

ECE 559 NEURAL NETWORKS ASSIGNMENT 8

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1. RBF NETWORK FOR K=20

Importing libraries

```
In [1]: import numpy as np
import matplotlib.pyplot as plt
import math
import random
```

Initializing variables

```
In [2]: x=np.random.rand(2,100)
d=np.zeros((100,1))
d1=np.zeros((100,1))
D=np.zeros((100,1))
Cp=[]
Cn=[]
```

Plotting the given data points

```
In [3]: X,Y=np.meshgrid(np.linspace(0,1,100),np.linspace(0,1,100))
sun=np.square(X-0.8)+np.square(Y-0.5)-np.square(0.15)
#plt.contour(Y,X,sun,[0])

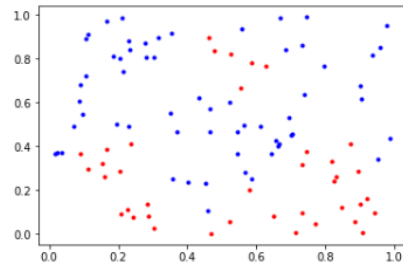
y=np.linspace(0,1,100)
mount=((1/5)*np.sin(10*y))+0.3
#plt.plot(y,mount)

for i in range(len(x[0])):

    d[i][0]=((1/5)*np.sin(10*x[0][i]))+0.3
    d1[i][0]=np.square(x[1][i]-0.8)+np.square(x[0][i]-0.5)

    if x[1][i] < d[i][0] or d1[i][0] < np.square(0.15):
        D[i][0]=1
        Cp.append((x[0][i],x[1][i]))
        cp=np.asarray(Cp)
        plt.plot(x[0][i],x[1][i], 'r.')

    else:
        D[i][0]=-1
        Cn.append((x[0][i],x[1][i]))
        cn=np.asarray(Cn)
        plt.plot(x[0][i],x[1][i], 'b.')
```



Picking the centroid from the given set of datapoints

```
In [4]: index_p=np.random.choice(len(cp),10,replace=0)
        print(index_p)

        index_n=np.random.choice(len(cn),10,replace=0)
        print(index_n)

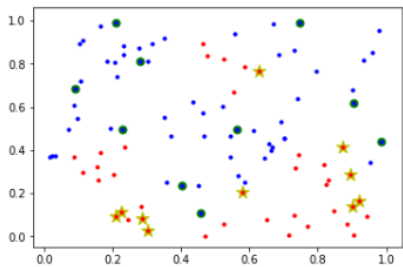
[32 36  9 18  7 30 31 14  0 34]
[ 3 31 41 30 33 19 28 40  2 26]
```

```
In [5]: center_p=np.zeros((10,2))
        center_n=np.zeros((10,2))
        for i in range(10):
            center_p[i]=Cp[index_p[i]]
            center_n[i]=Cn[index_n[i]]
```

Plotting The chosen centroid points

```
In [6]: plt.plot(cp[:,0],cp[:,1], 'r.')
        plt.scatter(center_p[:,0],center_p[:,1],marker='*',c='y',s=150)
        plt.plot(cn[:,0],cn[:,1], 'b.')
        plt.scatter(center_n[:,0],center_n[:,1],marker='o',c='g',s=50)
```

