

NCSI:Basic

1.0

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1 Non-canonical Symplectic Integrator: Basic

Minimalist implementation of guiding center trajectory calculation. A fourth-order Runge-Kutta and noncanonical symplectic algorithm are present for the calculation of charged particle guiding center trajectories in electric and magnetic fields. An axisymmetric tokamak field is used for demonstration.

Installation

The NCSI:Basic code uses the `BOOST::program_options` library for option specification and the `Eigen` library for linear algebra tasks. Eigen is a header-only library available at <http://eigen.tuxfamily.org/>. The compiler needs to know where to find the header files, so placing the Eigen package somewhere like `/usr/local/include` is a good idea.

Usage

After compiling and linking the executable "driver", see a summary of runtime options using `driver --help`

The options may be specified on the command line with `--option` or `-O`. Alternatively, one may specify input options using an input file. See `sample_input.cfg` for an example. Units are discussed in the documentation.

Upgrade to PRO Today!

Full version of NCSI includes:

- Additional ODE systems (oscillators, magnetic field line flow)
- Additional integrators (linear multistep methods, implicit midpoint)
- Improved class hierarchy (ImplicitIntegrator, MultistepIntegrator)
- Automatic differentiation (with [ADOLC](#))
- Field writing routines (with Python and Sympy)
- Unittests (using [gTest](#))

2 Users Guide

2.1 Command Line Use

To call `code_solver` from the command line, one must specify several “mandatory” options. From the command line, call: `code_solver --help` to see a help message summarizing the mandatory options and several commonly used options. For a full list of options, consult input_parser.cc.

2.2 Configuration File Use

Alternatively, one may specify all mandatory options and any optional options within a configuration file and pass the configuration file to `code_solver`. The syntax is: `code_solver input.cfg`

Within the input file, one specifies the options using: `option_name=option_value`

For multitoken options, the present method is to repeatedly specify the option: `multivalue_option=option_value1`
`multivalue_option=option_value2`

2.3 A note on units

Units are specified in the `input_sample.cfg` file, and conversions from standard units should be straight forward. The system of units listed emerges by starting with cgs units, then normalizing the vector potential A by (mc/e) and scalar potential ϕ by (m/e) where c is the speed of light in $[cm/s]$, e is the particle charge in $[StatCoulombs]$, and m is the particle mass in $[g]$. After normalizing these potentials, the units of A become $[length/time]$ or $[cm/s]$ and B become $[1/time]$ or $[1/s]$. To obtain order 1 quantities for typical fusion test particles, it is helpful to scale the time units from $[seconds]$ to $[10^{-8} seconds]$. A choice of $B_0 = 1$ then APPROXIMATELY corresponds to a magnetic field of 1 Tesla for a proton test particle. That is: $B_{0_SI} = 1 [Tesla]$, $B_{0_cgs} = 10^4 Gauss$, $B_{0_norm} = (1.0447 \cdot 10^8) [s^{-1}]$, $B_{0_norm} = 1 [10^{-8} s^{-1}]$. A choice of $B_0 = 1$ in normalized units corresponds to slightly less than 1 Tesla to the extent that (mc/e) for a proton is greater than 10^4 .

As a final note, one may more generally consider the coordinates by normalizing by B_0 , R_0 . The units of length then becomes R_0 's and the units of time $1/B_0$'s. Setting these parameters to 1.0 in the input file accomplishes this goal. However, the current units have been specified to be more intuitive.

3 Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

EMFields	6
AxisymmetricTokamak	4
GuidingCenter	7
InputParser	8
Integrator	9
NoncanonicalSymplectic	10
RungeKutta	12

4 Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

AxisymmetricTokamak	4
EMFields	6
GuidingCenter	7
InputParser	8
Integrator	9
NoncanonicalSymplectic	10
RungeKutta	12

5 File Index

5.1 File List

Here is a list of all documented files with brief descriptions:

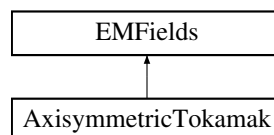
axisymmetric_tokamak.cc	
EMFields derived class which implements the axisymmetric fields in Qin_2009	14
axisymmetric_tokamak.h	
EMFields derived class which implements the axisymmetric fields in Qin_2009 in cylindrical coordinates	14
driver.cc	
Implements driver for integrating guiding center trajectories	15
em_fields.h	
Header for EMFields abstract base class which defines the interfaces for electromagnetic field quantities used in calculating, for instance, guiding center trajectories	16
guiding_center.cc	
Implementation of GuidingCenter system	16

guiding_center.h	Header for GuidingCenter system describing the motion of charged magnetized particles in magnetic fields	16
input_parser.cc	Implementation of InputParser class. Sets runtime options	17
input_parser.h	Interface for input parser class. Recieves command line input from driver and outputs essential information for running the driver	17
integrator.h	Header for Integrator abstract base class. Step is pure virtual. Declares members kdt_, model_ and kDimen_	18
noncanonical_symplectic.cc	Implementation of integrator resulting from a midpoint discretization of the guiding center Lagrangian. Implements a step which interfaces with the base class integrators and defines the update rule	18
noncanonical_symplectic.h	Header for integrator resulting from a midpoint discretization of the guiding center Lagrangian	19
runge-kutta.cc	Implementation of general Runge-Kutta	19
runge-kutta.h	Header for general Runge-Kutta integrator	20

6 Class Documentation

6.1 AxisymmetricTokamak Class Reference

Inheritance diagram for AxisymmetricTokamak:



Public Member Functions

- [AxisymmetricTokamak](#) (const double kB0, const double kR0)
Construct [AxisymmetricTokamak](#) which derives from [EMFields](#). Set constants b0, r0.
- void [VectorPotentialA](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &a) const
Evaluates Vector potential A.
- void [GradA](#) (const double kt, const Eigen::VectorXd &kx, Eigen::MatrixXd &grad_a) const
Evaluates Matrix of derivatives of vector potential A.
- void [BHat](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &b_hat) const
Evaluates Unit vector in the direction of the magnetic field.
- void [GradBHat](#) (const double kt, const Eigen::VectorXd &kx, Eigen::MatrixXd &grad_b_hat) const
Evaluates Gradient matrix of magnetic field unit vector.
- void [GradPhi](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &grad_phi) const

Evaluates Gradient of scalar potential ϕ .

- void [GradModB](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &grad_mod_b) const

Evaluates Gradient of magnetic field magnitude.

Private Attributes

- const double [kB0_](#)
Magnetic field on-axis amplitude in [Tesla].
- const double [kR0_](#)
Major radius of tokamak in [cm].

6.1.1 Constructor & Destructor Documentation

6.1.1.1 AxisymmetricTokamak::AxisymmetricTokamak (const double *kB0*, const double *kR0*)

Construct [AxisymmetricTokamak](#) which derives from [EMFields](#). Set constants b0, r0.

Parameters

in	<i>kB0</i>	Magnetic field strength in [Tesla] (see documentation)
in	<i>kR0</i>	Major radius of tokamak in [cm]

6.1.2 Member Function Documentation

6.1.2.1 void AxisymmetricTokamak::BHat (const double *kUnusedt*, const Eigen::VectorXd & *kx*, Eigen::Vector3d & *b_hat*) const [virtual]

Evaluates Unit vector in the direction of the magnetic field.

Parameters

in	<i>kUnusedt</i>	Current time (fields time independent)
in	<i>kx</i>	Position in cartesian coordinates
out	<i>b_hat</i>	Unit vector in the direction of the magnetic field

Implements [EMFields](#).

6.1.2.2 void AxisymmetricTokamak::GradA (const double *kUnusedt*, const Eigen::VectorXd & *kx*, Eigen::MatrixXd & *grad_a*) const [virtual]

Evaluates Matrix of derivatives of vector potential A.

Parameters

in	<i>kUnusedt</i>	Current time (fields time independent)
in	<i>kx</i>	Position in cartesian coordinates
out	<i>grad_a</i>	Matrix of derivatives of vector potential A

Implements [EMFields](#).

