

## Examples and Intuitions II

The  $\Theta^{(1)}$  matrices for AND, NOR, and OR are:

AND:

$$\Theta^{(1)}$$
 =[-30 20 20]

NOR:

$$\Theta^{(1)}$$
 =[10 -20 -20]

OR:

$$\Theta^{(1)} = [-10 \quad 20 \quad 20]$$

We can combine these to get the XNOR logical operator (which gives 1 if  $\mathbf{x_1}$  and  $\mathbf{x_2}$  are both 0 or both 1).

$$\begin{bmatrix} x_0 \\ x_1 \\ x_2 \end{bmatrix} \ \rightarrow \ \begin{bmatrix} a_1^{(2)} \\ a_2^{(2)} \end{bmatrix} \ \rightarrow \ [a^{(3)}] \ \rightarrow \ h_{\boldsymbol{\theta}} \big( \boldsymbol{x} \big)$$

For the transition between the first and second layer, we'll use a  $\,\Theta^{(1)}\,$  matrix that combines the values for AND and NOR:

$$\Theta^{(1)} = \begin{bmatrix} -30 & 20 & 20 \\ 10 & -20 & -20 \end{bmatrix}$$

For the transition between the second and third layer, we'll use a  $\Theta^{(2)}$  matrix that uses the value for OR:

$$\Theta^{(1)} = [-10 \quad 20 \quad 20]$$

Let's write out the values for all our nodes:

$$a^{(2)} = g (\Theta^{(1)} \cdot x)$$

$$a^{(3)} = g (\Theta^{(2)} \cdot a^{(2)})$$

$$h_{\Theta}(x) = a^{(3)}$$

And there we have the XNOR operator using a hidden layer with two nodes! The following summarizes the above algorithm:

