

Introduction to Deep Learning

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Parts of slides referenced from

Nvidia, *Deep Learning Institute (DLI) Teaching Kit*

Stanford, *CS231n: Convolutional Neural Networks for Visual Recognition*

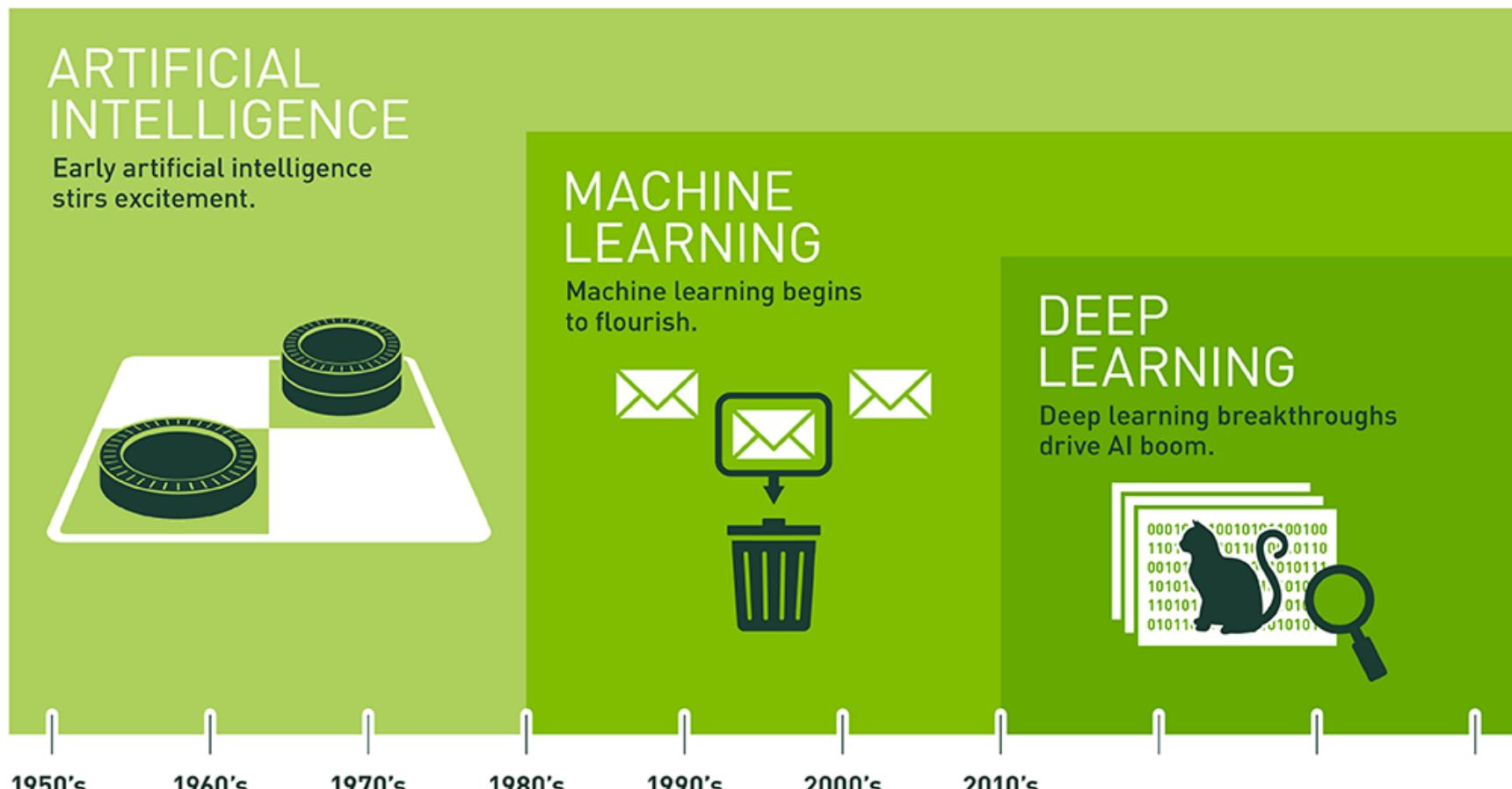
Martin Görner, *Learn TensorFlow and deep learning, without a Ph.D*

Luis Serrano, *A friendly introduction to Convolutional Neural Networks and Image Recognition*

Topics To Be Discussed

- **Fundamentals about Machine Learning**
 - What is *Deep Learning*?
 - What is a (deep) neural network
 - How to train it
 - Deep Learning Frameworks
- **Build a neural network model using Keras/TensorFlow**
 - MNIST example
 - Softmax classification
 - Cross-entropy cost function
 - A 5 layer deep neural network
 - Dropout
 - Convolutional networks

AI, Machine Learning and Deep Learning

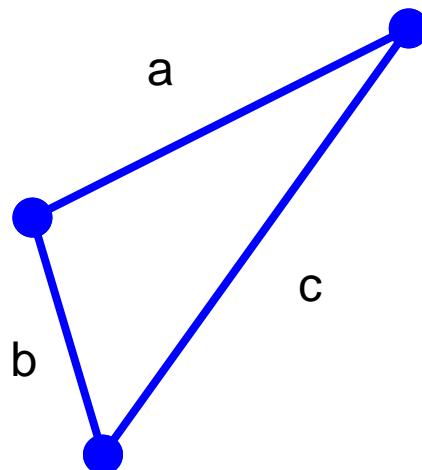


Since an early flush of optimism in the 1950s, smaller subsets of artificial intelligence – first machine learning, then deep learning, a subset of machine learning – have created ever larger disruptions.

Applications of Machine Learning

- **Computer Vision (CV)**
 - Image Classification
 - label images with appropriate categories (e.g. Google Photos)
 - Handwriting Recognition
 - convert written letters into digital letters
- **Natural Language Processing (NLP)**
 - Language Translation
 - translate spoken and or written languages (e.g. Google Translate)
 - Speech Recognition
 - convert voice snippets to text (e.g. Siri, Cortana, and Alexa)
- **Autonomous Driving**
 - enable cars to drive

How to recognize a triangle?



formula:

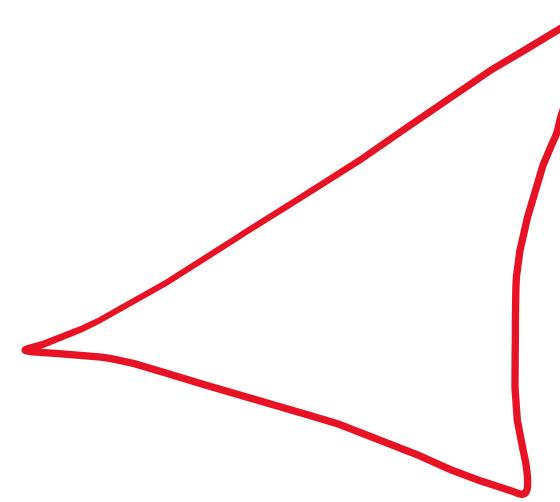
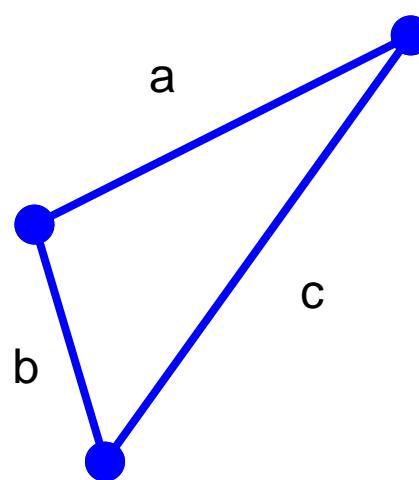
$$a + b > c$$
$$a + c > b$$
$$b + c > a$$

Given :

$$a = 7 \quad b = 10 \quad c = 5$$


wiki How to Determine if Three Side Lengths Are a Triangle

How to recognize a triangle?

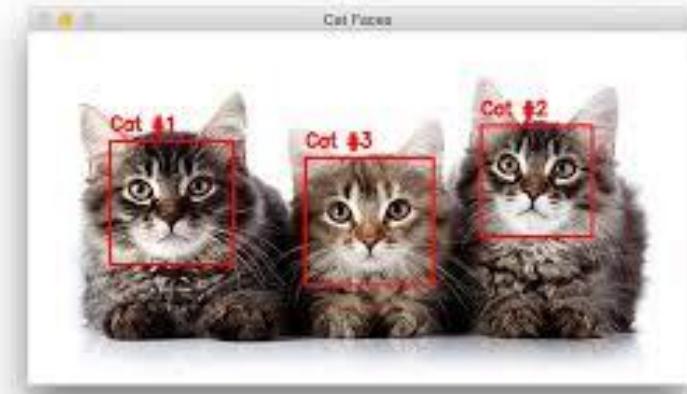
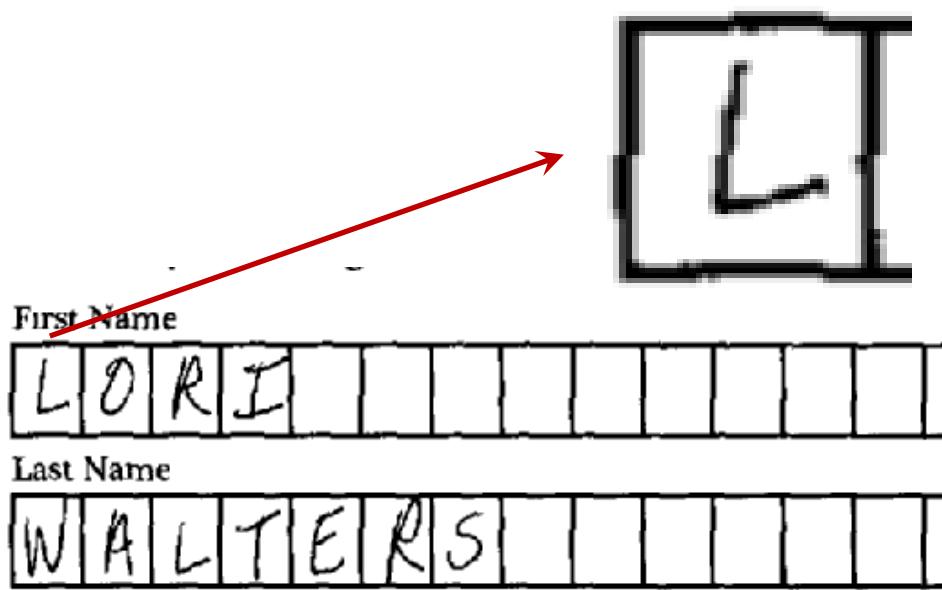


How about this?



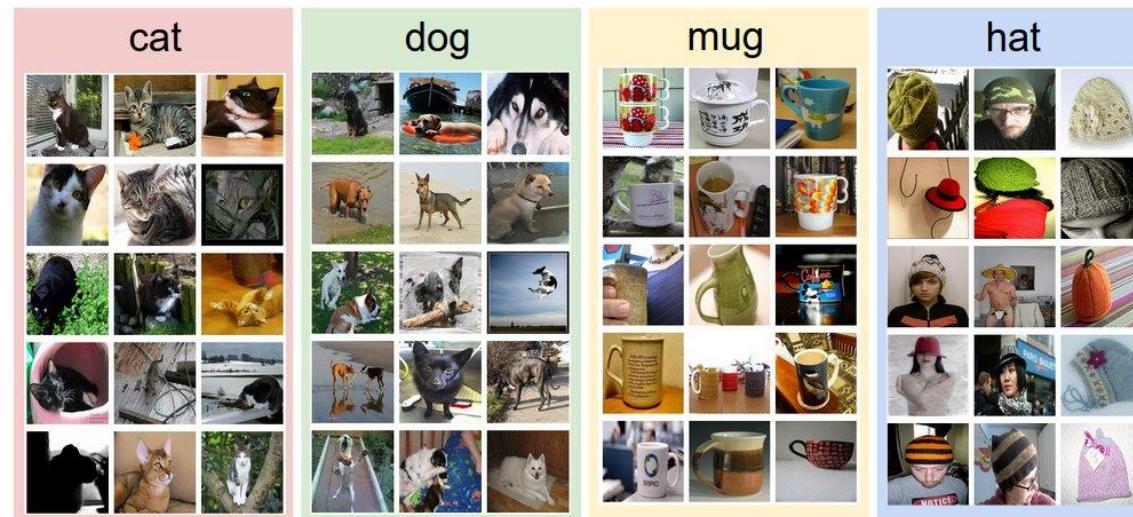
Machine Learning

- Machine Learning is the science of getting computers to learn, without being explicitly programmed.
- Examples are used to train computers to perform tasks that would be difficult to program



Data-driven Approach

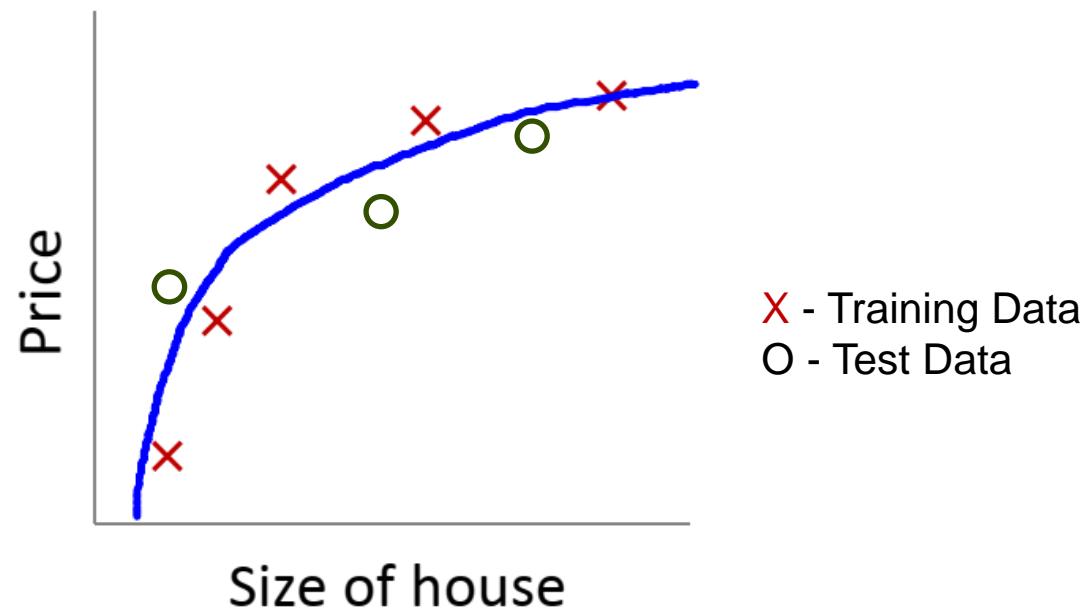
- Instead of trying to specify what every one of the categories of interest look like directly in code, the approach that we will take is not unlike one you would take with a child:
 - Provide the computer with many examples of each class
 - Develop learning algorithms that look at these examples and learn about the visual appearance of each class.
- This approach is referred to as a **data-driven approach**.



An example training set for four visual categories. In practice we may have thousands of categories and hundreds of thousands of images for each category. *(From Stanford CS231n)

Training and Test Data

- In machine learning, datasets are split into two subsets:
 - Training Data (Training set)
 - data used to learn a model
 - Test Data (Test set)
 - data used to assess the accuracy of model

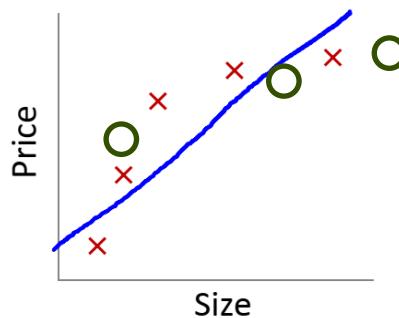


Simplest machine learning

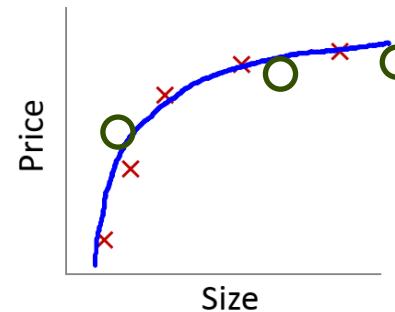
Slide from Andrew Ng, Machine Learning, Lecture 7

X - Training Data
O - Test Data

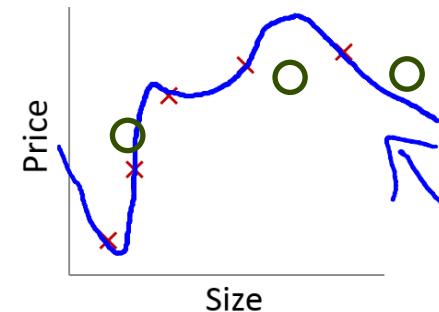
Example: Linear regression (housing prices)



Underfitting



“Just Right”



Overfitting

Underfitting:

- Model is unable to capture the relationship between the input and output variables accurately.

Overfitting:

- Model performs well on training data but poorly on test data

Types of Machine Learning

➤ **Supervised Learning**

- Training data is labeled
- Goal is correctly label new data

➤ **Unsupervised Learning**

- Training data is unlabeled
- Goal is to categorize the observations

➤ **Reinforcement Learning**

- Training data is unlabeled
- System receives feedback for its actions
- Goal is to perform better actions

Supervised Learning Algorithms

- **Linear Regression**
- **Neural Networks**
 - Deep Learning is the branch of Machine Learning based on Deep Neural Networks (DNNs, i.e., neural networks composed of more than 1 hidden layer).
 - Convolutional Neural Networks (CNNs) are one of the most popular DNN architectures (so CNNs are part of Deep Learning), but by no means the only one.
- **Decision Trees**
- **Support Vector Machines**
- **K-Nearest Neighbor**

Machine Learning Frameworks

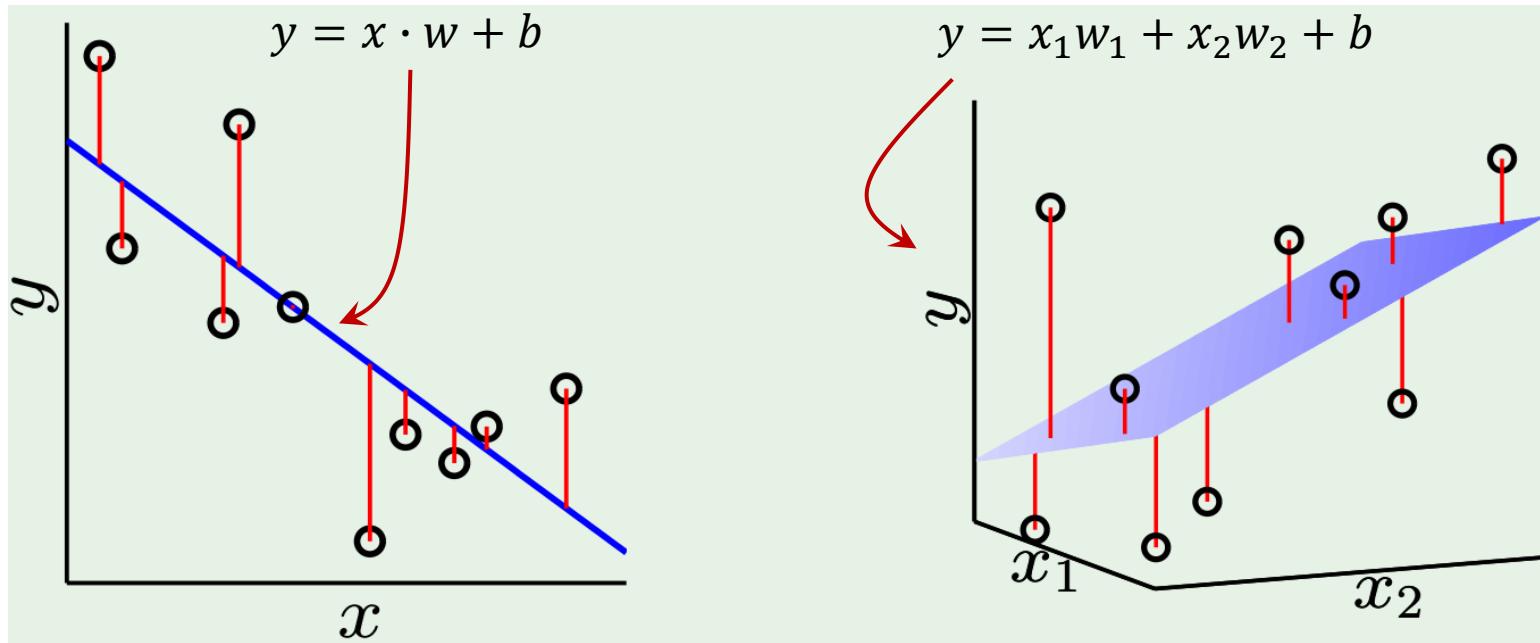
Tool	Uses	Language
Scikit-Learn	Classification, Regression, Clustering	Python
Spark MLlib	Classification, Regression, Clustering	Scala, R, Java
MXNet	Deep learning framework	Python, R, Julia, Scala, Go, Javascript and more
Caffe	Neural Networks	C++, Python
TensorFlow	Neural Networks	Python
PyTorch	Neural Networks	Python

What is Deep Learning

Machine Learning and Deep Learning

Recall From The Least Square Method

- Start from least square method...
- Trying to find
 - **Parameters (w, b)**: minimizes the sum of the squares of the errors
 - **Errors**: distance between known data points and predictions



❖ from Yaser Abu-Mustafa “Learning From Data” Lecture 3

Recall Least Square Method - How to?

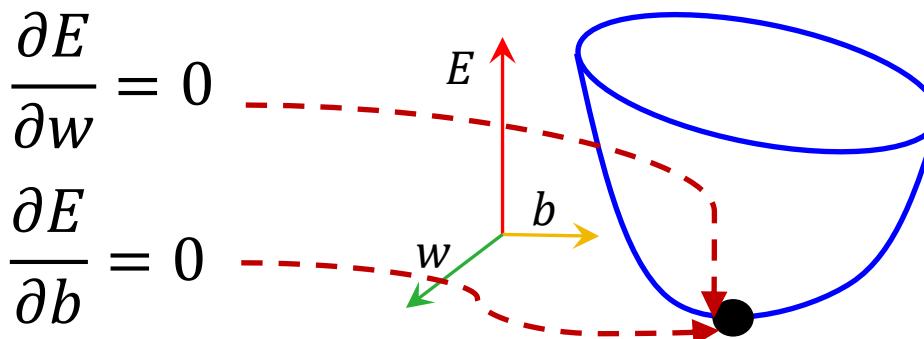
- Calculate the sum of square of errors (residual)

$$E = \sum \epsilon_i^2 = \sum (y_i - \hat{y}_i)^2$$

$$= \sum (y_i - (wx_i + b))^2$$

- Minimize the error function

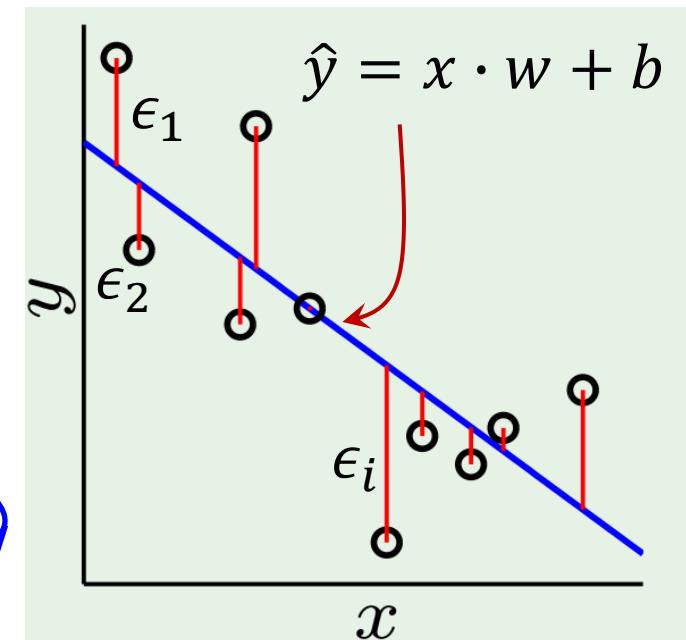
- How to minimize the error function?