6.1.2.3 void AxisymmetricTokamak::GradBHat (const double *kUnusedt*, const Eigen::VectorXd & *kx*, Eigen::MatrixXd & *grad_b_hat*) const [virtual]

Evaluates Gradient matrix of magnetic field unit vector.

Parameters

in	<i>kUnusedt</i>	Current time (fields time independent)
in	<i>kx</i>	Position in cartesian coordinates
out	<i>grad_b_hat</i>	Gradient matrix of magnetic field unit vector

Implements [EMFields](#).

6.1.2.4 `void AxisymmetricTokamak::GradModB (const double kUnusedt, const Eigen::VectorXd & kx, Eigen::Vector3d & grad_mod_b) const` [virtual]

Evaluates Gradient of magnetic field magnitude.

Parameters

in	<i>kUnusedt</i>	Current time (fields time independent)
in	<i>kx</i>	Position in cartesian coordinates
out	<i>grad_mod_b</i>	Gradient of magnetic field magnitude

Implements [EMFields](#).

6.1.2.5 `void AxisymmetricTokamak::GradPhi (const double kUnusedt, const Eigen::VectorXd & kUnusedx, Eigen::Vector3d & grad_phi) const` [virtual]

Evaluates Gradient of scalar potential phi.

Parameters

in	<i>kUnusedt</i>	Current time (fields time independent)
in	<i>kUnusedx</i>	Position in cartesian coordinates
out	<i>grad_phi</i>	Gradient of scalar potential phi

Implements [EMFields](#).

6.1.2.6 `void AxisymmetricTokamak::VectorPotentialA (const double kUnusedt, const Eigen::VectorXd & kx, Eigen::Vector3d & a) const` [virtual]

Evaluates Vector potential A.

Parameters

in	<i>kUnusedt</i>	Current time (fields time independent)
in	<i>kx</i>	Position in cartesian coordinates
out	<i>a</i>	Vector potential A

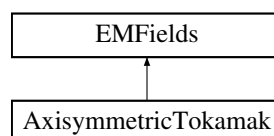
Implements [EMFields](#).

The documentation for this class was generated from the following files:

- [axisymmetric_tokamak.h](#)
- [axisymmetric_tokamak.cc](#)

6.2 EMFields Class Reference

Inheritance diagram for EMFields:



Public Member Functions

- virtual void [VectorPotentialA](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &a) const =0
Fetch vector potential A.
- virtual void [GradA](#) (const double kt, const Eigen::VectorXd &kx, Eigen::MatrixXd &grad_a) const =0
Fetch gradient matrix of the vector potential A.
- virtual void [BHat](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &b_hat) const =0
Fetch unit vector in direction of magnetic field.
- virtual void [GradBHat](#) (const double kt, const Eigen::VectorXd &kx, Eigen::MatrixXd &grad_b_hat) const =0
Fetch gradient matrix of magnetic field unit vector.
- virtual void [GradPhi](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &grad_phi) const =0
Fetch gradient of scalar potential.
- virtual void [GradModB](#) (const double kt, const Eigen::VectorXd &kx, Eigen::Vector3d &grad_mod_b) const =0
Fetch gradient of magnetic field magnitude.

The documentation for this class was generated from the following file:

- [em_fields.h](#)

6.3 GuidingCenter Class Reference

Public Member Functions

- [GuidingCenter](#) ([EMFields](#) *[em_fields](#), const double [kMu](#))
Constructor which sets magnetic moment and initializes fields.
- int [VectorField](#) (const double kt, const Eigen::VectorXd &kx, Eigen::VectorXd &fx) const
Evaluates vector field of ODE. f in $\text{dot}\{x\} = f(x)$
- [EMFields](#) * [em_fields](#) () const
Return pointer to [em_fields](#) instance.
- int [kDimen](#) () const
Return dimension of ODE system.
- double [kMu](#) () const
Return value of μ .

Private Attributes

- [EMFields](#) * [em_fields_](#)
Pointer to class defining electromagnetic fields.
- const double [kMu_](#)
Magnetic moment.

