

$$a^0 = 1 [a^0]$$

$$\arcsin(2)$$

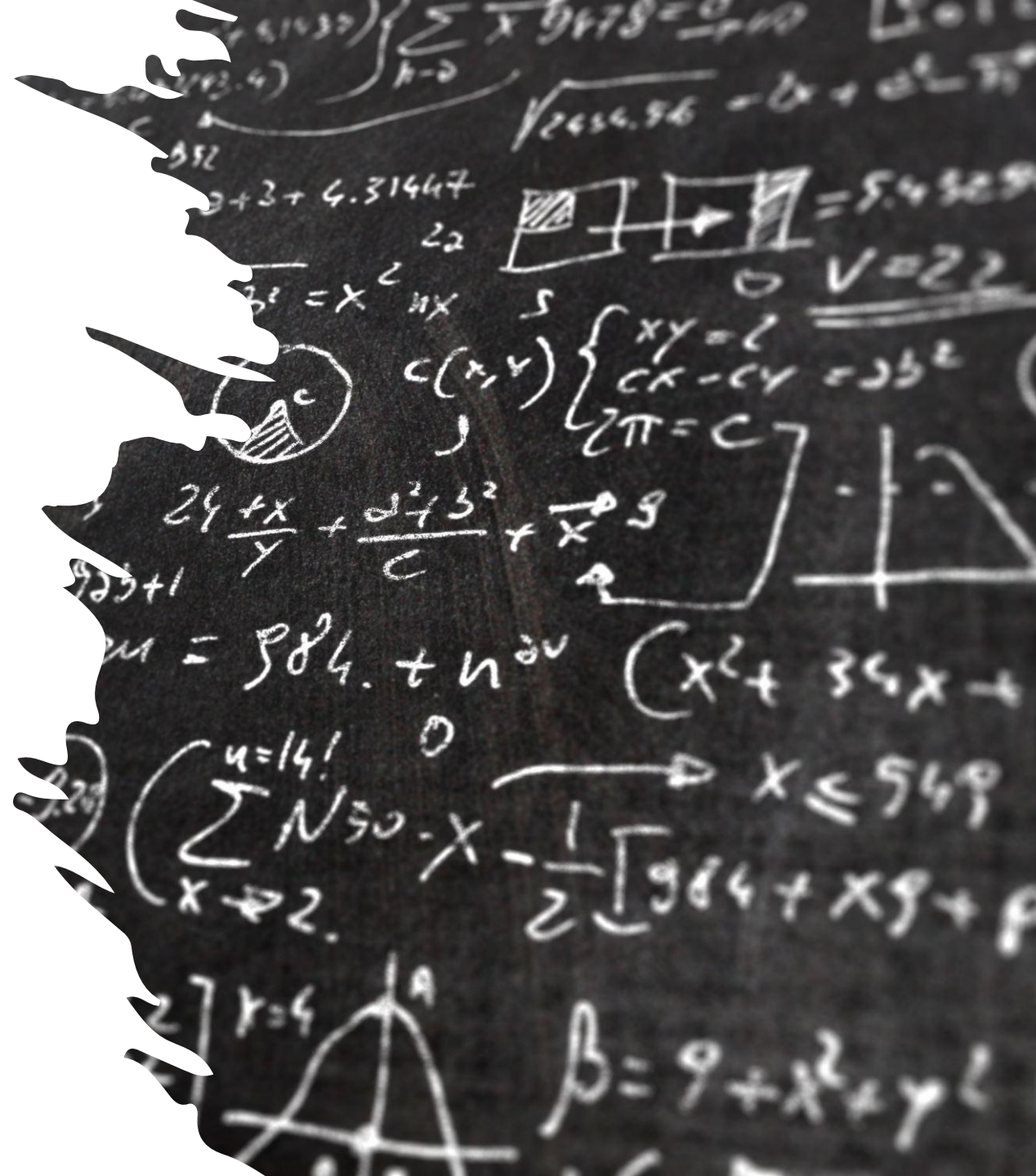
Hash Functions

Liron Shani

$$x_{n+1} =$$

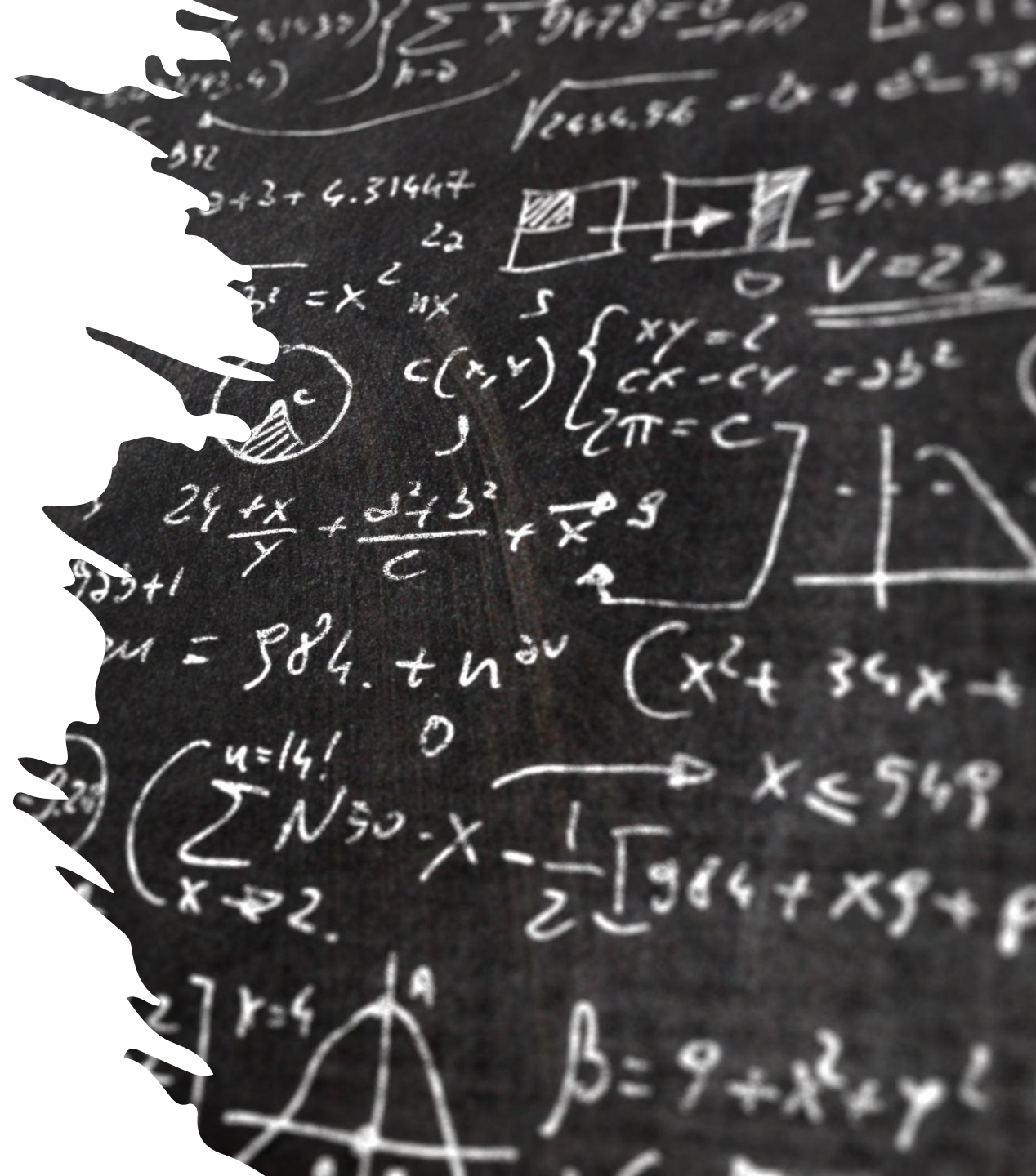
Background

- Hashing algorithms were first introduced in the 1950s by Hans Peter Luhn.
- Checksum algorithm
- The “check” number was used to easily verify if the result matched the final digit of the original number
- Would lead to several new developments of hash functions