- We will then get the expression of w and b

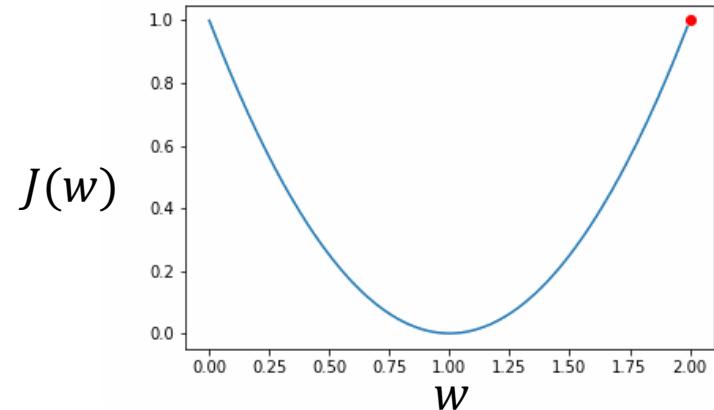
$$w = w(x_i, y_i)$$

$$b = b(x_i, y_i)$$

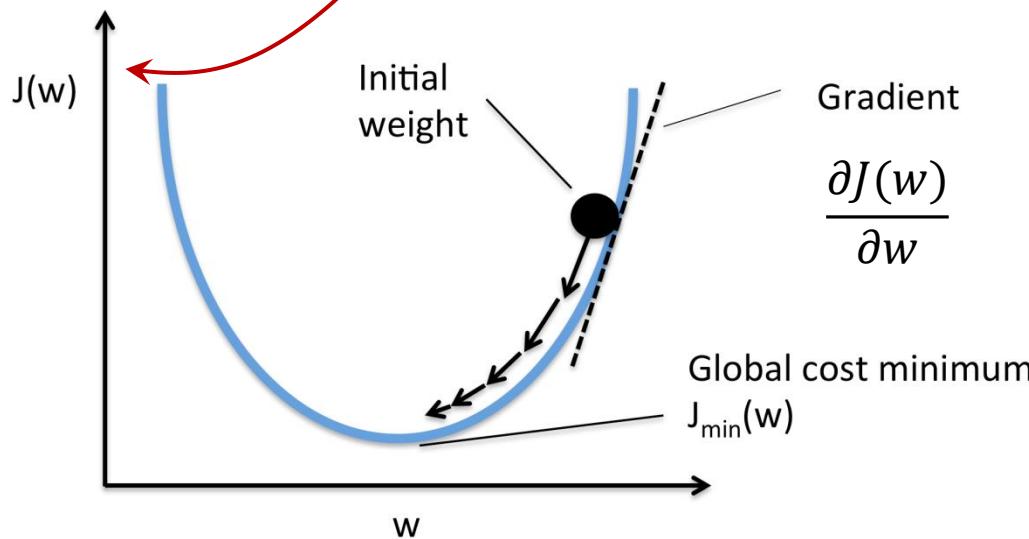


To The Machine Learning Language

- **Error (E)**
 - Cost Function (Loss): $J(w)$, C , L
- **Parameters**
 - Weights and Biases: (w, b)

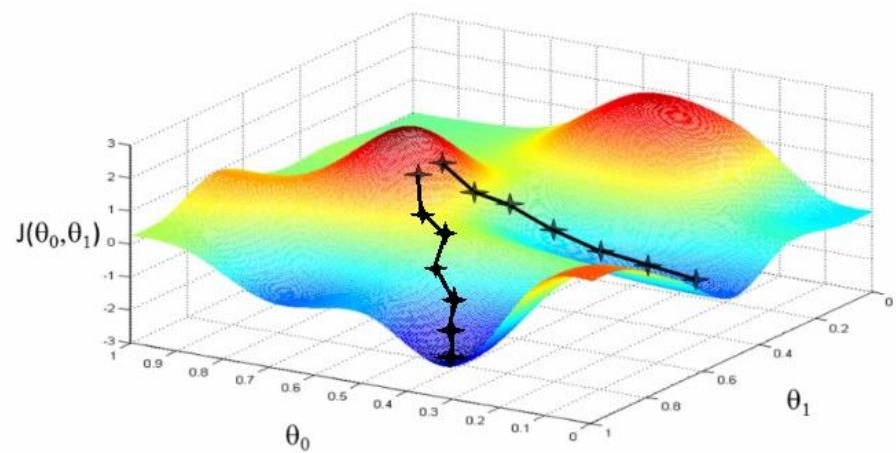
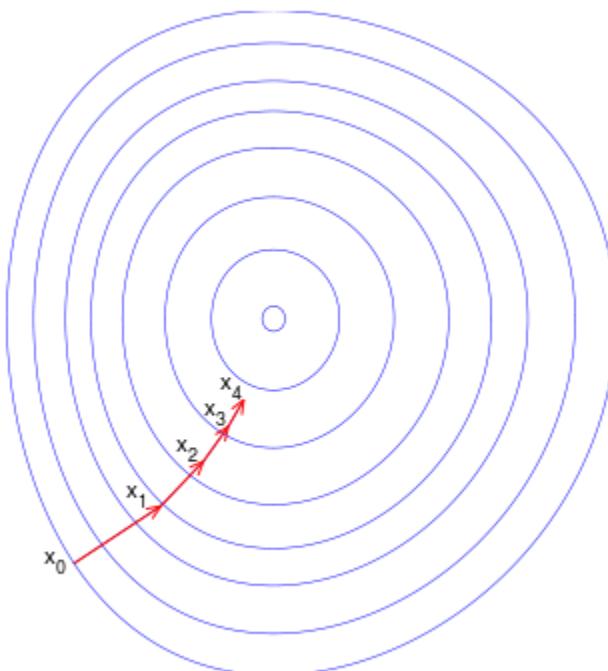


- **Define the cost function of your problem**
- **Find the set of weights that minimizes the cost function (loss)**



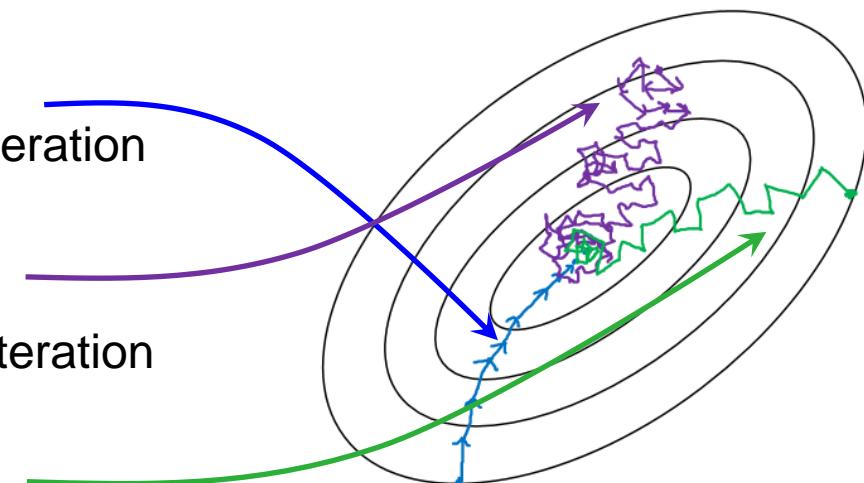
Theory: Gradient Descent

- Gradient descent is a first-order iterative optimization algorithm. To find a local minimum of a function using gradient descent, one takes steps proportional to the negative of the gradient (or of the approximate gradient) of the function at the current point.



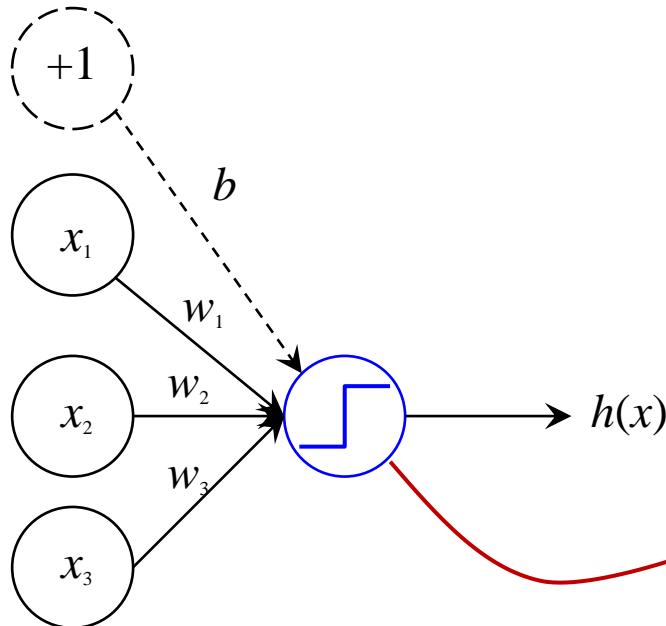
Mini-batch Gradient Descent

- **Batch gradient descent:**
 - Use all examples in each iteration
- **Stochastic gradient descent:**
 - Use one example in each iteration
- **Mini-batch gradient descent**
 - Splits the training dataset into small batches (size b) that are used to calculate model error and update model coefficients.
- **In the neural network terminology:**
 - One **epoch** consists of one full training cycle on the training set.
 - Using all your batches once is 1 **epoch**. If you have 10 epochs, it means that you will use all your data 10 times (split in batches).



What is a Neural Network?

- Start from a perceptron



Feature vector: \mathbf{x} Weight vector: \mathbf{w}

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

$$\mathbf{w} = \begin{bmatrix} w_1 \\ w_2 \\ w_3 \end{bmatrix}$$

Hypothesis
(Prediction: y)

x1	age	23
x2	gender	male
x3	annual salary	\$30,000
b	threshold	some value

h(x)	Approve credit if: $h(x) > 0$
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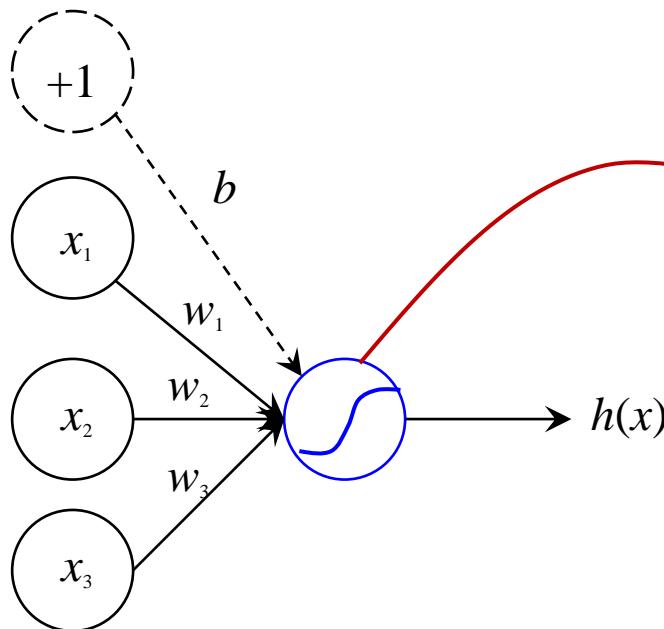
Activation function:
 $\sigma(z) = \text{sign}(z)$

Denote as: z

$$\begin{aligned}
 h(x) &= \text{sign}(w_1 x_1 + w_2 x_2 + w_3 x_3 + b) \\
 &= \text{sign}\left(\sum_i w_i x_i + b\right) \\
 &= \text{sign}(\mathbf{w}^T \mathbf{x} + b)
 \end{aligned}$$

Perceptron To Neuron

- Replace the sign to sigmoid



Activation function:

$$\sigma(z) = \text{sigmoid}(z)$$

$$\begin{aligned} h(x) &= \text{sigmoid}(w_1 x_1 + w_2 x_2 + w_3 x_3 + b) \\ &= \text{sigmoid}\left(\sum_i w_i x_i + b\right) \\ &= \text{sigmoid}(\mathbf{w}^T \mathbf{x} + b) \end{aligned}$$



$$z = \mathbf{w}^T \mathbf{x} + b$$

$$y = h(x) = \sigma(z)$$

Feature vector: \mathbf{X} Weight vector: \mathbf{W}

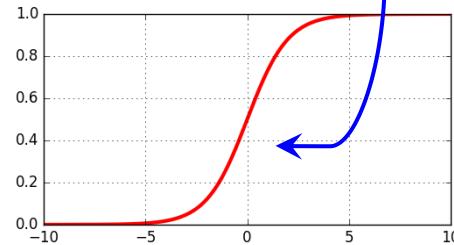
$$\mathbf{X} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad \mathbf{W} = \begin{bmatrix} w_1 \\ w_2 \\ w_3 \end{bmatrix}$$

Sigmoid Neurons

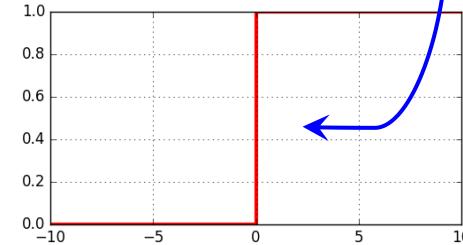
➤ Sigmoid activation Function

- In the field of Artificial Neural Networks, the sigmoid function is a type of activation function for artificial neurons.

$$\sigma(z) = \frac{1}{1 + e^{-z}}$$



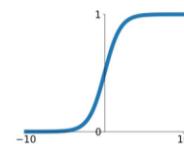
$$\sigma(z) = sign(z)$$



➤ There are many other activation functions. (We will touch later.)

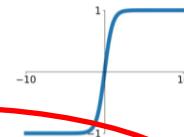
Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



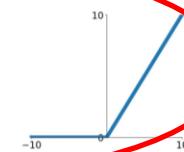
tanh

$$\tanh(x)$$



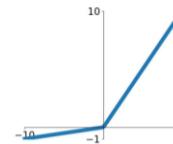
ReLU

$$\max(0, x)$$



Leaky ReLU

$$\max(0.1x, x)$$

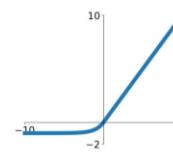


Maxout

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

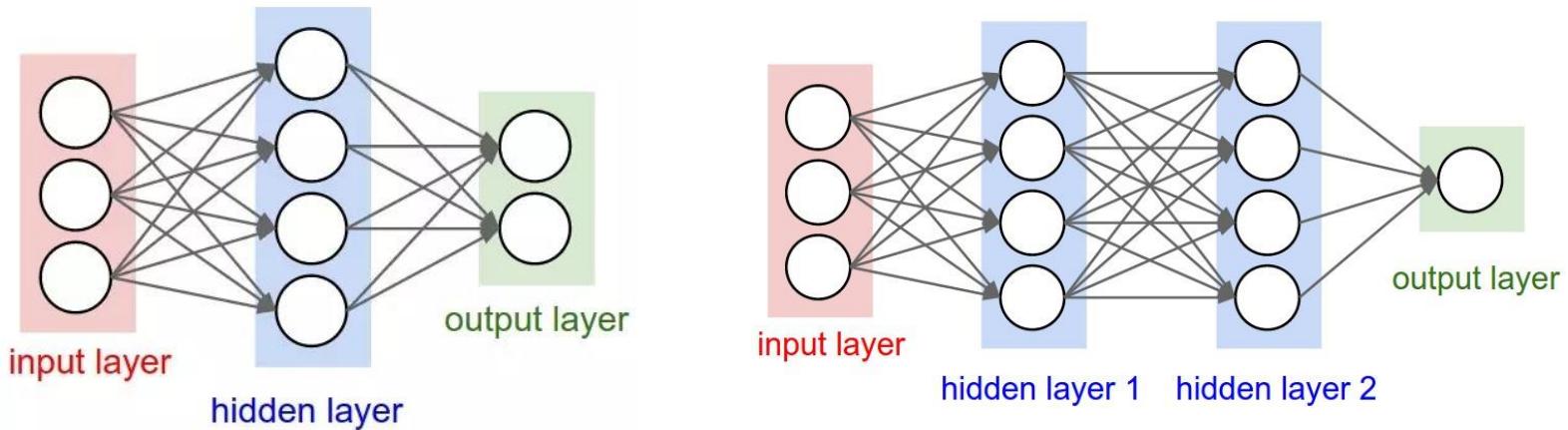
ELU

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

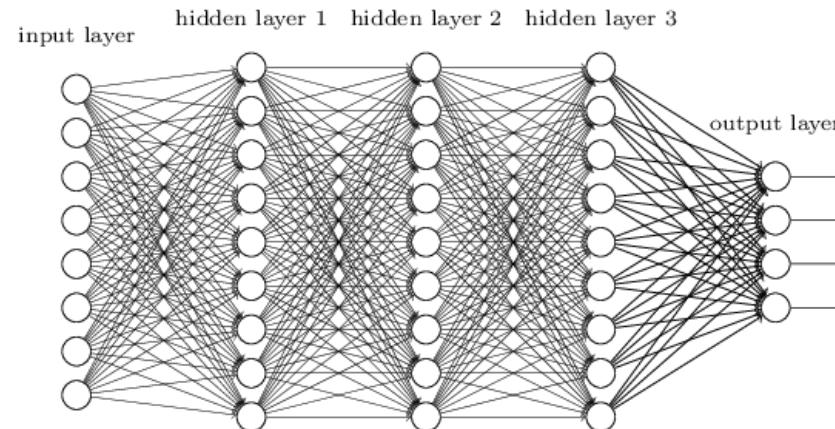


Network Of Neurons

- A complex network of neurons could make quite subtle decisions



- Deep Neuron Network: Number of hidden layers > 1



Types of Neural Networks

A mostly complete chart of

Neural Networks

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Backfed Input Cell

Input Cell

Noisy Input Cell

Hidden Cell

Probabilistic Hidden Cell

Spiking Hidden Cell

Output Cell

Match Input Output Cell

Recurrent Cell

Memory Cell

Different Memory Cell

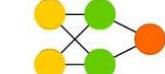
Kernel

Convolution or Pool

Perceptron (P)



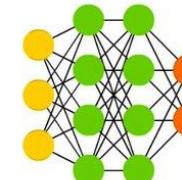
Feed Forward (FF)



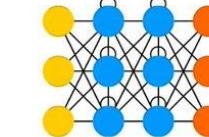
Radial Basis Network (RBF)



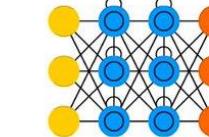
Deep Feed Forward (DFF)



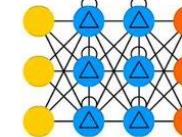
Recurrent Neural Network (RNN)



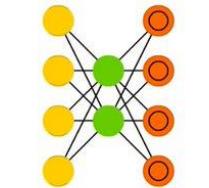
Long / Short Term Memory (LSTM)



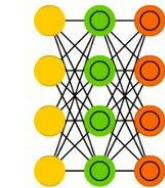
Gated Recurrent Unit (GRU)



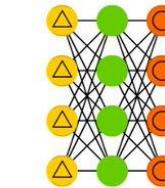
Auto Encoder (AE)



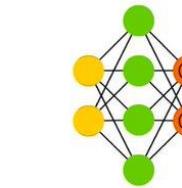
Variational AE (VAE)



Denoising AE (DAE)



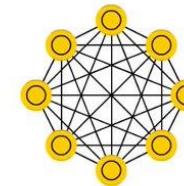
Sparse AE (SAE)



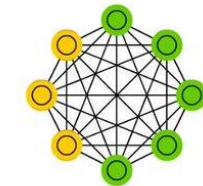
Markov Chain (MC)



Hopfield Network (HN)



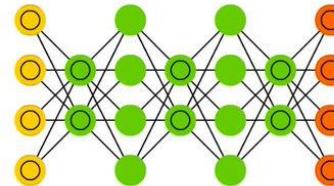
Boltzmann Machine (BM)



Restricted BM (RBM)



Deep Belief Network (DBN)



Ref: <http://www.asimovinstitute.org/neural-network-zoo/>

How to Train DNN?

➤ Backward Propagation

- The backward propagation of errors or backpropagation, is a common method of training artificial neural networks and used in conjunction with an optimization method such as gradient descent.

➤ Deep Neural Networks are hard to train

- learning machines with lots of (typically in range of million) parameters
- Unstable gradients issue
 - Vanishing gradient problem
 - Exploding gradient problem
- Choice of network architecture and other hyper-parameters is also important.
- Many factors can play a role in making deep networks hard to train
- Understanding all those factors is still a subject of ongoing research

Understanding Gradient Descent

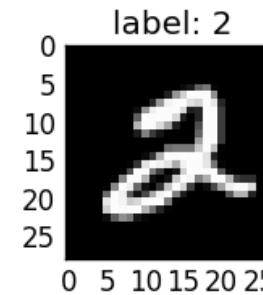
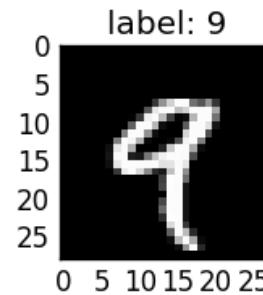
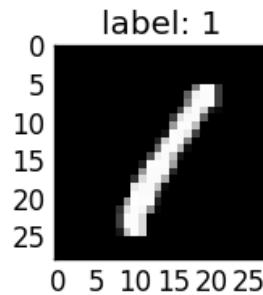
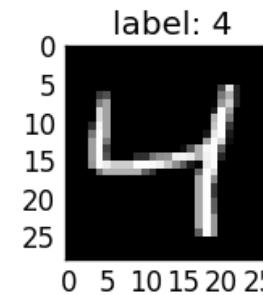
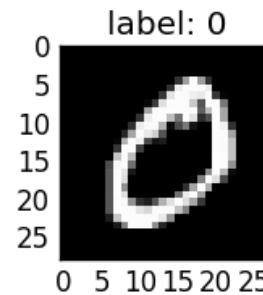
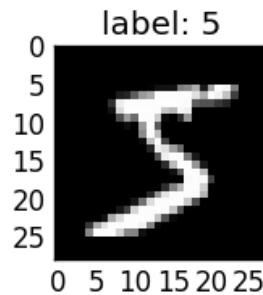
- An example to help you understand the gradient descent
 - https://github.com/lsuhpc/help/lbrnloniworkshop2022/blob/main/day5-6/gradient_descent_y_fx.ipynb

Deep Learning Example

Hello World of Deep Learning: Recognition of MNIST

Introducing the MNIST problem

- **MNIST (Mixed National Institute of Standards and Technology database)** is a large database of handwritten digits that is commonly used for training various image processing systems.
- It consists of images of handwritten digits like these:



- The MNIST database contains **60,000** training images and **10,000** testing images.

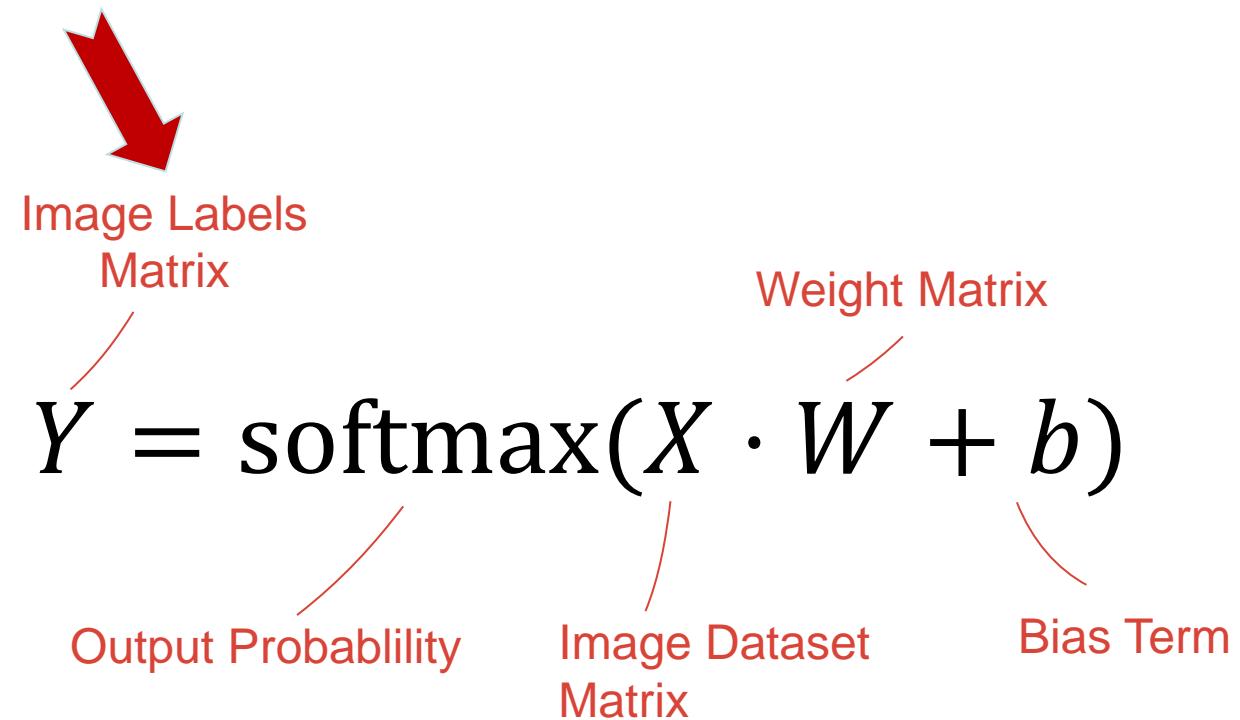
Example Problem - MNIST

- Recognizes handwritten digits.
- We uses the MNIST dataset, a collection of 60,000 labeled digits that has kept generations of PhDs busy for almost two decades. You will solve the problem with less than 100 lines of Python/Keras/TensorFlow code.
- We will gradually enhance the neural network to achieve above 99% accuracy by using the mentioned techniques.

Steps for MNIST recognition

- Understand the MNIST data
- Build the matrix regression function
- Softmax regression layer
- The cost function

$$y = x \cdot w + b$$

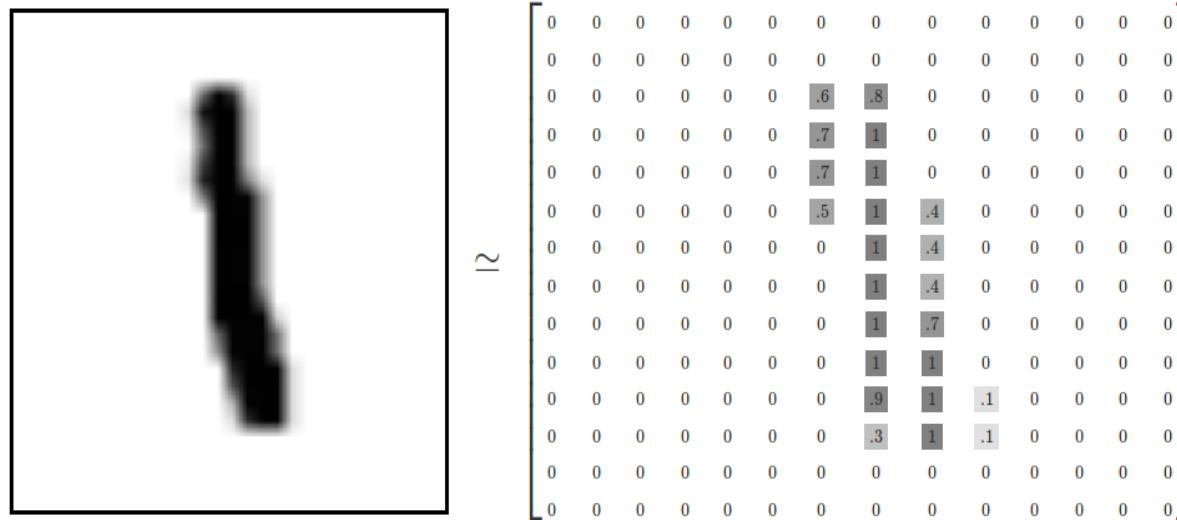

$$Y = \text{softmax}(X \cdot W + b)$$

The diagram illustrates the softmax regression equation $Y = \text{softmax}(X \cdot W + b)$. A large red arrow points downwards from the equation towards the text "Image Labels Matrix". Below the equation, several red lines point to its components with corresponding labels:

- A line points from the term $X \cdot W$ to the text "Image Dataset Matrix".
- A line points from the term b to the text "Bias Term".
- A line points from the term $\text{softmax}(\dots)$ to the text "Output Probablility".
- A line points from the term $(\dots) + b$ to the text "Weight Matrix".

