# NIOSH - Data Science for Everyone Workshop - Accidents Data Case Study (Python)

Created by Leonid Shpaner for use in **NIOSH - Data Science for Everyone Workshop.** The dataset originates for Data Mining from Business Analytics (Shmueli et., 2018). The functions and syntax are presented in the most basic format to facilitate ease of use.

The Accidents dataset is presented as a flat .csv file which is comprised of 42,183 recorded automobile accidents from 2001 in the United States. The following three outcomes are observed: "NO INJURY, INJURY, or FATALITY." Each accident is supplemented with additional information (i.e., day of the week, condition of weather, and road type). This may be of interest to an organization looking to develop "a system for quickly classifying the severity of an accident based on initial reports and associated data in the system (some of which rely on GPS-assisted reporting)" (Shmueli et al., 2018, p. 202).

# 1. Loading, Pre-Processing, and Exploring Data

Let's make sure the dataset is in the same path as our Python script. If you save the data somewhere else, you need to pass in the full path to where you saved the dataset, e.g. dataset = pd.read\_csv('C:/Downloads/dataset.csv').

Let's install the necessary libraries first, uncommenting (removing the # symbol) in front of the commands in the cell blocks, and then running them, respectively.

```
[1]: # pip install pandas; pip install statsmodels; pip install sklearn
```

```
[2]: # pip install pydotplus; pip install prettytable
```

Now, let's load these necessary libraries as follows:

```
[3]: import pandas as pd
     import numpy as np
     import matplotlib.pyplot as plt
     import seaborn as sns
     from prettytable import PrettyTable
     import statsmodels.api as sm
     from sklearn.model_selection import train_test_split
     from sklearn import metrics
     from sklearn.metrics import roc_curve, auc, mean_squared_error,\
     precision_score, recall_score, f1_score, accuracy_score,\
     confusion matrix, plot confusion matrix, classification report
     from sklearn.linear_model import LogisticRegression
     from sklearn.tree import DecisionTreeClassifier, export graphviz
     from sklearn.ensemble import RandomForestClassifier
     import warnings
     warnings.filterwarnings('ignore')
```

Now, we proceed to read in the flat .csv file, and examine the first 4 rows of data.

```
[4]: url = 'https://raw.githubusercontent.com/lshpaner/data_science_\
for_everyone/main/Case%20Study/accidentsFull.csv'
accidents = pd.read_csv(url)
```

Now let's inspect the dataset.

```
[5]: accidents.head(4)
```

| [5]: | HOUR_I_R  | ALCHL_I   | ALIGN_I  | STRATU | M_R | WRK_ZON  | E WKDY_I_R    | INT_HWY   | \   |   |
|------|-----------|-----------|----------|--------|-----|----------|---------------|-----------|-----|---|
| 0    | 0         | 2         | 2        |        | 1   |          | 0 1           | 0         |     |   |
| 1    | 1         | 2         | 1        |        | 0   |          | 0 1           | 1         |     |   |
| 2    | 1         | 2         | 1        |        | 0   |          | 0 1           | 0         |     |   |
| 3    | 1         | 2         | 1        |        | 1   |          | 0 0           | 0         |     |   |
|      | LGTCON_I_ | R MANCOL_ | _I_R PED | _ACC_R |     | SUR_COND | TRAF_CON_R    | TRAF_WAY  | \   |   |
| 0    |           | 3         | 0        | 0      |     | 4        | 0             | 3         |     |   |
| 1    |           | 3         | 2        | 0      |     | 4        | 0             | 3         |     |   |
| 2    |           | 3         | 2        | 0      |     | 4        | 1             | 2         |     |   |
| 3    |           | 3         | 2        | 0      | ••• | 4        | 1             | 2         |     |   |
|      | VEH_INVL  | WEATHER_F | R INJURY | _CRASH | NO_ | _INJ_I P | RPTYDMG_CRASI | H FATALIT | IES | \ |
| 0    | 1         | 1         | <u>[</u> | 1      |     | 1        | (             | )         | 0   |   |
| 1    | 2         | 2         | 2        | 0      |     | 0        | :             | L         | 0   |   |
| 2    | 2         | 2         | 2        | 0      |     | 0        |               | L         | 0   |   |
| 3    | 2         | 1         | L        | 0      |     | 0        |               | L         | 0   |   |
|      | MAX_SEV_I | R         |          |        |     |          |               |           |     |   |
| 0    |           | 1         |          |        |     |          |               |           |     |   |

0 1

2 0

3 0

[4 rows x 24 columns]

## **Data Dictionary**

Prior to delving deeper, let us first identify (describe) what each respective variable name really means. To this end, we have the following data dictionary:

- 1. **HOUR\_I\_R** rush hour classification: 1 = rush hour, 0 = not rush hour (rush hour = 6-9 am, or 4-7 pm)
- 2.  $\mathbf{ALCHL}_{\mathbf{I}}$  alcohol involvement: Alcohol involved = 1, alcohol not involved = 2
- 3. **ALIGN\_I** road alignment: 1 = straight, 2 = curve
- 4. **STRATUM\_R** National Automotive Sampling System stratum: 1 = NASS Crashes involving at least one passenger vehicle (i.e., a passenger car, sport utility Vehicle, pickup truck or van) towed due to damage from the crash scene and no medium or heavy trucks are involved. 0 = not
- 5. WRK ZONE work zone: 1 = yes, 0 = no
- 6. WKDY\_I\_R weekday or weekend: 1 = weekday, 0 = weekend
- 7. INT\_HWY interstate highway: 1 = yes, 0 = no
- 8. **LGTCON\_I\_R** light conditions 1=day, 2=dark (including dawn/dusk), 3 = dark, but lighted, 4 = dawn or dusk
- 9. MANCOL\_I type of collision: 0 = no collision, 1 = head-on, 2 = other form of collision

- 10. PED\_ACC\_R collision involvement type: 1=pedestrian/cyclist involved, 0=not
- 11. **RELJCT\_I\_R** whether the collision occurred at intersection: 1=accident at intersection/interchange, 0=not at intersection
- 12.  $\mathbf{REL}_{\mathbf{RWY}}$  related to roadway or not: 1 = accident on roadway, 0 = not on roadway
- 13. **PROFIL** I  $\mathbf{R}$  road profile: 1 = level, 0 = other
- 14. **SPD\_LIM** speed limit, miles per hour: numeric
- 15. **SUR\_CON** surface conditions (1 = dry, 2 = wet, 3 = snow/slush, 4 = ice, 5 = sand/dirt/oil, 8 = other, 9 = unknown)
- 16. **TRAF\_CON\_R** traffic control device: 0 = none, 1 = signal, 2 = other (sign, officer, . . . )
- 17.  $\mathbf{TRAF}_{\mathbf{WAY}}$  traffic type: 1 = two-way traffic, 2 = divided hwy, 3 = one-way road
- 18. **VEH INVL** vehicle involvement: number of vehicles involved (numeric)
- 19. **WEATHER\_R** weather conditions: 1=no adverse conditions, 2=rain, snow or other adverse condition
- 20. INJURY\_CRASH injury crash: 1 = yes, 0 = no
- 21. NO\_INJ\_I number of injuries: numeric
- 22. **PRPTYDMG\_CRASH** property damage: 1 = property damage, 2 = no property damage
- 23. **FATALITIES** fatalities: 1 = yes, 0 = no
- 24. MAX SEV IR maximum severity: 0 = no injury, 1 = non-fatal injury, 2 = fatal injury