Static Private Attributes

- static const int [kDimen_](#) = 4
Dimension of ODE system.

6.3.1 Constructor & Destructor Documentation

6.3.1.1 GuidingCenter::GuidingCenter ([EMFields](#) * [em_fields](#), const double [kMu](#))

Constructor which sets magnetic moment and initializes fields.

Parameters

in	<i>em_fields</i>	
in	<i>kMu</i>	Magnetic moment in [cm ² /10 ⁻⁸ s]

6.3.2 Member Function Documentation**6.3.2.1** `int GuidingCenter::VectorField (const double kt, const Eigen::VectorXd & kx, Eigen::VectorXd & fx) const`

Evaluates vector field of ODE. f in $\dot{x} = f(x)$

Evaluation of guiding center equations of motion.

Letting x be particle position and u the velocity: $\dot{x}_i = (B^{\wedge}_{\text{dag}}_i u - (b \times E^{\wedge}_{\text{dag}})_i) / B^{\wedge}_{\text{dag}}$

$$\dot{u} = (B^{\wedge}_{\text{dag}} \dot{E}^{\wedge}_{\text{dag}}) / B^{\wedge}_{\text{dag_par}}$$

Parameters

in	<i>kt</i>	Time
in	<i>kx</i>	Position of guiding center particle [x u]
out	<i>fx</i>	Right hand side of $\dot{x} = f(x)$

Returns

zero if success

The documentation for this class was generated from the following files:

- [guiding_center.h](#)
- [guiding_center.cc](#)

6.4 InputParser Class Reference**Public Member Functions**

- `int ReadInput (int argc, char **argv)`
- `template<typename T>`
`int GetValue (const char *key, T &value_out) const`

Private Attributes

- `po::variables_map variables_map_`
Program Options variables map.

6.4.1 Member Function Documentation**6.4.1.1** `template<typename T> int InputParser::GetValue (const char * key, T & value_out) const` [*inline*]

Accessors Retrieve the value at key and output it to value_out

6.4.1.2 `int InputParser::ReadInput (int argc, char ** argv)`

Read command line arguments and notify variables map of runtime options.

Parameters

in	<i>argc</i>	Number of input arguments
in	<i>argv</i>	Input arguments

Returns

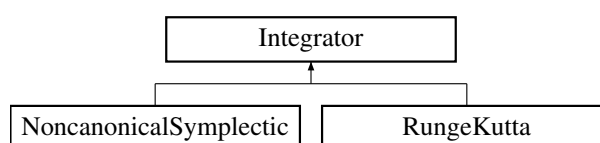
Zero for success

The documentation for this class was generated from the following files:

- [input_parser.h](#)
- [input_parser.cc](#)

6.5 Integrator Class Reference

Inheritance diagram for Integrator:



Public Member Functions

- [Integrator](#) (const double kdt, const [GuidingCenter](#) &kGuidingCenter)
Constructor - Save model, stepsize, and dimension.
- virtual int [Step](#) (double &t, Eigen::VectorXd &x)=0
Time-advance map from $(t_k, x_k) \rightarrow (t_{k+1}, x_{k+1})$.
- virtual void [Reset](#) ()
Method used in multistep integrators.

Protected Attributes

- const double [kdt_](#)
Numerical Step Size.
- const [GuidingCenter](#) & [kGuidingCenter_](#)
ODE model.
- const int [kDimen_](#)
Dimension of the ODE system.

6.5.1 Constructor & Destructor Documentation

6.5.1.1 Integrator::Integrator (const double kdt, const GuidingCenter &kGuidingCenter) [inline]

Constructor - Save model, stepsize, and dimension.

Parameters

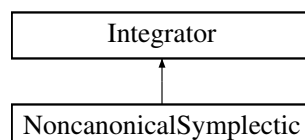
in	<i>kdt</i>	Numerical Step Size
in	<i>kGuidingCenter</i>	ODE Model instance

The documentation for this class was generated from the following file:

- [integrator.h](#)

6.6 NoncanonicalSymplectic Class Reference

Inheritance diagram for NoncanonicalSymplectic:



Public Member Functions

- [NoncanonicalSymplectic](#) (const double kdt, const [GuidingCenter](#) &kGuidingCenter, const double kNewtonTolerance, const double kMaxIterations)
- int [Step](#) (double &t, Eigen::VectorXd &x)
Advance t and x forward in time.
- void [Reset](#) ()
Method used in multistep integrators.

Protected Member Functions

- int [StoreHistory](#) (const Eigen::VectorXd &kx)
StoreHistory updates member x_history_ by knocking off the oldest data and putting on the newest.
- int [InitialStep](#) (double &t, Eigen::VectorXd &x) const
- int [UpdateRule](#) (const double kt, const Eigen::VectorXd &kx, Eigen::VectorXd &error) const
Function which should evaluate to zero(vector) when the algorithm is satisfied.
- int [NewtonGuess](#) (double &t, Eigen::VectorXd &x) const
Guess for initializing NewtonSolver. Uses ForwardEuler.
- int [Jacobian](#) (const double kt, const Eigen::VectorXd &kx, Eigen::MatrixXd &jacobian) const
Calculates Jacobian matrix used in nonlinear solve. This base-class version uses a centered finite difference on the update rule.

Protected Attributes

- const double [kMu_](#)
Magnetic moment of particle.
- const double [kNewtonTolerance_](#)
Error threshold for nonlinear solve.
- const double [kMaxIterations_](#)
Maximum allowable Newton iterations.
- bool [needs_initialization_](#)
Flag for needing initial conditions.
- Eigen::MatrixXd [x_history_](#)
Stores previous positions.
- [EMFields](#) * [em_fields_](#)
Field definitions pulled from [GuidingCenter](#).

6.6.1 Constructor & Destructor Documentation

6.6.1.1 NoncanonicalSymplectic::NoncanonicalSymplectic (const double *kdt*, const GuidingCenter & *kGuidingCenter*, const double *kNewtonTolerance*, const double *kMaxIterations*)

Constructor - Initializes members and base class [Integrator](#). Sets size of `x_history_` to have a number of rows equal to the dimension of the ODE system and number of columns equal to the number of steps in the multistep method. In this case, two.

Parameters

in	<i>kdt</i>	Numerical Step Size
in	<i>kGuidingCenter</i>	ODE being modeled
in	<i>kNewtonTolerance</i>	Error threshold for nonlinear solve
in	<i>kMaxIterations</i>	Maximum number of nonlinear solve iterations

6.6.2 Member Function Documentation

6.6.2.1 int NoncanonicalSymplectic::InitialStep (double & *t*, Eigen::VectorXd & *x*) const [protected]

InitialStep advances *t* and *x* using RK4. To be used while `needs_initialization_` is true.

Parameters

in, out	<i>t</i>	Simulation time. Advanced by <i>kdt</i> .
in, out	<i>x</i>	Position. At in: $x(t=t_k)$ At out: $x(t=t_{k+1})$

Returns

0 upon success

6.6.2.2 int NoncanonicalSymplectic::Jacobian (const double *kt*, const Eigen::VectorXd & *kx*, Eigen::MatrixXd & *jacobian*) const [protected]

Calculates Jacobian matrix used in nonlinear solve. This base-class version uses a centered finite difference on the update rule.

Parameters

in	<i>kt</i>	Simulation time at newest point.
in	<i>kx</i>	Position at newest point.
out	<i>jacobian</i>	derivative of the update rule w.r.t the new position

Returns

Integer code which is 0 if successful.

6.6.2.3 int NoncanonicalSymplectic::NewtonGuess (double & *t*, Eigen::VectorXd & *x*) const [protected]

Guess for initializing NewtonSolver. Uses ForwardEuler.

Parameters

in, out	<i>t</i>	Simulation time. Advanced by step size <i>kdt</i>
in, out	<i>x</i>	Position to advance to initial guess for solver

Returns

Zero for success

6.6.2.4 `int NoncanonicalSymplectic::Step (double & t, Eigen::VectorXd & x) [virtual]`

Advance t and x forward in time.

If this is the first step, some additional initial conditions need to be generated. At present, this is performed using RK4. Otherwise, solve the implicit map defined by the discrete Euler-Lagrange equations.

Parameters

in	t	Physical time at this step. For time-dependent systems.
in, out	x	Vector of current coordinates. Will be updated to x(t+h).

Returns

Integer code which is 0 if successful.

Implements [Integrator](#).

6.6.2.5 `int NoncanonicalSymplectic::StoreHistory (const Eigen::VectorXd & kx) [protected]`

StoreHistory updates member x_history_ by knocking off the oldest data and putting on the newest.

Parameters

in	kx	New position to store
----	----	-----------------------

Returns

0 upon success

6.6.2.6 `int NoncanonicalSymplectic::UpdateRule (const double kt, const Eigen::VectorXd & kx, Eigen::VectorXd & error) const [protected]`

Function which should evaluate to zero(vector) when the algorithm is satisfied.

Parameters

in	kt	Simulation time at proposed new position
in	kx	New position to test
out	error	Error vector which is zero for satisfied update rule.

Returns

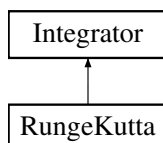
Zero for success

The documentation for this class was generated from the following files:

- [noncanonical_symplectic.h](#)
- [noncanonical_symplectic.cc](#)

6.7 RungeKutta Class Reference

Inheritance diagram for RungeKutta:



Public Member Functions

- [RungeKutta](#) (const double kdt, const [GuidingCenter](#) &kGuidingCenter, const Eigen::MatrixXd [a_coefficients](#), const Eigen::VectorXd [b_coefficients](#), const Eigen::VectorXd [c_coefficients](#))
Constructor for general runge-kutta methods. Specify the coefficients in eigen vectors/matrices.
- [RungeKutta](#) (const double kdt, const [GuidingCenter](#) &kGuidingCenter, const int kOrder)
Constructor which implements common methods for convenience. Specify an order with an integer, and this constructor will set the corresponding coefficients.
- int [Step](#) (double &t, Eigen::VectorXd &x)
Explicit advance $x(t)$ forward in time by step size kdt. RK: $x_{n+1} = x_n + \sum_{i=1}^s b_{i,k} k_i = h f(t_n + c_i h, y_n + \sum_{j=1}^{i-1} a_{ij} k_j$.
- Eigen::MatrixXd [a_coefficients](#) () const
- Eigen::VectorXd [b_coefficients](#) () const
Access $b_{\text{coefficients}}$ vector.
- Eigen::VectorXd [c_coefficients](#) () const
Access $c_{\text{coefficients}}$ vector.

Private Attributes

- Eigen::MatrixXd [a_](#)
Specifies for a_{ij} coefficients of the RK method.
- Eigen::VectorXd [b_](#)
Specifies b_i coefficients of the RK method.
- Eigen::VectorXd [c_](#)
Specifies c_i coefficients of the RK method.
- Eigen::MatrixXd [k_](#)
Temporary space for k_i evaluations.
- Eigen::VectorXd [xtemp_](#)
Temporary space used at internal stages.
- Eigen::VectorXd [ftemp_](#)
Temporary space for function evaluations.

Additional Inherited Members

6.7.1 Constructor & Destructor Documentation

6.7.1.1 [RungeKutta::RungeKutta](#) (const double kdt, const [GuidingCenter](#) & kGuidingCenter, const Eigen::MatrixXd [a_coefficients](#), const Eigen::VectorXd [b_coefficients](#), const Eigen::VectorXd [c_coefficients](#))

Constructor for general runge-kutta methods. Specify the coefficients in eigen vectors/matrices.

Parameters

in	<i>kdt</i>	Numerical step size
in	<i>kGuidingCenter</i>	ODE system being modeled
in	<i>a_coefficients</i>	Matrix with a_{ij} coefficients in Butch. tableau
in	<i>b_coefficients</i>	Vector with b_i coefficients in Butcher tableau
in	<i>c_coefficients</i>	Vector with c_i coefficients in Butcher tableau

6.7.1.2 [RungeKutta::RungeKutta](#) (const double kdt, const [GuidingCenter](#) & kGuidingCenter, const int kOrder)

Constructor which implements common methods for convenience. Specify an order with an integer, and this constructor will set the corresponding coefficients.

Parameters

in	<i>kdt</i>	Numerical step size
in	<i>kGuidingCenter</i>	ODE system being solved
in	<i>kOrder</i>	Order of Runge-Kutta method. 2 and 4 are implemented.

6.7.2 Member Function Documentation**6.7.2.1 Eigen::MatrixXd RungeKutta::a_coefficients () const [inline]**

Accessors Access a_ coefficients matrix

6.7.2.2 int RungeKutta::Step (double & t, Eigen::VectorXd & x) [virtual]

Explicit advance $x(t)$ forward in time by step size kdt . RK: $x_{n+1} = x_n + \sum_{i=1}^s b_i k_i$, $k_i = h f(t_n + c_i h, y_n + \sum_{j=1}^{i-1} a_{ij} k_j)$.

Parameters

in, out	<i>t</i>	Simulation time. Advanced by <i>kdt</i>
in, out	<i>x</i>	Position. At in: $x(t=t_k)$ At out: $x(t=t_{k+1})$

Implements [Integrator](#).

The documentation for this class was generated from the following files:

- [runge-kutta.h](#)
- [runge-kutta.cc](#)

7 File Documentation**7.1 axisymmetric_tokamak.cc File Reference**

[EMFields](#) derived class which implements the axisymmetric fields in Qin_2009.

```
#include "axisymmetric_tokamak.h"
```

7.1.1 Detailed Description

[EMFields](#) derived class which implements the axisymmetric fields in Qin_2009.

Date

Feb 2014

Author

C. Leland Ellison

7.2 axisymmetric_tokamak.h File Reference

[EMFields](#) derived class which implements the axisymmetric fields in Qin_2009 in cylindrical coordinates.

```
#include "em_fields.h"
#include <Eigen/Dense>
```


Classes

- class [AxisymmetricTokamak](#)

7.2.1 Detailed Description

[EMFields](#) derived class which implements the axisymmetric fields in Qin_2009 in cylindrical coordinates.

Date

Feb 2014

Author

C. Leland Ellison

7.3 driver.cc File Reference

Implements driver for integrating guiding center trajectories.

```
#include <stdlib.h>
#include <iostream>
#include <Eigen/Dense>
#include <ctime>
#include "input_parser.h"
#include "guiding_center.h"
#include "em_fields.h"
#include "axisymmetric_tokamak.h"
#include "integrator.h"
#include "runge-kutta.h"
#include "noncanonical_symplectic.h"
```

Functions

- void [PrintState](#) (double t, const Eigen::VectorXd &x, int n_digits)
Prints a line to standard out giving [time x[0] x[1]].
- int [main](#) (int argc, char *argv[])
Body of the driver. Use program options to specify ode, integrator, dt, and n_steps.

7.3.1 Detailed Description

Implements driver for integrating guiding center trajectories.

Date

Feb 2014

Author

C. Leland Ellison

7.3.2 Function Documentation

7.3.2.1 void PrintState (double t, const Eigen::VectorXd & x, int n_digits)

Prints a line to standard out giving [time x[0] x[1]].

Parameters

in	t	Time
in	x	Position vector
in	n_digits	Number of digits to display in output

7.4 em_fields.h File Reference

Header for [EMFields](#) abstract base class which defines the interfaces for electromagnetic field quantities used in calculating, for instance, guiding center trajectories.

```
#include <Eigen/Dense>
```

Classes

- class [EMFields](#)

7.4.1 Detailed Description

Header for [EMFields](#) abstract base class which defines the interfaces for electromagnetic field quantities used in calculating, for instance, guiding center trajectories.

