



A circular source of radius 10 km generates earthquakes of magnitude $M=6.7$ and a circular rupture area $RA=501.19 \text{ km}^2$ at a rate of $NM_{min}=2$ events per year. The source center is located at $XYZ(0,0,0)$. Use the Sadigh et al. 1997 GMM (strike-slip) to compute the seismic hazard curve for $Sa(T=0.001)$ at a rock site located at coordinates $XYZ(30 \text{ km}, 0, 0)$. Consider the hypocenter located at the center of the rupture plane.

Evaluating Sadigh et al 1997 at $T=0.001\text{s}$ for $M=6.7$ leads to

$$\ln Sa(0.001) = -1.274 + 1.1M - 2.1 \ln(r + \exp(-0.48451 + 0.5240M))$$

$$\ln Sa(0.001) = 6.096 - 2.1 \ln(r + 20.621) \quad \text{and} \quad \sigma = 1.39 - 0.14M = 0.452$$

The probability term $P(Sa > y|m = 6.7, r)$ is

$$P(Sa > y|m = 6.7, r) = 1 - \Phi\left(\frac{\log(y) - [6.096 - 2.1 \ln(r + 20.621)]}{0.452}\right)$$

$$\text{Where } r = \sqrt{(x - 30)^2 + y^2} - \sqrt{\frac{501.19}{\pi}}$$

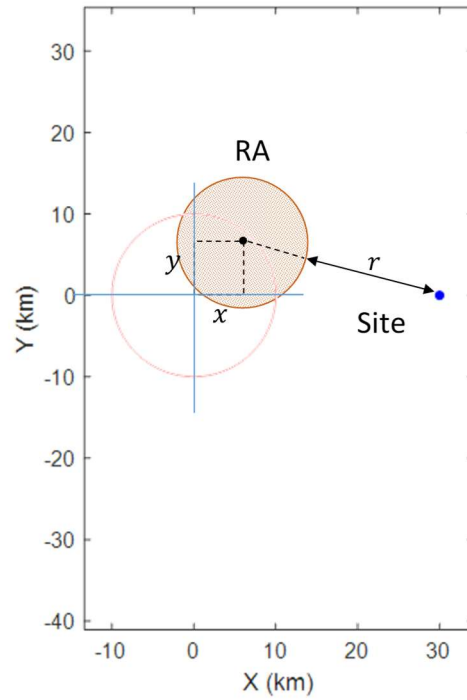
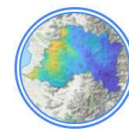


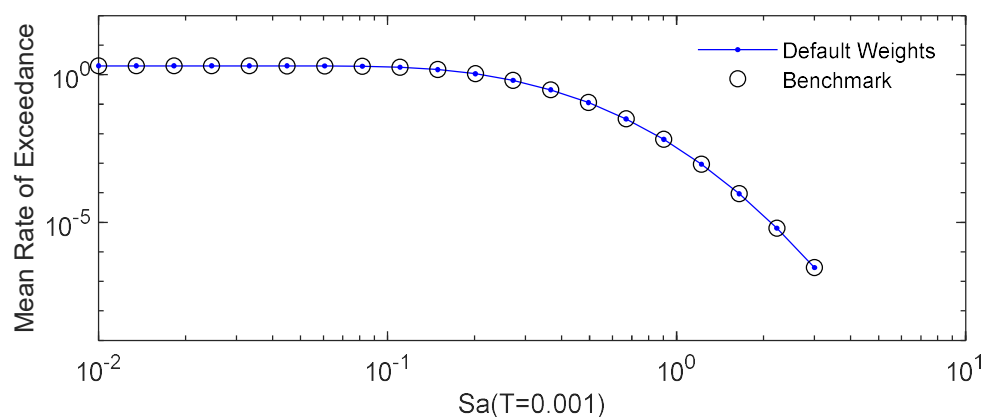
Figure 1 – Source geometry, rupture plane and site location