## **Initial Pre-Processing Steps**

Speed limit (SPD\_LIM) has valuable numerical information, so let us go ahead and create buckets for this data.

```
[6]: unique_speed = accidents['SPD_LIM'].unique()
unique_speed.sort()
unique_speed = pd.DataFrame(unique_speed)
unique_speed.T
```

- [6]:

```
accidents[['SPD_LIM', 'MPH Range']]
[7]:
            SPD_LIM MPH Range
     0
                  40
                       40 - 45
                  70
                       70 - 75
     1
     2
                  35
                       30 - 35
     3
                       30 - 35
                  35
     4
                  25
                       20 - 25
     42178
                  45
                       40 - 45
     42179
                  55
                       50 - 55
     42180
                       50 - 55
                  55
     42181
                  65
                       60 - 65
     42182
                  70
                       70 - 75
     [42183 rows x 2 columns]
[8]: accidents['MPH Range'] = accidents['SPD_LIM'].map({5:'5-10', 10:'5-10',
                                                            15: '15-20', 20:'15-20',
                                                            25: '25-30', 30: '25-30',
                                                            35: '35-40', 40: '35-40',
                                                            45: '45-50', 50: '45-50',
                                                            55: '55-60', 60: '55-60',
                                                            65: '65-70', 70: '65-70',
                                                            75: '75'})
     accidents['MPH Range']
[8]: 0
               35-40
     1
               65-70
     2
               35-40
     3
               35-40
     4
               25-30
     42178
               45-50
     42179
               55-60
     42180
               55-60
     42181
               65-70
               65-70
     42182
     Name: MPH Range, Length: 42183, dtype: object
    Next, we create a dummy variable called INJURY to determine if the accident resulted in an injury based
    on maximum severity. So, if the severity of the injury is greater than zero, we specify yes. Otherwise, we
    specify no.
[9]: | accidents['INJURY'] = np.where(accidents['MAX_SEV_IR'] > 0, 'yes', 'no')
     accidents.head()
[9]:
        HOUR_I_R
                  ALCHL_I
                            ALIGN_I
                                      STRATUM_R
                                                  WRK_ZONE
                                                             WKDY_I_R
                                                                       INT_HWY
     0
                0
                         2
                                   2
                                               1
                                                          0
                                                                    1
                                                                              0
```

0

0

0

1

1

0

1

0

0

0

0

1

1

2

3

1

1

1

2

2

2

1

1

1

```
4
           1
                     1
                                1
                                             0
                                                         0
                                                                    1
                                                                               0
                 MANCOL_I_R
                              PED_ACC_R
                                              TRAF_WAY
   LGTCON_I_R
                                                           VEH_INVL
                                                                      WEATHER_R
                                           •••
0
             3
                           0
                                        0
                                                       3
                                                                   1
                                                                                1
             3
                           2
                                                        3
                                                                   2
                                                                                2
1
                                        0
2
             3
                           2
                                                        2
                                                                   2
                                                                                2
                                        0
             3
                            2
                                                        2
                                                                   2
3
                                        0
                                                                                1
             3
                           2
                                                        2
                                                                   3
4
                                                                                1
                  NO_INJ_I
                              PRPTYDMG_CRASH
                                                 FATALITIES
                                                                            MPH Range
   INJURY_CRASH
                                                               MAX_SEV_IR
0
                            1
                                                            0
                                                                          1
                                                                                  35-40
                1
                                              0
                0
                           0
                                              1
                                                            0
                                                                          0
                                                                                  65-70
1
2
                           0
                                                                          0
                                                                                  35-40
                0
                                              1
                                                            0
3
                0
                           0
                                              1
                                                            0
                                                                          0
                                                                                  35 - 40
                           0
                                                            0
                                                                          0
4
                                                                                  25 - 30
   INJURY
0
      yes
1
       no
2
       no
3
       no
       no
```

[5 rows x 26 columns]

# **Exploratory Data Analysis**

Let us first examine the structure of this dataset so we can gather the details about the size, shape, and values of the dataframe holistically, and each column, respectively.

Number of Rows: 42183 Number of Columns: 26

```
[10]:
         Column/Variable Data Type # of Nulls
      0
                 HOUR_I_R
                               int64
                                                 0
      1
                  ALCHL_I
                               int64
                                                 0
      2
                  ALIGN_I
                                                 0
                               int64
      3
                STRATUM_R
                                                 0
                               int64
      4
                 WRK_ZONE
                               int64
                                                 0
```

```
5
           WKDY_I_R
                          int64
                                            0
6
            INT_HWY
                          int64
                                            0
7
        LGTCON_I_R
                          int64
                                            0
8
        MANCOL_I_R
                          int64
                                            0
9
          PED_ACC_R
                                            0
                          int64
         RELJCT_I_R
                                            0
10
                          int64
11
          REL_RWY_R
                          int64
                                            0
12
         PROFIL_I_R
                          int64
                                            0
13
            SPD_LIM
                          int64
                                            0
14
           SUR_COND
                          int64
                                            0
15
         TRAF_CON_R
                          int64
                                            0
           TRAF_WAY
16
                          int64
                                            0
17
           VEH_INVL
                          int64
                                            0
                                            0
18
          WEATHER_R
                          int64
19
      INJURY_CRASH
                          int64
                                            0
20
           NO_INJ_I
                                            0
                          int64
21
    PRPTYDMG_CRASH
                          int64
                                            0
22
         FATALITIES
                          int64
                                            0
                                            0
23
        MAX_SEV_IR
                          int64
24
                         object
                                            0
          MPH Range
                                            0
25
             INJURY
                         object
```

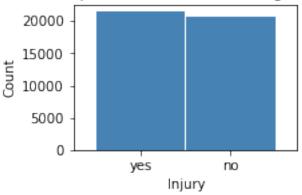
How many accidents resulted in injuries? We create a stylistic pandoc table from the PrettyTable() library to inspect these results.

What percentage of accidents resulted in injuries?

