| Model         | ResNet1  | 8     | Pretrained on ImageNet |       |             |               |
|---------------|----------|-------|------------------------|-------|-------------|---------------|
| Optimizer     | SGD      | 0.004 |                        |       |             |               |
| Learning rate |          | 0.001 |                        |       |             |               |
| Batch size    |          | 32    |                        |       |             |               |
|               |          |       |                        |       |             |               |
| Method        | Baseline |       |                        |       |             |               |
| <b>Epochs</b> |          | 51    |                        |       |             |               |
| Seed          | Benign   |       | FGSM 8/255 black-box   | AA    | Linf 4/255  | Training time |
|               | 0        | 95.11 |                        | 23.35 | 0           | 5239          |
|               | 1        | 95.13 |                        | 22.18 | 0           | 5225          |
|               | 2        | 95.15 |                        | 23.69 | 0           | 5308          |
|               | 3        | 95.1  |                        | 22.46 | 0           | 5293          |
|               | 4        | 95.01 |                        | 23.76 | 0           | 5282          |
| Mean          |          | 95.1  |                        | 23.09 | 0           | 5269.4        |
| Std           |          | 0.05  |                        | 0.72  | 0           | 35.71         |
|               |          |       |                        |       |             |               |
| Method        | Isoreg   |       |                        |       |             |               |
| Epochs        | isoley   | 51    |                        |       |             |               |
| Lambda        |          | 0.01  |                        |       |             |               |
| Warm-up       | 1 epoch  | 0.01  |                        |       |             |               |
| Epsilon       | т сросп  | 3.5   |                        |       |             |               |
| Norm          | Holder   | 0.0   |                        |       |             |               |
| Seed          | Benign   |       | FGSM 8/255 black-box   | Tra   | aining time |               |
| 3334          | 0        | 21.14 |                        | 20.68 | 25686       |               |
|               | 1        | 10.47 |                        | 11.16 | 24871       |               |
|               | 2        | 12.33 |                        | 10.58 | 24299       |               |
|               | 3        | 17.42 |                        | 12.32 | 24679       |               |
|               | 4        | 69.43 |                        | 33.15 | 25329       |               |
| Mean          |          | 26.16 |                        | 17.58 | 24972.8     |               |
| Std           |          | 24.55 |                        | 9.62  | 544.57      |               |
|               |          |       |                        |       |             |               |
| Method        | Isoreg   |       |                        |       |             |               |
|               | .00.09   |       |                        |       |             |               |

| Epochs<br>Lambda<br>Warm-up<br>Epsilon<br>Norm | 1 epoch<br>Holder | 51<br>0.001<br>3.5 |                                    |             |             |
|--|-------------------|--------------------|------------------------------------|-------------|-------------|
| Seed   | Benign            |                    | FGSM 8/255 black-box               | Tra         | aining time |
|  | 0                 | 94.11              |                                    | 27.31       | 24709       |
|  | 1                 | 94.27              |                                    | 25.95       | 24882       |
|  | 2                 | 94.92              |                                    | 25.44       | 24318       |
|  | 3                 | 94.51              |                                    | 25.5        | 24849       |
|  | 4                 | 94.22              |                                    | 26.32       | 24716       |
| Mean   |                   | 94.41              |                                    | 26.1        | 24694.8     |
| Std  |                   | 0.32               |                                    | 0.76        | 224.42      |
|  |                   |                    |                                    |             |             |
| Method   | Isoreg            |                    |                                    |             |             |
| Epochs   |                   | 51                 |                                    |             |             |
| Lambda   | 1 anaah           | 0.002              |                                    |             |             |
| Warm-up  | 1 epoch           | 3.5                |                                    |             |             |
| Epsilon<br>Norm                                | Holder            | 3.5                |                                    |             |             |
| Seed   | Benign            |                    | FGSM 8/255 black-box               | Trs         | aining time |
| Secu   | 5                 | 93.09              | 1 CSW 6/255 Black-BOX              | 28.27       | 25064       |
|  | 6                 | 94.51              |                                    | 25.59       | 24493       |
|  | 7                 | 93.68              |                                    | 27.78       | 23862       |
|  | 8                 | 94.11              |                                    | 27.65       | 23188       |
|  | 9                 | 93.4               |                                    | 29.38       | 22169       |
| Mean   |                   | 93.76              |                                    | 27.73       | 23755.2     |
| Std  |                   | 0.56               |                                    | 1.38        | 1129.87     |
| Method<br>Epochs                               | Tempera           | ture<br>51         | f_(x) = soft(alpha*s(x)) with alph | na.detach() |             |
| Warm-up  | 3 epoch           | 4                  |                                    |             |             |
| Epsilon  |                   | 1.74               |                                    |             |             |