Out[6]: <matplotlib.collections.PathCollection at 0x1e53b28b278>



Finding the new cluster centers for the positive class

```
In [7]: k_p=10
        center_p_old=np.zeros(center_p.shape)
        center_p_new=center_p
        cluster_p=np.zeros(len(cp))
        dist_p=np.zeros((len(cp),k_p))
        error_p = np.linalg.norm(center_p_new - center_p_old)

        while error_p != 0:
            # Measure the distance to every center
            for i in range(k_p):
                dist_p[:,i] = np.linalg.norm(cp - center_p_new[i], axis=1)
            # Assign all training data to closest center
            cluster_p = np.argmin(dist_p, axis = 1)

            center_p_old = center_p_new
            # Calculate mean for every cluster and update the center
            for i in range(k_p):
                center_p_new[i] = np.mean(cp[cluster_p == i], axis=0)
            error_p = np.linalg.norm(center_p_new - center_p_old)
        print('New cluster centers:',center_p_new)
        print('Updated clusters',cluster_p)
```

```

New cluster centers: [[0.83719803 0.07111055]
 [0.28514692 0.11024899]
 [0.16827221 0.30596912]
 [0.38583172 0.01426605]
 [0.58440672 0.11377916]
 [0.81988667 0.28753747]
 [0.9193406 0.16370677]
 [0.8089592 0.39475176]
 [0.53898096 0.79552125]
 [0.22629527 0.08491042]]
Updated clusters [8 2 0 2 2 0 5 4 0 2 8 2 4 9 7 8 0 5 3 5 2 3 8 0 0 7 8 1 0 8 5 6 0 2 9 2 1
5 4]

```

Finding the new cluster centers for the negative class

```

In [8]: k_n=10
center_n_old=np.zeros(center_n.shape)
center_n_new=center_n
cluster_n=np.zeros(len(cn))
dist_n=np.zeros((len(cn),k_n))
error_n = np.linalg.norm(center_n_new - center_n_old)

while error_n != 0:
    # Measure the distance to every center
    for i in range(k_n):
        dist_n[:,i] = np.linalg.norm(cn - center_n_new[i], axis=1)
    # Assign all training data to closest center
    cluster_n = np.argmin(dist_n, axis = 1)

    center_n_old = center_n_new
    # Calculate mean for every cluster and update the center
    for i in range(k_n):
        center_n_new[i] = np.mean(cn[cluster_n == i], axis=0)
    error_n = np.linalg.norm(center_n_new - center_n_old)
print('New cluster centers:',center_n_new)
print('Updated clusters',cluster_n)

```

```

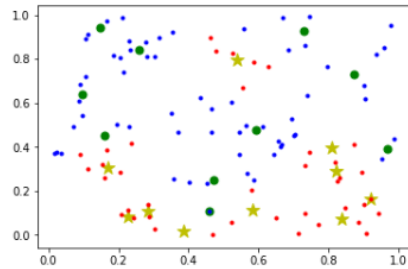
New cluster centers: [[0.4581932 0.10651131]
 [0.09557216 0.63916909]
 [0.59208229 0.47519462]
 [0.14803881 0.94097195]
 [0.72823202 0.92843928]
 [0.16143654 0.45270432]
 [0.47292781 0.25118446]
 [0.25984404 0.83889265]
 [0.96911661 0.39074612]
 [0.87237019 0.72824571]]
Updated clusters [7 6 8 0 4 2 2 9 5 2 9 7 8 4 9 7 1 2 1 5 4 2 3 7 3 7 9 5 6 3 3 1 2 4 2 4 2
1 5 9 7 2 2 5 9 7 7 7 6 6 2 5 5 2 2 2 4 6 7 5]

```

Plotting the updated centroids

```
In [9]: plt.plot(cp[:,0],cp[:,1], 'r.')
plt.scatter(center_p_new[:,0],center_p_new[:,1],marker='*',c='y',s=150)
plt.plot(cn[:,0],cn[:,1], 'b.')
plt.scatter(center_n[:,0],center_n[:,1],marker='o',c='g',s=50)
```

Out[9]: <matplotlib.collections.PathCollection at 0x1e53b2f2e48>



Concatenating the centers of both positive and negative classes

```
In [10]: center=np.row_stack((center_p_new,center_n_new))
print(center)
```

```
[[0.83719803 0.07111055]
 [0.28514692 0.11024899]
 [0.16827221 0.30596912]
 [0.38583172 0.01426605]
 [0.58440672 0.11377916]
 [0.81988667 0.28753747]
 [0.9193406 0.16370677]
 [0.8089592 0.39475176]
 [0.53898096 0.79552125]
 [0.22629527 0.08491042]
 [0.4581932 0.10651131]
 [0.09557216 0.63916909]
 [0.59208229 0.47519462]
 [0.14803881 0.94097195]
 [0.72823202 0.92843928]
 [0.16143654 0.45270432]
 [0.47292781 0.25118446]
 [0.25984404 0.83889265]
 [0.96911661 0.39074612]
 [0.87237019 0.72824571]]
```

