

Point/point distance

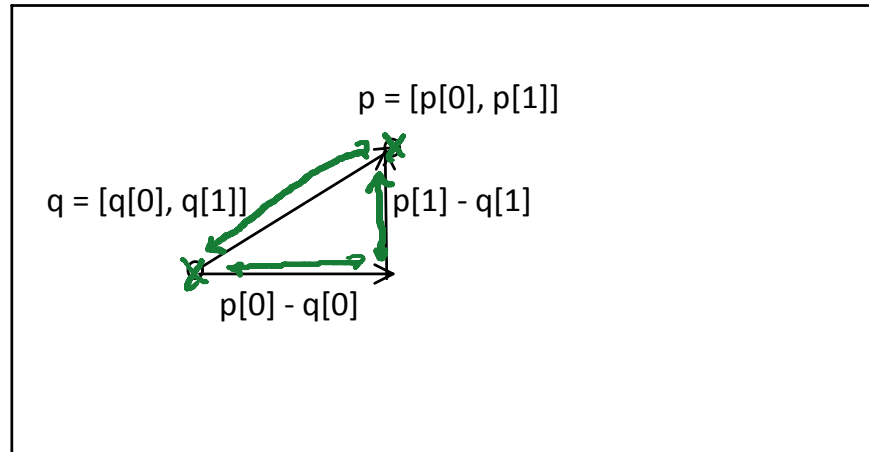
Two points

Math - points on canvas

p, q

Python - list of coordinates

$[p[0], p[1]], [q[0], q[1]]$



Pythagorean theorem

Math

$$\sqrt{\text{dist}(p, q)^2} = \sqrt{(p[0] - q[0])^2 + (p[1] - q[1])^2}$$

Python

def dist(p, q):

return math.sqrt((p[0] - q[0]) ** 2 + (p[1] - q[1]) ** 2)

Vectors and motion

Vector as difference of two points

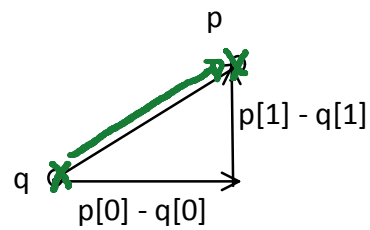
Math

$$\mathbf{v} = \mathbf{p} - \mathbf{q}$$

Python - list of components

$$\rightarrow v[0] = p[0] - q[0]$$

$$\rightarrow v[1] = p[1] - q[1]$$



Move/translate point using a vector

Math

$$\mathbf{p} = \mathbf{q} + \mathbf{v}$$

Python

$$\rightarrow p[0] = q[0] + v[0]$$

$$\rightarrow p[1] = q[1] + v[1]$$

Update for motion

Math - point at position p with velocity v

$$\mathbf{p} = \mathbf{p} + a * \mathbf{v}$$

Python

$$\rightarrow p[0] = p[0] + a * v[0]$$

$$\rightarrow p[1] = p[1] + a * v[1]$$

Collisions

Motion update

$$p[0] = p[0] + a * v[0]$$
$$p[1] = p[1] + a * v[1]$$

Collision of point p with wall

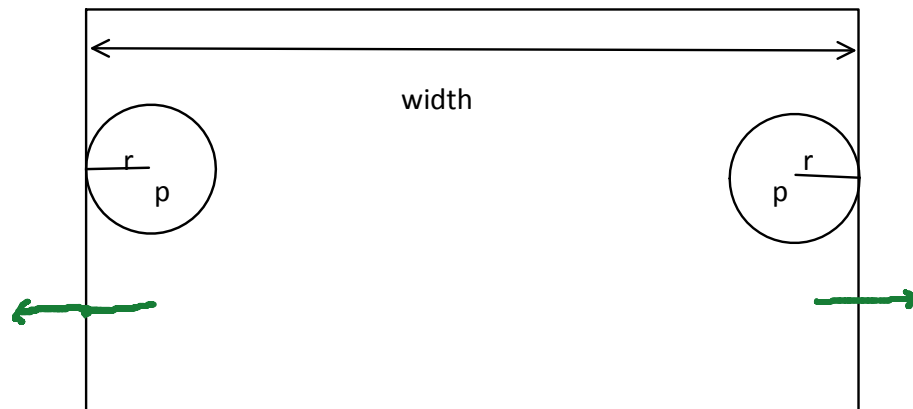
Left wall
 $p[0] \leq 0$

Right wall
 $p[0] \geq \text{width}$

Collision of ball of with center p and
radius r with wall

Left wall
 $p[0] \leq r$

Right wall
 $p[0] \geq \text{width} - r$



Reflections

Motion update

$$p[0] = p[0] + a * v[0]$$
$$p[1] = p[1] + a * v[1]$$

Reflections - update the velocity vector v

Left wall

Compute reflected velocity vector

$$v[0] = -v[0]$$

$$v[1] = v[1]$$