| Seed           | Benign F |       | FGSM 8/255 black-box | Training time |             |  |
|----------------|----------|-------|----------------------|---------------|-------------|--|
|                | 0        | 92.62 |                      | 24.16         | 24315       |  |
|                | 1        | 92.71 |                      | 25.55         | 24113       |  |
|                | 2        | 92.77 |                      | 25.47         | 22168       |  |
|                | 3        | 91.64 |                      | 22.76         | 22573       |  |
|                | 4        | 92.38 |                      | 26.37         | 23578       |  |
| Mean           |          | 92.42 |                      | 24.86         | 23349.4     |  |
| Std            |          | 0.46  |                      | 1.42          | 944.22      |  |
|                |          |       |                      |               |             |  |
| Method         | Randbou  | ınd   |                      |               |             |  |
| <b>Epochs</b>  |          | 51    |                      |               |             |  |
| Lambda         |          | 0.02  |                      |               |             |  |
| Warm-up        | 1 epoch  |       |                      |               |             |  |
| <b>Epsilon</b> |          | 3.5   |                      |               |             |  |
| Norm           | Holder   |       |                      |               |             |  |
| Seed           | Benign   |       | FGSM 8/255 black-box | Tra           | aining time |  |
|                | 0        | 80    |                      | 20.72         | 9056        |  |
|                | 1        | 81.96 |                      | 18.19         | 9087        |  |
|                | 2        | 81.84 |                      | 19.86         | 8930        |  |
|                | 3        | 82.43 |                      | 21.68         | 9046        |  |
|                | 4        | 80.05 |                      | 19.03         | 9041        |  |
| Mean           |          | 81.26 |                      | 19.9          | 9032        |  |
| Std            |          | 1.15  |                      | 1.37          | 59.75       |  |
|                |          |       |                      |               |             |  |
| Method         | Randbou  | ınd   |                      |               |             |  |
| <b>Epochs</b>  |          | 51    |                      |               |             |  |
| Lambda         |          | 0.005 |                      |               |             |  |
| Warm-up        | 1 epoch  |       |                      |               |             |  |
| <b>Epsilon</b> |          | 3.5   |                      |               |             |  |
| Norm           | Holder   |       |                      |               |             |  |
| Seed           | Benign   |       | FGSM 8/255 black-box |               | aining time |  |
|                | 5        | 91.94 |                      | 23.33         | 9139        |  |
|                | 6        | 93.42 |                      | 23.9          | 9425        |  |

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|               |         |               |                      | Resul          | ts            |
|---------------|---------|---------------|----------------------|----------------|---------------|
|               | 7       | 93.38         |                      | 23.84          | 9166          |
|               | 8       | 93.7          |                      | 24.2           | 9252          |
|               | 9       | 93.22         |                      | 22.33          | 9125          |
| Mean          |         | 93.13         |                      | 23.52          | 9221.4        |
| Std           |         | 0.69          |                      | 0.74           | 124.04        |
|               |         |               |                      |                |               |
| Method        | Gnbound | d             |                      |                |               |
| <b>Epochs</b> |         | 51            |                      |                |               |
| Lambda        |         | 0.005         |                      |                |               |
| Warm-up       | 1 epoch |               |                      |                |               |
| Epsilon       |         | 3.5           |                      |                |               |
| Std           | 16/255  |               |                      |                |               |
| Seed          | Benign  |               | FGSM 8/255 black-box |                | Training time |
|               | 0       | 93.61         |                      | 27.57          | 9418          |
|               | 1       | 93.66         |                      | 27.77          | 9637          |
|               | 2       | 93.16         |                      | 29.36          | 9205          |
|               | 3<br>4  | 93.63         |                      | 27.96          | 9231          |
|               | 4       | 93.37         |                      | 28.98          | 9428          |
| Mean          |         | 93.49         |                      | 28.33          | 9383.8        |
| Std           |         | 0.22          |                      | 0.79           | 175.04        |
| Method        | Gn      |               |                      |                |               |
| Epochs        |         | 51            |                      |                |               |
| Warm-up       | 0 epoch |               |                      |                |               |
| Std           | 8/255   |               |                      |                |               |
| Seed          | Benign  |               | FGSM 8/255 black-box |                | Training time |
|               | 0       | 94.46         |                      | 20.77          | 5414          |
|               | 1<br>2  | 94.47         |                      | 21.13          | 5454          |
|               | 3       | 94.39<br>94.7 |                      | 21.95<br>21.65 | 5427<br>5372  |
|               | 3<br>4  | 94.7<br>94.71 |                      | 21.05          | 5372<br>5254  |
|               | 4       |               |                      |                |               |
| Mean          |         | 94.55         |                      | 21.7           | 5384.2        |
| Std           |         | 0.15          |                      | 0.86           | 78.57         |

