NIOSH - Data Science for Everyone Workshop - Accidents Data Case Study (Python)

Created by Leonid Shpaner for use in **NIOSH - Data Science for Everyone Workshop.** The dataset originates from Data Mining from Business Analytics and is reduced in size as a simplified and introductory module to kickstart the course. The functions and syntax are presented in the most basic format to facilitate ease of use.

The Accidents dataset is presented as a flat .csv file which is comprised of 42,183 recorded automobile accidents from 2001 in the United States. Herein, the following three outcomes are observed: "NO INJURY, INJURY, or FATALITY." Each accident is supplemented with additional information (i.e., day of the week, condition of weather, and road type). This may be of interest to an organization looking to develop "a system for quickly classifying the severity of an accident based on initial reports and associated data in the system (some of which rely on GPS-assisted reporting)" (Shmueli et al., (2018), p. 202).

1. Loading, Pre-Processing, and Exploring Data

Let us get right into working with our dataset, which is to classify the severity of an automobile accident based on existing information.

Make sure the dataset is in the same path as our Python script. If you save the data somewhere else, you need to pass in the full path to where you saved the dataset, e.g. dataset = pd.read_csv('C:/Downloads/dataset.csv').

Let's load the necessary libraries first.

Overview

```
[1]: import pandas as pd
     import numpy as np
     import matplotlib.pyplot as plt
     import seaborn as sns
     from prettytable import PrettyTable
     import statsmodels.api as sm
     from sklearn.model selection import train test split
     from sklearn import metrics
     from sklearn.metrics import roc_curve, auc, mean_squared_error,\
     precision_score, recall_score, f1_score, accuracy_score,\
     confusion_matrix, plot_confusion_matrix, classification_report
     from sklearn.linear_model import LogisticRegression
     from sklearn.tree import DecisionTreeClassifier, export_graphviz
     from sklearn.ensemble import RandomForestClassifier
     import warnings
     warnings.filterwarnings('ignore')
```

Now we proceed to read in the flat .csv file, and examine the first 5 rows of data.

```
[2]: accidents = pd.read_csv('accidentsFull.csv')
```

Now let us inspect the dataset.

```
[3]: accidents.head().T
```

[3]:		0	1	2	3	4
	HOUR_I_R	0	1	1	1	1
	ALCHL_I	2	2	2	2	1
	ALIGN_I	2	1	1	1	1
	STRATUM_R	1	0	0	1	0
	WRK_ZONE	0	0	0	0	0
	WKDY_I_R	1	1	1	0	1
	INT_HWY	0	1	0	0	0
	LGTCON_I_R	3	3	3	3	3
	MANCOL_I_R	0	2	2	2	2
	PED_ACC_R	0	0	0	0	0
	RELJCT_I_R	1	1	1	1	0
	REL_RWY_R	0	1	1	1	1
	PROFIL_I_R	1	1	1	1	1
	SPD_LIM	40	70	35	35	25
	SUR_COND	4	4	4	4	4
	TRAF_CON_R	0	0	1	1	0
	TRAF_WAY	3	3	2	2	2
	VEH_INVL	1	2	2	2	3
	WEATHER_R	1	2	2	1	1
	INJURY_CRASH	1	0	0	0	0
	NO_INJ_I	1	0	0	0	0
	PRPTYDMG_CRASH	0	1	1	1	1
	FATALITIES	0	0	0	0	0
	MAX_SEV_IR	1	0	0	0	0

Data Dictionary

Prior to delving deeper, let us first identify (describe) what each respective variable name really means. To this end, we have the following data dictionary:

- 1. **HOUR_I_R** rush hour classification: 1 = rush hour, 0 = not rush hour (rush hour = 6-9 am, or 4-7 pm)
- 2. $\mathbf{ALCHL}_{\mathbf{I}}$ alcohol involvement: Alcohol involved = 1, alcohol not involved = 2
- 3. **ALIGN_I** road alignment: 1 = straight, 2 = curve
- 4. **STRATUM_R** National Automotive Sampling System stratum: 1 = NASS Crashes involving at least one passenger vehicle (i.e., a passenger car, sport utility Vehicle, pickup truck or van) towed due to damage from the crash scene and no medium or heavy trucks are involved. 0 = not
- 5. WRK ZONE work zone: 1 = yes, 0 = no
- 6. WKDY_I_R weekday or weekend: 1 = weekday, 0 = weekend
- 7. INT_HWY interstate highway: 1 = yes, 0 = no
- 8. **LGTCON_I_R** light conditions 1=day, 2=dark (including dawn/dusk), 3 = dark, but lighted, 4 = dawn or dusk
- 9. MANCOL_I type of collision: 0 = no collision, 1 = head-on, 2 = other form of collision

- 10. PED_ACC_R collision involvement type: 1=pedestrian/cyclist involved, 0=not
- 11. **RELJCT_I_R** whether the collision occurred at intersection: 1=accident at intersection/interchange, 0=not at intersection
- 12. $\mathbf{REL}_{\mathbf{RWY}}$ related to roadway or not: 1 = accident on roadway, 0 = not on roadway
- 13. **PROFIL_I_R** road profile: 1 = level, 0 = other
- 14. **SPD_LIM** speed limit, miles per hour: numeric
- 15. **SUR_CON** surface conditions (1 = dry, 2 = wet, 3 = snow/slush, 4 = ice, 5 = sand/dirt/oil, 8 = other, 9 = unknown)
- 16. **TRAF_CON_R** traffic control device: 0 = none, 1 = signal, 2 = other (sign, officer, . . .)
- 17. $\mathbf{TRAF}_{\mathbf{WAY}}$ traffic type: 1 = two-way traffic, 2 = divided hwy, 3 = one-way road
- 18. **VEH_INVL** vehicle involvement: number of vehicles involved (numeric)
- 19. **WEATHER_R** weather conditions: 1=no adverse conditions, 2=rain, snow or other adverse condition
- 20. INJURY_CRASH injury crash: 1 = yes, 0 = no
- 21. NO_INJ_I number of injuries: numeric
- 22. **PRPTYDMG_CRASH** property damage: 1 = property damage, 2 = no property damage
- 23. **FATALITIES** fatalities: 1 = yes, 0 = no
- 24. MAX SEV IR maximum severity: 0 = no injury, 1 = non-fatal injury, 2 = fatal injury

Initial Pre-Processing Steps

Speed limit (SPD_LIM) has valuable numerical information, so let us go ahead and create buckets for this data.

```
[4]: unique_speed = accidents['SPD_LIM'].unique()
unique_speed.sort()
unique_speed = pd.DataFrame(unique_speed)
unique_speed.T
```