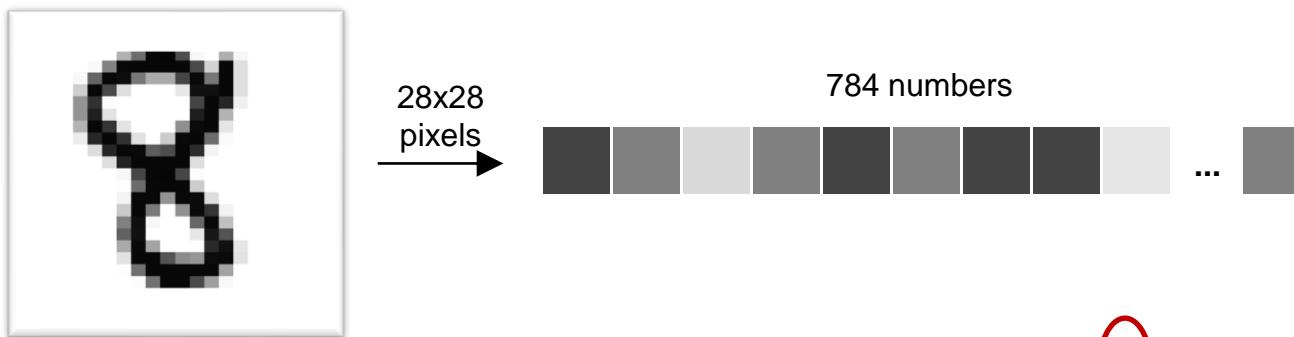
The MNIST Data

- Every MNIST data point has two parts: an image of a handwritten digit and a corresponding label. We'll call the images "x" and the labels "y". Both the training set and test set contain images and their corresponding labels;
- For each grayscale pixel value 0-255, we normalize it to 0-1;
- Each image is 28 pixels by 28 pixels. We can interpret this as a big array of numbers:



One Layer NN for MNIST Recognition

- We will start with a very simple model, called **Softmax Regression**.
- We can flatten each image array into a vector of $28 \times 28 = 784$ numbers. It doesn't matter how we flatten the array, as long as we're consistent between images.
- From this perspective, the MNIST images are just a bunch of points in a 784-dimensional vector space.

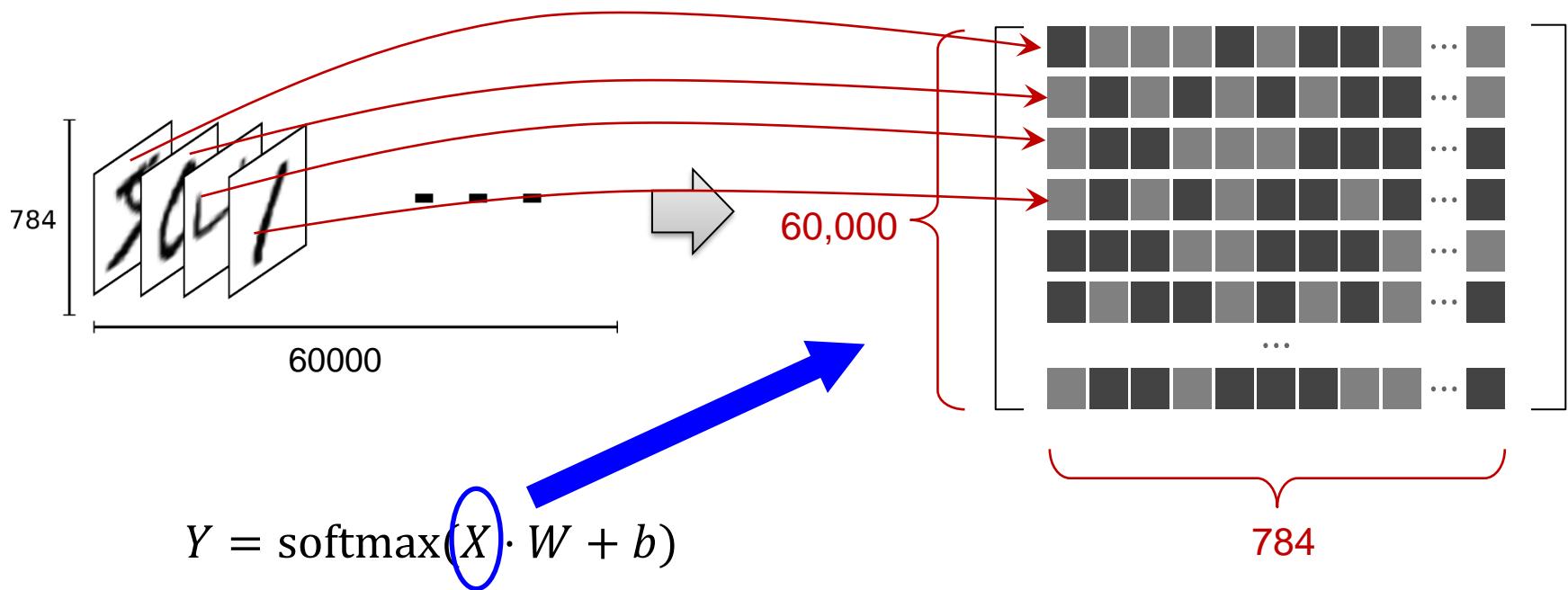


$$Y = \text{softmax}(X \cdot W + b)$$

- ❖ What are we missing here?

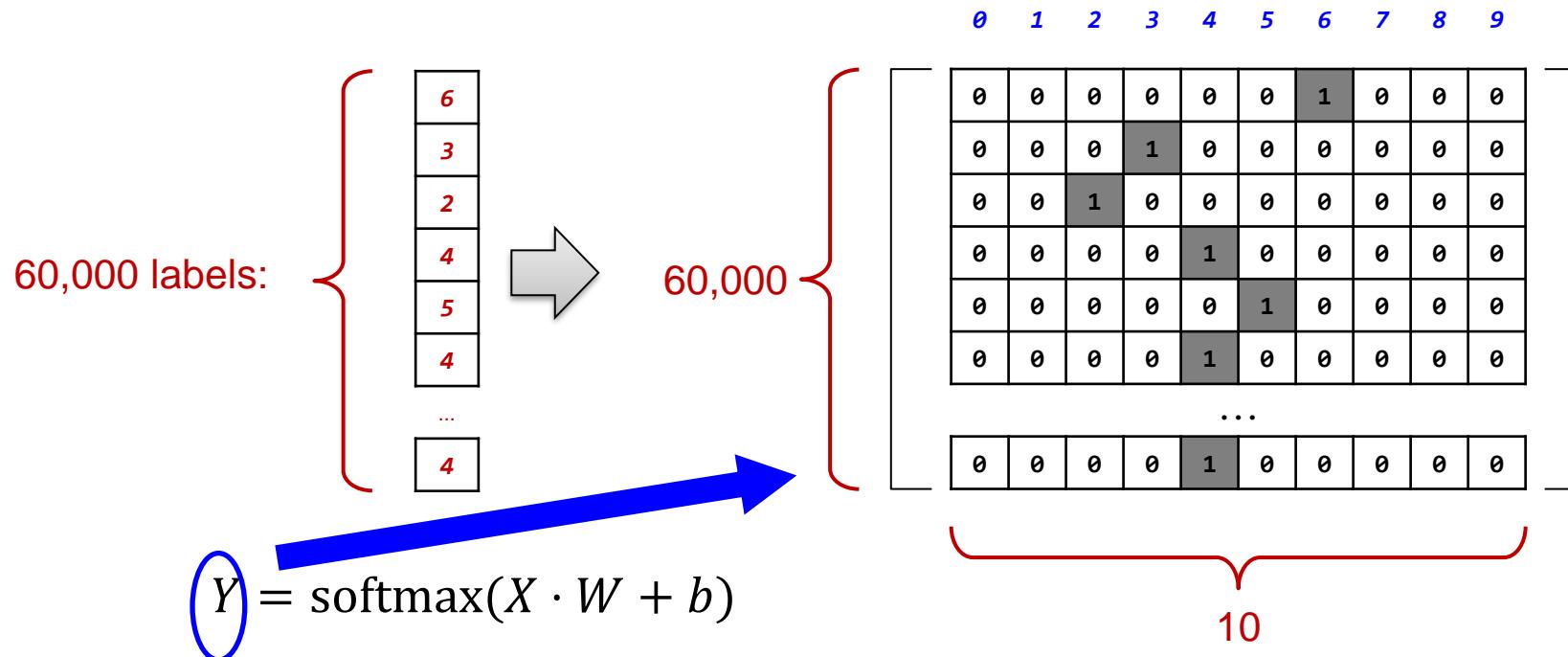
Result of the Flatten Operation

- The result is that the training images is a matrix (tensor) with a shape of [60000, 784].
- The first dimension is an index into the list of images and the second dimension is the index for each pixel in each image.
- Each entry in the tensor is a pixel intensity between 0 and 1, for a particular pixel in a particular image.



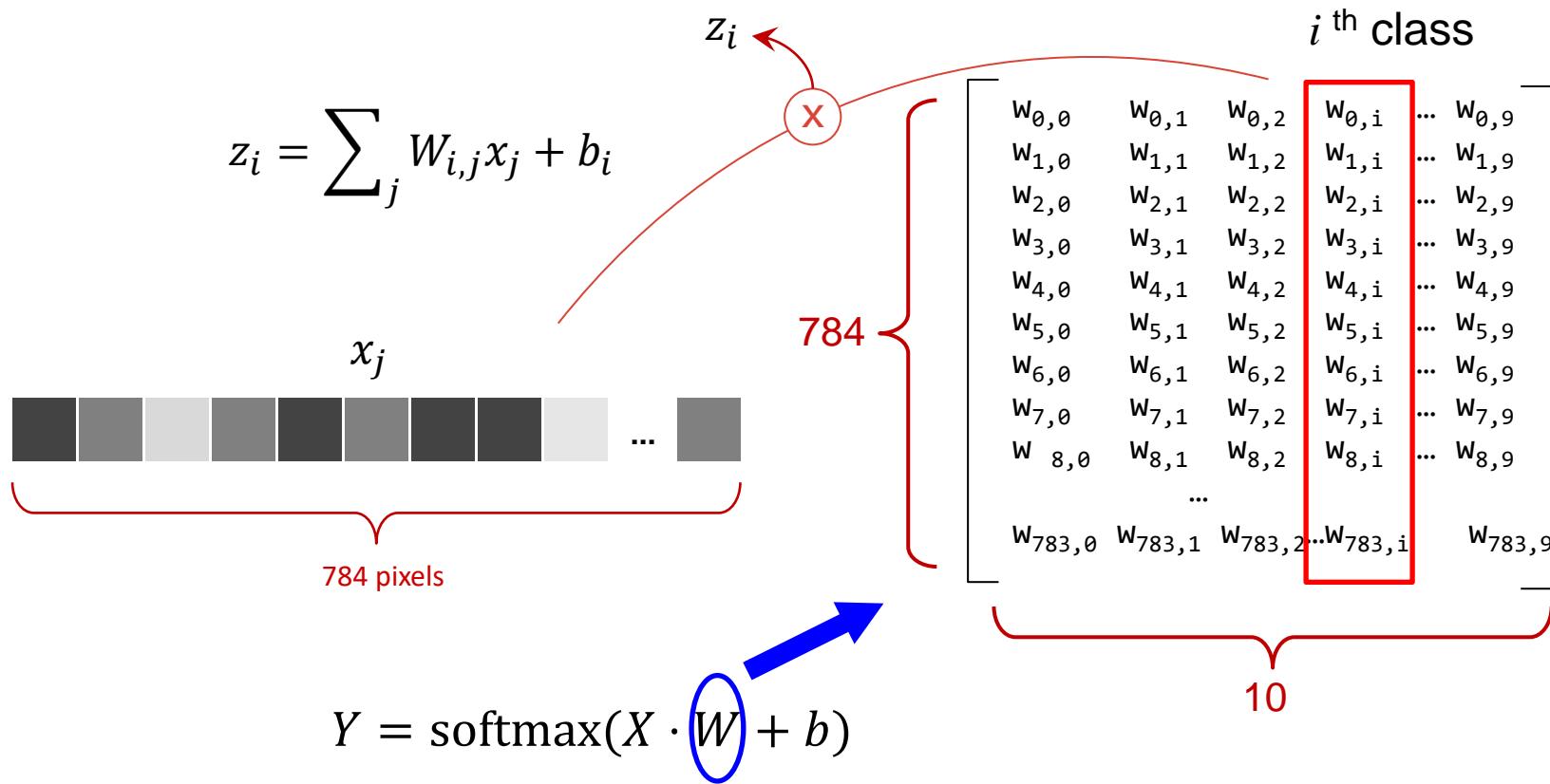
One-hot Vector (One vs All)

- For the purposes of this tutorial, we label the y's as "one-hot vectors".
- A one-hot vector is a vector which is 0 in most dimensions, and 1 in a single dimension.
- How to label an "8"?
 - $[0, 0, 0, 0, 0, 0, 0, 0, 1, 0]$
- What is the dimension of our y matrix (tensor)?

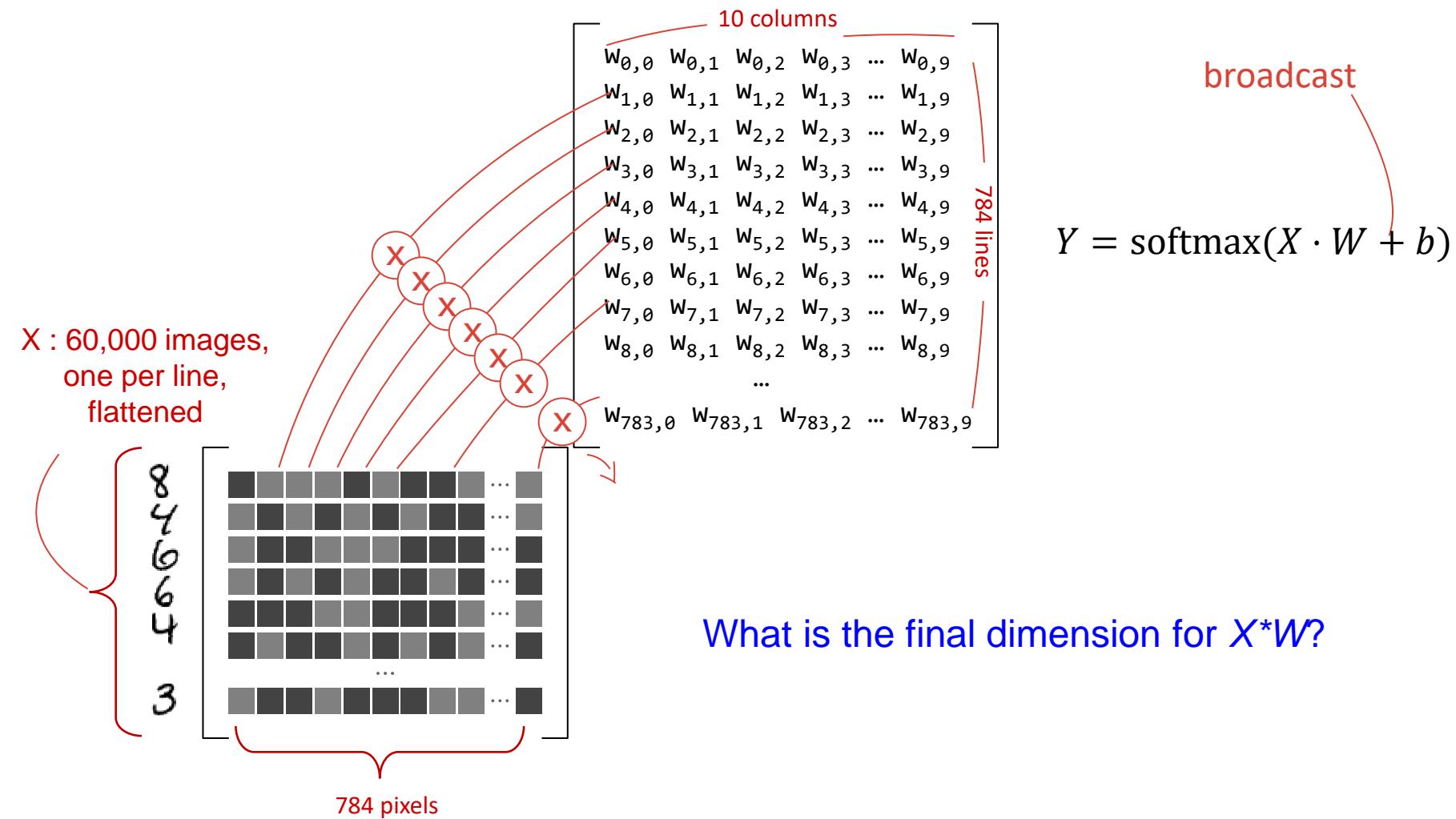


2 steps in softmax regression - Step 1

- **Step 1: Build the weight matrix W , do the matrix multiplication with X .**
 - Multiply each image with the weight matrix, we get 10 **score value** (z_i) for each image.

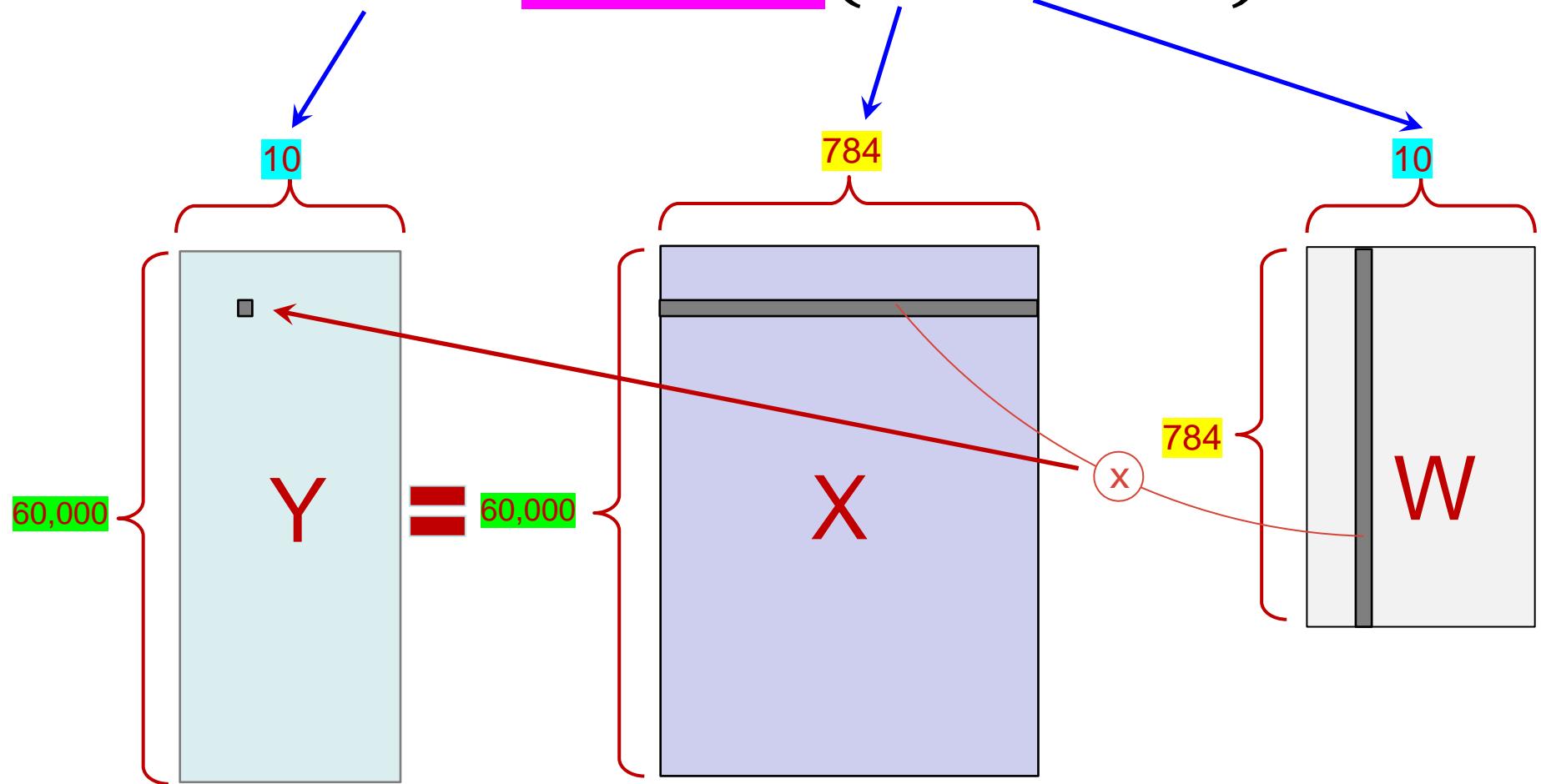


Matrix Representation of softmax layer



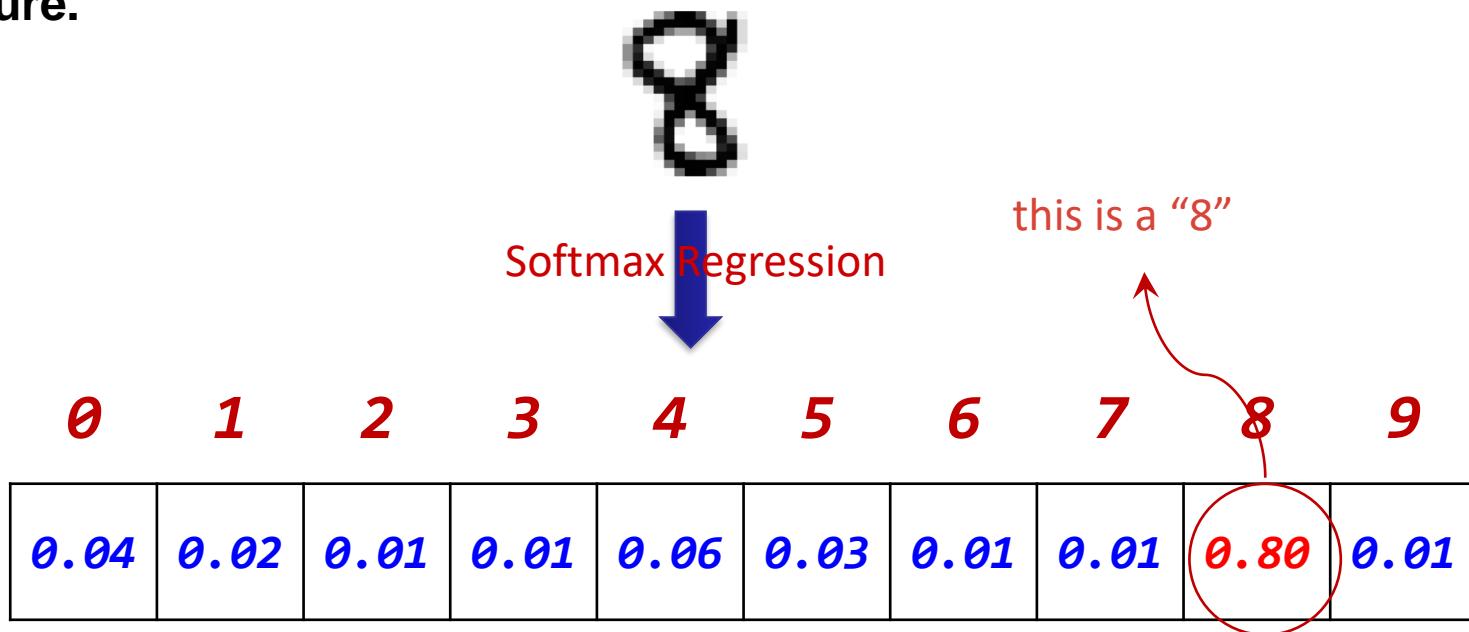
Matrix representation of the equation

$$Y = \text{softmax}(X \cdot W + b)$$



Softmax Regressions

- Every image in MNIST is of a handwritten digit between 0 and 9.
- So, there are only ten possible things that a given image can be. We want to be able to look at an image and give the probabilities for it being each digit.
- For example, our model might look at a picture of an eight and be 80% sure it's an 8, but give a 6% chance to it being a 4 (because of the top loop) and a bit of probability to all the others because it isn't 100% sure.