#### 51.0 % of accidents resulted in injuries

A little more than half of the accidents resulted in injuries; thus, we should intrinsically focus our predictions in favor of injuries. However, predictive analytics requires more than merely a cursory glance at first tier probability results. Therefore, we cannot make any assumptions at face value. We will proceed to model this behavior later, but for now let us continue exploring the data.

# Bar Graph of Accidents Resulting in Injury



## [14]: accidents.dtypes

```
[14]: HOUR_I_R
                          int64
      ALCHL_I
                          int64
                          int64
      ALIGN_I
      STRATUM_R
                          int64
      WRK_ZONE
                          int64
      WKDY_I_R
                          int64
      INT_HWY
                          int64
      LGTCON_I_R
                          int64
      MANCOL_I_R
                          int64
                          int64
      PED_ACC_R
      RELJCT_I_R
                          int64
      REL_RWY_R
                          int64
      PROFIL_I_R
                          int64
                          int64
      SPD_LIM
      SUR_COND
                          int64
      TRAF_CON_R
                          int64
      TRAF_WAY
                          int64
      VEH_INVL
                          int64
                          int64
      WEATHER_R
      INJURY_CRASH
                          int64
      NO_INJ_I
                          int64
      PRPTYDMG_CRASH
                          int64
      FATALITIES
                          int64
      MAX_SEV_IR
                          int64
```

MPH Range object INJURY object

dtype: object

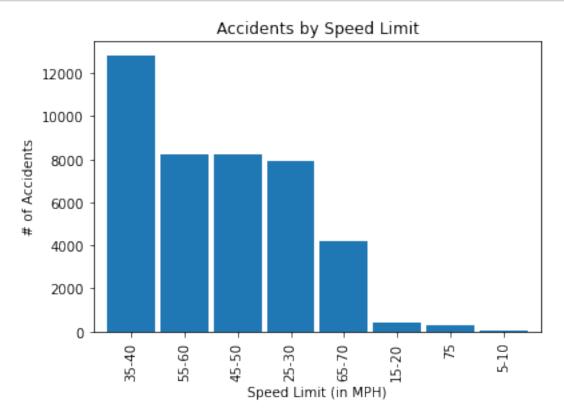
```
[15]: print("\033[1m"+'Injury Outcomes by Miles per Hour'+"\033[1m")
      def INJURY_by_MPH():
          INJURY_yes = accidents.loc[accidents.INJURY == 'yes'].groupby(
                                     ['MPH Range'])[['INJURY']].count()
          INJURY_yes.rename(columns = {'INJURY':'Yes'}, inplace=True)
          INJURY no = accidents.loc[accidents.INJURY == 'no'].groupby(
                                     ['MPH Range'])[['INJURY']].count()
         INJURY_no.rename(columns = {'INJURY':'No'}, inplace=True)
          INJURY_comb = pd.concat([INJURY_yes, INJURY_no], axis = 1)
          # sum row totals
          INJURY_comb['Total'] = INJURY_comb.sum(axis=1)
          INJURY_comb.loc['Total'] = INJURY_comb.sum(numeric_only = True,
                                                     axis=0)
          # get % total of each row
          INJURY_comb['% Injured'] = round((INJURY_comb['Yes'] /
                                            (INJURY comb['Yes']
                                           + INJURY_comb['No']))* 100, 2)
         return INJURY_comb.style.format("{:,.0f}")
      INJURY_by_MPH()
     mph_inj = INJURY_by_MPH().data # retrieve dataframe
     mph_inj
```

#### Injury Outcomes by Miles per Hour

```
[15]:
                   Yes
                           No Total % Injured
      MPH Range
      15-20
                   182
                          252
                                 434
                                          41.94
      25-30
                                7920
                                          48.84
                  3868
                         4052
      35-40
                  6873
                         5972 12845
                                          53.51
      45-50
                  4168
                         4084
                               8252
                                          50.51
      5-10
                                  28
                                          53.57
                    15
                           13
                  4219
                                          51.13
      55-60
                         4033
                                8252
      65-70
                  1980
                         2189
                                4169
                                          47.49
      75
                   157
                          126
                                 283
                                          55.48
      Total
                 21462 20721 42183
                                          50.88
```

```
[16]: mph_plt = mph_inj['Total'][0:8].sort_values(ascending=False)
mph_plt.plot(kind='bar', width=0.90)
```

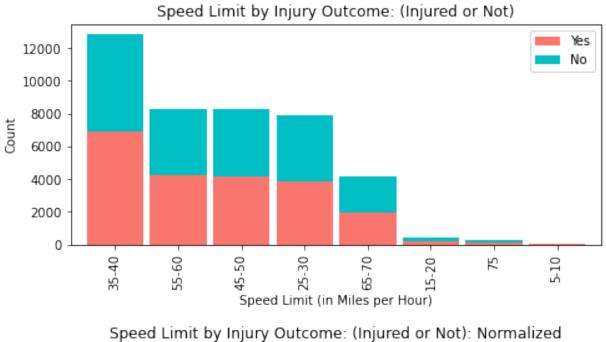
```
plt.title('Accidents by Speed Limit')
plt.xlabel('Speed Limit (in MPH)')
plt.ylabel('# of Accidents')
plt.show()
```

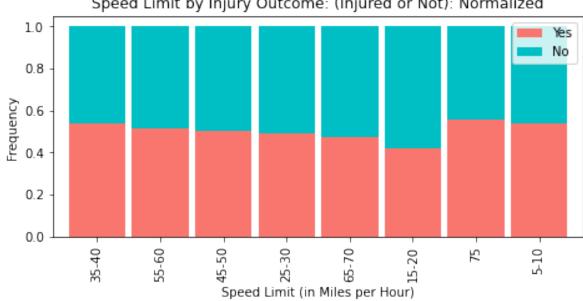


**Note.** The 35-40 mph speed limit shows the highest prevalence of accidents.

```
[17]: fig = plt.figure(figsize=(8,8))
      ax1 = fig.add_subplot(211)
      ax2 = fig.add_subplot(212)
      fig.tight_layout(pad=6)
      mph_plt2 = mph_inj[['Yes', 'No']][0:8].sort_values(by=['Yes'],
                                                          ascending=False)
      mph_plt2.plot(kind='bar', stacked=True,
                    ax=ax1, color = ['#F8766D', '#00BFC4'], width = 0.90)
      ax1.set_title('Speed Limit by Injury Outcome: (Injured or Not)')
      ax1.set_xlabel('Speed Limit (in Miles per Hour)')
      ax1.set_ylabel('Count')
      # normalize the plot and plot it
      mph_plt_norm = mph_plt2.div(mph_plt2.sum(1), axis = 0)
      mph_plt_norm.plot(kind='bar', stacked=True,
                        ax=ax2,color = ['#F8766D', '#00BFC4'], width = 0.90)
      ax2.set_title('Speed Limit by Injury Outcome: (Injured or Not): Normalized')
      ax2.set_xlabel('Speed Limit (in Miles per Hour)')
```

ax2.set\_ylabel('Frequency')
plt.show()





From the speed limit group bar graph overlayed with "injured" and "non-injured" accident results, it is evident that the speed limit of 35-40 mph has a greater incidence of injuries (more than any other speed limit group).