- [4]:

```
accidents[['SPD_LIM', 'MPH Range']]
[5]:
            SPD_LIM MPH Range
     0
                  40
                       40 - 45
                  70
                       70 - 75
     1
     2
                  35
                       30 - 35
     3
                       30 - 35
                  35
     4
                  25
                       20 - 25
     42178
                  45
                       40 - 45
     42179
                  55
                       50 - 55
     42180
                       50 - 55
                  55
     42181
                  65
                       60 - 65
     42182
                  70
                       70 - 75
     [42183 rows x 2 columns]
[6]: accidents['MPH Range'] = accidents['SPD_LIM'].map({5:'5-10', 10:'5-10',
                                                            15: '15-20', 20:'15-20',
                                                            25: '25-30', 30: '25-30',
                                                            35: '35-40', 40: '35-40',
                                                            45: '45-50', 50: '45-50',
                                                            55: '55-60', 60: '55-60',
                                                            65: '65-70', 70: '65-70',
                                                            75: '75'})
     accidents['MPH Range']
[6]: 0
               35-40
     1
               65-70
     2
               35-40
     3
               35-40
     4
               25-30
     42178
               45-50
     42179
               55-60
     42180
               55-60
     42181
               65-70
               65-70
     42182
     Name: MPH Range, Length: 42183, dtype: object
    Next, we create a dummy variable called INJURY to determine if the accident resulted in an injury based
    on maximum severity. So, if the severity of the injury is greater than zero, we specify yes. Otherwise, we
    specify no.
[7]: accidents['INJURY'] = np.where(accidents['MAX_SEV_IR'] > 0, 'yes', 'no')
     accidents.head()
[7]:
        HOUR_I_R
                  ALCHL_I
                            ALIGN_I
                                      STRATUM_R
                                                 WRK_ZONE
                                                            WKDY_I_R
                                                                       INT_HWY
```

0

0

0

0

1

1

1

0

0

1

0

0

1

0

0

1

0

1

2

3

0

1

1

1

2

2

2

2

2

1

1

1

```
4
           1
                     1
                                1
                                            0
                                                        0
                                                                    1
                                                                              0
                 MANCOL_I_R
                              PED_ACC_R
                                              TRAF_WAY
   LGTCON_I_R
                                                          VEH_INVL
                                                                      WEATHER_R
                                           •••
0
             3
                           0
                                        0
                                                       3
                                                                   1
                                                                                1
             3
                           2
                                                       3
                                                                   2
                                                                                2
1
                                        0
2
             3
                           2
                                                       2
                                                                   2
                                                                                2
                                        0
3
             3
                           2
                                                       2
                                                                   2
                                        0
                                                                                1
                           2
             3
                                                       2
                                                                   3
4
                                                                                1
                                                                            MPH Range
                  NO_INJ_I
                              PRPTYDMG_CRASH
                                                 FATALITIES
   INJURY_CRASH
                                                               MAX_SEV_IR
0
                           1
                                              0
                                                            0
                                                                          1
                                                                                  35-40
                1
1
                0
                           0
                                              1
                                                            0
                                                                          0
                                                                                  65-70
2
                           0
                                                                          0
                                                                                  35-40
                0
                                              1
                                                            0
3
                0
                           0
                                              1
                                                            0
                                                                          0
                                                                                  35 - 40
                           0
                                                            0
                                                                          0
4
                                              1
                                                                                  25 - 30
   INJURY
0
      yes
1
       no
2
       no
3
       no
       no
```

[5 rows x 26 columns]

Exploratory Data Analysis

Let us first examine the structure of this dataset so we can gather the details about the size, shape, and values of the dataframe holistically, and each column, respectively.

Number of Rows: 42183 Number of Columns: 26

```
[8]:
        Column/Variable Data Type # of Nulls
                HOUR_I_R
     0
                              int64
                                                0
     1
                 ALCHL_I
                              int64
                                                0
     2
                 ALIGN_I
                                                0
                              int64
               STRATUM_R
                                                0
     3
                              int64
     4
                WRK_ZONE
                              int64
                                                0
```

```
5
           WKDY_I_R
                          int64
                                            0
6
            INT_HWY
                          int64
                                            0
7
        LGTCON_I_R
                          int64
                                            0
8
        MANCOL_I_R
                          int64
                                            0
9
          PED_ACC_R
                                            0
                          int64
         RELJCT_I_R
                                            0
10
                          int64
11
          REL_RWY_R
                          int64
                                            0
12
         PROFIL_I_R
                          int64
                                            0
13
            SPD_LIM
                          int64
                                            0
14
           SUR_COND
                          int64
                                            0
15
         TRAF_CON_R
                          int64
                                            0
           TRAF_WAY
16
                          int64
                                            0
17
           VEH_INVL
                          int64
                                            0
                                            0
18
          WEATHER_R
                          int64
19
      INJURY_CRASH
                          int64
                                            0
20
           NO_INJ_I
                                            0
                          int64
21
    PRPTYDMG_CRASH
                          int64
                                            0
22
         FATALITIES
                          int64
                                            0
                                            0
23
        MAX_SEV_IR
                          int64
24
          MPH Range
                        object
                                            0
                                            0
25
             INJURY
                        object
```

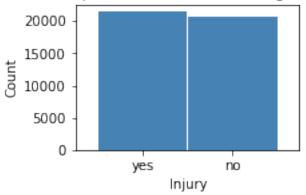
How many accidents resulted in injuries? We create a stylistic pandoc table from the PrettyTable() library to inspect these results.

What percentage of accidents resulted in injuries?

51.0 % of accidents resulted in injuries

A little more than half of the accidents resulted in injuries; thus, we should intrinsically focus our predictions in favor of injuries. However, predictive analytics requires more than merely a cursory glance at first tier probability results. Therefore, we cannot make any assumptions at face value. We will proceed to model this behavior later, but for now let us continue exploring the data.