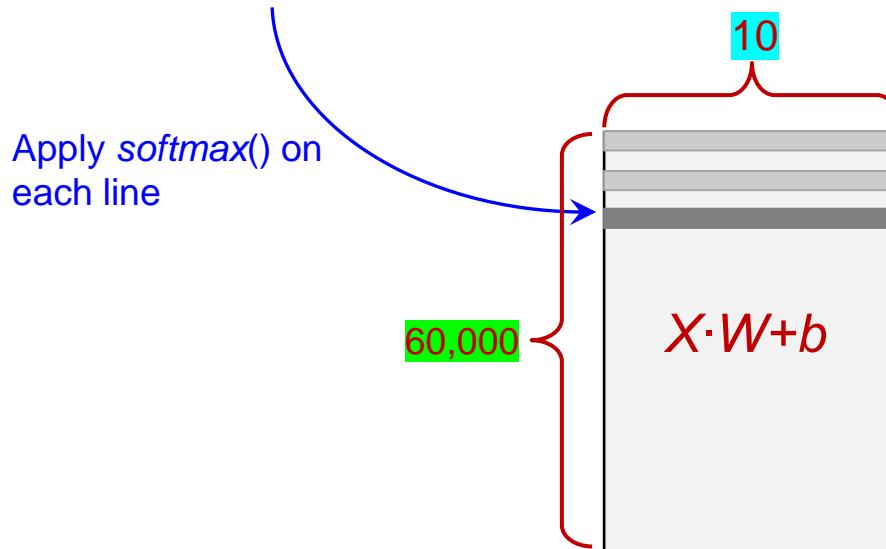
2 steps in softmax regression - Step 2

- Step 2: Convert the evidence tallies into our predicted probabilities y using the "softmax" function:

$$h(\mathbf{x}_i) = \text{softmax}(z_i) = \text{softmax}\left(\sum_j W_{i,j}x_j + b_i\right)$$

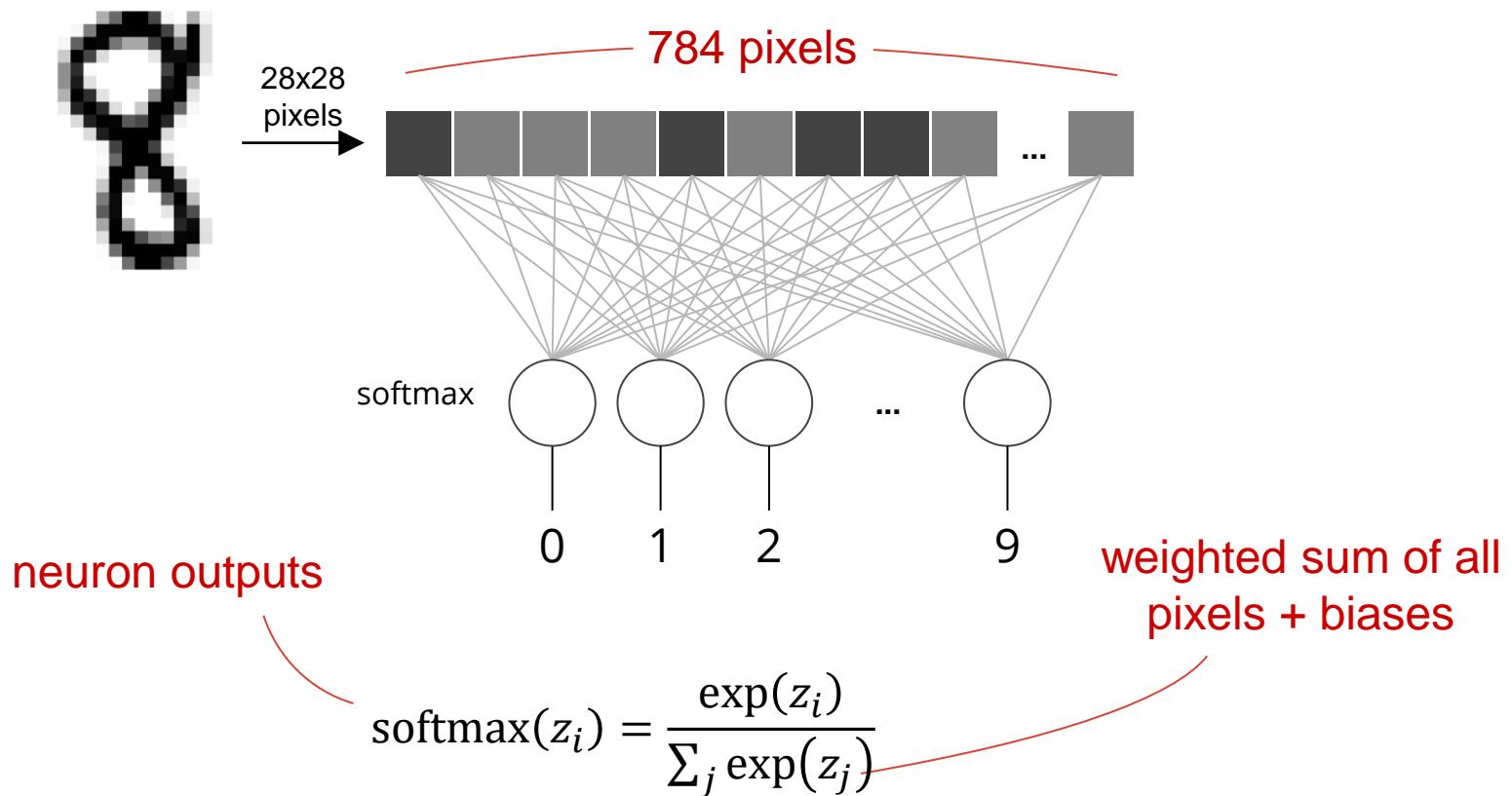
- Here softmax is serving as an "activation" function, shaping the output of our linear function a probability distribution over 10 cases, defined as:

$$\text{softmax}(z_i) = \text{normalize}(\exp(z)) = \frac{\exp(z_i)}{\sum_j \exp(z_j)}$$



The softmax layer

- The output from the softmax layer is a set of probability distribution, positive numbers which sum up to 1.



Softmax on a batch of images

- More compact representation for “softmaxing” on all the images

$$Y = \text{softmax}(X \cdot W + b)$$

Diagram illustrating the components of the softmax equation:

- Predictions: $Y[60000, 10]$
- Images: $[60000, 784]$
- Weights: $W[784, 10]$
- Biases: $b[10]$

Annotations:

- Red arrows point from the matrix dimensions to the corresponding terms in the equation.
- The term $X \cdot W$ is annotated with "matrix multiply" and the dimension $[60000, 10]$.
- The term $+ b$ is annotated with "broadcast on all lines".
- The term $\text{softmax}(\dots)$ is annotated with "applied on each line".

Very similar to 2D linear regression: $y = x \cdot w + b$

The Cross-Entropy Cost Function

- For classification problems, the Cross-Entropy cost function works better than quadratic cost function.
- We define the cross-entropy cost function for the neural network by:

0	0	0	0	0	0	1	0	0	0
---	---	---	---	---	---	---	---	---	---

Cross entropy

“one-hot” encoded ground truth “6”

$$C = - \sum_i y'_i \cdot \log P(Y = y_i | X = x_i)$$

for gradient descent

0.01	0.01	0.01	0.01	0.01	0.01	0.90	0.01	0.02	0.01
------	------	------	------	------	------	------	------	------	------

0 1 2 3 4 5 6 7 8 9

this is a “6”

Short Summary

➤ How MNIST data is organized

- X:
 - Flattened image pixels matrix
- Y:
 - One-hot vector

➤ Softmax regression layer

- Linear regression
- Output probability for each category

$$Y = \text{softmax}(X \cdot W + b)$$

➤ Cost function

- Cross-entropy

❖ How to implement the gradient descent for W?

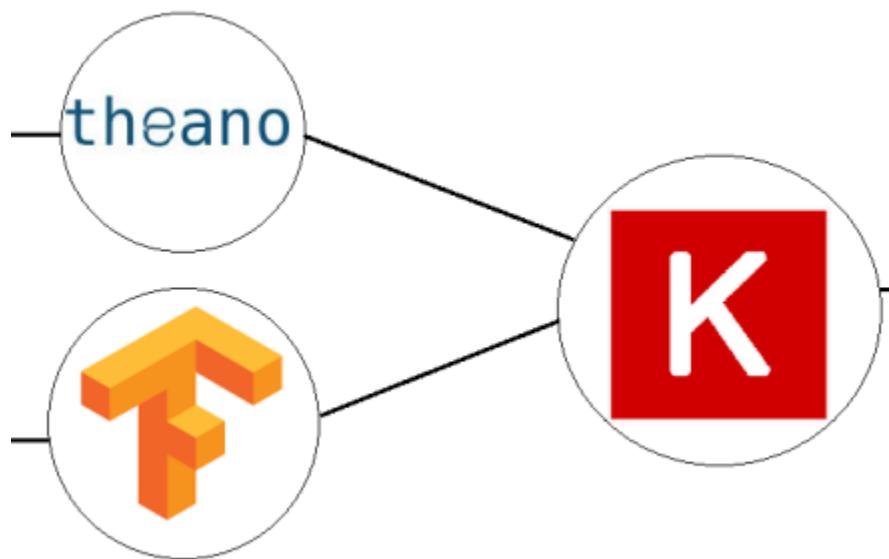


Deep Learning Example

Implementation in Keras/Tensorflow

Few Words about Keras, Tensorflow and Theano

- **Keras** is a high-level neural networks library, written in Python and capable of running on top of either TensorFlow or Theano.
- **TensorFlow** is an open source software library for numerical computation using data flow graphs.
- ~~Theano is a Python library that allows you to define, optimize, and evaluate mathematical expressions involving multi-dimensional arrays efficiently. (No longer under development)~~



Introducing Keras

- Keras is a high-level neural networks library,
- Written in Python and capable of running on top of either TensorFlow or Theano.
- It was developed with a focus on enabling fast experimentation. Being able to go from idea to result with the least possible delay is key to doing good research.
- See more at: <https://github.com/fchollet/keras>

Typical Code Structure

- **Load the dataset (MNIST)**
 - Read the file, convert format, normalization, etc
- **Build the Neural Network/Machine Learning Model**
 - Using the high level Keras-Tensorflow API
- **Train the model**
 - Monitor the loss and accuracy

Software Environment

- **What you'll need**
 - Python 2 or 3 (Python 3 recommended)
 - TensorFlow and Keras
 - Matplotlib (Python visualization library)
- **We will use the Google Colaboratory**
 - Colaboratory is a research tool for machine learning education and research. It's a Jupyter notebook environment that requires no setup to use. You can refer to: <https://research.google.com/colaboratory/faq.html> for more information.
 - See next slide for starting the Colab notebook

Open Colab Notebook from Github

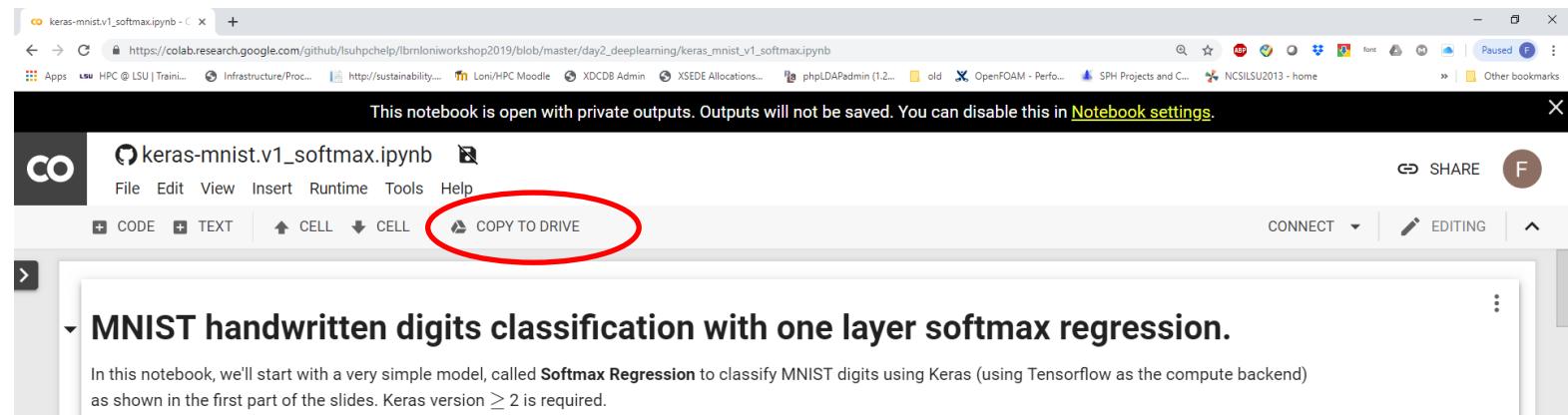
➤ Open the below link:

- https://github.com/lshuhpc/help/lbrnloniworkshop2022/blob/main/day5-6/2022_keras_mnist_v1_softmax.ipynb
- Or navigate yourself in the github repo:
 - <https://github.com/lshuhpc/help/lbrnloniworkshop2022>
- Select "day5-6 > 2022_keras_mnist_v1_softmax.ipynb"

➤ Click the “Open in Colab” link:

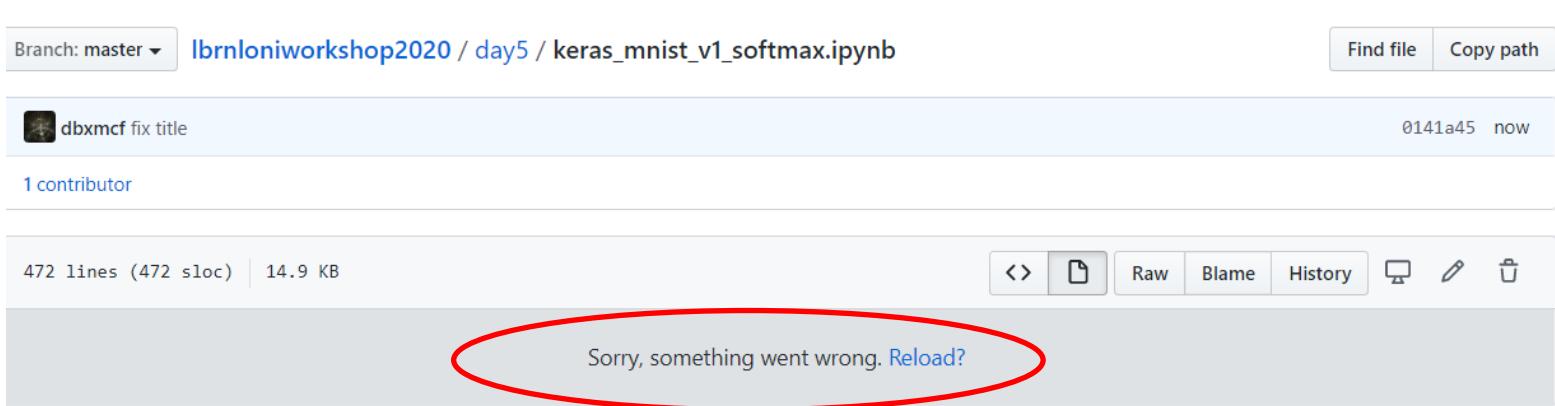


➤ After the Colab notebook is laid out, you need one more step, save the Colab notebook to your google drive by “COPY TO DRIVE”, or you will be editing the notebook in “Playground” (read only) mode:



Possible Bug of Github

- In case of the “Something went wrong, try again later?”



A screenshot of a GitHub repository page for 'lbrnloniworkshop2020 / day5 / keras_mnist_v1_softmax.ipynb'. The page shows a single commit by 'dbxmcf' titled 'fix title' with hash '0141a45' made 'now'. It has 1 contributor. The file details show 472 lines (472 sloc) and 14.9 KB. Below the file content area, there is a message 'Sorry, something went wrong. [Reload?](#)' which is circled in red.

- Copy and paste the github link from the browser URL box (https://github.com/lsuhpc/help/lbrnloniworkshop2022/blob/master/day5-6/2022_keras_mnist_v1_softmax.ipynb) into the below the location to have it rendered: <https://nbviewer.jupyter.org/>

Keras - Initialization

```
# import necessary modules
# The Sequential model is a linear stack of layers.
from keras.models import Sequential
from keras.layers import Dense, Dropout, Activation, Flatten
from keras.layers import Convolution2D, MaxPooling2D
from keras.utils import np_utils
from keras import backend as K
```

Load The MNIST Dataset

```
# load the mnist training and test dataset
# download https://s3.amazonaws.com/img-datasets/mnist.pkl.gz
# to use in this tutorial
from keras.datasets import mnist
(X_train, y_train), (X_test, y_test) = mnist.load_data()
print(X_train.shape, y_train.shape, X_test.shape, y_test.shape)
```

Output of the print line:

(60000, 28, 28) (60000,) (10000, 28, 28) (10000,)

Preprocessing the MNIST Dataset

```
# Flatten the image to 1D                                Flatten 28x28 image to 1D
X_train = X_train.reshape(X_train.shape[0], img_rows*img_cols)
X_test = X_test.reshape(X_test.shape[0], img_rows*img_cols)
input_shape = (img_rows*img_cols,)

# convert all data to 0.0-1.0 float values                All grayscale values to 0.0-1.0
X_train = X_train.astype('float32')
X_test = X_test.astype('float32')
X_train /= 255
X_test /= 255

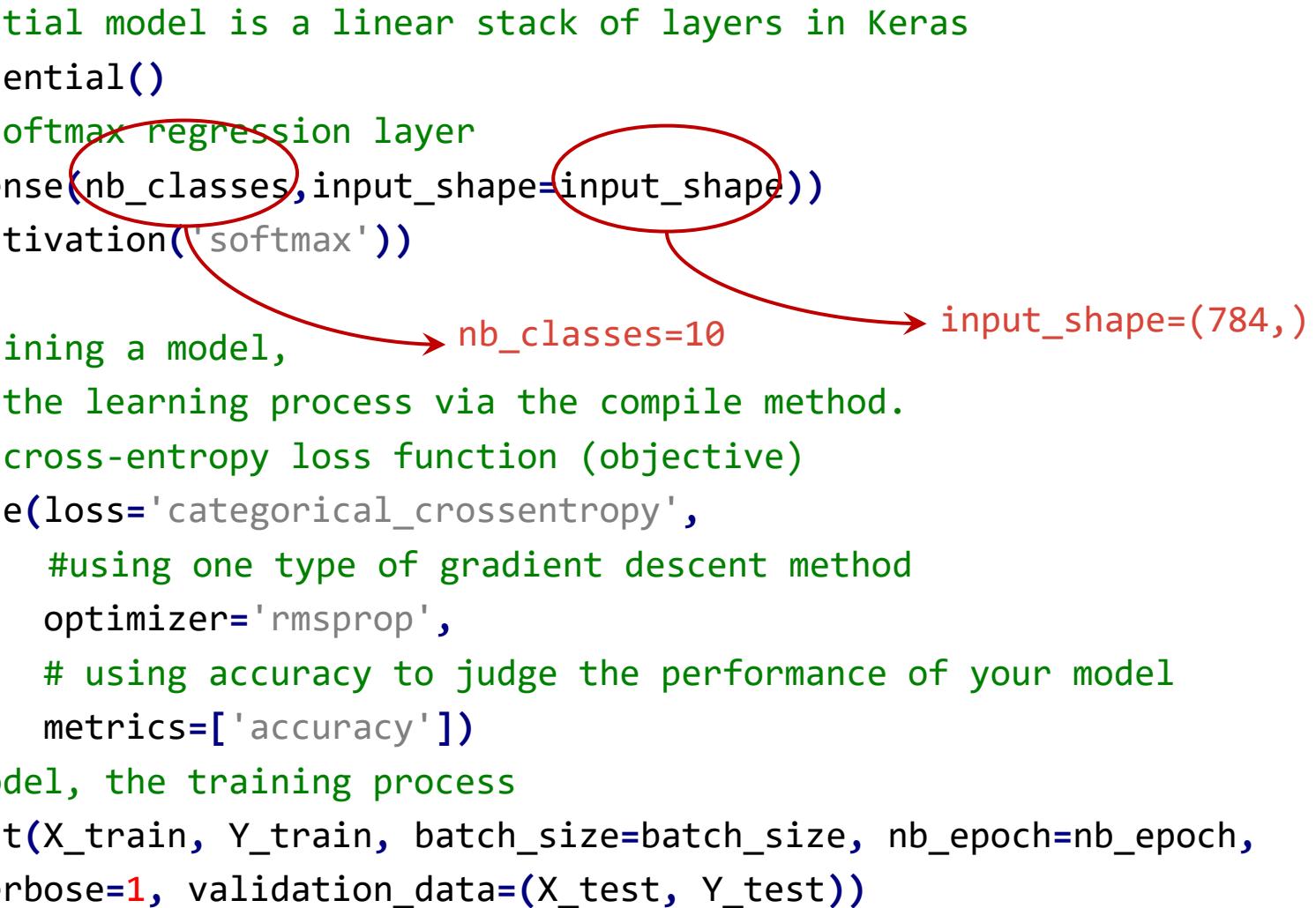
# convert class vectors to binary class matrices          One-hot encoding
Y_train = np_utils.to_categorical(y_train, nb_classes)
Y_test = np_utils.to_categorical(y_test, nb_classes)
```

Build The First softmax Layer

```
# The Sequential model is a linear stack of layers in Keras
model = Sequential()
#build the softmax regression layer
model.add(Dense(nb_classes, input_shape=input_shape))
model.add(Activation('softmax'))

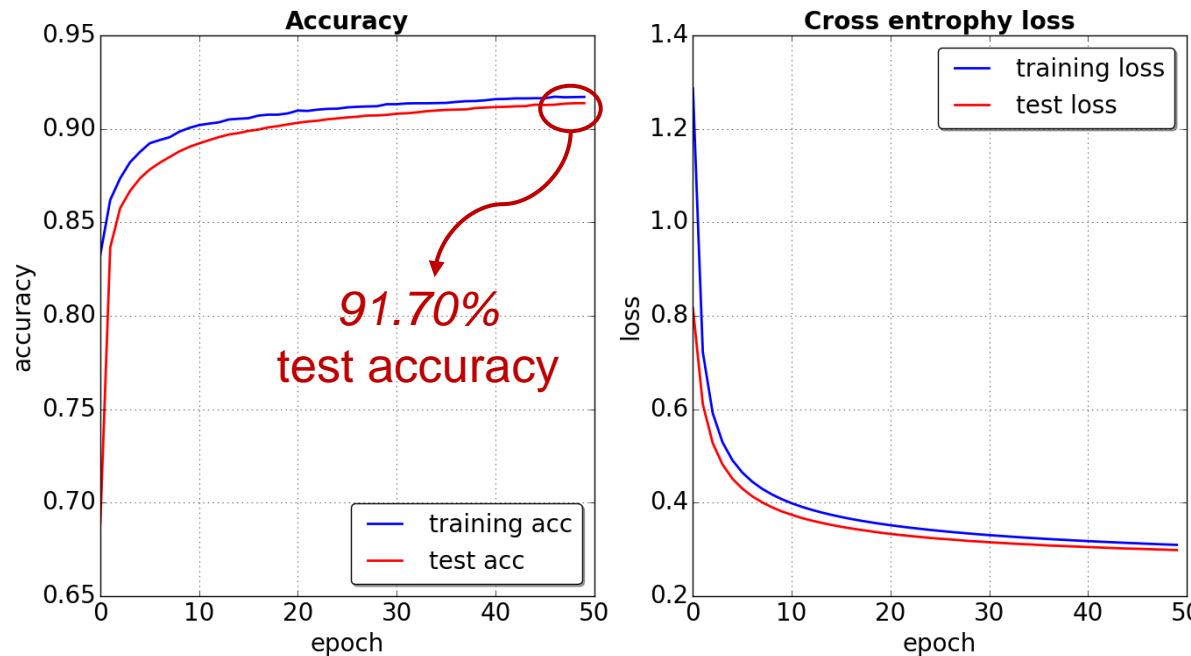
# Before training a model,
# configure the learning process via the compile method.
# using the cross-entropy loss function (objective)
model.compile(loss='categorical_crossentropy',
                #using one type of gradient descent method
                optimizer='rmsprop',
                # using accuracy to judge the performance of your model
                metrics=['accuracy'])

# fit the model, the training process
h = model.fit(X_train, Y_train, batch_size=batch_size, nb_epoch=nb_epoch,
               verbose=1, validation_data=(X_test, Y_test))
```



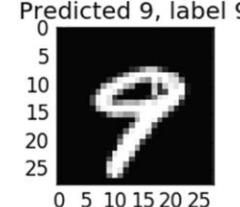
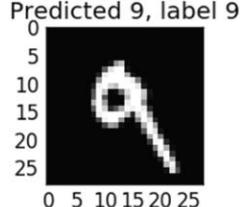
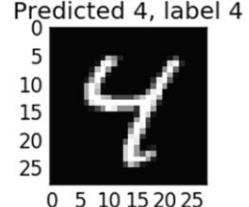
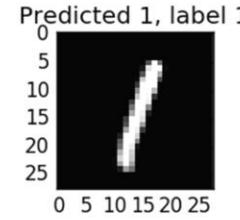
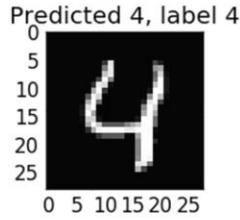
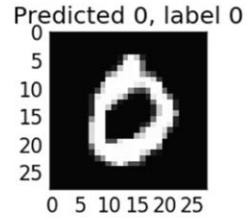
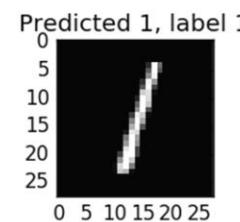
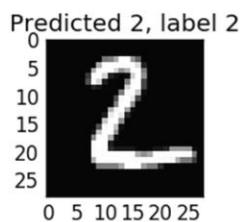
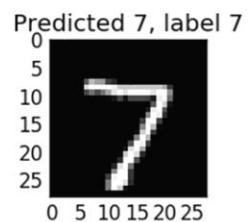
Results Of The First softmax Regression

