l and j_l at locus l and location k

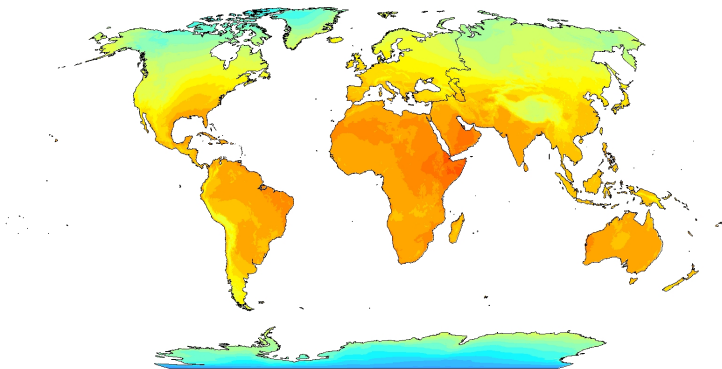
$$p(S|f, k) = \prod_l p_l(i_l, j_l|f, k)$$
$$p_l(i_l, j_l|f, k) = \begin{cases} \gamma p_l(i_l|f, k) + (1 - \gamma) p_l(i_l|f, k)^2 & \text{if } i_l = j_l \\ (1 - \gamma) p_l(i_l|f, k) p_l(j_l|f, k) & \text{if } i_l \neq j_l \end{cases}$$

$$p_l(i_l|f, k) = (1 - \delta) f_{lik} + \delta / m_l$$

where δ is the probability only one of the alleles amplified and γ is the probability of a genotyping error.