Computing the RBF function

```
In [28]: x_mu=np.zeros((100,len(center)))
for i in range(100):
    for j in range(len(center)):
        x_mu[i][j]=np.linalg.norm(x[:,i]-center[j,:])
rbf=np.exp(-16*np.square(x_mu))
```

Perceptron training algorithm

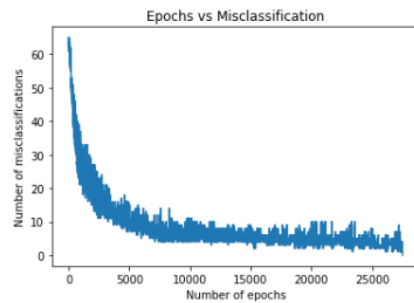
```
In [32]: K=20
W=np.zeros((K,1))
W=np.random.normal(size=(K,1))           #Initializing the weight vector
bias=np.random.randn(1)
errors=0                                #Initializing the misclassifications
Mc=[]                                    #Storing the misclassification values after every epoch
epoch=0
lr=0.01
#rbf=np.row_stack([rbf_p,rbf_n])
```

```
In [35]: while(epoch==0 or Mc[epoch-1] > 0):
#         errors=0
        for i in range(len(rbf)):
            #errors=0
            y=np.sign(np.matmul(W.reshape(1,20),rbf[i].reshape(20,1))+bias)
            #Y=np.heaviside(y,1)
            print('actual',y)
            E=D[i]-y
            print('Error',E)
            Q=E*rbf[i].reshape(20,1)
            W=W+lr*Q
            bias=bias+lr*E
            errors = 0
            for j in range(len(rbf)):
                Y=np.sign(np.matmul(W.reshape(1,20),rbf[j].reshape(20,1))+bias)
                if Y != D[j]:
                    errors=errors+1
#             print('count',errors)

        Mc.append(errors)
        print('Misclassification',Mc[epoch])
        epoch=epoch+1
```

Plotting Number of epochs against Misclassifications

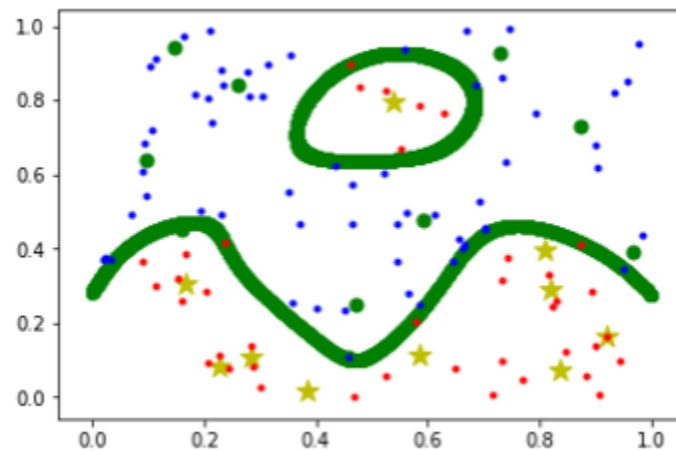
```
In [36]: plt.plot(Mc)
plt.xlabel('Number of epochs')
plt.ylabel('Number of misclassifications')
plt.title('Epochs vs Misclassification')
plt.show()
```