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| Method<br>Epochs<br>Warm-up | Gn 51 0 epoch      |       |                     |       |                   |  |  |
|-----------------------------|--------------------|-------|---------------------|-------|-------------------|--|--|
| Std<br>Seed                 | 16/255             | _     | GSM 8/255 black-box | Troi  | ning time         |  |  |
| Seed                        | <b>Benign</b><br>0 | 93.05 | GSW 8/255 DIACK-DOX | 30.46 | ning time<br>5301 |  |  |
|                             | 1                  | 93.05 |                     | 28.66 | 5325              |  |  |
|                             | 2                  | 92.92 |                     | 29.92 | 5395              |  |  |
|                             | 3                  | 92.90 |                     | 28.93 | 5510              |  |  |
|                             | 4                  | 93.18 |                     | 29.85 | 5320              |  |  |
| Mean                        | •                  | 93.01 |                     | 29.56 | 5370.2            |  |  |
| Std                         |                    | 0.11  |                     | 0.75  | 85.89             |  |  |
| <b></b>                     |                    | 0.11  |                     | 0.10  | 00.00             |  |  |
| Method                      | FGSM               |       |                     |       |                   |  |  |
| <b>Epochs</b>               |                    | 51    |                     |       |                   |  |  |
| Warm-up                     | 0 epoch            |       |                     |       |                   |  |  |
| Std                         | 8/255              |       |                     |       |                   |  |  |
| Seed                        | Benign             |       | GSM 8/255 black-box |       | ning time         |  |  |
|                             | 0                  | 61.79 |                     | 61.62 | 8598              |  |  |
|                             | 1                  | 61.28 |                     | 61.59 | 8624              |  |  |
|                             | 2                  | 61.8  |                     | 62.95 | 8777              |  |  |
|                             | 3                  | 65.51 |                     | 67.16 | 8592              |  |  |
|                             | 4                  | 64.99 |                     | 64.74 | 8546              |  |  |
| Mean                        |                    | 63.07 |                     | 63.61 | 8627.4            |  |  |
| Std                         |                    | 2.01  |                     | 2.36  | 88.23             |  |  |
| Method                      | Jacreg             |       |                     |       |                   |  |  |
| <b>Epochs</b>               |                    | 51    |                     |       |                   |  |  |
| Lambda                      |                    | 1000  |                     |       |                   |  |  |
| Warm-up                     | 0 epoch            |       |                     |       |                   |  |  |
| Norm                        | Holder             |       |                     |       |                   |  |  |

| Seed          | Benign      | F     | GSM 8/255 black-box |       | Training time |               |
|---------------|-------------|-------|---------------------|-------|---------------|---------------|
|               | 0           | 95.11 |                     | 23.35 | 24449         |               |
|               | 1           | 95.13 |                     | 22.18 | 23756         |               |
|               | 2           | 95.15 |                     | 23.69 | 24687         |               |
|               | 3           | 95.1  |                     | 22.46 | 24887         |               |
|               | 4           | 95.01 |                     | 23.76 | 24633         |               |
| Mean          |             | 95.1  |                     | 23.09 | 24482.4       |               |
| Std           |             | 0.05  |                     | 0.72  | 435.03        |               |
|               |             |       |                     |       |               |               |
| Method        | Teacher     |       |                     |       |               |               |
| <b>Epochs</b> |             | 51    |                     |       |               |               |
| Temp          |             | 20    |                     |       |               |               |
| Seed          | Benign      | F     | GSM 8/255 black-box |       | Training time |               |
|               | -5          | 94.52 |                     | 23.28 | 5340          |               |
|               | -4          | 94.02 |                     | 28.07 | 5340          |               |
|               | -3          | 94.21 |                     | 25.89 | 5338          |               |
|               | -2          | 94.04 |                     | 27.01 | 5267          | ,             |
|               | -1          | 94.03 |                     | 27.78 | 5212          | •             |
| Mean          |             | 94.16 |                     | 26.41 | 5299.4        |               |
| Std           |             | 0.21  |                     | 1.94  | 58.04         |               |
|               |             |       |                     |       |               |               |
| Method        | Distillatio |       |                     |       |               |               |
| <b>Epochs</b> |             | 51    |                     |       |               |               |
| Temp          |             | 20    |                     |       |               |               |
| Seed          | Benign      |       | GSM 8/255 black-box |       | AA Linf 4/255 | Training time |
|               | 0           | 93.9  |                     | 26.63 | 0             |               |
|               | 1           | 94.13 |                     | 27.39 | 0             |               |
|               | 2           | 94.37 |                     | 25.31 | 0             |               |
|               | 3           | 93.89 |                     | 26.65 | 0             |               |
|               | 4           | 93.95 |                     | 25.34 | 0             |               |
| Mean          |             | 94.05 |                     | 26.26 | 0             |               |
| Std           |             | 0.2   |                     | 0.91  | 0             | 75.59         |