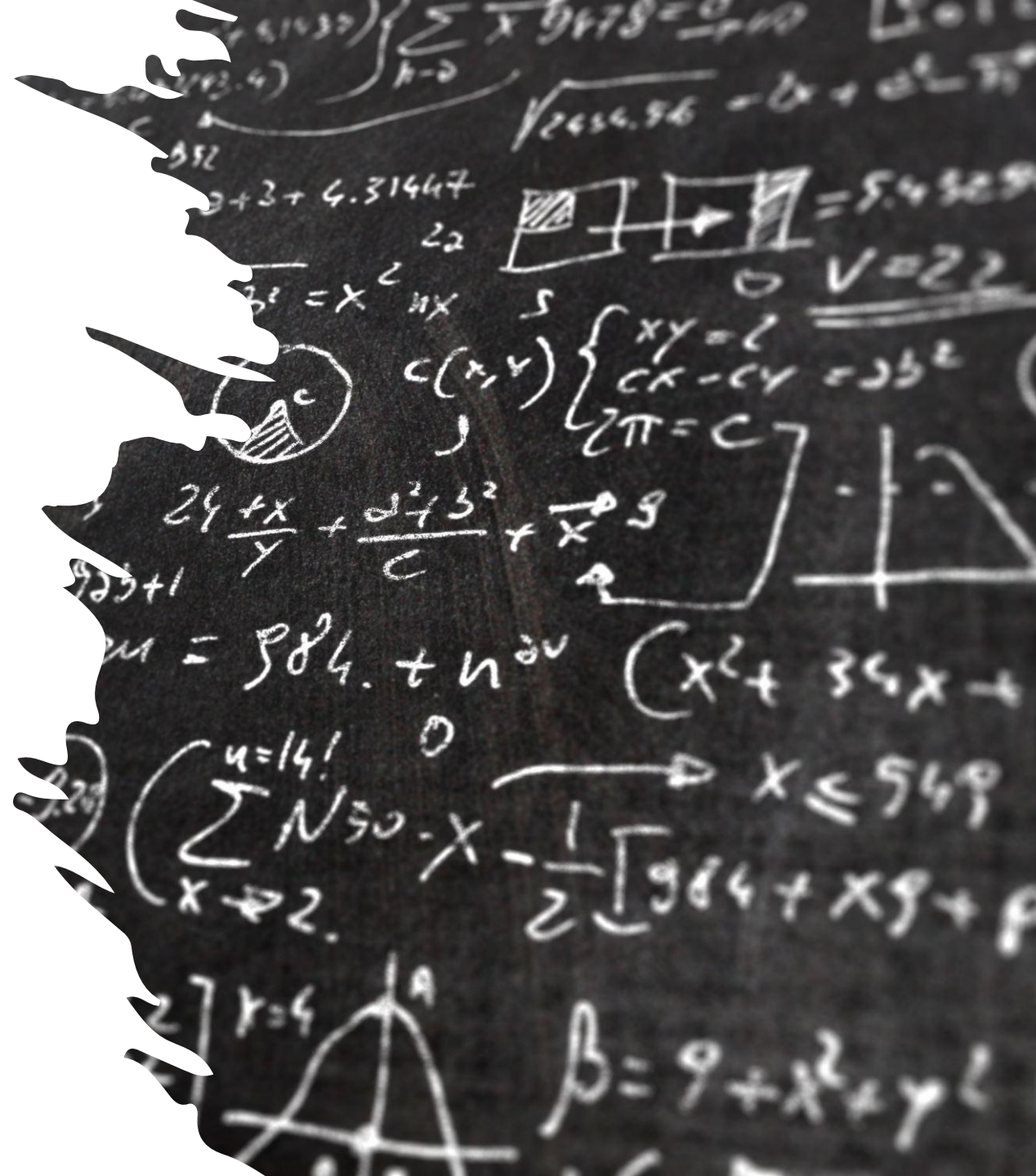
Definitions

- Hash functions are cryptographic functions that can map data inputs of any size to a fixed-size length of bits.
- Typically run faster than symmetric encryptions
- Properties:
 - Irreversible
 - Collision-resistant
 - Avalanche effect