Bar Graph of Accidents Resulting in Injury



[12]: accidents.dtypes

```
[12]: HOUR_I_R
                          int64
      ALCHL_I
                          int64
                          int64
      ALIGN_I
      STRATUM_R
                          int64
      WRK_ZONE
                          int64
      WKDY_I_R
                          int64
      INT_HWY
                          int64
      LGTCON_I_R
                          int64
      MANCOL_I_R
                          int64
                          int64
      PED_ACC_R
      RELJCT_I_R
                          int64
      REL_RWY_R
                          int64
      PROFIL_I_R
                          int64
                          int64
      SPD_LIM
      SUR_COND
                          int64
      TRAF_CON_R
                          int64
      TRAF_WAY
                          int64
      VEH_INVL
                          int64
                          int64
      WEATHER_R
      INJURY_CRASH
                          int64
      NO_INJ_I
                          int64
      PRPTYDMG_CRASH
                          int64
      FATALITIES
                          int64
      MAX_SEV_IR
                          int64
```

MPH Range object INJURY object

dtype: object

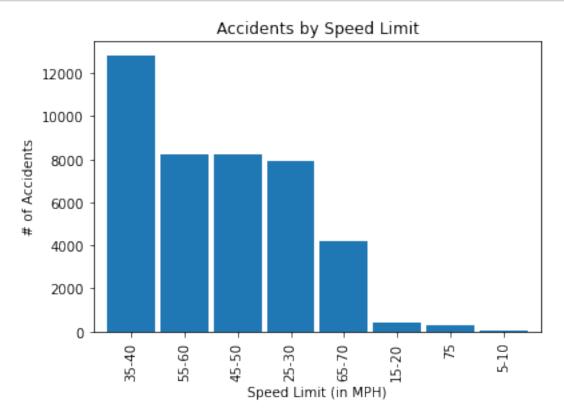
```
[13]: print("\033[1m"+'Injury Outcomes by Miles per Hour'+"\033[1m")
      def INJURY_by_MPH():
          INJURY_yes = accidents.loc[accidents.INJURY == 'yes'].groupby(
                                     ['MPH Range'])[['INJURY']].count()
          INJURY_yes.rename(columns = {'INJURY':'Yes'}, inplace=True)
          INJURY no = accidents.loc[accidents.INJURY == 'no'].groupby(
                                     ['MPH Range'])[['INJURY']].count()
         INJURY_no.rename(columns = {'INJURY':'No'}, inplace=True)
          INJURY_comb = pd.concat([INJURY_yes, INJURY_no], axis = 1)
          # sum row totals
          INJURY_comb['Total'] = INJURY_comb.sum(axis=1)
          INJURY_comb.loc['Total'] = INJURY_comb.sum(numeric_only = True,
                                                     axis=0)
          # get % total of each row
          INJURY_comb['% Injured'] = round((INJURY_comb['Yes'] /
                                            (INJURY comb['Yes']
                                           + INJURY_comb['No']))* 100, 2)
         return INJURY_comb.style.format("{:,.0f}")
      INJURY_by_MPH()
     mph_inj = INJURY_by_MPH().data # retrieve dataframe
     mph_inj
```

Injury Outcomes by Miles per Hour

```
[13]:
                   Yes
                           No Total % Injured
      MPH Range
      15-20
                   182
                          252
                                 434
                                          41.94
      25-30
                                7920
                                          48.84
                  3868
                         4052
      35-40
                  6873
                         5972 12845
                                          53.51
      45-50
                  4168
                         4084
                               8252
                                          50.51
      5-10
                                  28
                                          53.57
                    15
                           13
                  4219
                                          51.13
      55-60
                         4033
                                8252
      65-70
                  1980
                         2189
                                4169
                                          47.49
      75
                   157
                          126
                                 283
                                          55.48
      Total
                 21462 20721 42183
                                          50.88
```

```
[14]: mph_plt = mph_inj['Total'][0:8].sort_values(ascending=False)
mph_plt.plot(kind='bar', width=0.90)
```

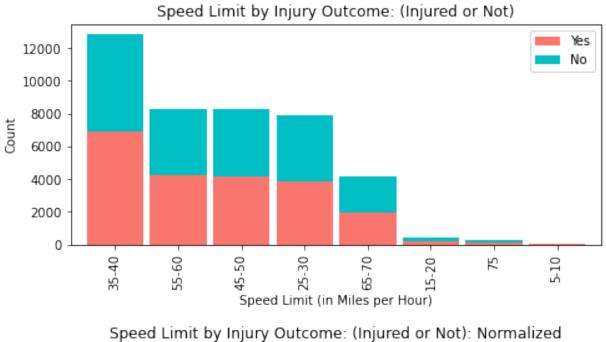
```
plt.title('Accidents by Speed Limit')
plt.xlabel('Speed Limit (in MPH)')
plt.ylabel('# of Accidents')
plt.show()
```

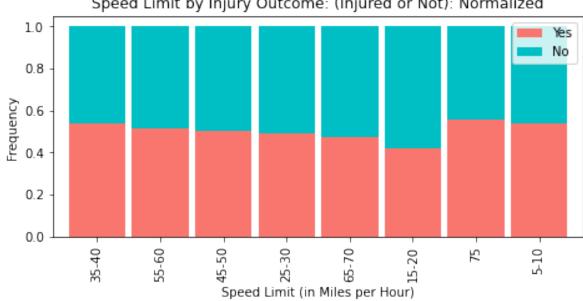


Note. The 35-40 mph speed limit shows the highest prevalence of accidents.

```
[15]: fig = plt.figure(figsize=(8,8))
      ax1 = fig.add_subplot(211)
      ax2 = fig.add_subplot(212)
      fig.tight_layout(pad=6)
      mph_plt2 = mph_inj[['Yes', 'No']][0:8].sort_values(by=['Yes'],
                                                          ascending=False)
      mph_plt2.plot(kind='bar', stacked=True,
                    ax=ax1, color = ['#F8766D', '#00BFC4'], width = 0.90)
      ax1.set_title('Speed Limit by Injury Outcome: (Injured or Not)')
      ax1.set_xlabel('Speed Limit (in Miles per Hour)')
      ax1.set_ylabel('Count')
      # normalize the plot and plot it
      mph_plt_norm = mph_plt2.div(mph_plt2.sum(1), axis = 0)
      mph_plt_norm.plot(kind='bar', stacked=True,
                        ax=ax2,color = ['#F8766D', '#00BFC4'], width = 0.90)
      ax2.set_title('Speed Limit by Injury Outcome: (Injured or Not): Normalized')
      ax2.set_xlabel('Speed Limit (in Miles per Hour)')
```

ax2.set_ylabel('Frequency')
plt.show()





From the speed limit group bar graph overlayed with "injured" and "non-injured" accident results, it is evident that the speed limit of 35-40 mph has a greater incidence of injuries (more than any other speed limit group).

While the strength of this graph is in its depiction of the overall distribution (providing us with injuries vs. non-injuries in each speed related accident), it does little to provide a comparison of the frequency (incidence rate) of injuries among the speed limit groups.