- Training accuracy vs Test accuracy, loss function
- We reach a test accuracy at **91.7%**

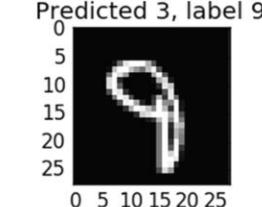
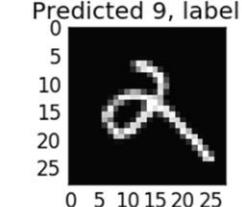
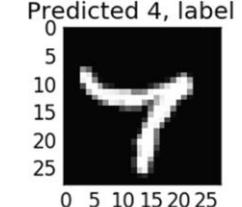
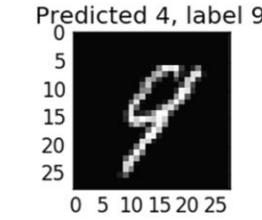
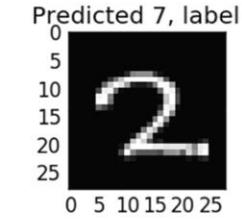
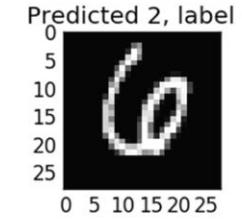
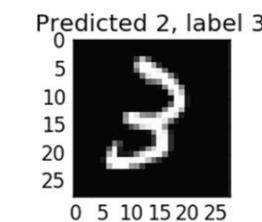
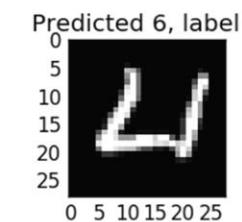
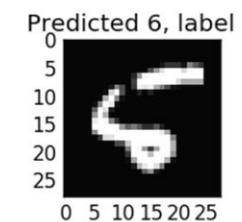


Review The Classified Results

Correctly classified

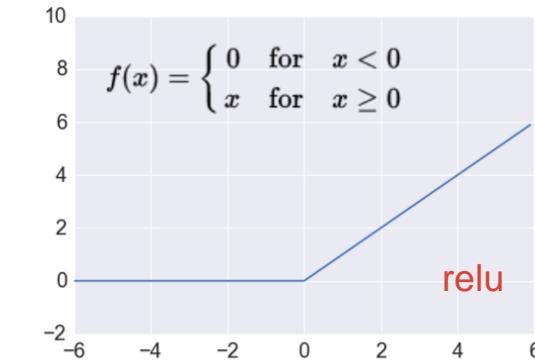
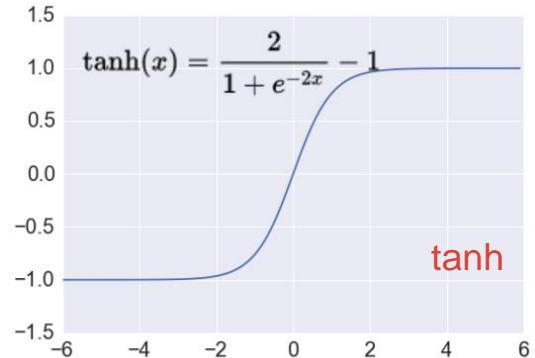
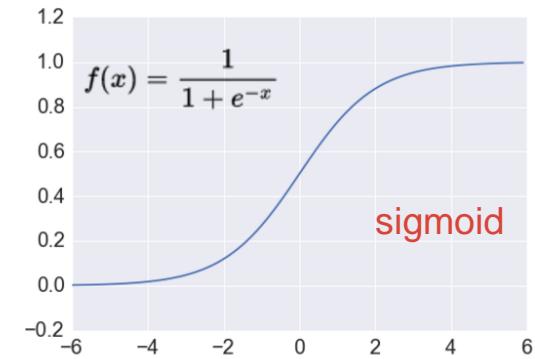
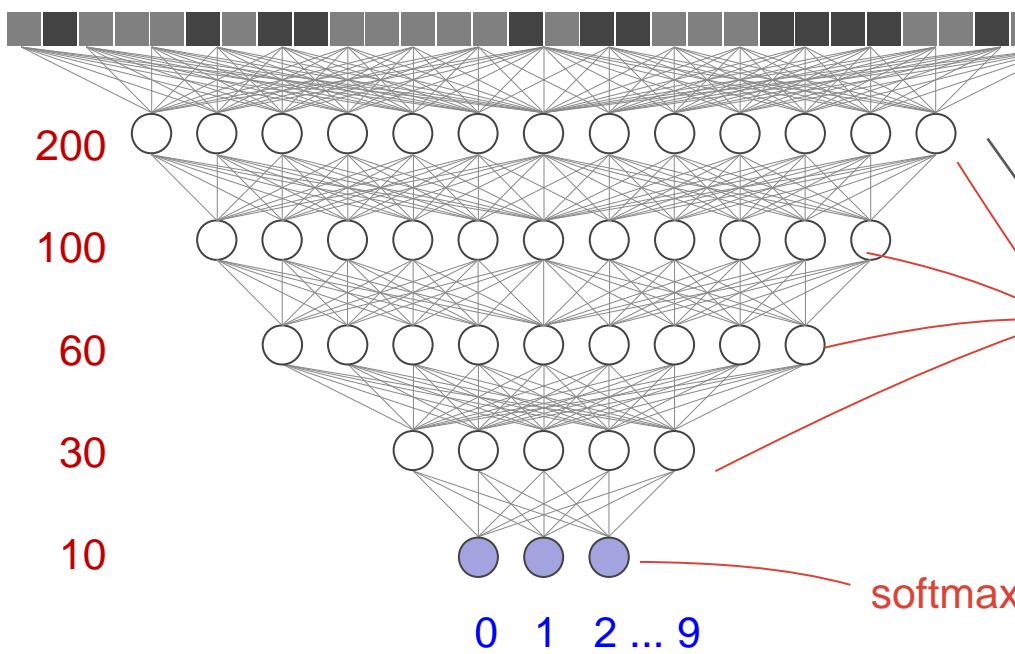


Incorrectly classified



Adding More Layers?

- Using a 5 fully connected layer model:

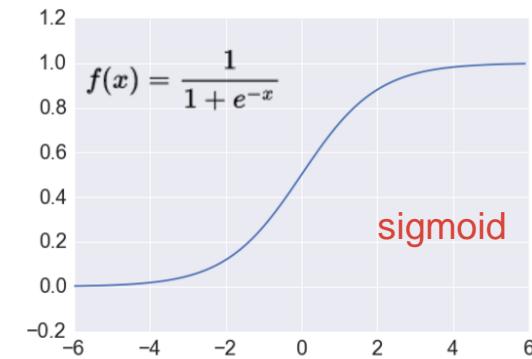
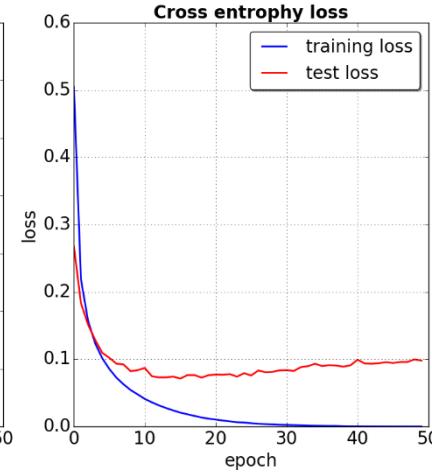
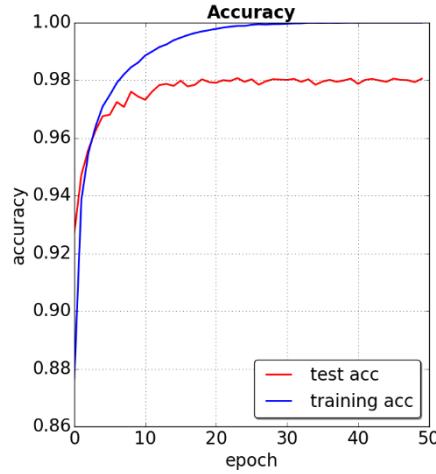
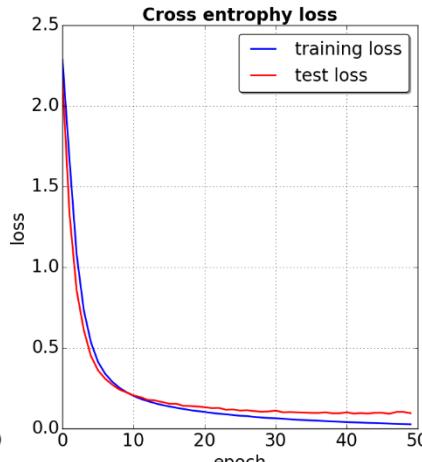
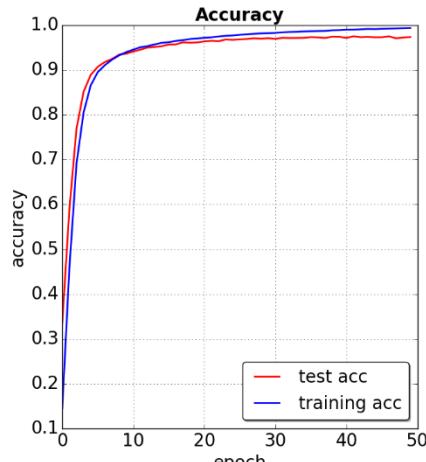


5 Layer Model In Keras

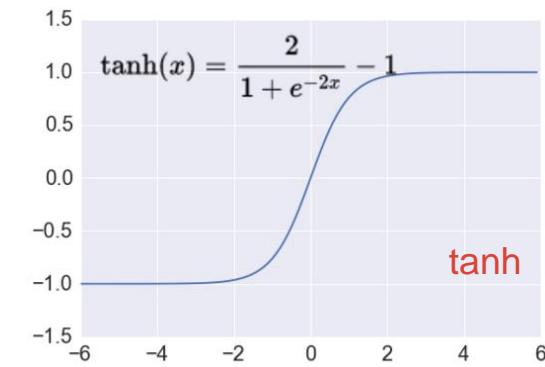
```
model = Sequential()
# try also tanh, sigmoid
act_func='relu'
model.add(Dense(200,activation=act_func,input_shape=input_shape))
model.add(Dense(100,activation=act_func))
model.add(Dense( 60,activation=act_func))
model.add(Dense( 30,activation=act_func))
model.add(Dense(nb_classes,activation='softmax'))
model.compile(loss='categorical_crossentropy',optimizer='rmsprop',
               metrics=['accuracy'])
h = model.fit(X_train, Y_train, batch_size=batch_size,nb_epoch=nb_epoch,
               verbose=1, validation_data=(X_test, Y_test))
```

5 Layer Regression – Different Activation

- Training accuracy vs Test accuracy, loss function
- We reach a Test accuracy at **97.35% (sigmoid), 98.06% (tanh)**



sigmoid



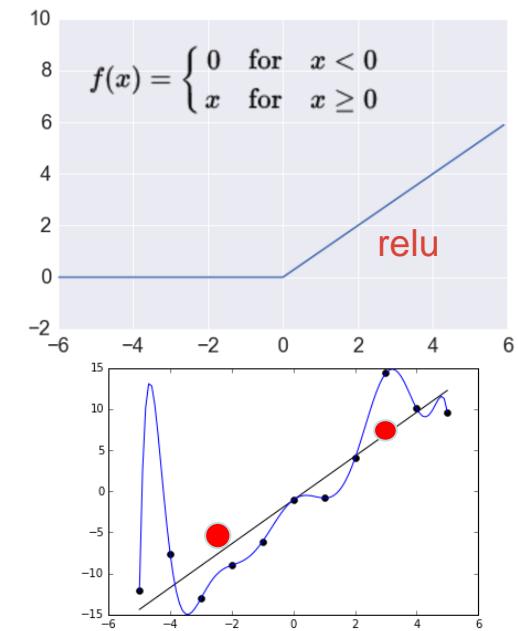
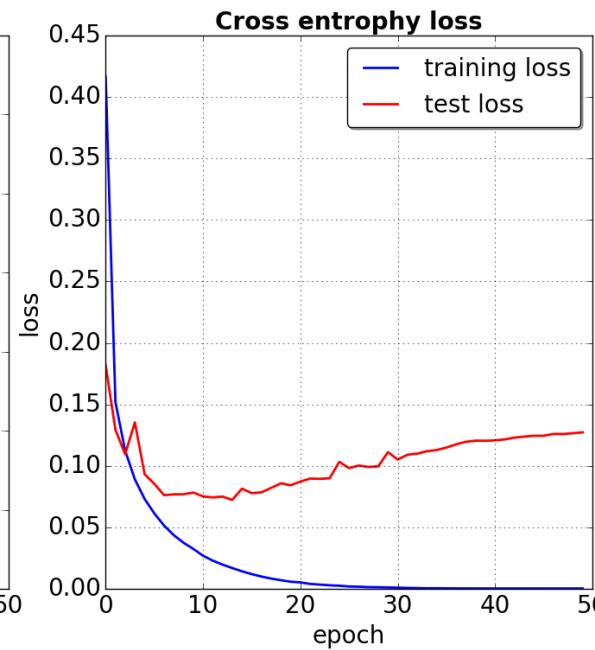
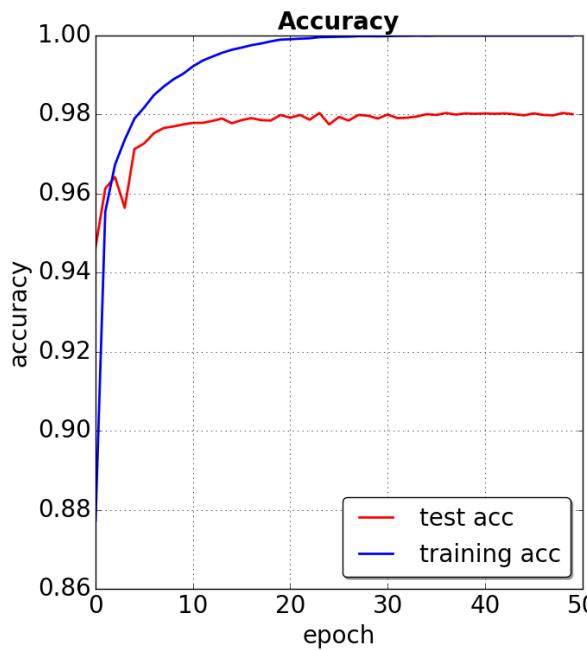
tanh

Rectified Linear Unit (ReLU) activation function

- ReLU - The Rectified Linear Unit has become very popular in the last few years:

$$f(z) = \max(0, z)$$

- We get a test accuracy of **98.07%** with ReLU

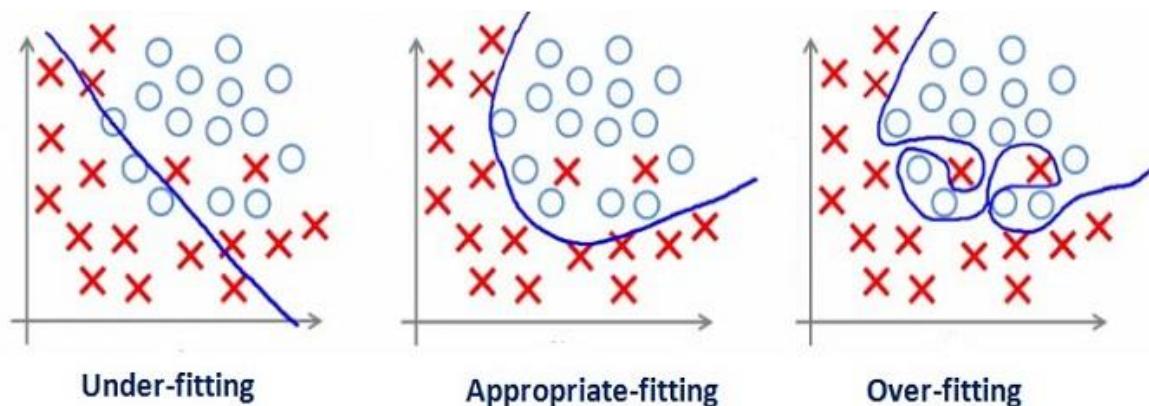


Overfitting

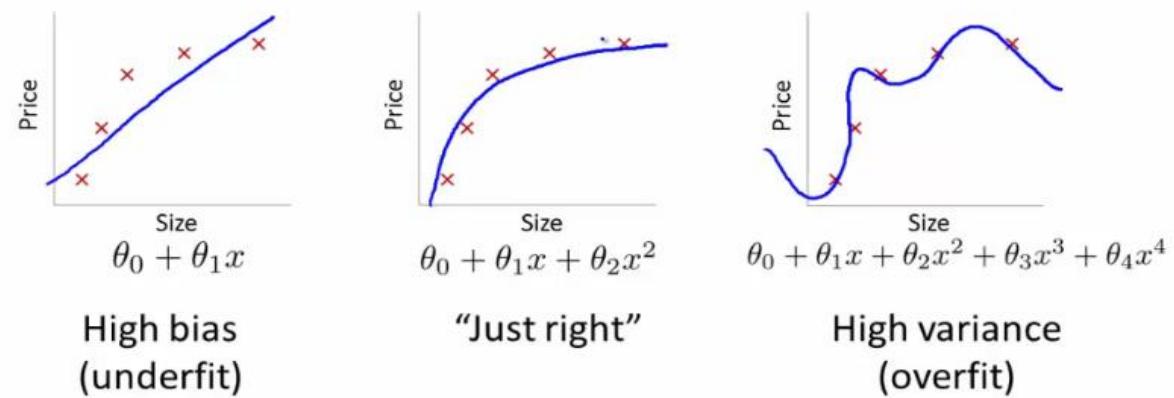
Overfitting

- Overfitting occurs when a model is excessively complex, such as having too many parameters relative to the number of observations. A model that has been overfit has poor predictive performance, as it overreacts to minor fluctuations in the training data.

Classification:

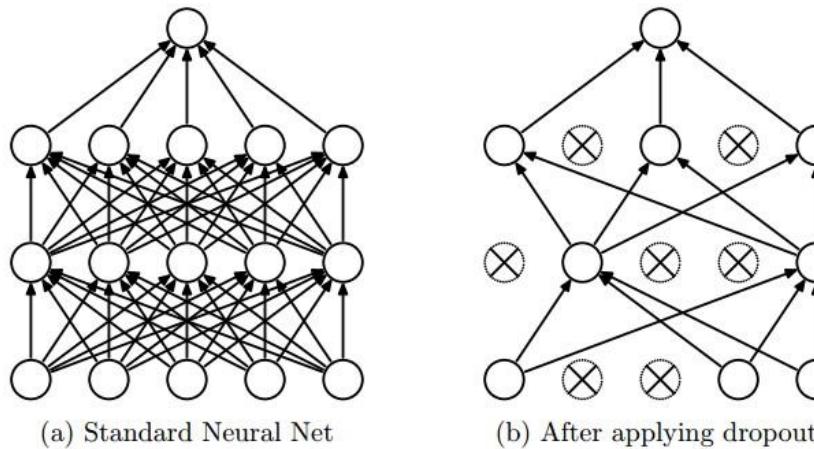


Regression:



Regularization - Dropout

- Dropout is an extremely effective, simple and recently introduced regularization technique by Srivastava et al (2014).



- While training, dropout is implemented by only keeping a neuron active with some probability p (a hyperparameter), or setting it to zero otherwise.
- It is quite simple to apply dropout in Keras.

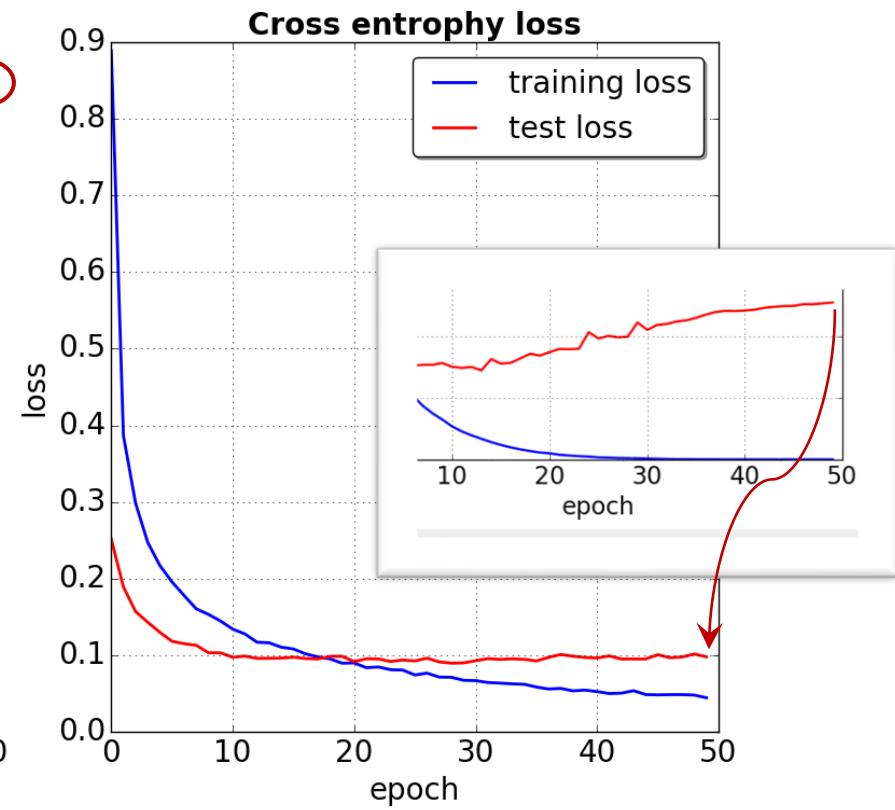
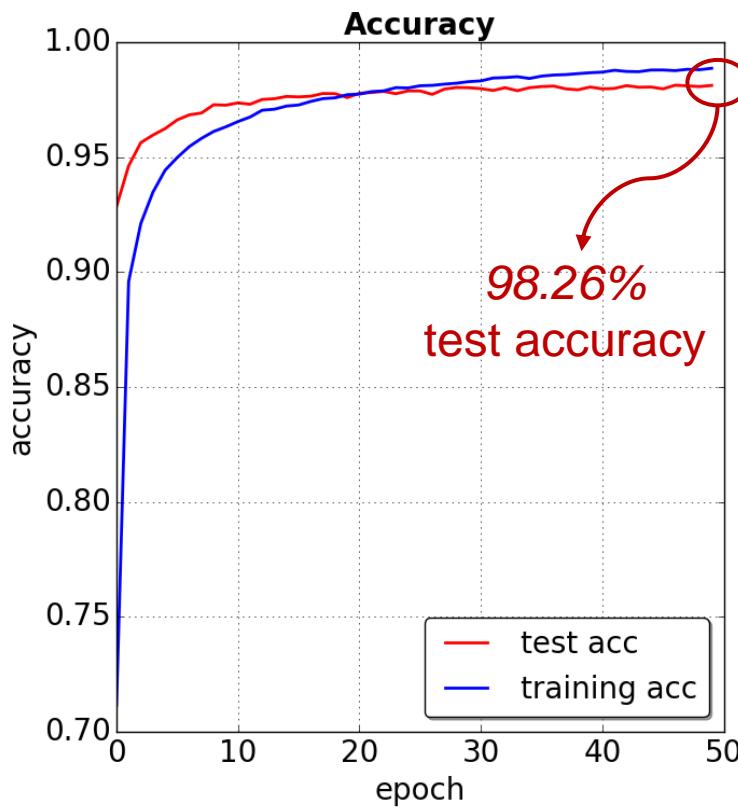
```
# apply a dropout rate 0.25 (drop 25% of the neurons)
model.add(Dropout(0.25))
```

Apply Dropout To The 5 Layer NN

```
model = Sequential()
act_func='relu'
p_dropout=0.25 # apply a dropout rate 25 %
model.add(Dense(200,activation=act_func,input_shape=input_shape))
model.add(Dropout(p_dropout))
model.add(Dense(100,activation=act_func))
model.add(Dropout(p_dropout))
model.add(Dense( 60,activation=act_func))
model.add(Dropout(p_dropout))
model.add(Dense( 30,activation=act_func))
model.add(Dropout(p_dropout))
model.add(Dense(nb_classes,activation='softmax'))
model.compile(loss='categorical_crossentropy',optimizer='sgd',
               metrics=['accuracy'])
h = model.fit(X_train, Y_train, batch_size=batch_size,nb_epoch=nb_epoch,
               verbose=1, validation_data=(X_test, Y_test))
```

Results Using $p_{dropout}=0.25$

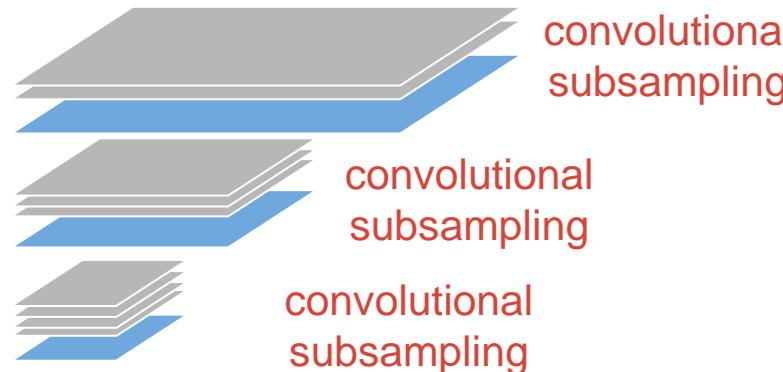
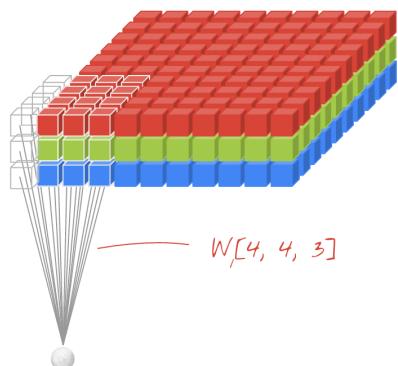
- Resolve the overfitting issue
- Sustained **98.26%** accuracy



Why Using Fully Connected Layers?