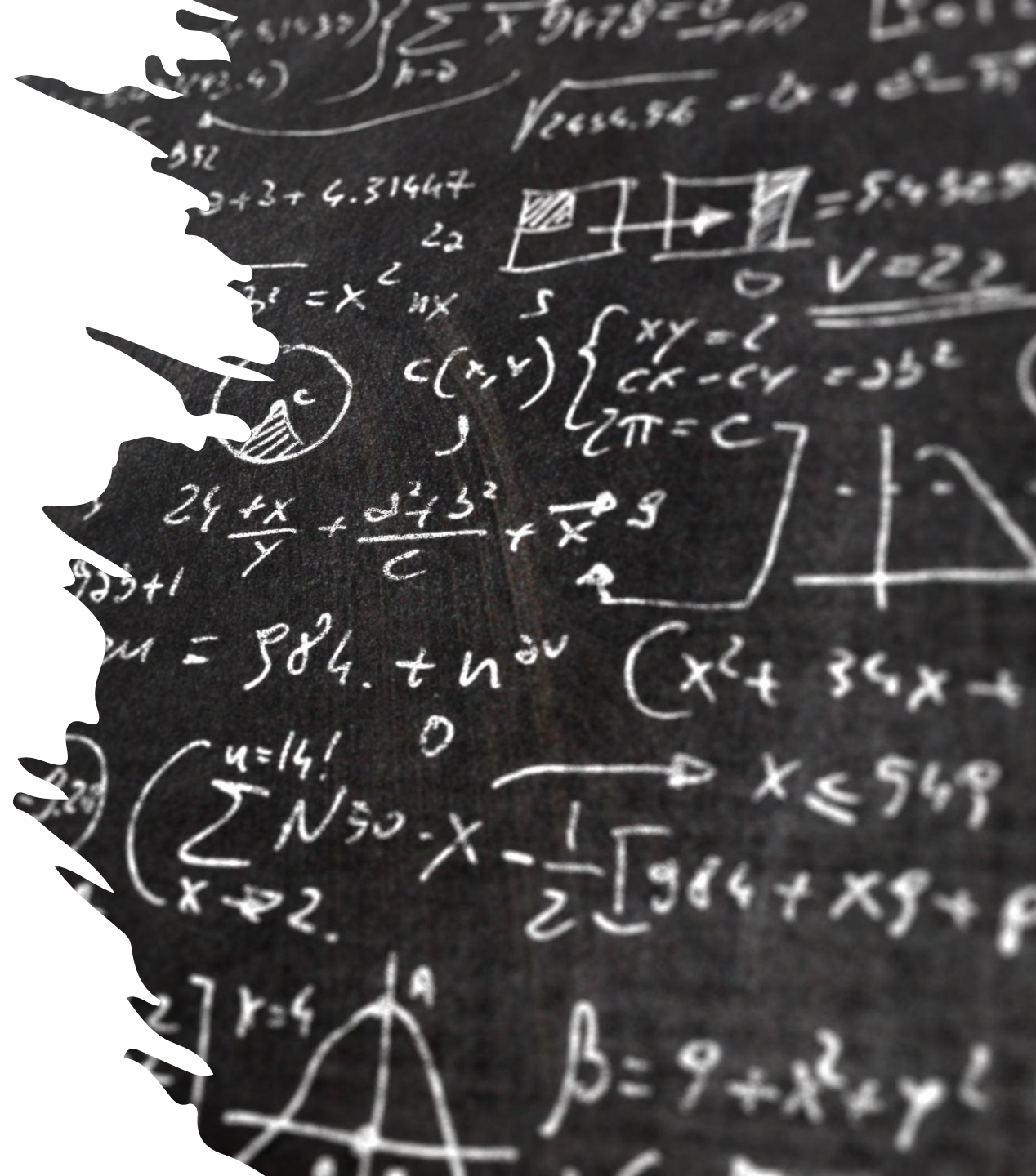
Quick example

- Message: "test"
- Hashing algorithm: $20+5+19+20=64$
- Hash value: 64
- New message: "best"
- Hashing algorithm: $2+5+19+20=46$
- New hash value: 46