Normalizing the speed limit groups by our target (INJURY) assuages this analysis in such capacity. From here, it is easier to see that speed limits of 5-10 miles per hour, and 35-40 miles per hour, respectively had

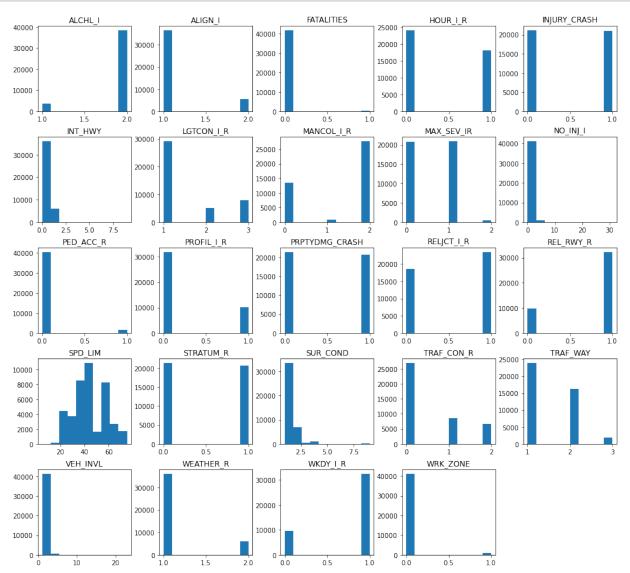
roughly 50% injury rates, whereas (notably), 75 miles per hour exhibited the highest injury rate of all.

Note. There are precisely 12,845 accidents that occurred between the 35-40 mph speed limit. 6,873 (or 53.51%) of them resulted in injuries. Now, let us plot the histogram distributions from each respective variable of the dataset. Figure 3 below visually illustrates these distributions.

Histogram Distributions

```
[16]: # checking for degenerate distributions
accidents.hist(grid=False, figsize=(16,15))

plt.show()
```



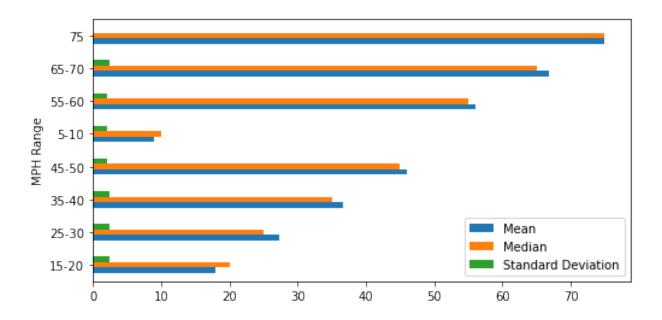
23 out of the original 24 variables are categorical, and thus judging from the histograms presented herein it is possible to uncover degenerate distributions with relative ease, as one category represents higher values over another. However, we look to the speed limit as the sole quantitative predictor which yields a positively skewed distribution.

The following summary statistics corroborate this claim since the mean of 44 is greater than the median of

40.

plt.show()

```
[17]: summ_stats = pd.DataFrame(accidents['SPD_LIM'].describe()).T
      summ_stats
[17]:
                                         std min
                                                     25%
                                                           50%
                                                                 75%
                 count
                             mean
                                                                       max
                                  12.948396 5.0 35.0 40.0 55.0
      SPD_LIM 42183.0 43.547875
                                                                     75.0
     print("\033[1m"+'Accidents by Speed Limit: \
[18]:
      Summary Statistics'+"\033[1m")
      def accident_stats_by_mph():
          pd.options.display.float_format = '{:,.2f}'.format
          new2 = accidents.groupby('MPH Range')['SPD_LIM']\
          .agg(["mean", "median", "std", "min", "max"])
          new2.loc['Total'] = new2.sum(numeric_only=True, axis=0)
          column_rename = {'mean': 'Mean', 'median': 'Median',
                           'std': 'Standard Deviation',\
                           'min':'Minimum','max': 'Maximum'}
          dfsummary = new2.rename(columns = column_rename)
          return dfsummary
      acc_stats_mph = accident_stats_by_mph()
      accident_stats_by_mph()
     Accidents by Speed Limit: Summary Statistics
[18]:
                  Mean Median Standard Deviation Minimum Maximum
      MPH Range
                                              2.47
                                                                20.00
      15-20
                 17.89
                         20.00
                                                       15.00
      25-30
                 27.35
                         25.00
                                              2.50
                                                       25.00
                                                                30.00
                 36.68
                                                       35.00
                                                                40.00
      35-40
                         35.00
                                              2.36
      45-50
                 46.01
                         45.00
                                              2.01
                                                       45.00
                                                                50.00
                 8.93
                         10.00
                                              2.09
                                                       5.00
                                                                10.00
      5-10
      55-60
                         55.00
                                                                60.00
                 56.00
                                              2.00
                                                       55.00
      65-70
                 66.74
                         65.00
                                              2.38
                                                       65.00
                                                                70.00
      75
                 75.00
                         75.00
                                              0.00
                                                       75.00
                                                                75.00
      Total
                334.60 330.00
                                              15.81
                                                      320.00
                                                               355.00
[19]: acc_stats_mph.iloc[:, 0:3][0:8].plot.barh(figsize=(8,4))
```



Selected Boxplot Distribution - Speed Limit

```
[20]: # selected boxplot distributions
     print("\033[1m"+'Boxplot Distribution'+"\033[1m")
      # Boxplot of age as one way of showing distribution
      fig = plt.figure(figsize = (10,1.5))
     plt.title ('Boxplot: Speed Limit')
     plt.xlabel('Speed Limit')
     plt.ylabel('Value')
      sns.boxplot(data=accidents['SPD_LIM'],
                  palette="coolwarm", orient='h',
                  linewidth=2.5)
     plt.show()
     IQR = summ_stats['75%'][0] - summ_stats['25%'][0]
     print('The first quartile is %s. '%summ_stats['25%'][0])
     print('The third quartile is %s. '%summ_stats['75%'][0])
     print('The IQR is %s.'%round(IQR,2))
     print('The mean is %s. '%round(summ_stats['mean'][0],2))
     print('The standard deviation is %s. '%round(summ_stats['std'][0],2))
     print('The median is %s. '%round(summ_stats['50%'][0],2))
```