While the strength of this graph is in its depiction of the overall distribution (providing us with injuries vs. non-injuries in each speed related accident), it does little to provide a comparison of the frequency (incidence rate) of injuries among the speed limit groups.

Normalizing the speed limit groups by our target (INJURY) assuages this analysis in such capacity. From here, it is easier to see that speed limits of 5-10 miles per hour, and 35-40 miles per hour, respectively had

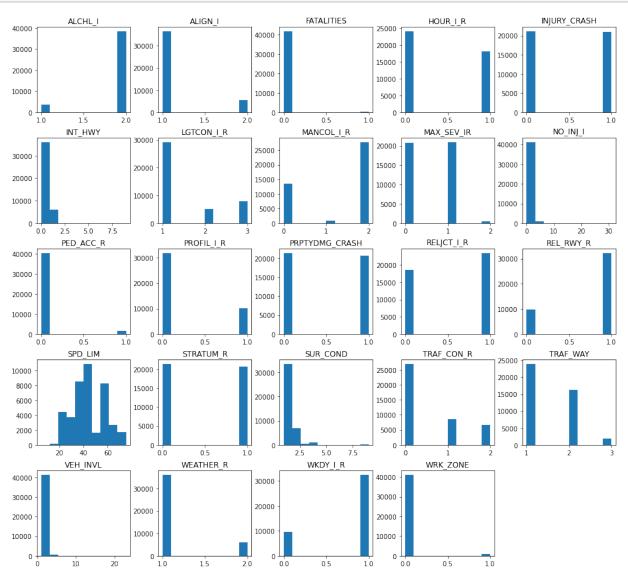
roughly 50% injury rates, whereas (notably), 75 miles per hour exhibited the highest injury rate of all.

**Note.** There are precisely 12,845 accidents that occurred between the 35-40 mph speed limit. 6,873 (or 53.51%) of them resulted in injuries. Now, let us plot the histogram distributions from each respective variable of the dataset. Figure 3 below visually illustrates these distributions.

#### **Histogram Distributions**

```
[18]: # checking for degenerate distributions
accidents.hist(grid=False, figsize=(16,15))

plt.show()
```



23 out of the original 24 variables are categorical, and from the histograms presented herein it is possible to uncover degenerate distributions with relative ease, as one category represents higher values over another. However, we look to the speed limit as the sole quantitative predictor which yields a positively skewed distribution. The following summary statistics corroborate this claim since the mean of 44 is greater than the median of 40.

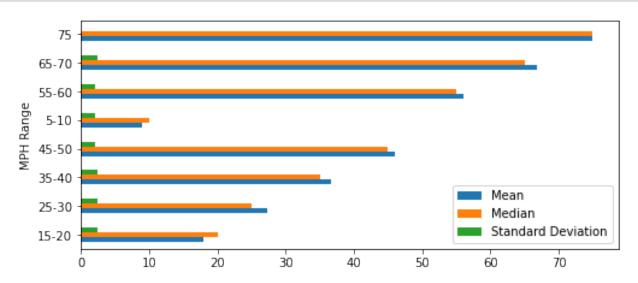
```
[19]: summ_stats = pd.DataFrame(accidents['SPD_LIM'].describe()).T summ_stats
```

[19]: count mean std min 25% 50% 75% max SPD\_LIM 42183.0 43.547875 12.948396 5.0 35.0 40.0 55.0 75.0

## Accidents by Speed Limit Summary

```
[20]:
                   Mean Median Standard Deviation Minimum Maximum
      MPH Range
                          20.00
      15-20
                  17.89
                                                 2.47
                                                          15.00
                                                                   20.00
                  27.35
                          25.00
                                                          25.00
                                                                   30.00
      25-30
                                                 2.50
      35 - 40
                  36.68
                          35.00
                                                 2.36
                                                          35.00
                                                                   40.00
                                                                   50.00
      45-50
                  46.01
                          45.00
                                                 2.01
                                                         45.00
                  8.93
                                                 2.09
                                                          5.00
                                                                   10.00
      5-10
                          10.00
      55-60
                  56.00
                          55.00
                                                 2.00
                                                         55.00
                                                                   60.00
      65-70
                  66.74
                                                 2.38
                                                          65.00
                                                                   70.00
                          65.00
      75
                  75.00
                          75.00
                                                 0.00
                                                         75.00
                                                                   75.00
      Total
                 334.60 330.00
                                                15.81
                                                        320.00
                                                                  355.00
```

```
[21]: acc_stats_mph.iloc[:, 0:3][0:8].plot.barh(figsize=(8,3.5))
plt.show()
```



## Selected Boxplot Distribution - Speed Limit

```
[22]: # selected boxplot distributions
     print("\033[1m"+'Boxplot Distribution'+"\033[1m")
      # Boxplot of age as one way of showing distribution
     fig = plt.figure(figsize = (10,1.5))
     plt.title ('Boxplot: Speed Limit')
     plt.xlabel('Speed Limit')
     plt.ylabel('Value')
      sns.boxplot(data=accidents['SPD_LIM'],
                  palette="coolwarm", orient='h',
                  linewidth=2.5)
     plt.show()
     IQR = summ_stats['75%'][0] - summ_stats['25%'][0]
     print('The first quartile is %s. '%summ_stats['25%'][0])
     print('The third quartile is %s. '%summ_stats['75%'][0])
     print('The IQR is %s.'%round(IQR,2))
     print('The mean is %s. '%round(summ_stats['mean'][0],2))
     print('The standard deviation is %s. '%round(summ_stats['std'][0],2))
     print('The median is %s. '%round(summ_stats['50%'][0],2))
```