- Such a network architecture does not consider the spatial structure of the images.
 - For instance, it treats input pixels which are far apart and close together on exactly the same weight.
- Spatial structure must instead be inferred from the training data.
- ❖ Is there an architecture which tries to take advantage of the spatial structure?

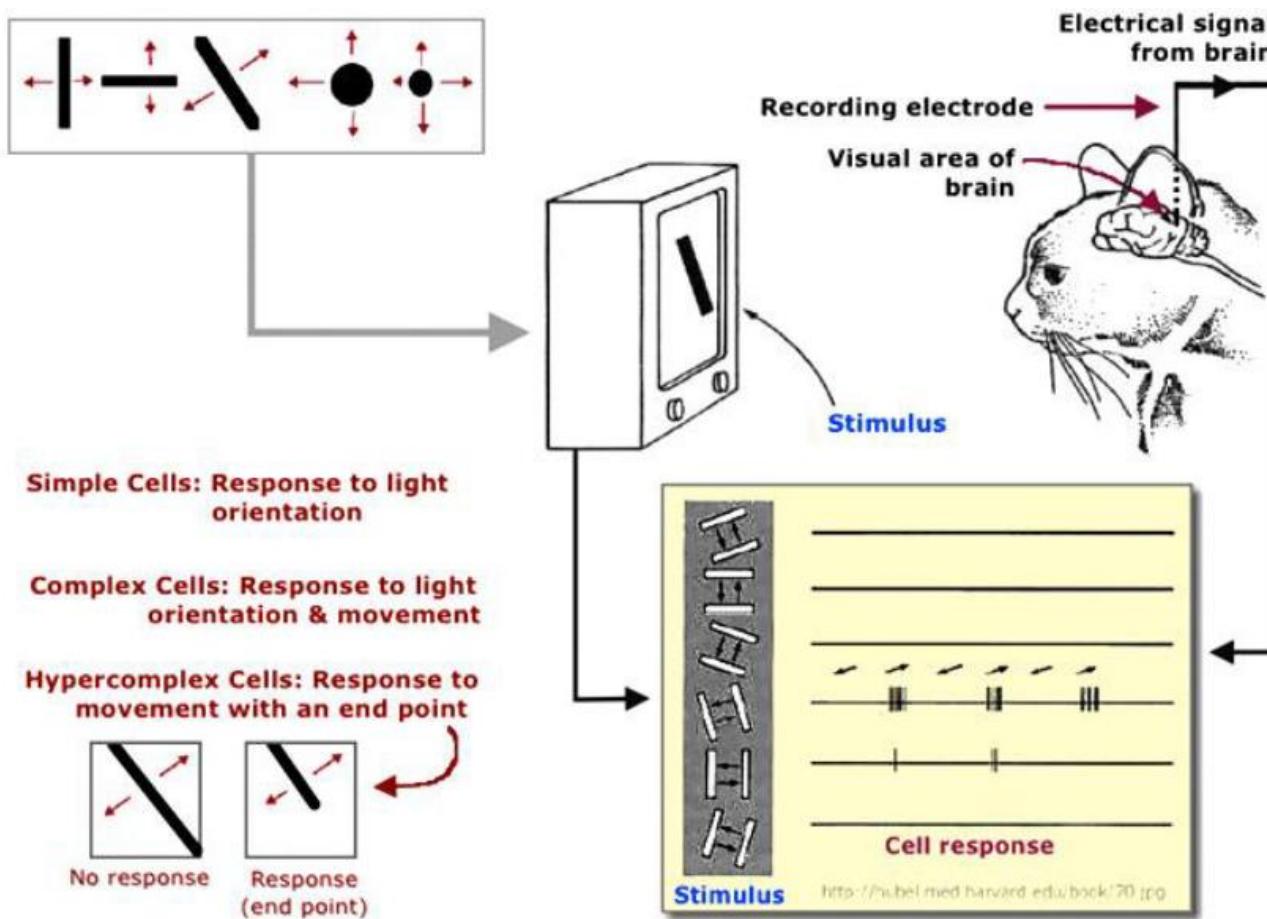
Convolution Neuron Network (CNN)



from Martin Görner [Learn TensorFlow and deep learning, without a Ph.D](#)

- Deep convolutional network is one of the most widely used types of deep network.
- In a layer of a convolutional network, one "neuron" does a weighted sum of the pixels just above it, across a small region of the image only. It then acts normally by adding a bias and feeding the result through its activation function.
- The big difference is that each neuron reuses the same weights whereas in the fully-connected networks seen previously, each neuron had its own set of weights.

Why use CNN?



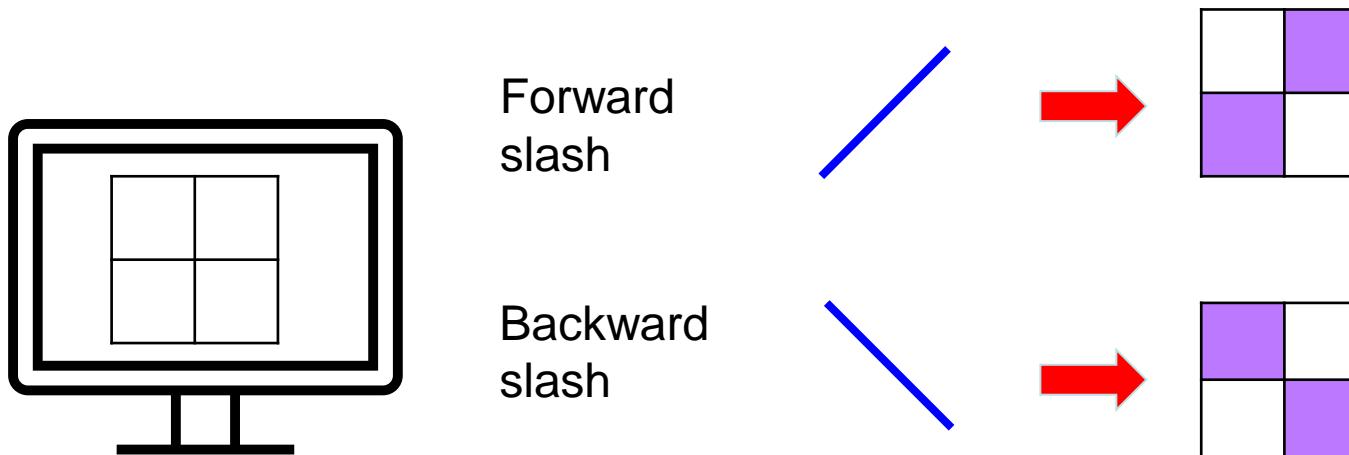
Hubel & Wiesel, 1959

Slide referred from Stanford, CS231n, winter 2016, Lecture 1

A simple example shows how CNN works

➤ Simplified world

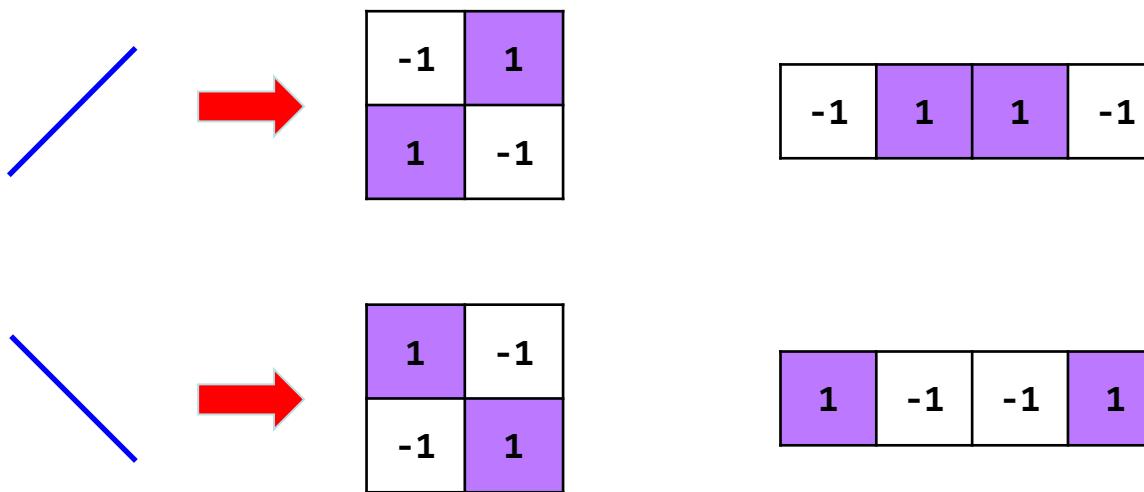
- Only has two characters: “/” and “\”
- Image only has 2x2 resolution



Slides referenced from Luis Serrano,
A friendly introduction to Convolutional Neural Networks and Image Recognition,
<https://youtu.be/2-OI7ZB0MmU>

A simple example shows how CNN works

- Simplified image in binary world



Think about a way using the above 2x2 matrix elements to differentiate them?

A simple example shows how CNN works

➤ Solution:

- Use a filter, overlay with the image, do a dot product:

Image

-1	1
1	-1

Filter

-1	+1
+1	-1



-1	1
1	-1



$$=(-1)(-1) + 1 \cdot 1 + 1 \cdot 1 + (-1)(-1) = 4$$

1	-1
-1	1

-1	+1
+1	-1



1	-1
-1	1



$$=(1)(-1) + (-1) \cdot 1 + (-1) \cdot 1 + 1(-1) = -4$$

You can use this filter
for the same effect:

+1	-1
-1	+1

A simple example shows how CNN works

➤ How about the below figures?

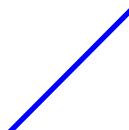
- Use the same filter, overlay with the image, do a dot product:

Image

-1	1
1	1

Filter

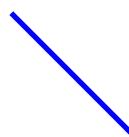
-1	+1
+1	-1



-1	1
1	-1



$$=(-1)(-1) + 1 \cdot 1 + 1 \cdot 1 \\ +(1)(-1) = 2$$



-1	-1
-1	1



$$=(-1)(-1) + (-1) \cdot 1 \\ + (-1) \cdot 1 + 1(-1) = -2$$

-1	-1
-1	1

-1	+1
+1	-1

If the result >0, poorly drawn “/”
 If the result <0, incomplete “\”

You can use this filter
 for the same effect:

+1	-1
-1	+1

A simple example shows how CNN works

➤ As an exercise?

- Use the same filter, to classify below images:

Image

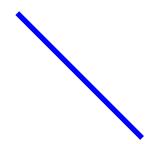
-1	1
-1	1

Filter

-1	+1
+1	-1



-1	-1
1	1



-1	+1
+1	-1

You can use this filter
for the same effect:

+1	-1
-1	+1

A simple example shows how CNN works

➤ As an exercise?

- Use the same filter, overlay with the image, do a dot product:

Image

-1	1
-1	1

Filter

-1	+1
+1	-1



-1	1
-1	1



$$= (-1)(-1) + 1 \cdot 1 - 1 \cdot 1 + (1)(-1) = 0$$

-1	-1
1	1

-1	+1
+1	-1



-1	-1
1	1



$$= (-1)(-1) + (-1) \cdot 1 + (1) \cdot 1 + 1(-1) = 0$$

Results are zeros..., No idea!



You can use this filter for the same effect:

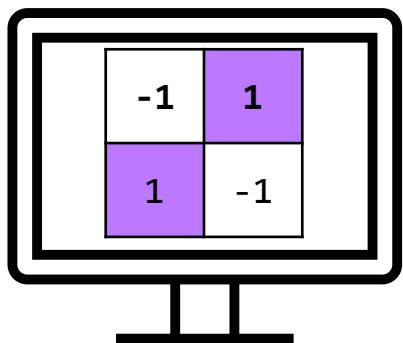
+1	-1
-1	+1

A simple example shows how CNN works

➤ How do we find this filter that works?

– Vanilla way:

1. Check all possible combinations ($2^2 \cdot 2^2 \cdot 2^2 = 16$)
2. Run them
3. Select the best filter



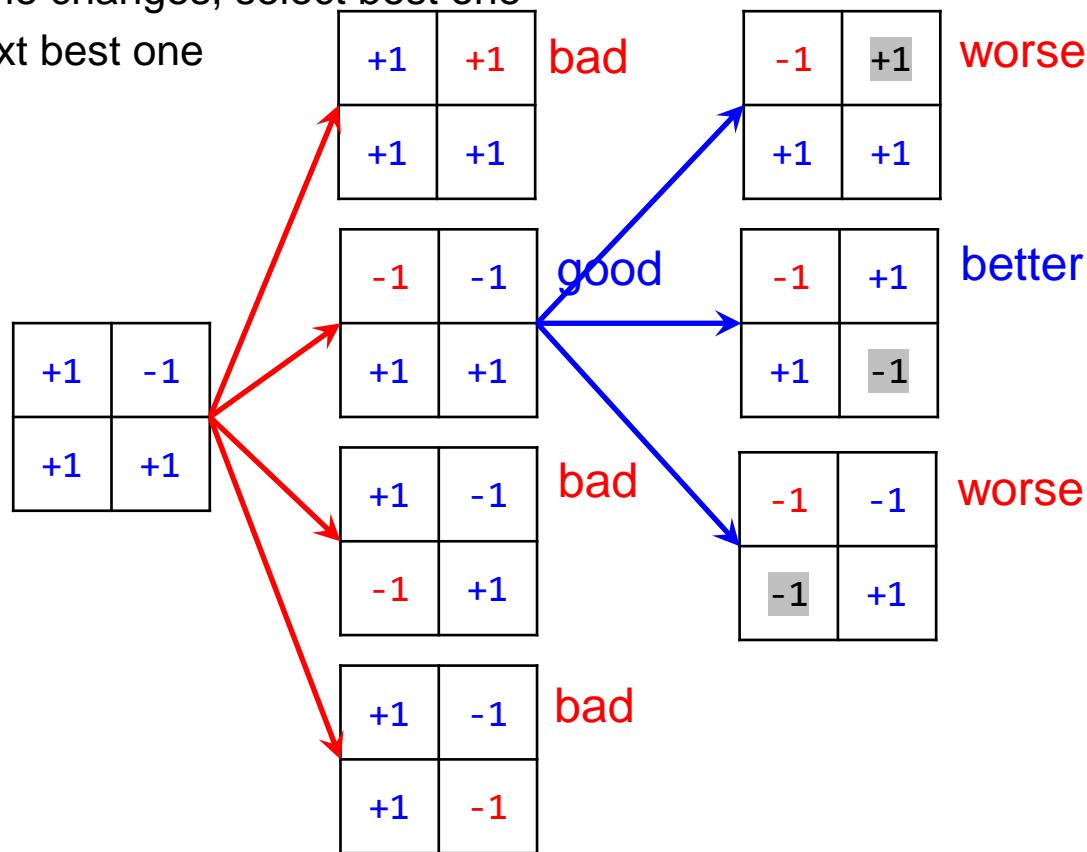
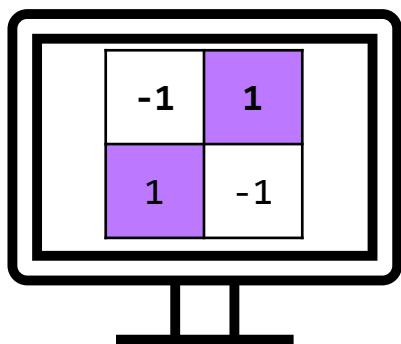
+1	+1	+1	-1	-1	+1	-1	-1
+1	+1	+1	+1	+1	+1	+1	+1
-1	+1	-1	+1	+1	-1	+1	-1
+1	+1	-1	+1	-1	-1	+1	-1
-1	+1	-1	+1	+1	-1	-1	+1
+1	+1	+1	-1	-1	-1	+1	-1
-1	+1	-1	+1	+1	-1	-1	+1
+1	+1	-1	-1	-1	-1	-1	-1

A simple example shows how CNN works

➤ How do we find this filter that works?

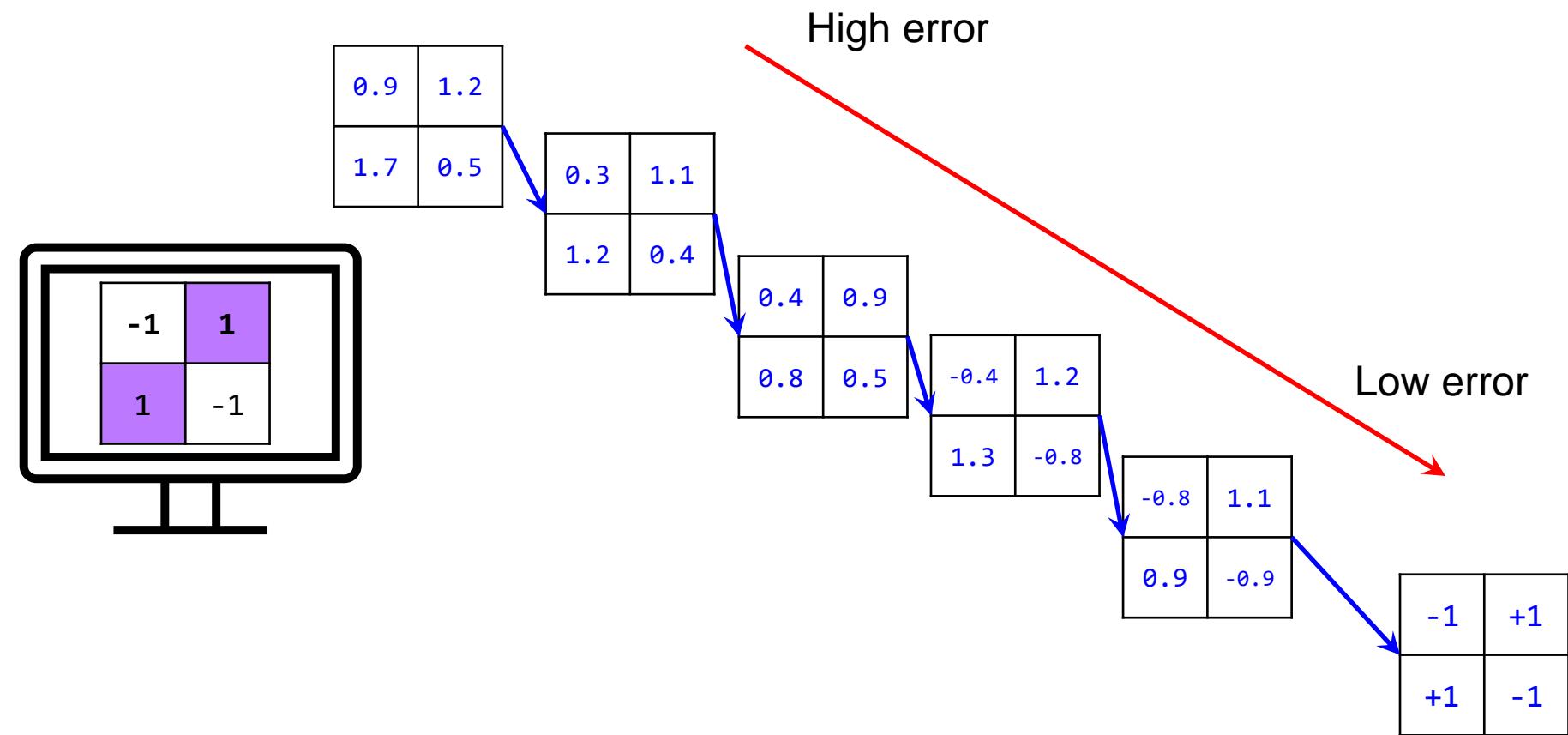
– Better way:

1. Start from a random filter
2. Make some changes, select best one
3. Select next best one



A simple example shows how CNN works

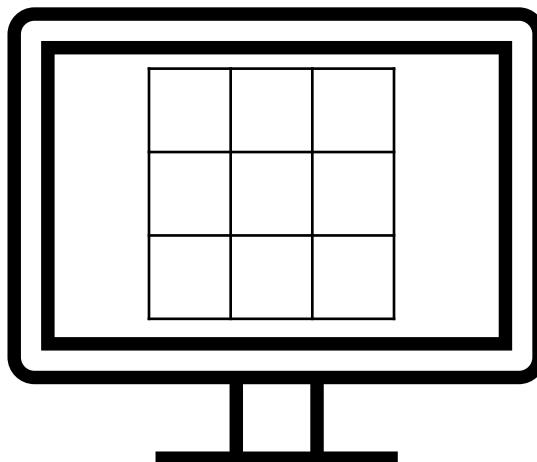
- How do we find this filter that works?
 - What did we learn yesterday?
 - Gradient Descent



A slightly complex example

➤ A more complex world:

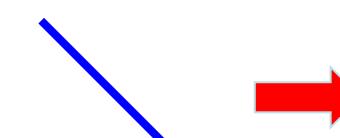
- Image has 3x3 resolution
- 4 characters:
 - "/", "\", "X", "0"



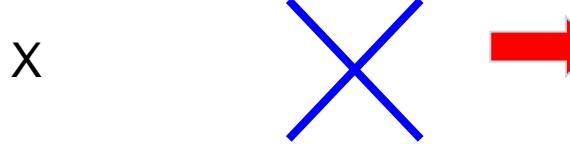
Forward
slash



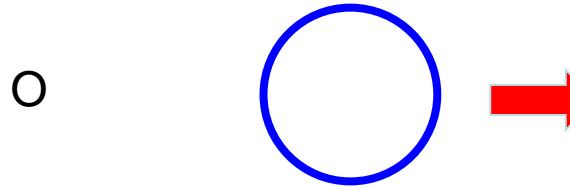
Backward
slash



X



O



-1	-1	1
-1	1	-1
1	-1	-1

1	-1	-1
-1	1	-1
-1	-1	1

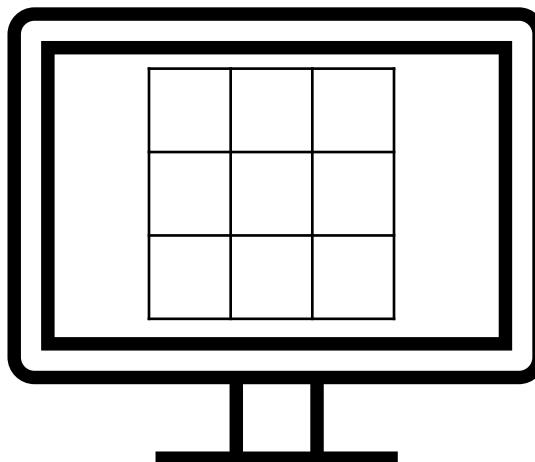
1	-1	1
-1	1	-1
1	-1	1

-1	1	-1
1	-1	1
-1	1	-1

A slightly complex example

➤ A more complex world:

- Image has 3x3 resolution
- 4 characters:
 - “/”, “\”, “X”, “0”