Boxplot Distribution

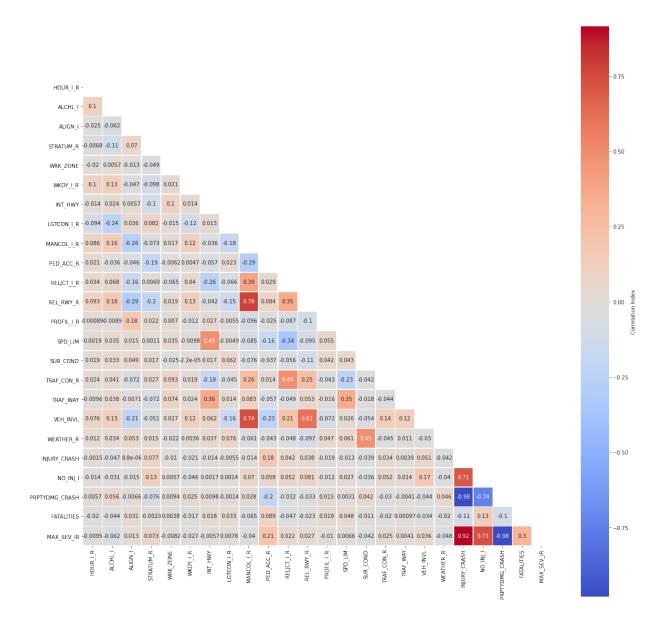


```
The first quartile is 35.0. The third quartile is 55.0. The IQR is 20.0. The mean is 43.55. The standard deviation is 12.95. The median is 40.0.
```

Whereas no outliers are present in the speed limit variable, there exists some skewness where the mean (43.55) is slightly greater than the median (40.00). Whereas typically a Box-Cox transformation could mitigate against skewness by transforming the variable(s) of interest, we will not be making such transformation to avoid misrepresenting the speed limit variable.

Correlation Matrix

Accidents Data: Correlation Matrix



Multicollinearity

Let us narrow our focus by removing highly correlated predictors and passing the rest into a new dataframe.

```
These are the columns we should drop: ['REL_RWY_R', 'PRPTYDMG_CRASH', 'MAX_SEV_IR']
```

```
accidents_1 = accidents_1.drop(to_drop, axis=1)
print(accidents_1.dtypes, '\n')
print('Number of Rows:', accidents_1.shape[0])
print('Number of Columns:', accidents_1.shape[1])
```

```
HOUR_I_R
               int64
ALCHL_I
               int64
ALIGN_I
               int64
STRATUM_R
               int64
WRK_ZONE
               int64
WKDY_I_R
               int64
LGTCON I R
               int64
PED_ACC_R
               int64
RELJCT_I_R
               int64
PROFIL_I_R
               int64
SPD_LIM
               int64
SUR_COND
               int64
TRAF CON R
               int64
VEH_INVL
               int64
WEATHER_R
               int64
dtype: object
```

Number of Rows: 42183 Number of Columns: 15

Additional Pre-Processing

MPH_Range was created strictly for exploratory data analysis purposes. The INJURY column was based off the maximum injury severity column MAX_SEV_IR, so, we will binarize the INJURY column into a new Injured column in lieu of the prior two.

```
[24]: accidents['Injured'] = accidents['INJURY'].map({'yes':1, 'no':0})
```

Furthermore, we must remove the REL_RWY_R, PRPTYDMG_CRASH, and MAX_SEV_IR columns from the dataframe resulting from the inherent between-predictor and predictor-target relationships, respectively. However, there are still a few predictors that warrant subsequent ommission. Number of injuries (NO_INJ_I) and fatalities (FATALATIES) are inherently and intrinsically related to the outcome by virtue of their meaning. Therefore, in order to avoid overfitting the model, we remove them.

```
HOUR_I_R int64
ALCHL_I int64
ALIGN_I int64
STRATUM_R int64
WRK_ZONE int64
WKDY_I_R int64
```

INT_HWY int64 LGTCON_I_R int64 PED_ACC_R int64 RELJCT I R int64 PROFIL_I_R int64 SPD_LIM int64 SUR_COND int64 TRAF_CON_R int64 TRAF_WAY int64 VEH_INVL int64 WEATHER_R int64 Injured int64

dtype: object

Number of Rows: 42183 Number of Columns: 18

Checking for Statistical Significance Via Baseline Model

The logistic regression model is introduced as a baseline because establishing impact of coefficients on each independent feature can be carried with relative ease. Moreover, it is possible to guage statistical significance from the reported p-values of the summary output table below.

Generalized Linear Model - Logistic Regression Baseline

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p + \varepsilon$$

Logistic Regression - Parametric Form

$$p(y) = \frac{\exp(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p)}{1 + \exp(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n)} + \varepsilon$$

Logistic Regression - Descriptive Form

$$\hat{p}(y) = \frac{\exp(b_0 + b_1 x_1 + b_2 x_2 + \dots + b_p x_p)}{1 + \exp(b_0 + b_1 x_1 + b_2 x_2 + \dots + b_p x_p)}$$

```
[26]: X = accidents_1.drop(columns=['Injured'])
X = sm.add_constant(X)
y = pd.DataFrame(accidents_1[['Injured']])
log_results = sm.Logit(y,X, random_state=222).fit()
log_results.summary()
```

Optimization terminated successfully.

Current function value: 0.650360

Iterations 9

[26]: <class 'statsmodels.iolib.summary.Summary'>

Logit Regression Results

Dep. Variable: Injured No. Observations: 42183

Model: Method: Date: Time: converged: Covariance		Logit MLE n, 16 Jan 2022 12:29:40 True nonrobust	E Df Mod Pseudo Log-Li LL-Nul	R-squ.: kelihood:		42165 17 0.06152 -27434. -29233. 0.000
	coef	std err	z	P> z	[0.025	0.975]
const	-0.6001	0.109	-5.510	0.000	-0.814	-0.387
HOUR_I_R	-0.0568	0.021	-2.740	0.006	-0.097	-0.016
ALCHL_I	-0.3613	0.038	-9.428	0.000	-0.436	-0.286
ALIGN_I	0.2351	0.031	7.535	0.000	0.174	0.296
STRATUM_R	0.5008	0.021	24.079	0.000	0.460	0.542
WRK_ZONE	-0.0956	0.069	-1.379	0.168	-0.231	0.040
WKDY_I_R	-0.1037	0.025	-4.207	0.000	-0.152	-0.055
INT_HWY	-0.0227	0.029	-0.786	0.432	-0.079	0.034
LGTCON_I_R	-0.0184	0.014	-1.364	0.173	-0.045	0.008
PED_ACC_R	5.4058	0.260	20.755	0.000	4.895	5.916
RELJCT_I_R	0.0553	0.025	2.169	0.030	0.005	0.105
PROFIL_I_R	-0.0413	0.024	-1.719	0.086	-0.088	0.006
SPD_LIM	0.0080	0.001	8.260	0.000	0.006	0.010
SUR_COND	-0.0384	0.015	-2.558	0.011	-0.068	-0.009
TRAF_CON_R	0.0370	0.016	2.345	0.019	0.006	0.068
TRAF_WAY	0.0060	0.019	0.310	0.757	-0.032	0.044
VEH_INVL	0.3755	0.017	21.759	0.000	0.342	0.409
WEATHER_R	-0.1611	0.033	-4.851	0.000	-0.226	-0.096
========	========	========		:=======	========	=======

