



SAPIENZA
UNIVERSITÀ DI ROMA

LA SAPIENZA UNIVERSITÀ DI ROMA

DIPARTIMENTO DI INGEGNERIA INFORMATICA, AUTOMATICA E
GESTIONALE

TRAJECTORY ENCODING

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1 Trajectory Learning

2017 - Identifying Human Mobility via Trajectory Embeddings

[1] classifies users based on trajectory data. The problem is hard because there are many more trajectories than users.

[Recurrent Neural Network \(RNN\)](#) is used, and said to be good for classification when the number of labels is small. In particular uses a [Long Short-Term Memory \(LSTM\)](#) for processing sub-trajectories.

There is a location embedding, not sure how that is computed. But the trajectories are points on google maps, so there maybe be semantic information in there. The sequence of location embedding is passed onto the [LSTM](#), not sure how they handle different trajectory lengths.

2018 - Self-Consistent Trajectory Autoencoder: Hierarchical Reinforcement Learning with Trajectory Embeddings

Code on: <https://github.com/wyndwarrior/Sectar>

[2] learns an embedding for trajectories with one encoder and two decoders: a state decoder to decode from the latent space back into trajectories, and a policy decoder, which generates the trajectory in the environment. As such the state decoder predict the trajectory of the policy. The encoder is used in a hierarchical [Reinforcement Learning \(RL\)](#) setup.

The state encoder and decoder are [RNNs](#) and the policy decoder is a feed-forward [Neural Network \(NN\)](#).

note: if the encoder is trained with trajectories from different tasks, the policy will be conditioned to each task, what is sort of parameterizing the policy to tasks.

In the paper, the policy has unknown dynamics, and hence the [RL](#) setup. Trajectories are continuous poses of joints over time. Tested in simulation.

2018 - Anomalous Trajectory Detection Using Recurrent Neural Network

Code on: <https://github.com/LeeSongt/ATD-RNN>

[3] proposes anomalous trajectory detection using [RNN](#).

The trajectories are discretized, using a grid, and feed to a stacked [RNN](#) for learning the embedding, then a multi-layered perceptron and a soft-max layer detects if the trajectory is anomalous. The stacked [RNN](#) is made by feeding the hidden states of the previous to the next [RNN](#).

The trajectories are padded in order to get trajectories of the same length.

[LSTM](#) and [Gated Recurrent Unit \(GRU\)](#) are two special types of [RNNs](#) are tested. [GRUs](#) seems to work better.

2018 - Deep Representation Learning for Trajectory Similarity Computation

Code on: <https://github.com/boathit/t2vec>

[4] [Deep Learning \(DL\)](#) approach for trajectory similarity. States that using [RNN](#) is not a very good idea because you cannot reconstruct the trajectory and it fails to consider spatial proximity, which is inherited in trajectory data.

called in the paper as `t2vec` or `seq2seq`?

The approach is based on the encoder-decoder framework. Handling varying sampling rates is done by augmenting the training data creating sub-trajectories by sub-sampling and noise addition. They also propose a spatial-aware loss, and pre-train the `??cells??` and let them to be optimized during training.

Notes: The paper is very confusing. I do not really know that are the inputs and outputs or how the sequences are fed in the [RNN](#) inside the encoder.

2019 - Predicting Dynamic Embedding Trajectory in Temporal Interaction Networks

[5]

2019 - Computing Trajectory Similarity in Linear Time: A Generic Seed-Guided Neural Metric Learning Approach

[6]

2020 - Trembr: Exploring Road Networks for Trajectory Representation Learning
[\[7\]](#)

2020 - Trajectory similarity learning with auxiliary supervision and optimal matching
[\[8\]](#)

2020 - Semantic trajectory representation and retrieval via hierarchical embedding
[\[9\]](#)

2020 - MARC: a robust method for multiple-aspect trajectory classification via space, time, and semantic embeddings
[\[10\]](#)

2021 - Multiple Object Tracking by Trajectory Map Regression with Temporal Priors Embedding
[\[11\]](#)

2021 - Embedding-Based Similarity Computation for Massive Vehicle Trajectory Data
[\[12\]](#)

2021 - STENet: A hybrid spatio-temporal embedding network for human trajectory forecasting
[\[13\]](#)

2021 - A Graph-Based Approach for Trajectory Similarity Computation in Spatial Networks
[\[14\]](#)

2021 - T3S: Effective Representation Learning for Trajectory Similarity Computation
[\[15\]](#)

2021 - How meaningful are similarities in deep trajectory representations?
[\[16\]](#)

2022 - Deep Fuzzy Contrast-Set Deviation Point Representation and Trajectory Detection
[\[17\]](#)

2022 - Contrastive Pre-training of Spatial-Temporal Trajectory Embeddings
[\[18\]](#)

2022 - TMN: Trajectory Matching Networks for Predicting Similarity
[\[19\]](#)

2022 - TSNE: Trajectory Similarity Network Embedding

[\[20\]](#)

2022 - Towards robust trajectory similarity computation: Representation-based spatio-temporal similarity quantification

[\[21\]](#)

2023 - GRLSTM: Trajectory Similarity Computation with Graph-Based Residual LSTM

[\[22\]](#)

2023 - Spatial-temporal fusion graph framework for trajectory similarity computation

[\[23\]](#)

2023 - Contrastive Trajectory Similarity Learning with Dual-Feature Attention

[\[24\]](#)

2023 - Spatio-Temporal Trajectory Similarity Measures: A Comprehensive Survey and Quantitative Study

[\[25\]](#)

2 Trajectory Learning on Robotics

1991 - Solving the moving obstacle path planning problem using embedded variational methods

[\[26\]](#)

2016 - Robobarista: Learning to Manipulate Novel Objects via Deep Multimodal Embedding

[\[27\]](#)

2020 - Controlling Assistive Robots with Learned Latent Actions

[\[28\]](#)

2020 - DiversityGAN: Diversity-Aware Vehicle Motion Prediction via Latent Semantic Sampling

[\[29\]](#)

2021 - Use of Embedding Spaces for Transferring Robot Skills in Diverse Sensor Settings

[\[30\]](#)

2022 - STL2vec: Signal Temporal Logic Embeddings for Control Synthesis With Recurrent Neural Networks

[\[31\]](#)

2022 - Learning latent actions to control assistive robots

[\[32\]](#)

2022 - Promoting Quality and Diversity in Population-based Reinforcement Learning via Hierarchical Trajectory Space Exploration

[\[33\]](#)

2023 - SIRL: Similarity-Based Implicit Representation Learning

[\[34\]](#)

3 Comparison

4 Challenges

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