#### Boxplot Distribution

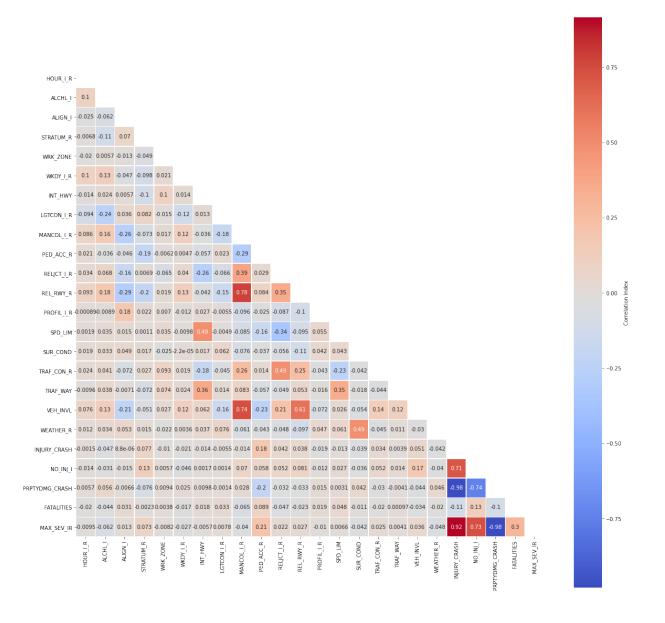


```
The first quartile is 35.0. The third quartile is 55.0. The IQR is 20.0. The mean is 43.55. The standard deviation is 12.95. The median is 40.0.
```

Whereas no outliers are present in the speed limit variable, there exists some skewness where the mean (43.55) is slightly greater than the median (40.00). Whereas typically a Box-Cox transformation could mitigate against skewness by transforming the variable(s) of interest, we will not be making such transformation to avoid misrepresenting the speed limit variable.

## **Correlation Matrix**

Accidents Data: Correlation Matrix



#### Multicollinearity

Let us narrow our focus by removing highly correlated predictors and passing the rest into a new dataframe.

These are the columns we should drop: ['REL\_RWY\_R', 'PRPTYDMG\_CRASH', 'MAX\_SEV\_IR']

```
HOUR_I_R
               int64
ALCHL I
               int64
ALIGN_I
               int64
STRATUM R
               int64
WRK_ZONE
               int64
WKDY_I_R
               int64
LGTCON_I_R
               int64
PED_ACC_R
               int64
RELJCT_I_R
               int64
PROFIL_I_R
               int64
SPD_LIM
               int64
SUR_COND
               int64
TRAF_CON_R
               int64
VEH_INVL
               int64
WEATHER_R
               int64
dtype: object
```

Number of Rows: 42183 Number of Columns: 15

# Additional Pre-Processing

MPH\_Range was created strictly for exploratory data analysis purposes. The INJURY column was based off the maximum injury severity column MAX\_SEV\_IR, so, we will binarize the INJURY column into a new Injured column in lieu of the prior two.

```
[26]: accidents['Injured'] = accidents['INJURY'].map({'yes':1, 'no':0})
```

Furthermore, we must remove the REL RWY R, PRPTYDMG CRASH, and MAX SEV IR columns from the

dataframe resulting from the inherent between-predictor and predictor-target relationships, respectively. However, there are still a few predictors that warrant subsequent omission. Number of injuries (NO\_INJ\_I) and fatalities (FATALATIES) are inherently and intrinsically related to the outcome by virtue of their meaning. Therefore, in order to avoid overfitting the model, we remove them.

```
HOUR I R
               int64
ALCHL I
               int64
ALIGN_I
               int64
STRATUM R
               int64
WRK_ZONE
               int64
WKDY_I_R
               int64
INT_HWY
               int64
LGTCON_I_R
               int64
PED_ACC_R
               int64
RELJCT_I_R
               int64
PROFIL_I_R
               int64
SPD_LIM
               int64
SUR_COND
               int64
TRAF_CON_R
               int64
TRAF_WAY
               int64
VEH INVL
               int64
WEATHER R
               int64
Injured
               int64
dtype: object
```

Number of Rows: 42183 Number of Columns: 18

## Checking for Statistical Significance Via Baseline Model

The logistic regression model is introduced as a baseline because establishing impact of coefficients on each independent feature can be carried with relative ease. Moreover, it is possible to gauge statistical significance from the reported *p*-values of the summary output table below.

## Generalized Linear Model - Logistic Regression Baseline

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + \varepsilon$$

Logistic Regression - Parametric Form

$$p(y) = \frac{\exp(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p)}{1 + \exp(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p)} + \varepsilon$$

Logistic Regression - Descriptive Form

$$\hat{p}(y) = \frac{\exp(b_0 + b_1 x_1 + b_2 x_2 + \dots + b_p x_p)}{1 + \exp(b_0 + b_1 x_1 + b_2 x_2 + \dots + b_p x_p)}$$

```
[28]: X = accidents_1.drop(columns=['Injured'])
X = sm.add_constant(X)
y = pd.DataFrame(accidents_1[['Injured']])
log_results = sm.Logit(y,X, random_state=222).fit()
log_results.summary()
```

Optimization terminated successfully.

Current function value: 0.650360

Iterations 9

[28]: <class 'statsmodels.iolib.summary.Summary'>

Logit Regression Results

| ========     | ======== | :=======   | :=======  |              |        |          |
|--------------|----------|------------|-----------|--------------|--------|----------|
| Dep. Variabl | e:       | Inj        | ured No.  | Observations | •      | 42183    |
| Model:       |          | I          | ogit Df E | Residuals:   |        | 42165    |
| Method:      |          |            | MLE Df N  | Model:       |        | 17       |
| Date:        | Th       | nu, 20 Jan | 2022 Pset | ıdo R-squ.:  |        | 0.06152  |
| Time:        |          | 20:0       | 5:53 Log- | -Likelihood: |        | -27434.  |
| converged:   |          |            | True LL-1 | Vull:        |        | -29233.  |
| Covariance T | 'ype:    | nonro      | bust LLR  | p-value:     |        | 0.000    |
| ========     | coef     | std err    | z         | P> z         | [0.025 | 0.975]   |
|              |          |            |           |              |        |          |
| const        | -0.6001  | 0.109      | -5.510    | 0.000        | -0.814 | -0.387   |
| HOUR_I_R     | -0.0568  | 0.021      | -2.740    | 0.006        | -0.097 | -0.016   |
| ALCHL_I      | -0.3613  | 0.038      | -9.428    | 0.000        | -0.436 | -0.286   |
| ALIGN_I      | 0.2351   | 0.031      | 7.535     | 0.000        | 0.174  | 0.296    |
| STRATUM_R    | 0.5008   | 0.021      | 24.079    | 0.000        | 0.460  | 0.542    |
| WRK_ZONE     | -0.0956  | 0.069      | -1.379    | 0.168        | -0.231 | 0.040    |
| WKDY_I_R     | -0.1037  | 0.025      | -4.207    | 0.000        | -0.152 | -0.055   |
| INT_HWY      | -0.0227  | 0.029      | -0.786    | 0.432        | -0.079 | 0.034    |
| LGTCON_I_R   | -0.0184  | 0.014      | -1.364    | 0.173        | -0.045 | 0.008    |
| PED_ACC_R    | 5.4058   | 0.260      | 20.755    | 0.000        | 4.895  | 5.916    |
| RELJCT_I_R   | 0.0553   | 0.025      | 2.169     | 0.030        | 0.005  | 0.105    |
| PROFIL_I_R   | -0.0413  | 0.024      | -1.719    | 0.086        | -0.088 | 0.006    |
| SPD_LIM      | 0.0080   | 0.001      | 8.260     | 0.000        | 0.006  | 0.010    |
| SUR_COND     | -0.0384  | 0.015      | -2.558    | 0.011        | -0.068 | -0.009   |
| TRAF_CON_R   | 0.0370   | 0.016      | 2.345     | 0.019        | 0.006  | 0.068    |
| TRAF_WAY     | 0.0060   | 0.019      | 0.310     | 0.757        | -0.032 | 0.044    |
| VEH_INVL     | 0.3755   | 0.017      | 21.759    | 0.000        | 0.342  | 0.409    |
| WEATHER_R    | -0.1611  | 0.033      | -4.851    | 0.000        | -0.226 | -0.096   |
|              | ======== |            | :=======  |              |        | ======== |