11 11 11

From the summary output table, we observe that WRK_ZONE, INT_HWY, LGTCON_I_R, and TRAF_WAY have p-values of 0.168, 0.173, and 0.757, respectively, thereby making these variables statistically significant where = 0.05. We will thus remove them from the refined dataset.

Train_Test_Split

training size: 0.8 test size: 0.2

Training: 33746 Test: 8437 Total: 42183

Model Building Strategies

Logistic Regression

```
[30]: # Un-Tuned Logistic Regression Model
      logit_reg = LogisticRegression(random_state=222)
      logit_reg.fit(X_train, y_train)
      # Predict on test set
      logit_reg_pred1 = logit_reg.predict(X_test)
      # accuracy and classification report
      print('Untuned Logistic Regression Model')
      print('Accuracy Score')
      print(accuracy_score(y_test, logit_reg_pred1))
      print('Classification Report \n',
             classification_report(y_test, logit_reg_pred1))
      # Tuned Logistic Regression Model
      C = [0.01, 0.1, 0.5, 1, 5, 10, 50]
      LRtrainAcc = []
      LRtestAcc = []
      for param in C:
          tuned_lr = LogisticRegression(solver = 'saga',
                                        C = param,
                                        max_iter = 200,
                                        n_{jobs} = -1,
                                        random_state = 222)
          tuned_lr.fit(X_train, y_train)
          # Predict on train set
         tuned_lr_pred_train = tuned_lr.predict(X_train)
          # Predict on test set
          tuned_lr1 = tuned_lr.predict(X_test)
         LRtrainAcc.append(accuracy_score(y_train, tuned_lr_pred_train))
          LRtestAcc.append(accuracy_score(y_test, tuned_lr1))
      # accuracy and classification report
      print('Tuned Logistic Regression Model')
      print('Accuracy Score')
      print(accuracy_score(y_test, tuned_lr1))
      print('Classification Report \n',
             classification_report(y_test, tuned_lr1))
```

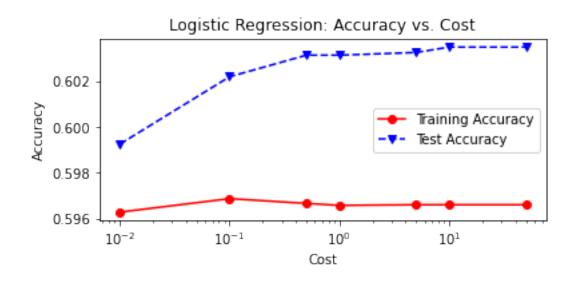
```
# plot cost by accuracy
fig, ax = plt.subplots(figsize=(6,2.5))
ax.plot(C, LRtrainAcc, 'ro-', C, LRtestAcc,'bv--')
ax.legend(['Training Accuracy','Test Accuracy'])
plt.title('Logistic Regression: Accuracy vs. Cost')
ax.set_xlabel('Cost'); ax.set_xscale('log')
ax.set_ylabel('Accuracy'); plt.show()
```

Untuned Logistic Regression Model Accuracy Score 0.6025838568211449 Classification Report

	precision	recall	f1-score	support
0	0.59	0.63	0.61	4200
1	0.61	0.57	0.59	4237
accuracy			0.60	8437
macro avg	0.60	0.60	0.60	8437
weighted avg	0.60	0.60	0.60	8437

Tuned Logistic Regression Model Accuracy Score 0.6035320611591798 Classification Report

	precision	recall	f1-score	support
0	0.60	0.63	0.61	4200
1	0.61	0.58	0.59	4237
accuracy			0.60	8437
macro avg	0.60	0.60	0.60	8437
weighted avg	0.60	0.60	0.60	8437



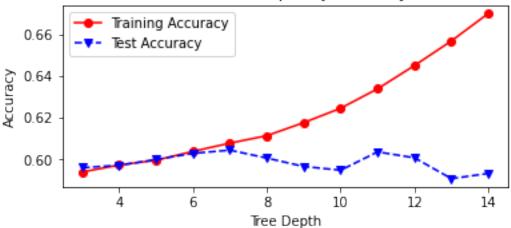
Decision Trees

Before we print the classification report for the un-tuned decision tree, let us establish the optimal maximum depth hyperparameter by varying it in a for-loop as follows:

```
[31]: # Vary the decision tree depth in a loop,
      # increasing depth from 3 to 14.
      accuracy_depth=[]
      for depth in range(3,15):
          varied_tree = DecisionTreeClassifier(max_depth = depth,
                                                random state = 222)
          varied_tree=varied_tree.fit(X_train,y_train)
          tree test pred = varied tree.predict(X test)
          tree_train_pred = varied_tree.predict(X_train)
          accuracy_depth.append({'depth':depth,
                                  'test_accuracy':accuracy_score\
                                  (y_test, tree_test_pred),
                                  'train_accuracy':accuracy_score\
                                  (y_train,tree_train_pred)
          print('Depth = %2.0f \t Test Accuracy = %2.2f \t \
          Training Accuracy = %2.2f'% (depth,accuracy_score\
                                       (y_test, tree_test_pred),
                                        accuracy_score(y_train,
                                        tree_train_pred)))
      abd df = pd.DataFrame(accuracy depth)
      abd_df.index = abd_df['depth']
      # plot tree depth by accuracy
      fig, ax=plt.subplots(figsize=(6,2.5))
      ax.plot(abd_df.depth,abd_df.train_accuracy,
              'ro-',label='Training Accuracy')
      ax.plot(abd_df.depth,abd_df.test_accuracy,
              'bv--',label='Test Accuracy')
      plt.title('Varied Tree Depth by Accuracy')
      ax.set_xlabel('Tree Depth')
      ax.set_ylabel('Accuracy')
      plt.legend()
      plt.show()
```

```
Training Accuracy = 0.60
Depth =
                 Test Accuracy = 0.60
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.61
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.61
Depth = 9
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.62
Depth = 10
                 Test Accuracy = 0.59
                                              Training Accuracy = 0.62
Depth = 11
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.63
Depth = 12
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.64
Depth = 13
                 Test Accuracy = 0.59
                                              Training Accuracy = 0.66
                                              Training Accuracy = 0.67
Depth = 14
                 Test Accuracy = 0.59
```