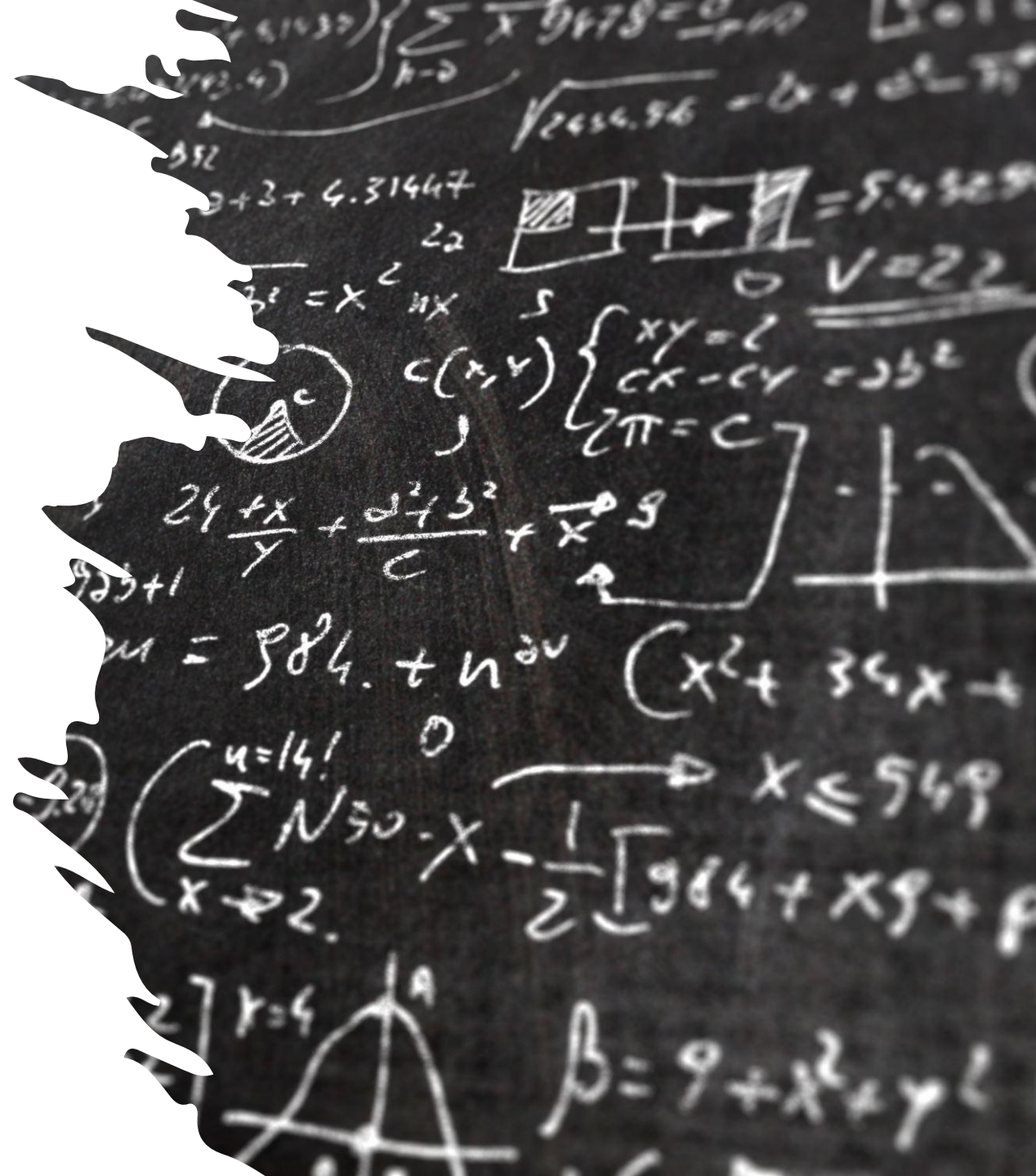
Implementations

- Originally used for organizing and classifying data
- Digital signatures
- Verify message and file integrity
- Used for cryptocurrencies
- Password verification