Plotting the Decision Boundary

```
In [42]: plt.plot(cp[:,0],cp[:,1], 'r-')
plt.scatter(center_p_new[:,0],center_p_new[:,1],marker='*',c='y',s=150)
plt.plot(cn[:,0],cn[:,1], 'b-')
plt.scatter(center_n[:,0],center_n[:,1],marker='o',c='g',s=50)
K_mu=0

for i in np.linspace(0,1,1000):
    for j in np.linspace(0,1,1000):
        g=0
        for k in range(len(center)):
            K_mu=np.linalg.norm(np.asarray([i,j])-center[k,:])
            RBF=np.exp(-16*np.square(K_mu))
            g=g+np.multiply(w[k],RBF)
        g=g+bias
        print('G:',g)
        if np.abs(g)<0.005:
            plt.scatter(i,j,c='g')
```



2. RBF NETWORK FOR K=4

Importing Libraries

```
In [1]: import numpy as np
import matplotlib.pyplot as plt
import math
import random
```

Initializing variables

```
In [2]: x=np.random.rand(2,100)
d=np.zeros((100,1))
d1=np.zeros((100,1))
D=np.zeros((100,1))
Cp=[]
Cn=[]
```

Plotting the given data points

```
In [3]: X,Y=np.meshgrid(np.linspace(0,1,100),np.linspace(0,1,100))
sun=np.square(X-0.8)+np.square(Y-0.5)-np.square(0.15)
#plt.contour(Y,X,sun,[0])

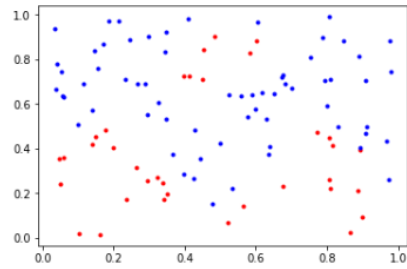
y=np.linspace(0,1,100)
mount=((1/5)*np.sin(10*y))+0.3
#plt.plot(y,mount)

for i in range(len(x[0])):

    d[i][0]=((1/5)*np.sin(10*x[0][i]))+0.3
    d1[i][0]=np.square(x[1][i]-0.8)+np.square(x[0][i]-0.5)

    if x[1][i] < d[i][0] or d1[i][0] < np.square(0.15):
        D[i][0]=1
        Cp.append((x[0][i],x[1][i]))
        cp=np.asarray(Cp)
        plt.plot(x[0][i],x[1][i], 'r. ')

    else:
        D[i][0]=-1
        Cn.append((x[0][i],x[1][i]))
        cn=np.asarray(Cn)
        plt.plot(x[0][i],x[1][i], 'b. ')
```



Picking the centroid from the given set of points

```
In [4]: index_p=np.random.choice(len(cp),2,replace=0)
        print(index_p)

        index_n=np.random.choice(len(cn),2,replace=0)
        print(index_n)
```

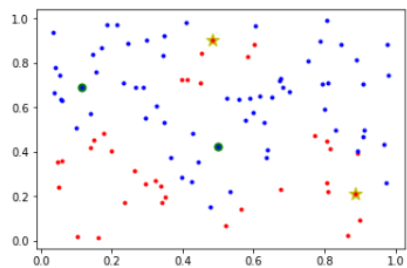
```
[17  6]
[63 10]
```

```
In [5]: center_p=np.zeros((2,2))
        center_n=np.zeros((2,2))
        for i in range(2):
            center_p[i]=Cp[index_p[i]]
            center_n[i]=Cn[index_n[i]]
```

Plotting the centroids

```
In [6]: plt.plot(cp[:,0],cp[:,1],'r.')
        plt.scatter(center_p[:,0],center_p[:,1],marker='*',c='y',s=150)
        plt.plot(cn[:,0],cn[:,1],'b.')
        plt.scatter(center_n[:,0],center_n[:,1],marker='o',c='g',s=50)
```