11 11 11

From the summary output table, we observe that WRK\_ZONE, INT\_HWY, LGTCON\_I\_R, and TRAF\_WAY have p-values of 0.168, 0.173, and 0.757, respectively, thereby making these variables statistically significant where = 0.05. We will thus remove them from the refined dataset.

## Train\_Test\_Split

Training: 33746 Test: 8437 Total: 42183

## Model Building Strategies

## Logistic Regression

```
[32]: # Un-Tuned Logistic Regression Model
      logit_reg = LogisticRegression(random_state=222)
      logit_reg.fit(X_train, y_train)
      # Predict on test set
      logit_reg_pred1 = logit_reg.predict(X_test)
      # accuracy and classification report
      print('Untuned Logistic Regression Model')
      print('Accuracy Score')
      print(accuracy_score(y_test, logit_reg_pred1))
      print('Classification Report \n',
             classification_report(y_test, logit_reg_pred1))
      # Tuned Logistic Regression Model
      C = [0.01, 0.1, 0.5, 1, 5, 10, 50]
      LRtrainAcc = []
      LRtestAcc = []
      for param in C:
          tuned_lr = LogisticRegression(solver = 'saga',
```

```
C = param,
                                   max_iter = 200,
                                   n_{jobs} = -1,
                                   random_state = 222)
    tuned_lr.fit(X_train, y_train)
    # Predict on train set
    tuned_lr_pred_train = tuned_lr.predict(X_train)
    # Predict on test set
    tuned_lr1 = tuned_lr.predict(X_test)
    LRtrainAcc.append(accuracy_score(y_train, tuned_lr_pred_train))
    LRtestAcc.append(accuracy_score(y_test, tuned_lr1))
# accuracy and classification report
print('Tuned Logistic Regression Model')
print('Accuracy Score')
print(accuracy_score(y_test, tuned_lr1))
print('Classification Report \n',
       classification_report(y_test, tuned_lr1))
# plot cost by accuracy
fig, ax = plt.subplots(figsize=(6,2.5))
ax.plot(C, LRtrainAcc, 'ro-', C, LRtestAcc, 'bv--')
ax.legend(['Training Accuracy', 'Test Accuracy'])
plt.title('Logistic Regression: Accuracy vs. Cost')
ax.set_xlabel('Cost'); ax.set_xscale('log')
ax.set_ylabel('Accuracy'); plt.show()
Untuned Logistic Regression Model
Accuracy Score
0.6025838568211449
Classification Report
               precision
                            recall f1-score
                                                support
           0
                   0.59
                             0.63
                                       0.61
                                                  4200
           1
                   0.61
                             0.57
                                       0.59
                                                  4237
```

Tuned Logistic Regression Model

0.60

0.60

Accuracy Score

accuracy

macro avg

weighted avg

0.6035320611591798

Classification Report

| OldSD111Cd01OL | precision | recall | f1-score | support |
|----------------|-----------|--------|----------|---------|
| 0              | 0.60      | 0.63   | 0.61     | 4200    |
| 1              | 0.61      | 0.58   | 0.59     | 4237    |
| accuracy       |           |        | 0.60     | 8437    |
| macro avg      | 0.60      | 0.60   | 0.60     | 8437    |
| weighted avg   | 0.60      | 0.60   | 0.60     | 8437    |

0.60

0.60

0.60

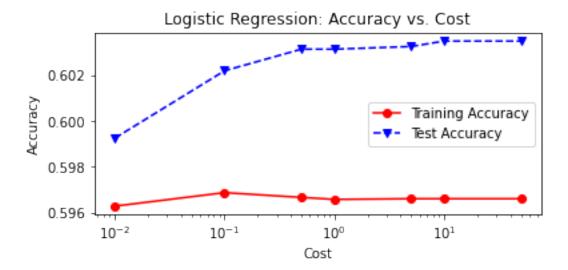
0.60

0.60

8437

8437

8437



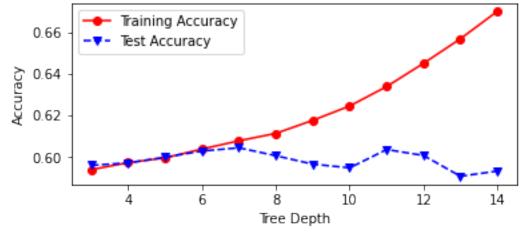
## **Decision Trees**

Before we print the classification report for the un-tuned decision tree, let us establish the optimal maximum depth hyperparameter by varying it in a for-loop as follows:

```
[33]: # Vary the decision tree depth in a loop,
      # increasing depth from 3 to 14.
     accuracy_depth=[]
     for depth in range(3,15):
          varied_tree = DecisionTreeClassifier(max_depth = depth,
                                               random_state = 222)
         varied_tree=varied_tree.fit(X_train,y_train)
         tree_test_pred = varied_tree.predict(X_test)
         tree_train_pred = varied_tree.predict(X_train)
          accuracy_depth.append({'depth':depth,
                                 'test accuracy':accuracy score\
                                 (y_test, tree_test_pred),
                                 'train_accuracy':accuracy_score\
                                 (y_train,tree_train_pred)
                                })
         print('Depth = %2.0f \t Test Accuracy = %2.2f \t \
         Training Accuracy = %2.2f'% (depth,accuracy_score\
                                       (y_test, tree_test_pred),
                                       accuracy_score(y_train,
                                       tree_train_pred)))
     abd_df = pd.DataFrame(accuracy_depth)
     abd_df.index = abd_df['depth']
```

```
Depth = 3
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.59
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.60
Depth =
                                              Training Accuracy = 0.60
                 Test Accuracy = 0.60
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.60
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.61
        7
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.61
Depth =
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.62
Depth = 10
                 Test Accuracy = 0.59
                                              Training Accuracy = 0.62
Depth = 11
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.63
Depth = 12
                 Test Accuracy = 0.60
                                              Training Accuracy = 0.64
Depth = 13
                 Test Accuracy = 0.59
                                              Training Accuracy = 0.66
                                              Training Accuracy = 0.67
Depth = 14
                 Test Accuracy = 0.59
```