Varied Tree Depth by Accuracy



The optimal maximum depth exists where test and training accuracy are both highest (60% and 64%, respectively). This is where depth is equal to 12. Now we can print the classification reports for both the un-tuned and tuned models, noting some improvement in performance.

```
[32]: # Untuned Decision Tree Classifier
      untuned_tree = DecisionTreeClassifier(random_state=222)
      untuned_tree = untuned_tree.fit(X_train, y_train)
      # Predict on test set
      untuned_tree1 = untuned_tree.predict(X_test)
      # accuracy and classification report
      print('Untuned Decision Tree Classifier')
      print('Accuracy Score')
      print(accuracy_score(y_test, untuned_tree1))
      print('Classification Report \n',
             classification_report(y_test, untuned_tree1))
      # Tuned Decision Tree Classifier
      tuned tree = DecisionTreeClassifier(max depth = 12,
                                          random_state=222)
      tuned_tree = tuned_tree.fit(X_train, y_train)
      # Predict on test set
      tuned_tree1 = tuned_tree.predict(X_test)
```

Untuned Decision Tree Classifier Accuracy Score 0.5661965153490577

Classification Report

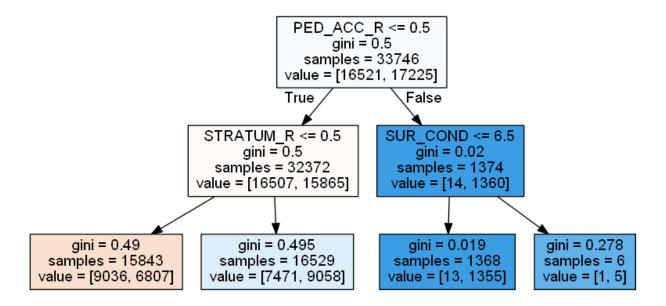
	precision	recall	f1-score	support
0	0.56	0.61	0.58	4200
1	0.58	0.52	0.55	4237
accuracy			0.57	8437
macro avg	0.57	0.57	0.57	8437
weighted avg	0.57	0.57	0.57	8437

Tuned Decision Tree Classifier Accuracy Score 0.6008059736873296

Classification Report

	precision	recall	f1-score	support
0	0.59	0.63	0.61	4200
1	0.61	0.57	0.59	4237
accuracy			0.60	8437
macro avg	0.60	0.60	0.60	8437
weighted avg	0.60	0.60	0.60	8437

[33]:

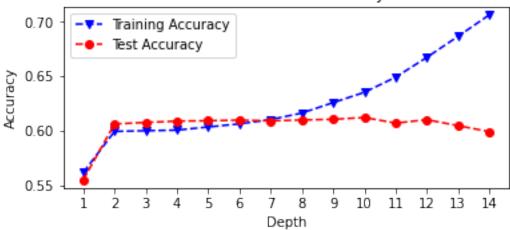


Random Forest Classifier

```
[34]: # Random Forest Tuning
      rf_train_accuracy = []
      rf_test_accuracy = []
      for n in range(1, 15):
          rf = RandomForestClassifier(max_depth = n,
                                      random_state=222)
         rf = rf.fit(X_train, y_train)
          rf_pred_train = rf.predict(X_train)
          rf_pred_test = rf.predict(X_test)
         rf_train_accuracy.append(accuracy_score(y_train,
                                                   rf_pred_train))
         rf_test_accuracy.append(accuracy_score(y_test,
                                                   rf_pred_test))
          print('Max Depth = %2.0f \t Test Accuracy = %2.2f \t \
          Training Accuracy = %2.2f'% (n, accuracy_score(y_test,
                                                         rf pred test),
                                     accuracy_score(y_train,
                                                    rf_pred_train)))
      max_depth = list(range(1, 15))
      fig, plt.subplots(figsize=(6,2.5))
      plt.plot(max_depth, rf_train_accuracy, 'bv--',
               label='Training Accuracy')
      plt.plot(max_depth, rf_test_accuracy, 'ro--',
               label='Test Accuracy')
      plt.title('Random Forest Accuracy')
      plt.xlabel('Depth')
      plt.ylabel('Accuracy')
      plt.xticks(max_depth)
      plt.legend()
      plt.show()
```

```
Training Accuracy = 0.56
Max Depth = 1
                 Test Accuracy = 0.56
Max Depth = 2
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.60
Max Depth = 3
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.60
Max Depth = 4
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.60
Max Depth = 5
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.60
Max Depth = 6
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.61
Max Depth = 7
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.61
Max Depth = 8
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.62
                                             Training Accuracy = 0.63
Max Depth = 9
                 Test Accuracy = 0.61
Max Depth = 10
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.64
Max Depth = 11
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.65
Max Depth = 12
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.67
Max Depth = 13
                 Test Accuracy = 0.60
                                             Training Accuracy = 0.69
Max Depth = 14
                                             Training Accuracy = 0.71
                 Test Accuracy = 0.60
```

Random Forest Accuracy



Untuned Random Forest Model Accuracy Score 0.5749674054758801 Classification Report

	precision	recall	f1-score	support
0	0.57	0.58	0.58	4200
1	0.58	0.57	0.57	4237
accuracy			0.57	8437
macro avg	0.58	0.57	0.57	8437
weighted avg	0.58	0.57	0.57	8437

Tuned Random Forest Model Accuracy Score 0.6104065426099324

Classification Report

	precision	recall	f1-score	support
0	0.60	0.63	0.62	4200
1	0.62	0.59	0.60	4237
accuracy			0.61	8437
macro avg	0.61	0.61	0.61	8437
weighted avg	0.61	0.61	0.61	8437