1	-1	1
-1	1	-1
1	-1	1

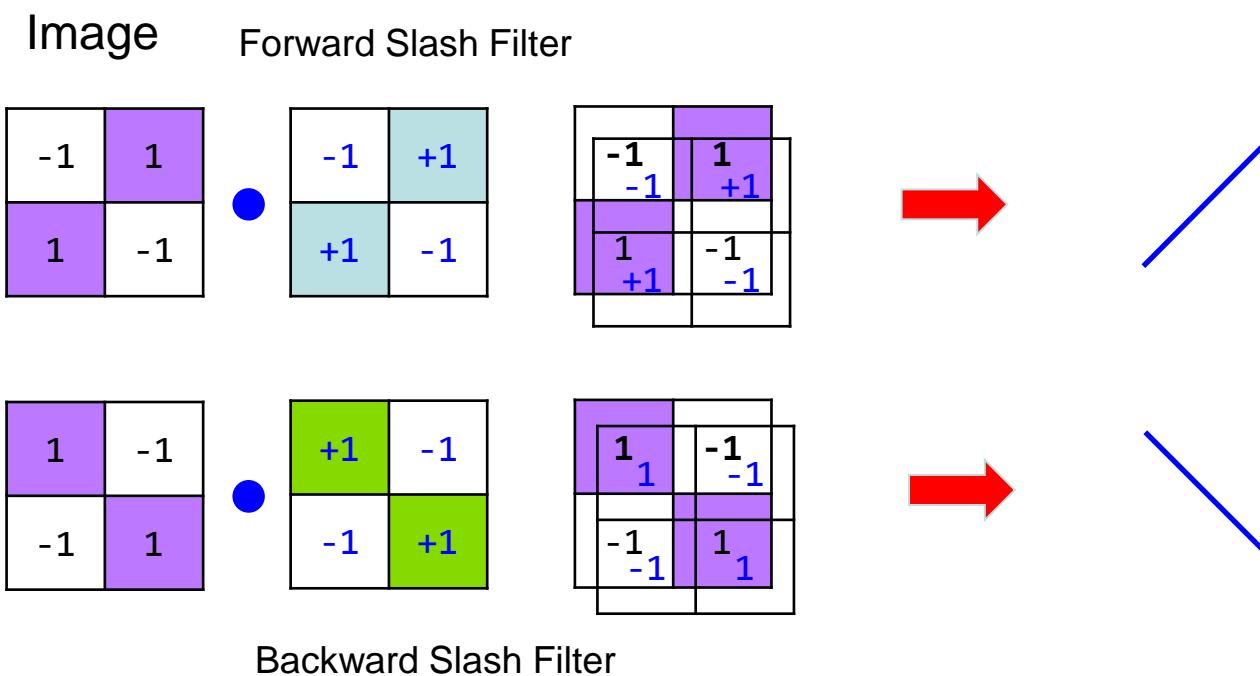
1	-1	1
-1	1	-1
1	-1	1

1 1	-1 -1	1 1
-1 -1	1 1	-1 -1
1 1	-1 -1	1 1

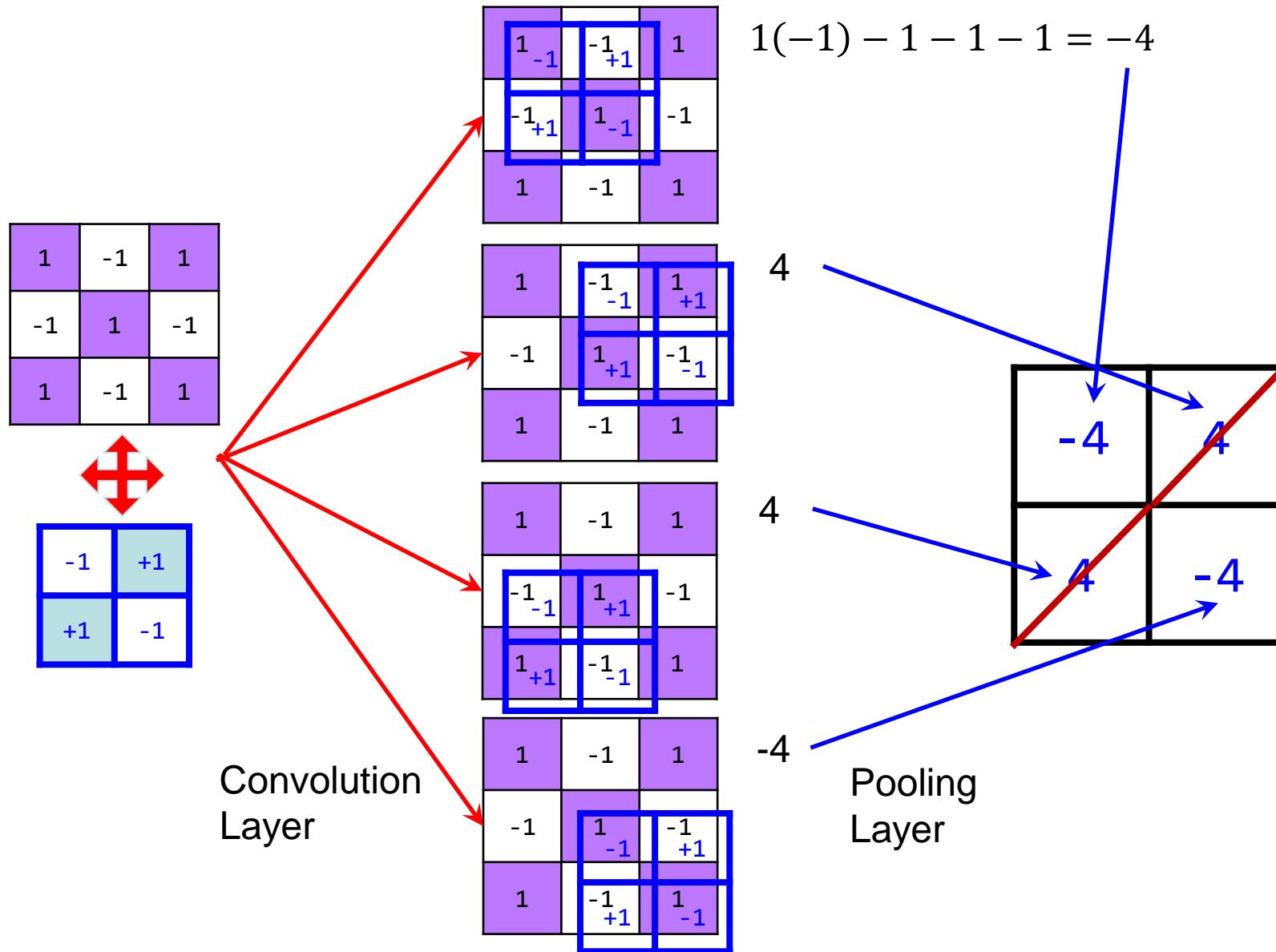
Can we simply use the same strategy as the 2x2 world??

A slightly complex example

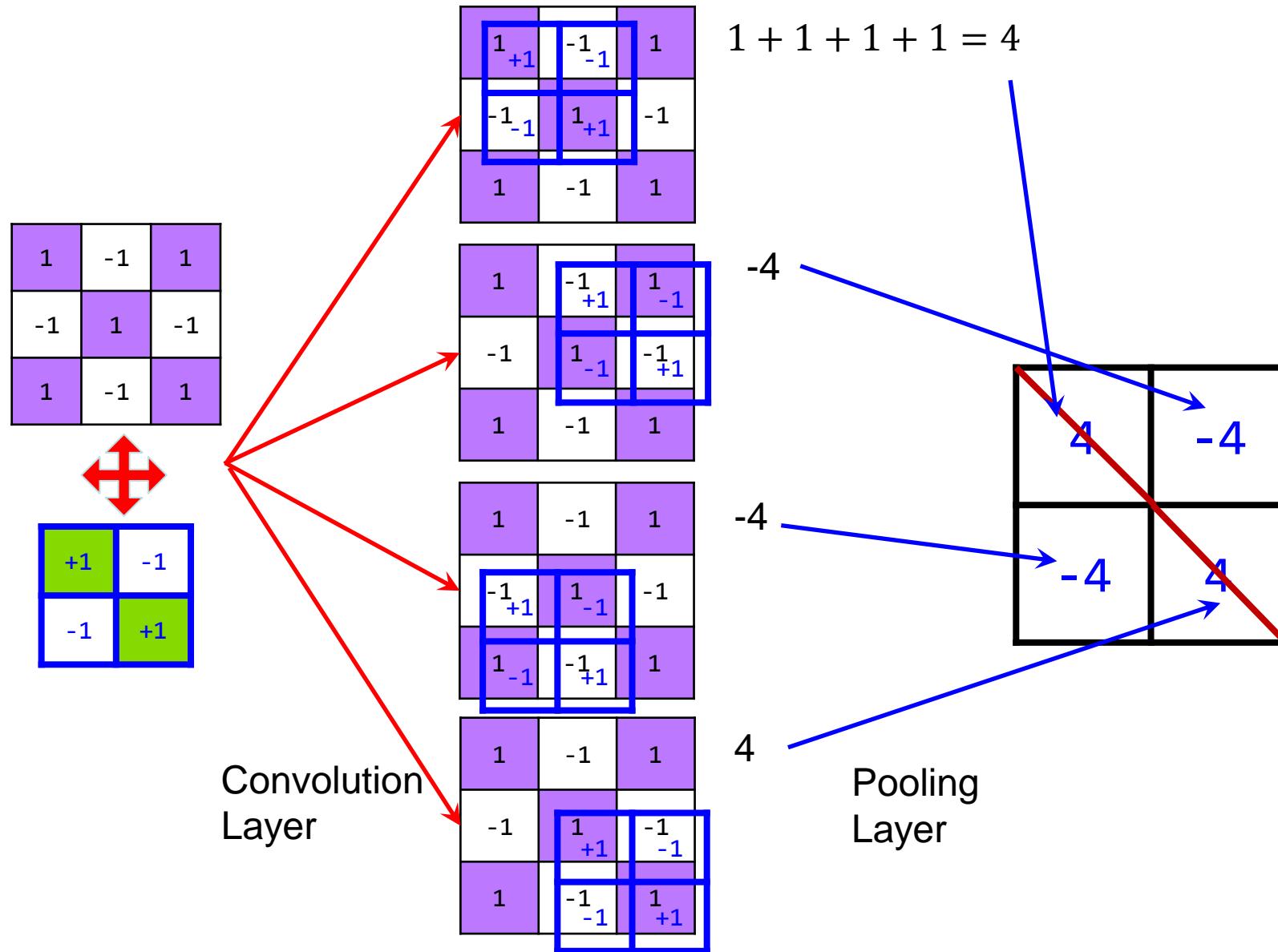
- Use our previous 2×2 world experience:



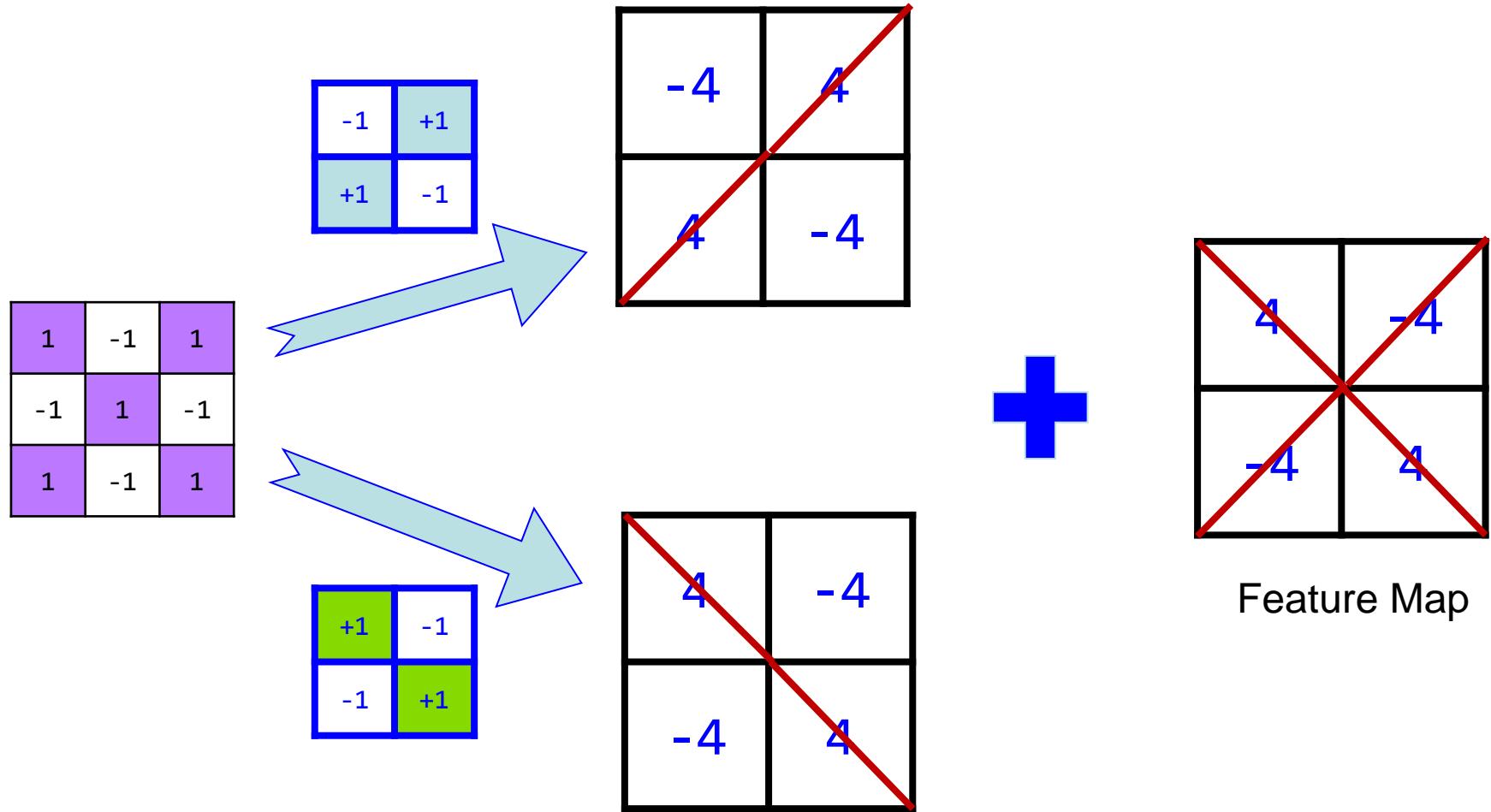
Using our previous knowledge



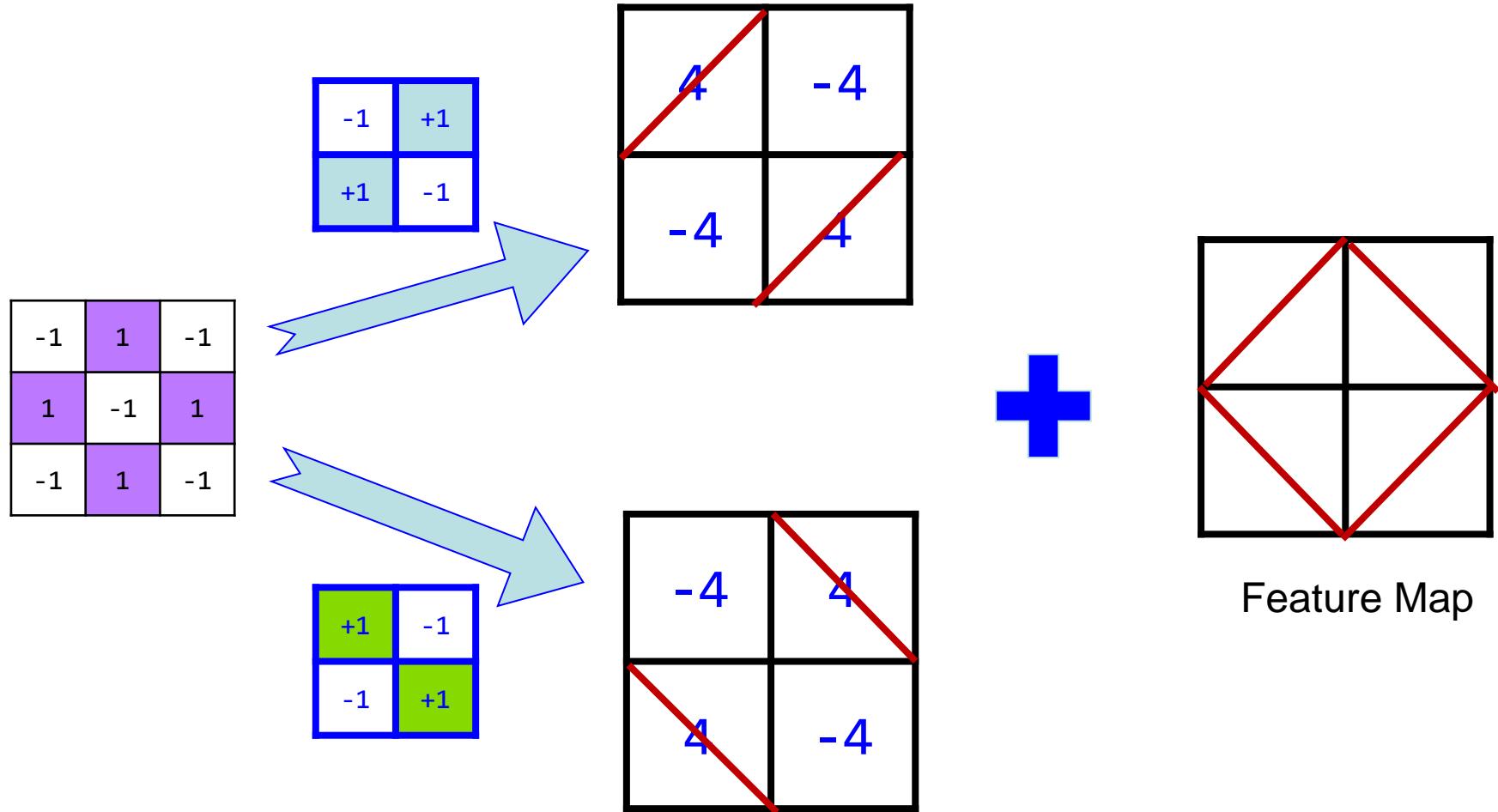
Using our previous knowledge



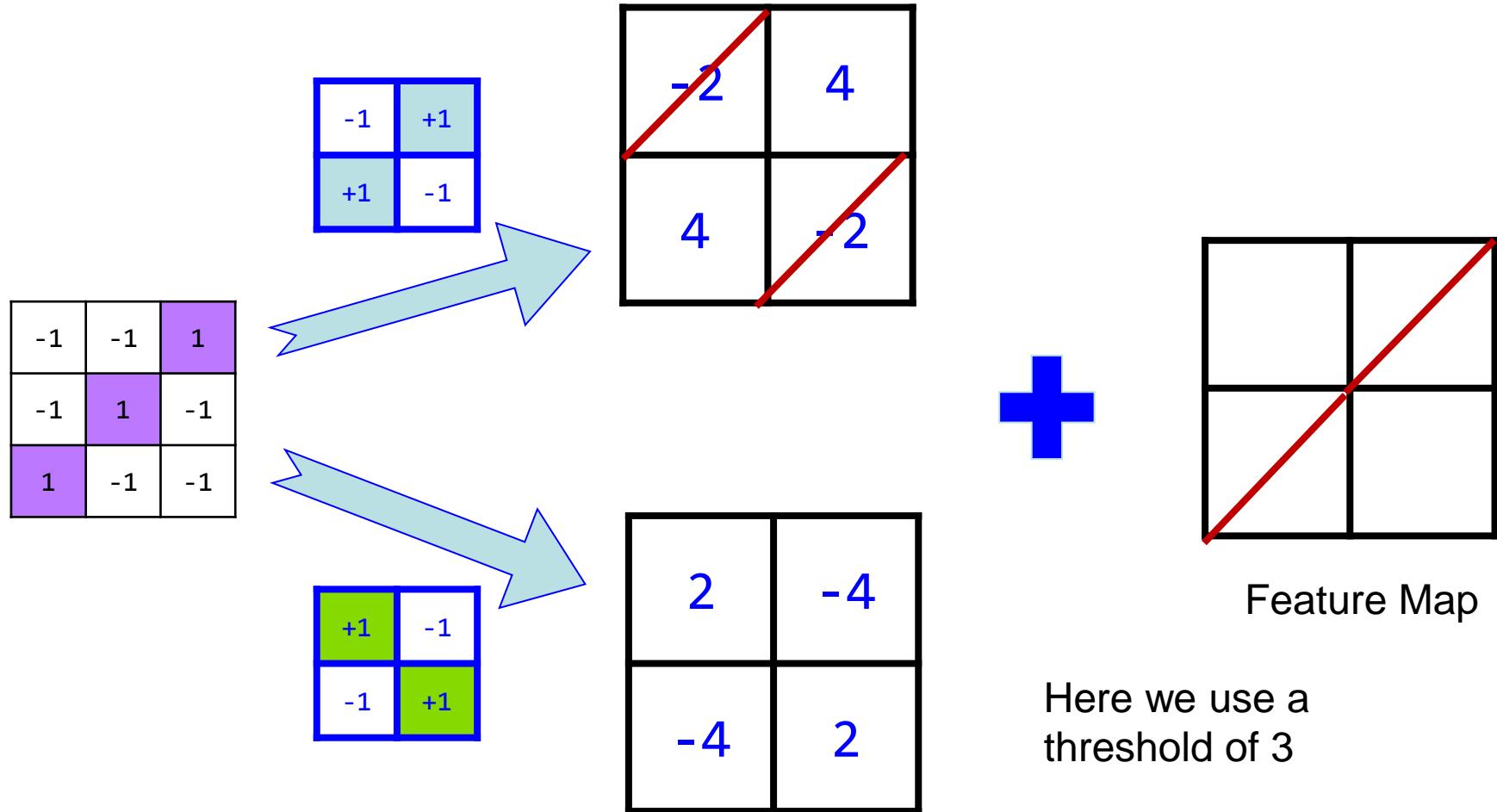
Combine the last two results



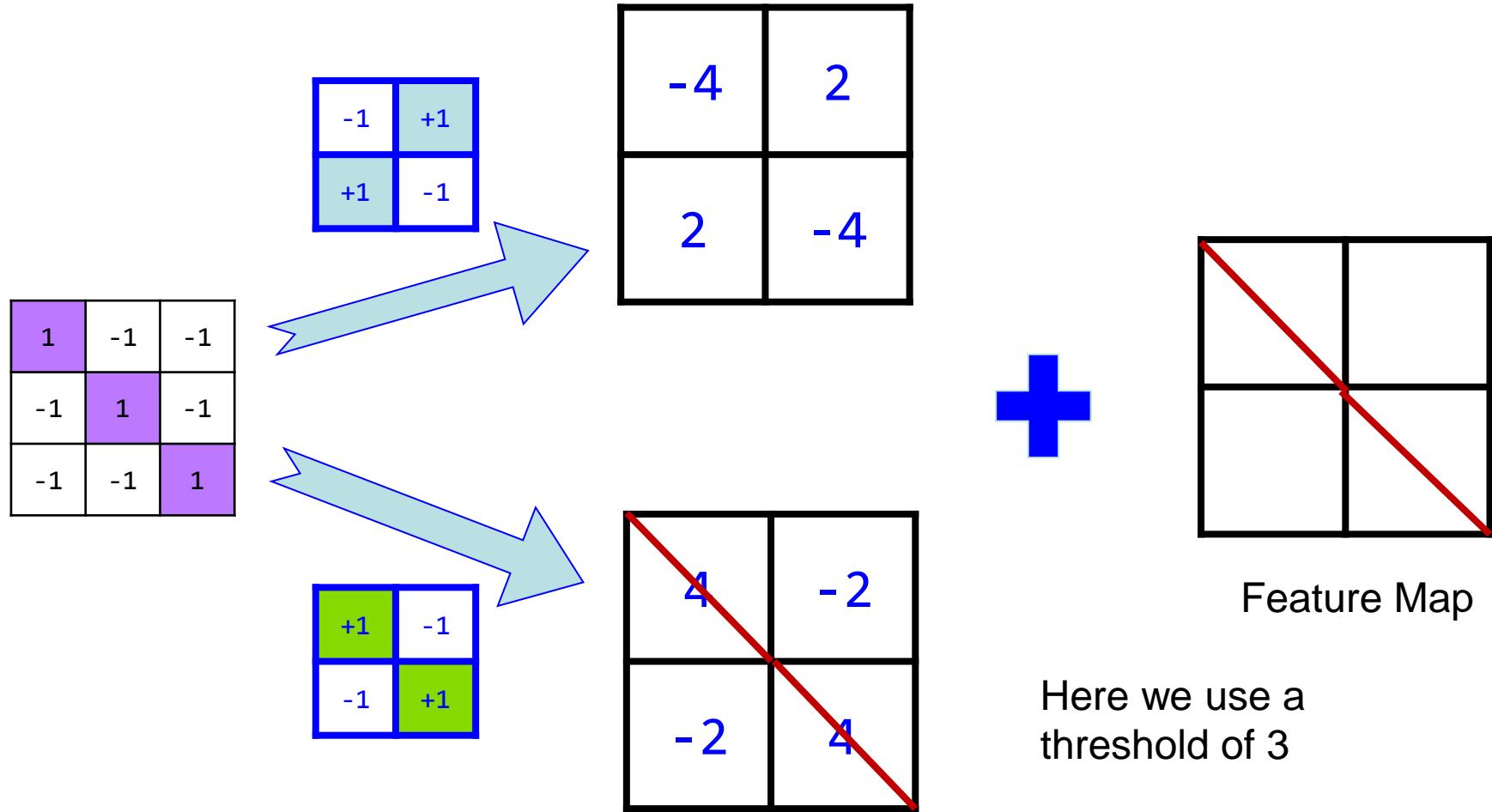
We can do same operation on “O”



Do the same operation on forward slash “/”



Do the same operation on backward slash “\”