# Varied Tree Depth by Accuracy



The optimal maximum depth exists where test and training accuracy are both highest (60% and 64%, respectively). This is where depth is equal to 12. Now we can print the classification reports for both the un-tuned and tuned models, noting some improvement in performance.

```
[34]: # Untuned Decision Tree Classifier
untuned_tree = DecisionTreeClassifier(random_state=222)
```

```
untuned_tree = untuned_tree.fit(X_train, y_train)
# Predict on test set
untuned_tree1 = untuned_tree.predict(X_test)
# accuracy and classification report
print('Untuned Decision Tree Classifier')
print('Accuracy Score')
print(accuracy_score(y_test, untuned_tree1))
print('Classification Report \n',
       classification_report(y_test, untuned_tree1))
# Tuned Decision Tree Classifier
tuned_tree = DecisionTreeClassifier(max_depth = 12,
                                     random_state=222)
tuned_tree = tuned_tree.fit(X_train, y_train)
# Predict on test set
tuned_tree1 = tuned_tree.predict(X_test)
# accuracy and classification report
print('Tuned Decision Tree Classifier')
print('Accuracy Score')
print(accuracy_score(y_test, tuned_tree1))
print('Classification Report \n',
       classification_report(y_test, tuned_tree1))
Untuned Decision Tree Classifier
Accuracy Score
```

0.5661965153490577

|              | precision | recall | f1-score | support |
|--------------|-----------|--------|----------|---------|
| 0            | 0.56      | 0.61   | 0.58     | 4200    |
| 1            | 0.58      | 0.52   | 0.55     | 4237    |
| accuracy     |           |        | 0.57     | 8437    |
| macro avg    | 0.57      | 0.57   | 0.57     | 8437    |
| weighted avg | 0.57      | 0.57   | 0.57     | 8437    |

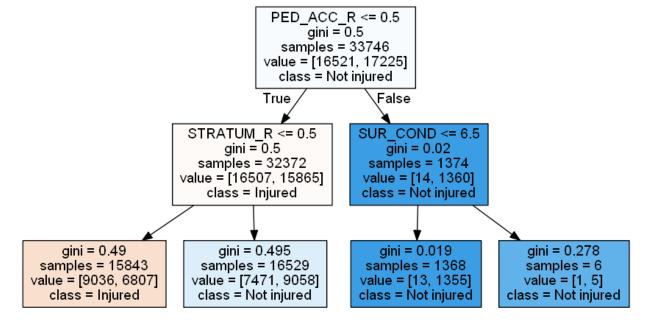
Tuned Decision Tree Classifier Accuracy Score 0.6008059736873296

Classification Report

Classification Report

|              | precision | recall | f1-score | support |
|--------------|-----------|--------|----------|---------|
| 0            | 0.59      | 0.63   | 0.61     | 4200    |
| 1            | 0.61      | 0.57   | 0.59     | 4237    |
| accuracy     |           |        | 0.60     | 8437    |
| macro avg    | 0.60      | 0.60   | 0.60     | 8437    |
| weighted avg | 0.60      | 0.60   | 0.60     | 8437    |

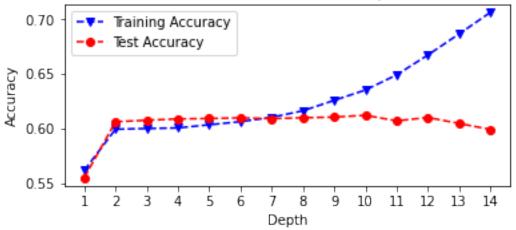
[35]:



#### Random Forest Classifier

```
Max Depth =
                 Test Accuracy = 0.56
                                              Training Accuracy = 0.56
Max Depth =
                 Test Accuracy = 0.61
                                              Training Accuracy = 0.60
Max Depth = 3
                 Test Accuracy = 0.61
                                              Training Accuracy = 0.60
Max Depth = 4
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.60
Max Depth = 5
                                              Training Accuracy = 0.60
                 Test Accuracy = 0.61
Max Depth = 6
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.61
Max Depth = 7
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.61
Max Depth = 8
                 Test Accuracy = 0.61
                                              Training Accuracy = 0.62
Max Depth = 9
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.63
                                             Training Accuracy = 0.64
Max Depth = 10
                 Test Accuracy = 0.61
Max Depth = 11
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.65
Max Depth = 12
                 Test Accuracy = 0.61
                                             Training Accuracy = 0.67
                                             Training Accuracy = 0.69
Max Depth = 13
                 Test Accuracy = 0.60
Max Depth = 14
                 Test Accuracy = 0.60
                                             Training Accuracy = 0.71
```

# Random Forest Accuracy



```
[37]: # Untuned Random Forest
untuned_rf = RandomForestClassifier(random_state=222)
untuned_rf = untuned_rf.fit(X_train, y_train)
```

```
# Predict on test set
untuned_rf1 = untuned_rf.predict(X_test)
 # accuracy and classification report
print('Untuned Random Forest Model')
print('Accuracy Score')
print(accuracy_score(y_test, untuned_rf1))
print('Classification Report \n',
        classification_report(y_test, untuned_rf1))
 # Tuned Random Forest
 tuned_rf = RandomForestClassifier(random_state=222,
                                   max_depth = 12)
tuned_rf = tuned_rf.fit(X_train, y_train)
 # Predict on test set
tuned_rf1 = tuned_rf.predict(X_test)
 # accuracy and classification report
print('Tuned Random Forest Model')
print('Accuracy Score')
print(accuracy_score(y_test, tuned_rf1))
print('Classification Report \n',
        classification_report(y_test, tuned_rf1))
Untuned Random Forest Model
Accuracy Score
0.5749674054758801
Classification Report
               precision
                            recall f1-score
                                                support
           0
                   0.57
                             0.58
                                        0.58
                                                  4200
           1
                   0.58
                             0.57
                                        0.57
                                                  4237
    accuracy
                                        0.57
                                                  8437
                   0.58
                                        0.57
   macro avg
                             0.57
                                                  8437
                   0.58
                             0.57
                                        0.57
                                                  8437
weighted avg
Tuned Random Forest Model
Accuracy Score
0.6104065426099324
Classification Report
               precision
                            recall f1-score
                                                support
```