Date

Feb 2014

Author

C. Leland Ellison

7.5 guiding_center.cc File Reference

Implementation of [GuidingCenter](#) system.

```
#include "guiding_center.h"
```

7.5.1 Detailed Description

Implementation of [GuidingCenter](#) system.

Date

Feb 2014

Author

C. Leland Ellison

7.6 guiding_center.h File Reference

Header for [GuidingCenter](#) system describing the motion of charged magnetized particles in magnetic fields.

```
#include <Eigen/Dense>
#include "em_fields.h"
```

Classes

- class [GuidingCenter](#)

7.6.1 Detailed Description

Header for [GuidingCenter](#) system describing the motion of charged magnetized particles in magnetic fields. Guiding center equations of motion $\dot{x}_i = (B^{\wedge} \text{dag}_i u - (b \times E^{\wedge} \text{dag})_i) / B^{\wedge} \text{dag}_i$

$$\dot{u} = (B^{\wedge} \text{dag} \cdot E^{\wedge} \text{dag}) / B^{\wedge} \text{dag}_{\text{par}}$$

Date

Feb 2014

Author

C. Leland Ellison

7.7 input_parser.cc File Reference

Implementation of [InputParser](#) class. Sets runtime options.

```
#include "input_parser.h"
```

7.7.1 Detailed Description

Implementation of [InputParser](#) class. Sets runtime options.

Date

Jan 2014

Author

C. Leland Ellison

Version

0.1

7.8 input_parser.h File Reference

Interface for input parser class. Recieves command line input from driver and outputs essential information for running the driver.

```
#include <stdlib.h>
#include <fstream>
#include <boost/program_options.hpp>
```

Classes

- class [InputParser](#)

7.8.1 Detailed Description

Interface for input parser class. Recieves command line input from driver and outputs essential information for running the driver.

Date

Jan 2014

Author

C. Leland Ellison

Version

0.1

7.9 integrator.h File Reference

Header for [Integrator](#) abstract base class. Step is pure virtual. Declares members kdt_, model_ and kDimen_.

```
#include "guiding_center.h"
#include <Eigen/Dense>
```

Classes

- class [Integrator](#)

7.9.1 Detailed Description

Header for [Integrator](#) abstract base class. Step is pure virtual. Declares members kdt_, model_ and kDimen_.

Date

Feb 2014

Author

C. Leland Ellison

7.10 noncanonical_symplectic.cc File Reference

Implementation of integrator resulting from a midpoint discretization of the guiding center Lagrangian. Implements a step which interfaces with the base class integrators and defines the update rule.

```
#include "noncanonical_symplectic.h"
```

7.10.1 Detailed Description

Implementation of integrator resulting from a midpoint discretization of the guiding center Lagrangian. Implements a step which interfaces with the base class integrators and defines the update rule.

Date

Jan 2014

Author

C. Leland Ellison

7.11 noncanonical_symplectic.h File Reference

Header for integrator resulting from a midpoint discretization of the guiding center Lagrangian.

```
#include "guiding_center.h"
#include "em_fields.h"
#include "integrator.h"
#include <iostream>
#include <Eigen/Dense>
#include "runge-kutta.h"
```

Classes

- class [NoncanonicalSymplectic](#)

7.11.1 Detailed Description

Header for integrator resulting from a midpoint discretization of the guiding center Lagrangian.

Date

Feb 2014

Author

C. Leland Ellison

7.12 runge-kutta.cc File Reference

Implementation of general Runge-Kutta.

```
#include "runge-kutta.h"
```

7.12.1 Detailed Description

Implementation of general Runge-Kutta.

Date

October 2013

Author

C. Leland Ellison

Version

0.1

7.13 runge-kutta.h File Reference

Header for general Runge-Kutta integrator.

```
#include "integrator.h"
#include <Eigen/Dense>
#include "guiding_center.h"
#include <iostream>
```

Classes

- class [RungeKutta](#)

7.13.1 Detailed Description

Header for general Runge-Kutta integrator.

Date

Feb 2014

Author

C. Leland Ellison

Version

0.1

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