Example: SHA-1

- Developed and published by the NSA
- 40-digit hexadecimal hash value
- Wide use in the early 2000s
- No longer considered secure



Step 1 – Take an input text and split up each character. Convert to ASCII codes

Message: "A Test"



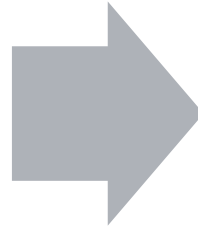
[A, , T, e, s, t]



Result: [65, 32, 84, 101, 115, 116]

Step 2 – Convert ASCII codes to binary

[65, 32, 84, 101,
115, 116]



Result: [1000001,
100000, 1010100,
1100101, 1110011,
1110100]

Step 3 – Attach zeros to the front of each value until they are each 8 bits long

[1000001, 100000,
1010100, 1100101,
1110011, 1110100]

Result: [01000001,
00100000, 01010100,
01100101, 01110011,
01110100]

Step 4 – Join the values and attach a 1 to the end

```
[01000001, 00100000, 01010100, 01100101, 01110011,  
01110100]
```



Result:

```
10000011000001010100110010111100111110  
1001
```

Step 5 – Add zeros
to the end until
the value's length
is 448 characters
(or $448 \bmod(512)$)

100000110000010101001100101111001111101001

Result:

[illegible]

Step 6 – Take the values from step 3 and get the total length. Convert that number to binary.

[1000001, 100000, 1010100, 1100101, 1110011, 1110100]



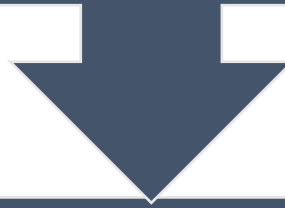
Length = 48



Result: 110000

Step 7 – Attach zeros to the front until it has 64 characters

110000



Result:

[illegible]

Step 8 – Attach
the value from
step 7 to the
binary message
from step 5

Result:

[illegible]

Step 9 – Break up the value into chunks of 512 characters

Result:

[illegible]

Step 10 – Break up the value into smaller chunks of sixteen 32-bit messages

Result:

[illegible]

Step 11 – Loop through each chunk of sixteen 32-bit messages and extend each to 80 messages using bitwise operations.

Part of the Result:

[illegible]

Step 12 – Initialize these variables

Result:

a = 01100111010001010010001100000001

b = 11101111110011011010101110001001

c = 10011000101110101101110011111110

d = 00010000001100100101010001110110

e = 11000011110100101110000111110000

$y = g(x)$

Secant Lines

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$
$$f(x) = \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - x^2}{h}$$
$$= \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - x^2}{h}$$
$$= \lim_{h \rightarrow 0} \frac{2xh + h^2}{h}$$
$$= \lim_{h \rightarrow 0} h(2x + h)$$

Step 13 – loop through the chunks to perform bitwise operations and variable reassignment on the variables

Result:

a = 10001111000011000000100001010101

b = 10010001010101100011001111100100

c = 10100111110111100001100101000110

d = 10001011001110000111010011001000

e = 10010000000111011111000001000011

Step 14 – Convert each of the binary values to hexadecimal

a = 10001111000011000000100001010101

b = 10010001010101100011001111100100

c = 10100111110111100001100101000110

d = 10001011001110000111010011001000

e = 10010000000111011111000001000011

Result:

a = 8f0c0855

b = 915633e4

c = a7de1946

d = 8b3874c8

e = 901df043

Step 15 – Join the hexadecimals to get the final hash value

a = 8f0c0855

b = 915633e4

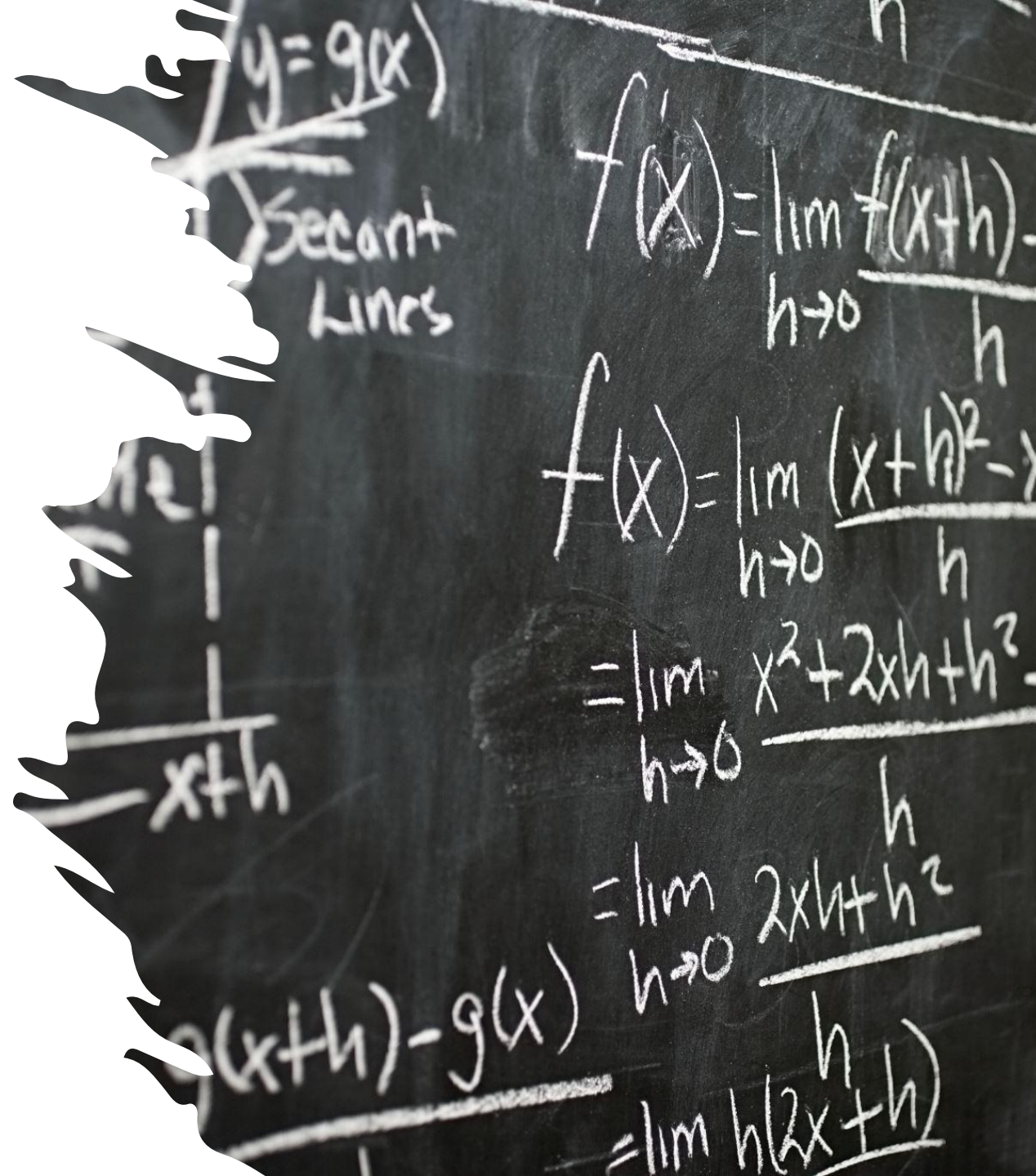
c = a7de1946

d = 8b3874c8

e = 901df043

Final Hash Value:

8f0c0855915633e4a7de19468b3
874c8901df043



Citations

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Thank
you for
listening