macro avg 0.61 0.61 0.61 8437 weighted avg 0.61 0.61 0.61 8437

0.63

0.59

0.60

0.62

0

1

accuracy

0.62

0.60

0.61

4200

4237

8437

## **Model Evaluation**

#### Confusion Matrices

ò

Predicted label

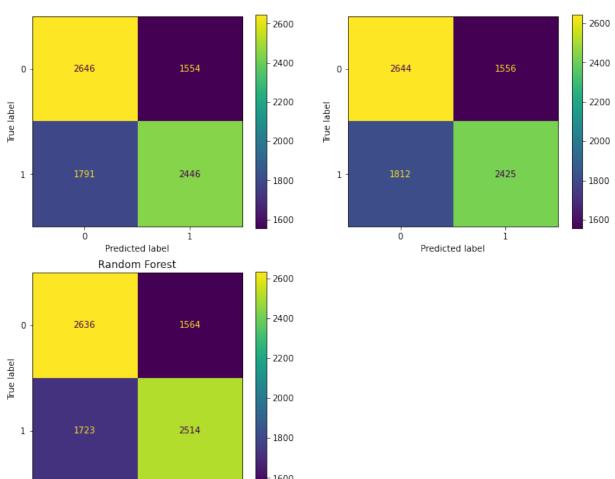
i

```
[38]: fig = plt.figure(figsize=(12,10))
    ax1 = fig.add_subplot(221)
    ax2 = fig.add_subplot(222)
    ax3 = fig.add_subplot(223)

# logistic regression confusion matrix
    plot_confusion_matrix(tuned_lr, X_test, y_test, ax=ax1)
    plt.title('Logistic Regression')

# Decision tree confusion matrix
    plot_confusion_matrix(tuned_tree, X_test, y_test, ax=ax2)
    plt.title('Decision Tree')

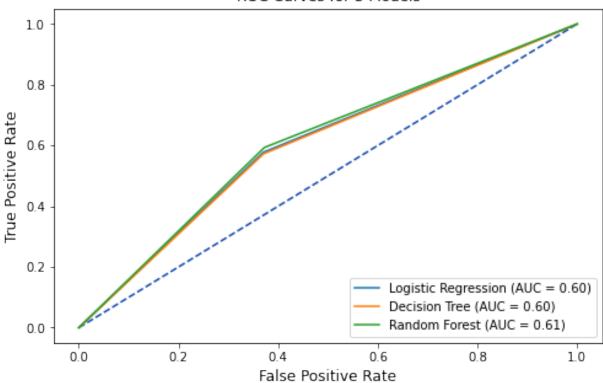
# random forest confusion matrix
    plot_confusion_matrix(tuned_rf, X_test, y_test, ax=ax3)
    plt.title('Random Forest')
    plt.show()
```



#### **ROC Curves**

```
[39]: # plot all of the roc curves on one graph
      tuned_lr_roc = metrics.roc_curve(y_test,tuned_lr1)
      fpr,tpr,thresholds = metrics.roc_curve(y_test,tuned_lr1)
      tuned lr auc = metrics.auc(fpr, tpr)
      tuned_lr_plot = metrics.RocCurveDisplay(fpr=fpr,tpr=tpr,
      roc auc = tuned lr auc,
      estimator_name = 'Logistic Regression')
      tuned_tree_roc = metrics.roc_curve(y_test,tuned_tree1)
      fpr,tpr,thresholds = metrics.roc_curve(y_test,tuned_tree1)
      tuned_tree_auc = metrics.auc(fpr, tpr)
      tuned_tree_plot = metrics.RocCurveDisplay(fpr=fpr,tpr=tpr,
      roc_auc=tuned_tree_auc,
      estimator_name = 'Decision Tree')
      tuned_rf1_roc = metrics.roc_curve(y_test, tuned_rf1)
      fpr,tpr,thresholds = metrics.roc_curve(y_test,tuned_rf1)
      tuned_rf1_auc = metrics.auc(fpr, tpr)
      tuned rf1 plot = metrics.RocCurveDisplay(fpr=fpr,tpr=tpr,
      roc_auc=tuned_rf1_auc,
      estimator_name = 'Random Forest')
      # plot set up
      fig, ax = plt.subplots(figsize=(8,5))
      plt.title('ROC Curves for 3 Models',fontsize=12)
      plt.plot([0, 1], [0, 1], linestyle = '--',
               color = '#174ab0')
      plt.xlabel('',fontsize=12)
      plt.ylabel('',fontsize=12)
      # Model ROC Plots Defined above
      tuned_lr_plot.plot(ax)
      tuned_tree_plot.plot(ax)
      tuned_rf1_plot.plot(ax)
      plt.show()
```

## ROC Curves for 3 Models



#### **Performance Metrics**

```
[40]: # Logistic Regression Performance Metrics
      report1 = classification_report(y_test,tuned_lr1,
      output_dict=True)
      accuracy1 = round(report1['accuracy'],4)
      precision1 = round(report1['1']['precision'],4)
      recall1 = round(report1['1']['recall'],4)
      fl_score1 = round(report1['1']['f1-score'],4)
      # Decision Tree Performance Metrics
      report2 = classification_report(y_test,tuned_tree1,
      output_dict=True)
      accuracy2 = round(report2['accuracy'],4)
      precision2 = round(report2['1']['precision'],4)
      recall2 = round(report2['1']['recall'],4)
      fl_score2 = round(report2['1']['f1-score'],4)
      # Random Forest Performance Metrics
      report3 = classification_report(y_test,tuned_rf1,
      output_dict=True)
      accuracy3 = round(report3['accuracy'],4)
      precision3 = round(report3['1']['precision'],4)
      recall3 = round(report3['1']['recall'],4)
      fl_score3 = round(report3['1']['f1-score'],4)
```

```
-----
          | Test Accuracy | Precision | Recall | F1-score |
    Model
+----+
| Logistic Regression |
              0.6035
                     0.6115 | 0.5773 | 0.5939 |
 Decision Tree
              0.6008
                  0.6091 | 0.5723 | 0.5902 |
  Random Forest
              0.6104
                  - 1
                     0.6165 | 0.5933 |
                               0.6047
+----+
```

| +                   | -+ |        | -+- |        | -+ |
|---------------------|----|--------|-----|--------|----|
| Model               | İ  | AUC    |     | MSE    | 1  |
| +                   | -+ |        | -+- |        | -+ |
| Logistic Regression |    | 0.6036 |     | 0.3965 | -  |
| Decision Tree       | -  | 0.6009 |     | 0.3992 | -  |
| Random Forest       | -  | 0.6105 | -   | 0.3896 |    |
| +                   | -+ |        | -+- |        | -+ |

#### Reference

Shmueli, G., Bruce, P. C., Gedeck, P., & Patel, N. R. (2020). Data mining for business analytics: Concepts, techniques and applications in Python. John Wiley & Sons, Inc.