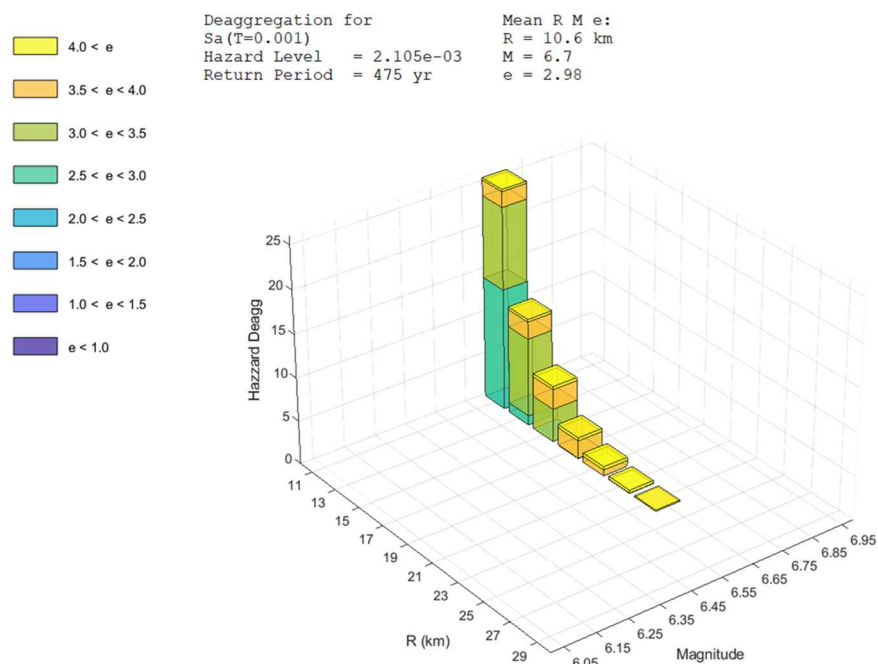
If $f_M(m) = \delta(m - 6.7)$, the hazard integral can be written as

$$\lambda_z = NM_{min} \int P(Sa > z|m, r) f_M(m) f_R(r) dm dr = NM_{min} \int_0^{2\pi} \int_0^{10} P(Sa > z|m = 6.7, r) \cdot \left(\frac{r dr d\theta}{\pi \cdot 10^2} \right)$$

$$\lambda_z = NM_{min} \int_0^{2\pi} \int_0^{10} \left\{ 1 - \Phi \left(\frac{\log(y) - [6.096 - 2.1 \ln(r + 20.621)]}{0.452} \right) \right\} \left(\frac{r dr d\theta}{\pi \cdot 10^2} \right)$$



Hazard deaggregation for T=0.001 and 475 years return period (M-R-ε Deaggregation)





Independent calculation in MATLAB:

```
NMmin = 2;
M      = 6.7;
Rad    = 10;
Area   = pi*Rad^2;
r0     = linspace(0, Rad, 30);
rint   = r0(1:end-1);
rext   = r0(2:end);
rmid   = 1/2*(rint+rext);
theta0 = linspace(0, 2*pi, 360);
theta  = (theta0(1:end-1)+theta0(2:end))/2;
x      = rmid'*cos(theta);
y      = rmid'*sin(theta);
rate   = 1/2*(rext.^2-rint.^2)*diff(theta0)/Area;
RA     = 10^(1*M-4);
r      = sqrt((x(:)-30).^2+y(:).^2)-sqrt(RA/pi);
mu     = -1.274+1.1*M-2.1*log(r+exp(-0.48451+0.5240*M));
sigma  = 1.39-0.14*M;
z      = logsp(0.01, 3, 20);
lambda = zeros(size(z));
for i=1:length(z)
    P = (1-normcdf((log(z(i)) - mu)/sigma));
    lambda(i) = NMmin*rate(:)'*P;
end
```