Out[6]: <matplotlib.collections.PathCollection at 0x1ef9669c320>



Finding the cluster centers for positive class

```
In [7]: k_p=2
        center_p_old=np.zeros(center_p.shape)
        center_p_new=center_p
        cluster_p=np.zeros(len(cp))
        dist_p=np.zeros((len(cp),k_p))
        error_p = np.linalg.norm(center_p_new - center_p_old)

        while error_p != 0:
            # Measure the distance to every center
            for i in range(k_p):
                dist_p[:,i] = np.linalg.norm(cp - center_p_new[i], axis=1)
            # Assign all training data to closest center
            cluster_p = np.argmin(dist_p, axis = 1)

            center_p_old = center_p_new
            # Calculate mean for every cluster and update the center
            for i in range(k_p):
                center_p_new[i] = np.mean(cp[cluster_p == i], axis=0)
            error_p = np.linalg.norm(center_p_new - center_p_old)
        print('New cluster centers:',center_p_new)
        print('Updated clusters',cluster_p)

New cluster centers: [[0.29813113 0.57743738]
 [0.57296773 0.21630267]]
Updated clusters [0 0 0 1 0 0 1 0 1 1 1 1 1 1 1 1 0 0 1 1 0 0 1 0 1 1 1 1 1 0 1 0 0 0]
```


Finding cluster centers for the negative class

```
In [8]: k_n=2
center_n_old=np.zeros(center_n.shape)
center_n_new=center_n
cluster_n=np.zeros(len(cn))
dist_n=np.zeros((len(cn),k_n))
error_n = np.linalg.norm(center_n_new - center_n_old)

while error_n != 0:
    # Measure the distance to every center
    for i in range(k_n):
        dist_n[:,i] = np.linalg.norm(cn - center_n_new[i], axis=1)
    # Assign all training data to closest center
    cluster_n = np.argmin(dist_n, axis = 1)

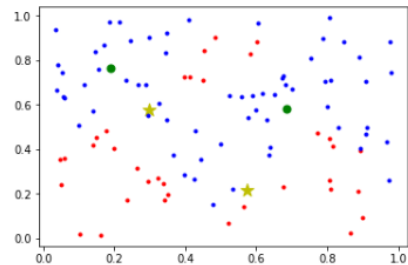
    center_n_old = center_n_new
    # Calculate mean for every cluster and update the center
    for i in range(k_n):
        center_n_new[i] = np.mean(cn[cluster_n == i], axis=0)
    error_n = np.linalg.norm(center_n_new - center_n_old)
print('New cluster centers:',center_n_new)
print('Updated clusters',cluster_n)

New cluster centers: [[0.19039576 0.76472406]
 [0.68544756 0.5807676 ]]
Updated clusters [0 1 0 1 0 1 1 0 1 1 1 0 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 0 0
 0 1 0 0 1 0 1 1 1 0 0 1 1 1 0 0 1 1 1 0 0 1 1 0 0]
```

Plotting the updated centers

```
In [9]: plt.plot(cp[:,0],cp[:,1], 'r-')
plt.scatter(center_p_new[:,0],center_p_new[:,1],marker='*',c='y',s=150)
plt.plot(cn[:,0],cn[:,1], 'b-')
plt.scatter(center_n[:,0],center_n[:,1],marker='o',c='g',s=50)
```

Out[9]: <matplotlib.collections.PathCollection at 0x1ef96703ef0>



Concatenating the updated centers of positive and negative class

```
In [10]: center=np.row_stack((center_p_new,center_n_new))
print(center)

[[0.29813113 0.57743738]
 [0.57296773 0.21630267]
 [0.19039576 0.76472406]
 [0.68544756 0.5807676 ]]
```

Computing the RBF function

```
In [11]: x_mu=np.zeros((100,len(center)))
for i in range(100):
    for j in range(len(center)):
        x_mu[i][j]=np.linalg.norm(x[:,i]-center[j,:])
rbf=np.exp(-16*np.square(x_mu))
```