Spatial Posteriors - Hermit Thrush

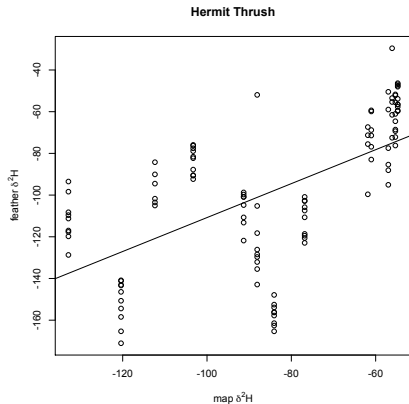


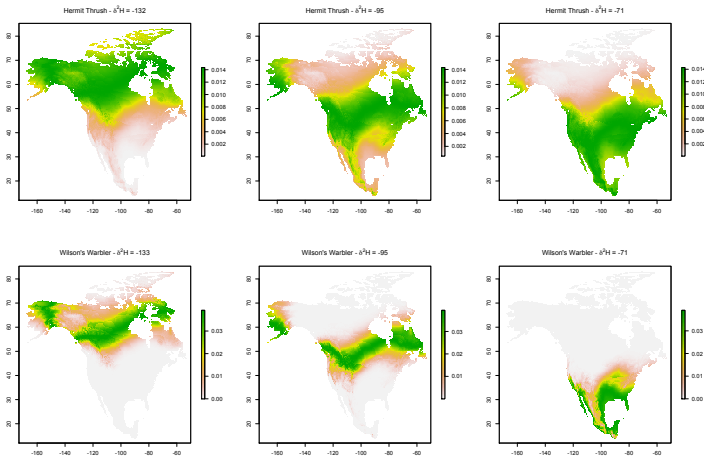


$\delta^2\text{H}$ of Annual Precipitation

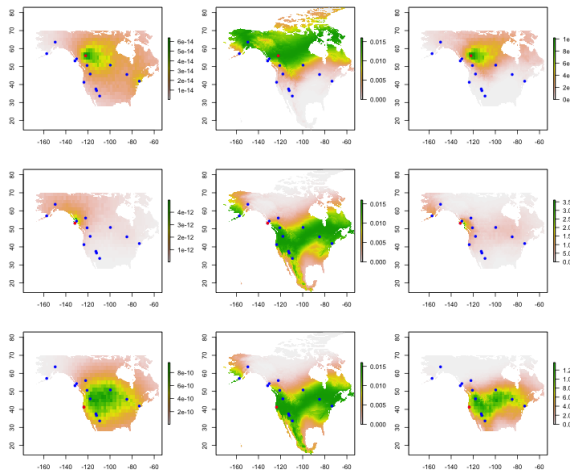


Mapping isotope values

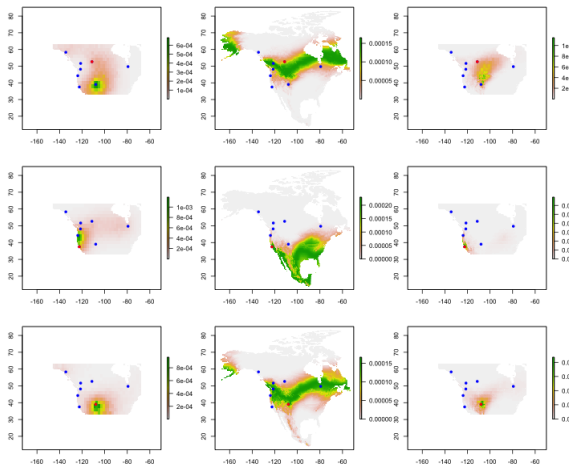




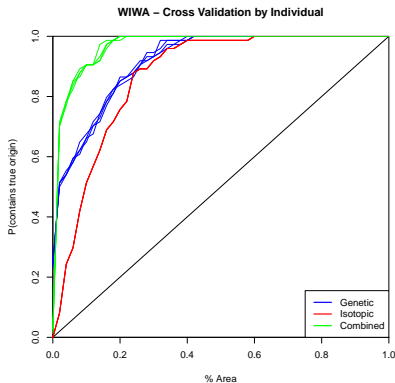
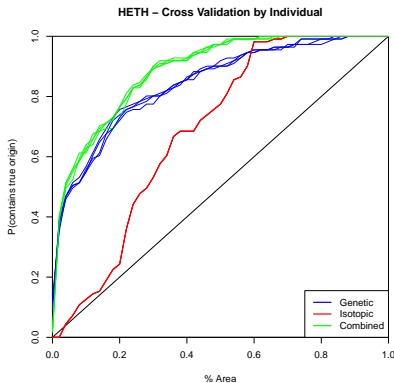
Combined - Hermit Thrush



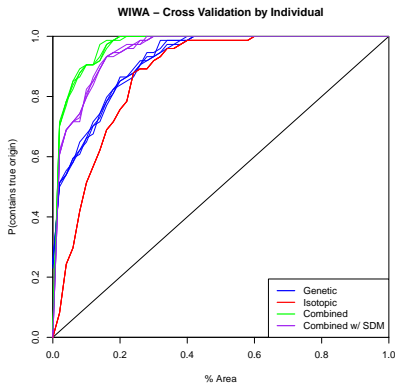
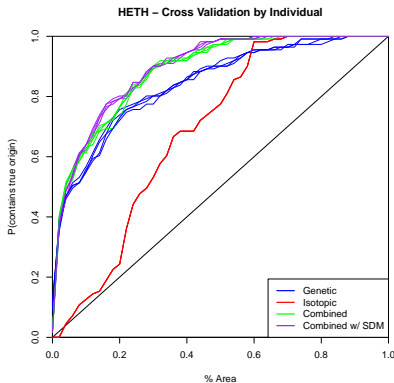
Combined - Wilson's Warbler



Classifier Results



Classifier Results + SDM



Conclusion

- Simple unified framework for combining Genetic and Isotopic models
- Combined results dramatically outperform either model alone
- Future Work
 - Fully bayesian isoscape model
 - Refine SDM priors
- R packages (available soon):
 - Genetic - Rscat
 - Isotopic - isoscape

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Genetic Methods:

- John Novembre, UCLA
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- Andrew Schuh, Colorado State

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