Model Evaluation

Confusion Matrices

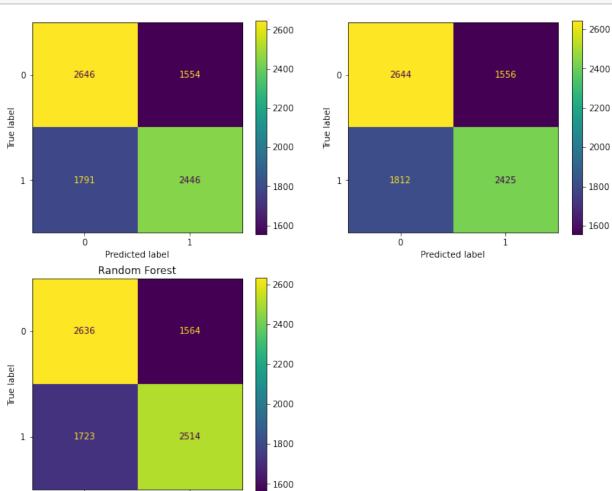
```
[36]: fig = plt.figure(figsize=(12,10))
    ax1 = fig.add_subplot(221)
    ax2 = fig.add_subplot(222)
    ax3 = fig.add_subplot(223)

# logistic regression confusion matrix
    plot_confusion_matrix(tuned_lr, X_test, y_test, ax=ax1)
    plt.title('Logistic Regression')

# Decision tree confusion matrix
    plot_confusion_matrix(tuned_tree, X_test, y_test, ax=ax2)
```

```
plt.title('Decision Tree')

# random forest confusion matrix
plot_confusion_matrix(tuned_rf, X_test, y_test, ax=ax3)
plt.title('Random Forest')
plt.show()
```



ROC Curves

Ó

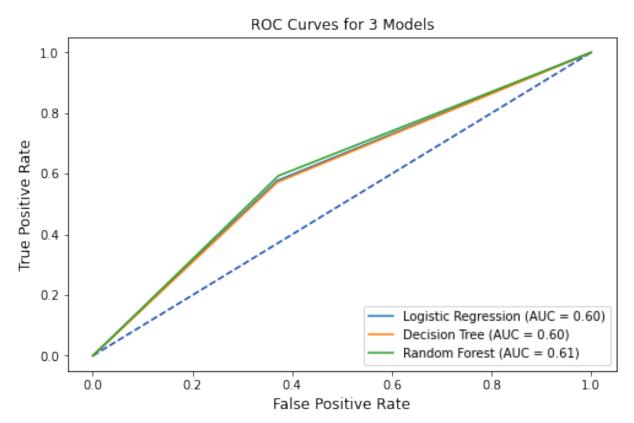
Predicted label

```
[47]: # plot all of the roc curves on one graph
    tuned_lr_roc = metrics.roc_curve(y_test,tuned_lr1)
    fpr,tpr,thresholds = metrics.roc_curve(y_test,tuned_lr1)
    tuned_lr_auc = metrics.auc(fpr, tpr)
    tuned_lr_plot = metrics.RocCurveDisplay(fpr=fpr,tpr=tpr,
    roc_auc = tuned_lr_auc,
    estimator_name = 'Logistic Regression')

tuned_tree_roc = metrics.roc_curve(y_test,tuned_tree1)
    fpr,tpr,thresholds = metrics.roc_curve(y_test,tuned_tree1)
```

i

```
tuned_tree_auc = metrics.auc(fpr, tpr)
tuned_tree_plot = metrics.RocCurveDisplay(fpr=fpr,tpr=tpr,
roc_auc=tuned_tree_auc,
estimator_name = 'Decision Tree')
tuned_rf1_roc = metrics.roc_curve(y_test, tuned_rf1)
fpr,tpr,thresholds = metrics.roc_curve(y_test,tuned_rf1)
tuned_rf1_auc = metrics.auc(fpr, tpr)
tuned_rf1_plot = metrics.RocCurveDisplay(fpr=fpr,tpr=tpr,
roc_auc=tuned_rf1_auc,
estimator_name = 'Random Forest')
# plot set up
fig, ax = plt.subplots(figsize=(8,5))
plt.title('ROC Curves for 3 Models',fontsize=12)
plt.plot([0, 1], [0, 1], linestyle = '--',
         color = '#174ab0')
plt.xlabel('',fontsize=12)
plt.ylabel('',fontsize=12)
# Model ROC Plots Defined above
tuned_lr_plot.plot(ax)
tuned_tree_plot.plot(ax)
tuned_rf1_plot.plot(ax)
plt.show()
```



Performance Metrics

```
[39]: # Logistic Regression Performance Metrics
     report1 = classification_report(y_test,tuned_lr1,
     output_dict=True)
     accuracy1 = round(report1['accuracy'],4)
     precision1 = round(report1['1']['precision'],4)
     recall1 = round(report1['1']['recall'],4)
     fl_score1 = round(report1['1']['f1-score'],4)
     # Decision Tree Performance Metrics
     report2 = classification_report(y_test,tuned_tree1,
     output dict=True)
     accuracy2 = round(report2['accuracy'],4)
     precision2 = round(report2['1']['precision'],4)
     recall2 = round(report2['1']['recall'],4)
     fl_score2 = round(report2['1']['f1-score'],4)
     # Random Forest Performance Metrics
     report3 = classification_report(y_test,tuned_rf1,
     output_dict=True)
     accuracy3 = round(report3['accuracy'],4)
     precision3 = round(report3['1']['precision'],4)
     recall3 = round(report3['1']['recall'],4)
     fl_score3 = round(report3['1']['f1-score'],4)
[40]: table1 = PrettyTable()
     table1.field names = ['Model', 'Test Accuracy',
                         'Precision', 'Recall',
                         'F1-score']
     table1.add_row(['Logistic Regression', accuracy1,
                    precision1, recall1, fl_score1])
     table1.add_row(['Decision Tree', accuracy2,
                    precision2, recall2, fl_score2])
     table1.add_row(['Random Forest', accuracy3,
                    precision3, recall3, fl_score3])
     print(table1)
     ______
                       | Test Accuracy | Precision | Recall | F1-score |
     +----+
    | Logistic Regression | 0.6035 | 0.6115 | 0.5773 | 0.5939 | Decision Tree | 0.6008 | 0.6091 | 0.5723 | 0.5902 |
         Random Forest
                              0.6104 | 0.6165 | 0.5933 | 0.6047 |
     +----+
[42]: # Mean-Squared Errors
     mse1 = round(mean_squared_error(y_test, tuned_lr1),4)
     mse2 = round(mean_squared_error(y_test, tuned_tree1),4)
     mse3 = round(mean_squared_error(y_test, tuned_rf1),4)
     table2 = PrettyTable()
```

+	Model	-+- -+-	AUC	-+- -	MSE	-+ -+
	Logistic Regression Decision Tree	١	0.6009		0.3992	1
+-	Random Forest	 -	0.6105 	 -	0.3896 	 -+