Perceptron training algorithm

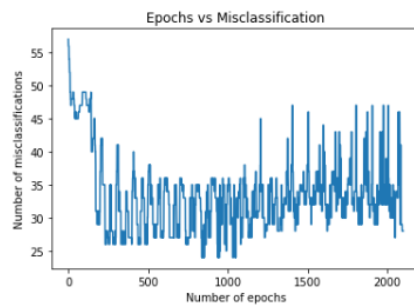
```
In [13]: K=4
W=np.zeros((K,1))
W=np.random.normal(size=(K,1))           #Initializing the weight vector
bias=np.random.randn(1)
errors=0                                  #Initializing the misclassifications
Mc=[]                                      #Storing the misclassification values after every epoch
epoch=0
lr=0.01
#rbf=np.row_stack([rbf_p,rbf_n])
```

```
In [15]: while(epoch==0 or Mc[epoch-1] > 28):
#       errors=0
       for i in range(len(rbf)):
           #errors=0
           y=np.sign(np.matmul(W.reshape(1,4),rbf[i].reshape(4,1))+bias)
           #Y=np.heaviside(y,1)
           print('actual',y)
           E=D[i]-y
           print('Error',E)
           Q=E*rbf[i].reshape(4,1)
           W=W+lr*Q
           bias=bias+lr*E
           errors = 0
       for j in range(len(rbf)):
           Y=np.sign(np.matmul(W.reshape(1,4),rbf[j].reshape(4,1))+bias)
           if Y != D[j]:
               errors=errors+1
       #       print('count',errors)

       Mc.append(errors)
       print('Misclassification',Mc[epoch])
       epoch=epoch+1
```

Plotting number of epochs against misclassification

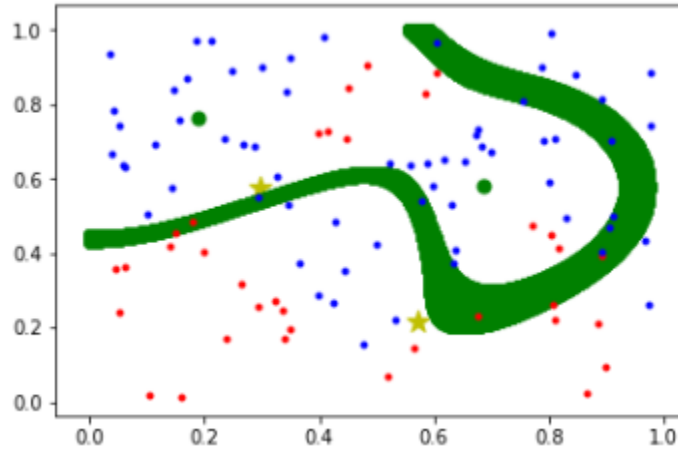
```
In [20]: plt.plot(Mc)
plt.xlabel('Number of epochs')
plt.ylabel('Number of misclassifications')
plt.title('Epochs vs Misclassification')
plt.show()
```



Plotting the decision boundary

```
In [21]: plt.plot(cp[:,0],cp[:,1], 'r-')
plt.scatter(center_p_new[:,0],center_p_new[:,1],marker='**',c='y',s=150)
plt.plot(cn[:,0],cn[:,1], 'b-')
plt.scatter(center_n[:,0],center_n[:,1],marker='o',c='g',s=50)
K_mu=0

for i in np.linspace(0,1,1000):
    for j in np.linspace(0,1,1000):
        g=0
        for k in range(len(center)):
            K_mu=np.linalg.norm(np.asarray([i,j])-center[k,:])
            RBF=np.exp(-16*np.square(K_mu))
            g=g+np.multiply(W[k],RBF)
        g=g+bias
        print('G:',g)
        if np.abs(g)<0.005:
            plt.scatter(i,j,c='g')
```



Observations:

1. Gaussian Radial Basis Function was used in designing this RBF network.

$$\phi(\|X - C_i\|) = e^{-\beta(\|X - C_i\|^2)}, \text{ where } i=1,2,\dots,\text{total number of centers}$$

2. It is seen that the network generated an accurate data classification boundary for the data points with 20 centers. As we decrease the number of clusters to 4, the network doesn't show a converging behavior, thereby not providing an accurate classification boundary.