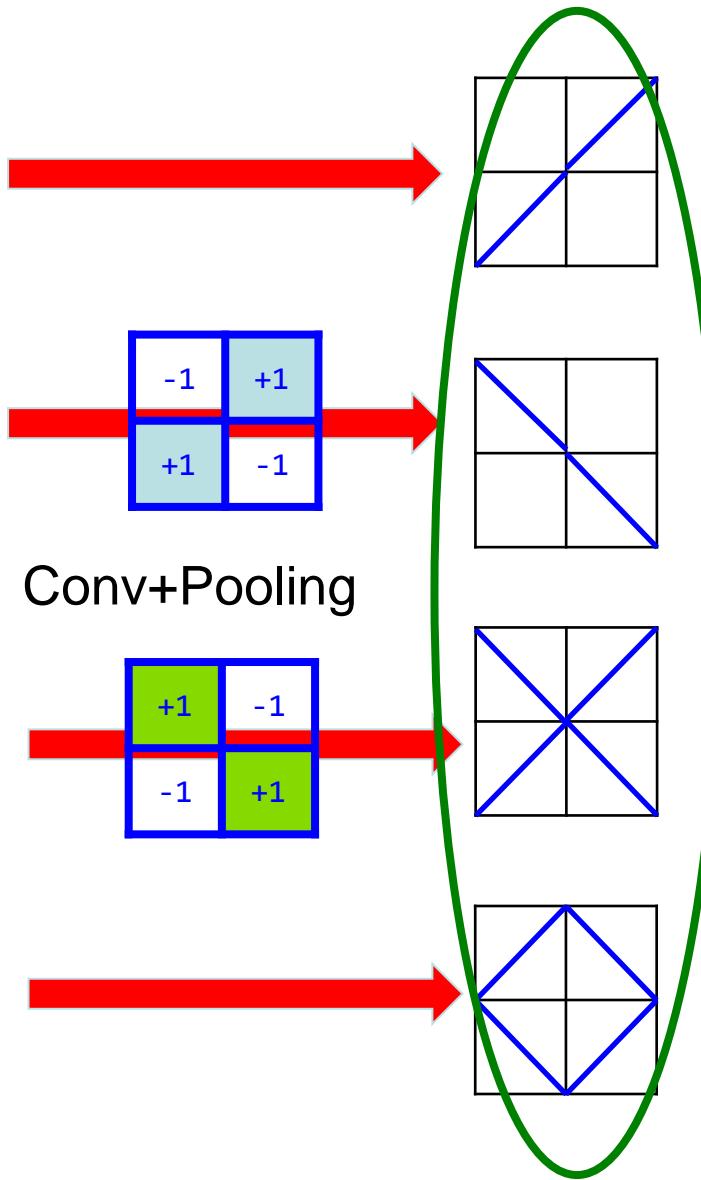
A short summary

-1	-1	1
-1	1	-1
1	-1	-1

1	-1	-1
-1	1	-1
-1	-1	1

1	-1	1
-1	1	-1
1	-1	1

-1	1	-1
1	-1	1
-1	1	-1

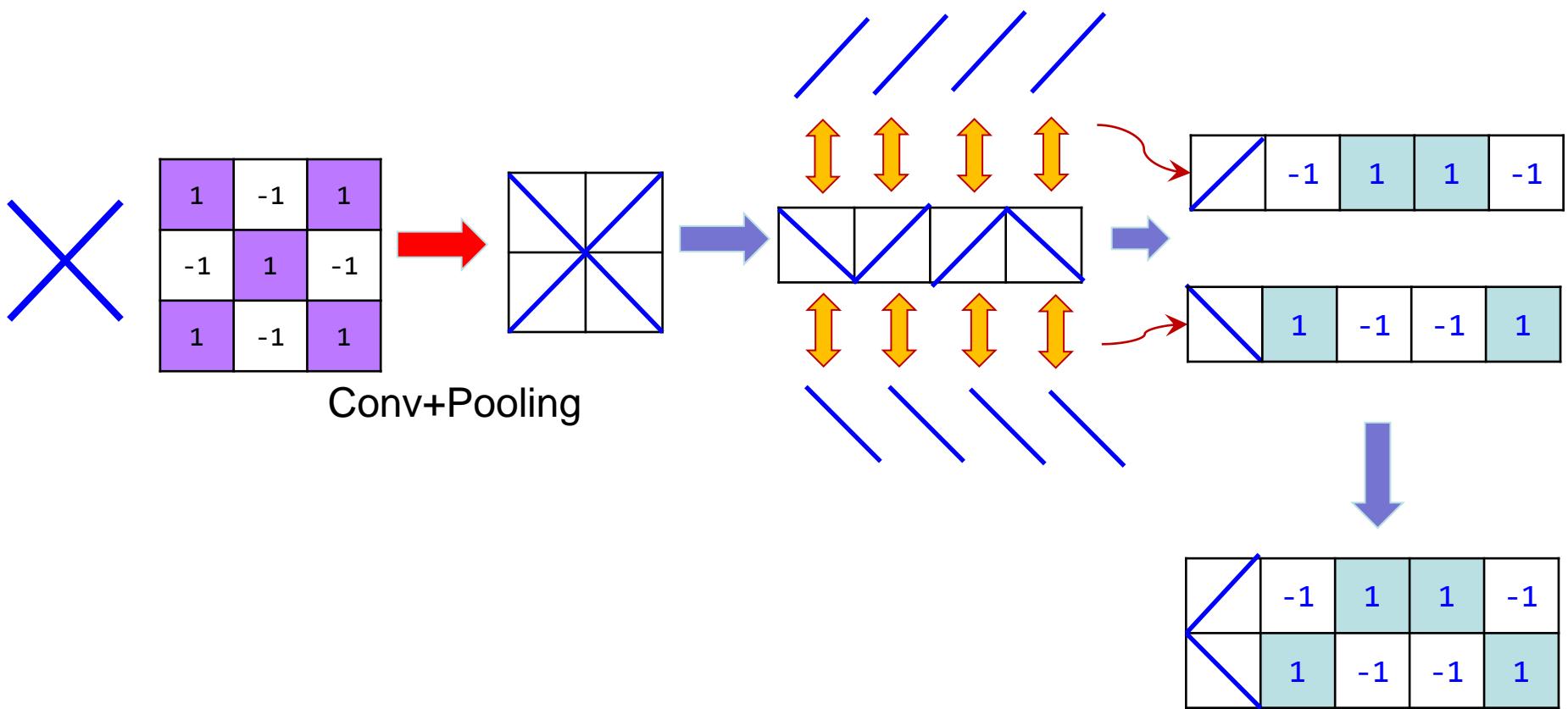


- Convolution layer
 - ✓ Use small filter to slide over the large image
- Pooling layer
 - ✓ Check if we find something using a threshold

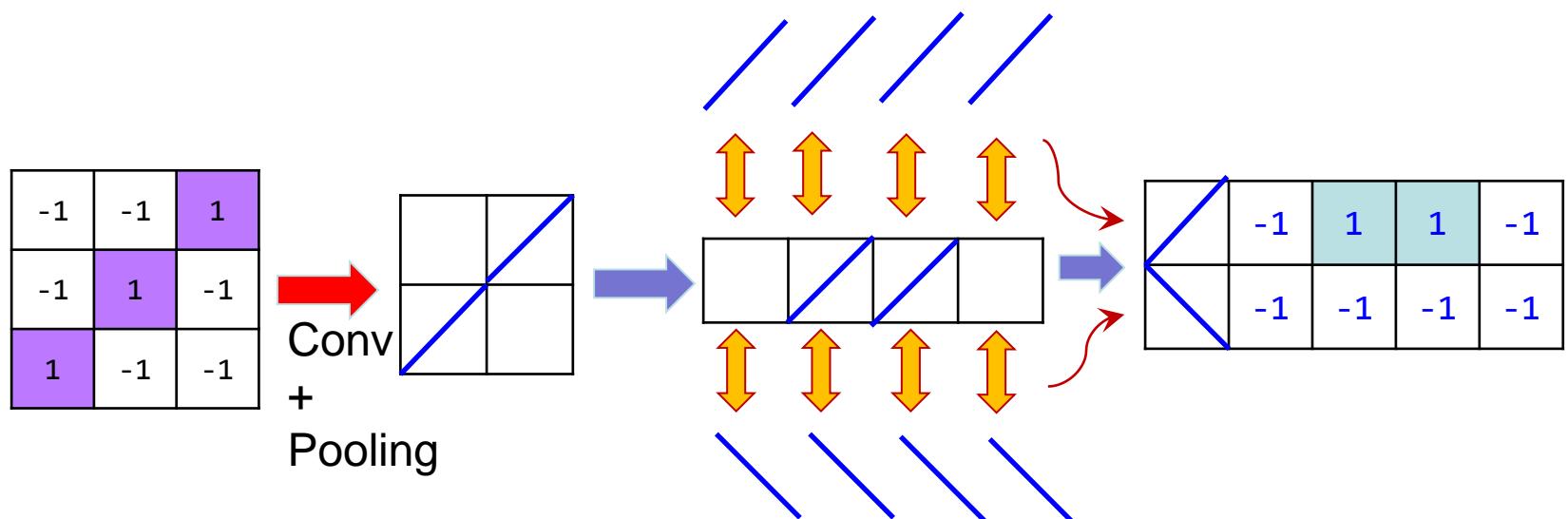
Feature Map

What about the fully connected layer?

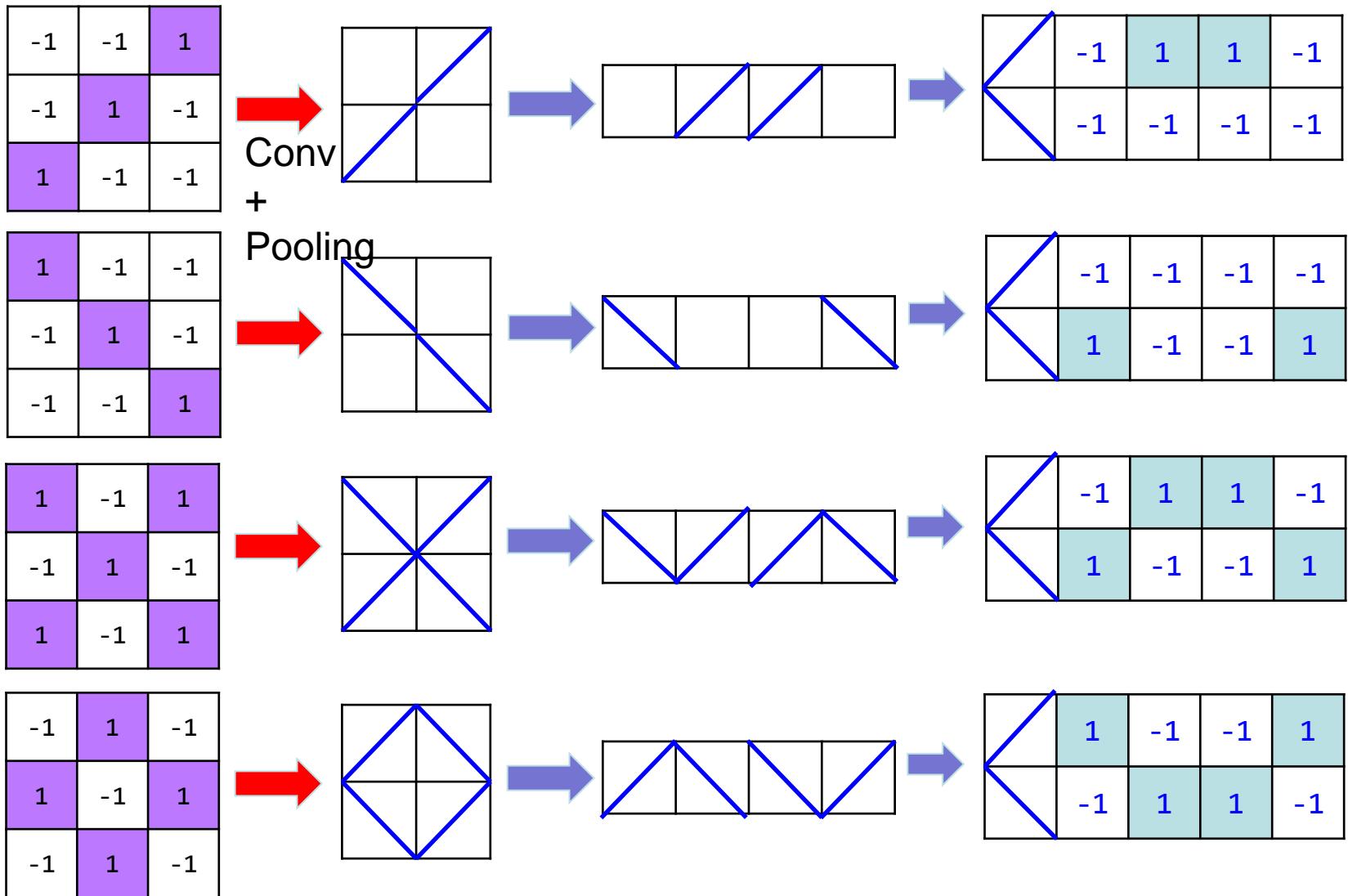
How to let computer know our characters?



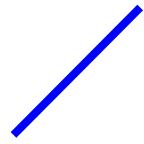
How to let computer know our characters?



A slightly complex example



Create our filters



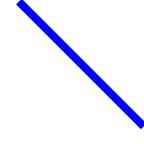
-1	-1	1
-1	1	-1
1	-1	-1



	-1	1	1	-1
	-1	-1	-1	-1



	-1	1	1	-1
	-1	-1	-1	-1



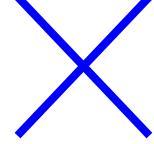
1	-1	-1
-1	1	-1
-1	-1	1



	-1	-1	-1	-1
	1	-1	-1	1



	-1	-1	-1	-1
	1	-1	-1	1



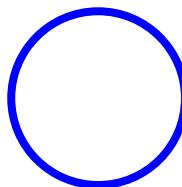
1	-1	1
-1	1	-1
1	-1	1



	-1	1	1	-1
	1	-1	-1	1



	-1	1	1	-1
	1	-1	-1	1



-1	1	-1
1	-1	1
-1	1	-1

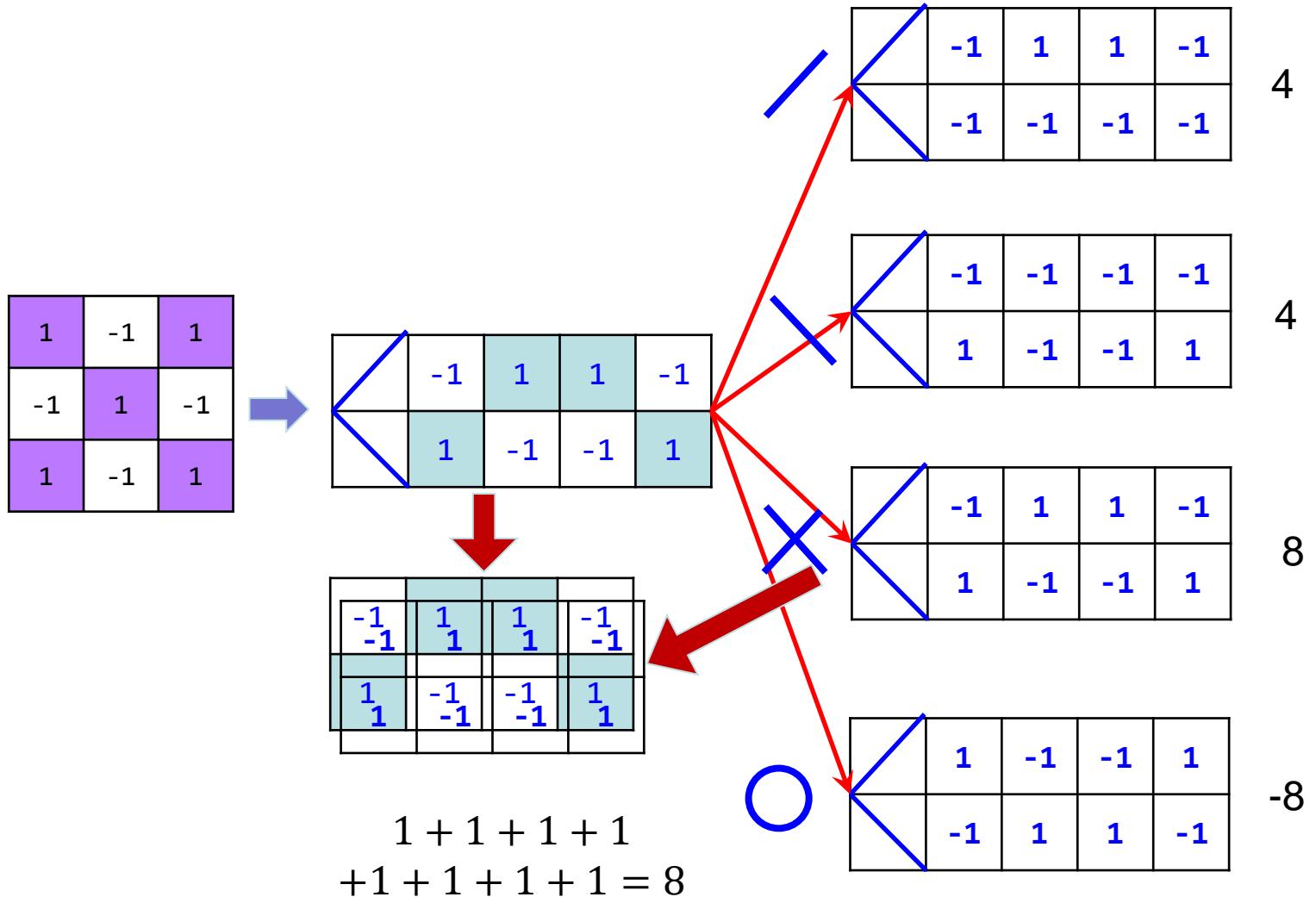


	1	-1	-1	1
	-1	1	1	-1

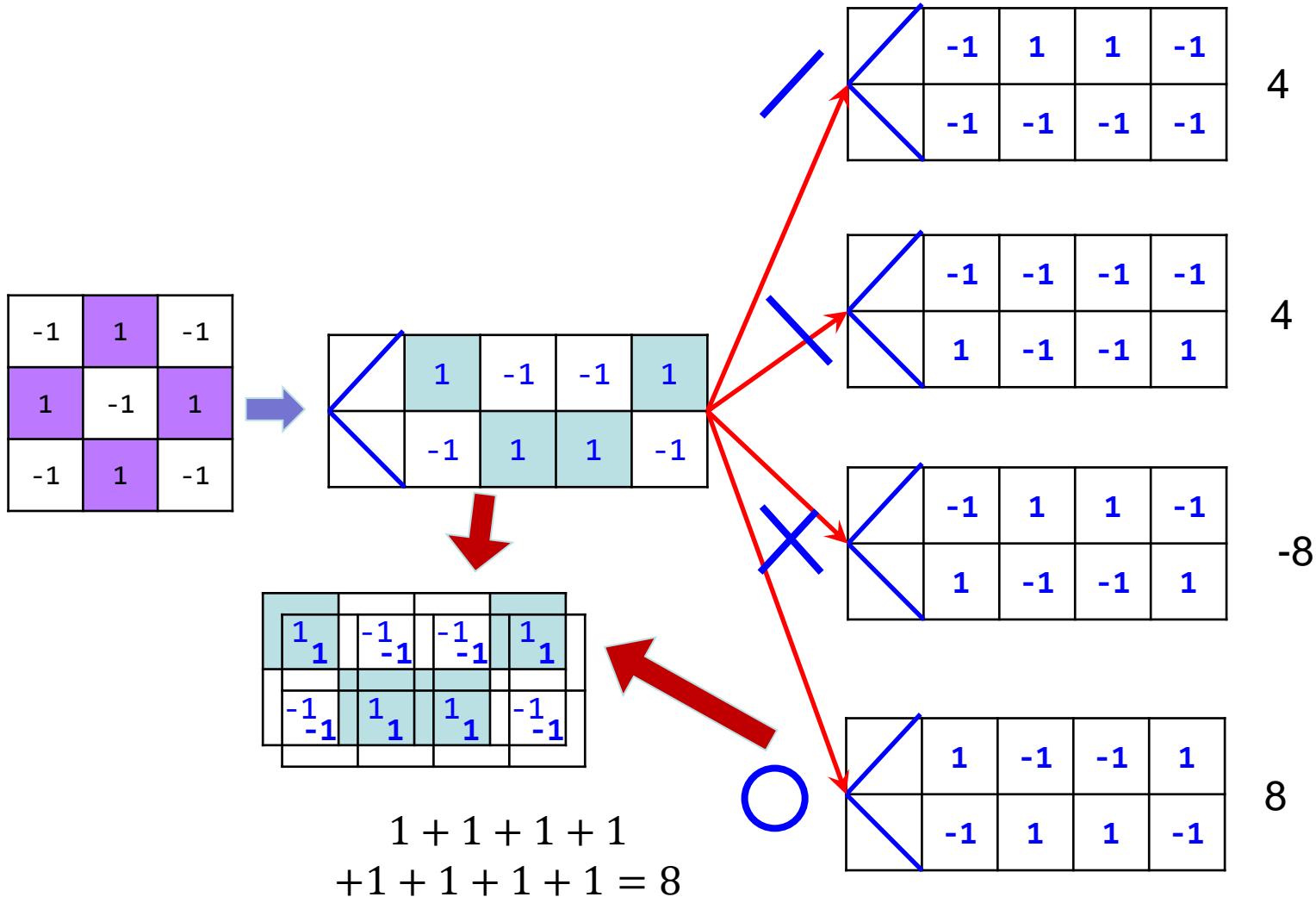


	1	-1	-1	1
	-1	1	1	-1

Use filters to score images



Use filters to score images



As an exercise...

-1	-1	1
-1	1	-1
1	-1	-1



		-1	1	1	-1
		-1	-1	-1	-1

1	-1	-1
-1	1	-1
-1	-1	1



	-1	-1	-1	-1
	1	-1	-1	1

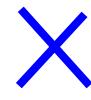
?

		-1	1	1	-1
		-1	-1	-1	-1

?

	-1	-1	-1	-1
	1	-1	-1	1

?



	-1	1	1	-1
	1	-1	-1	1

?



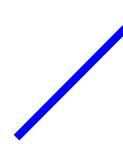
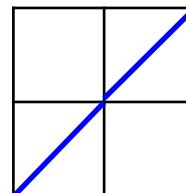
	1	-1	-1	1
	-1	1	1	-1

A slightly complex example

-1	-1	1
-1	1	-1
1	-1	-1



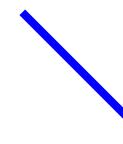
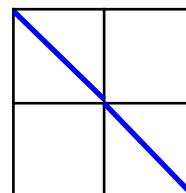
Feature Map



1	-1	-1
-1	1	-1
-1	-1	1



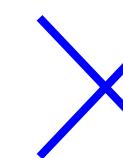
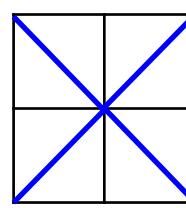
Convolution Layer



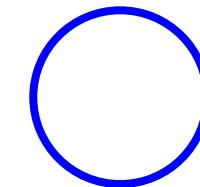
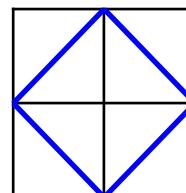
1	-1	1
-1	1	-1
1	-1	1



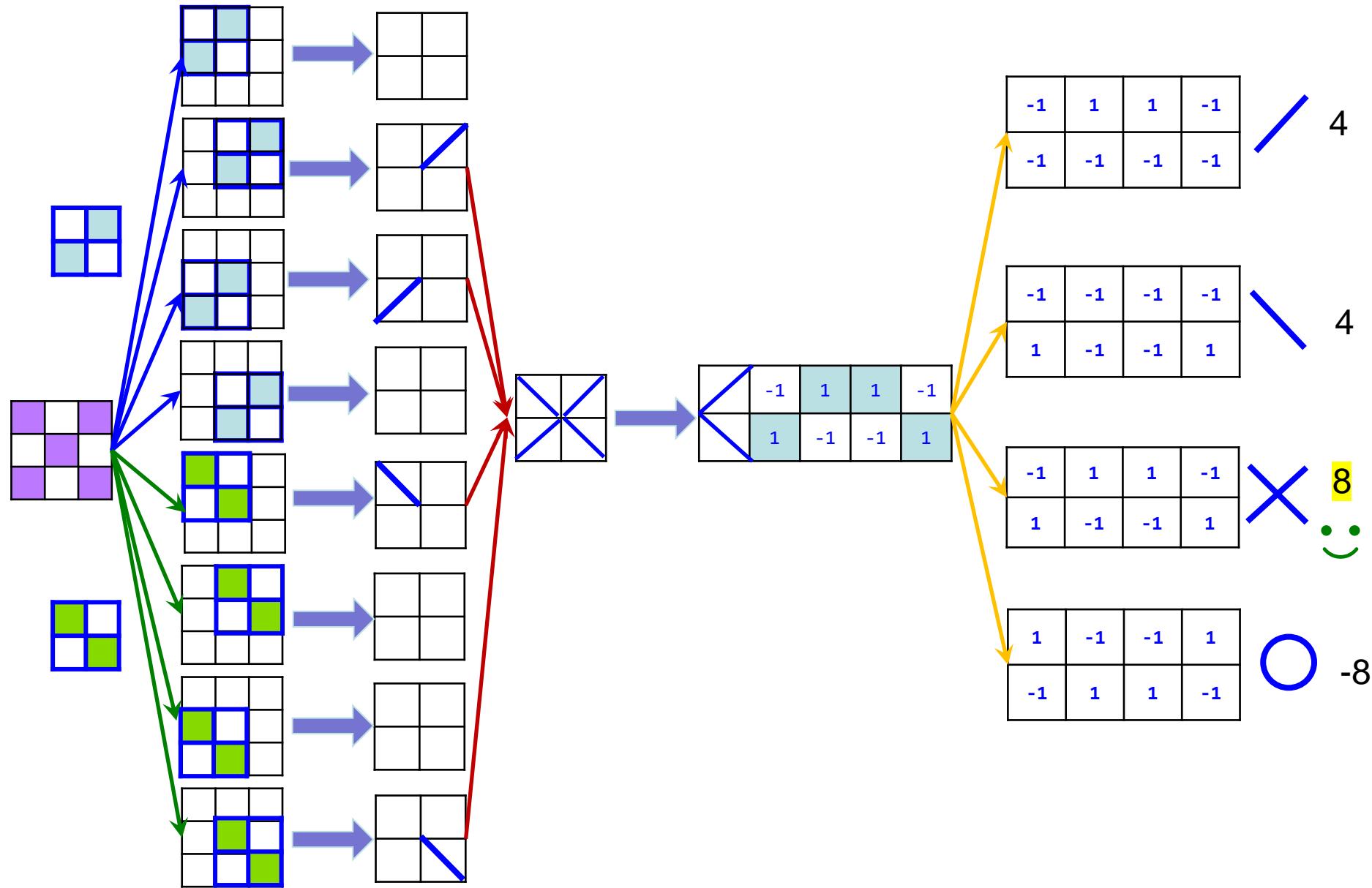
+
Pooling Layer



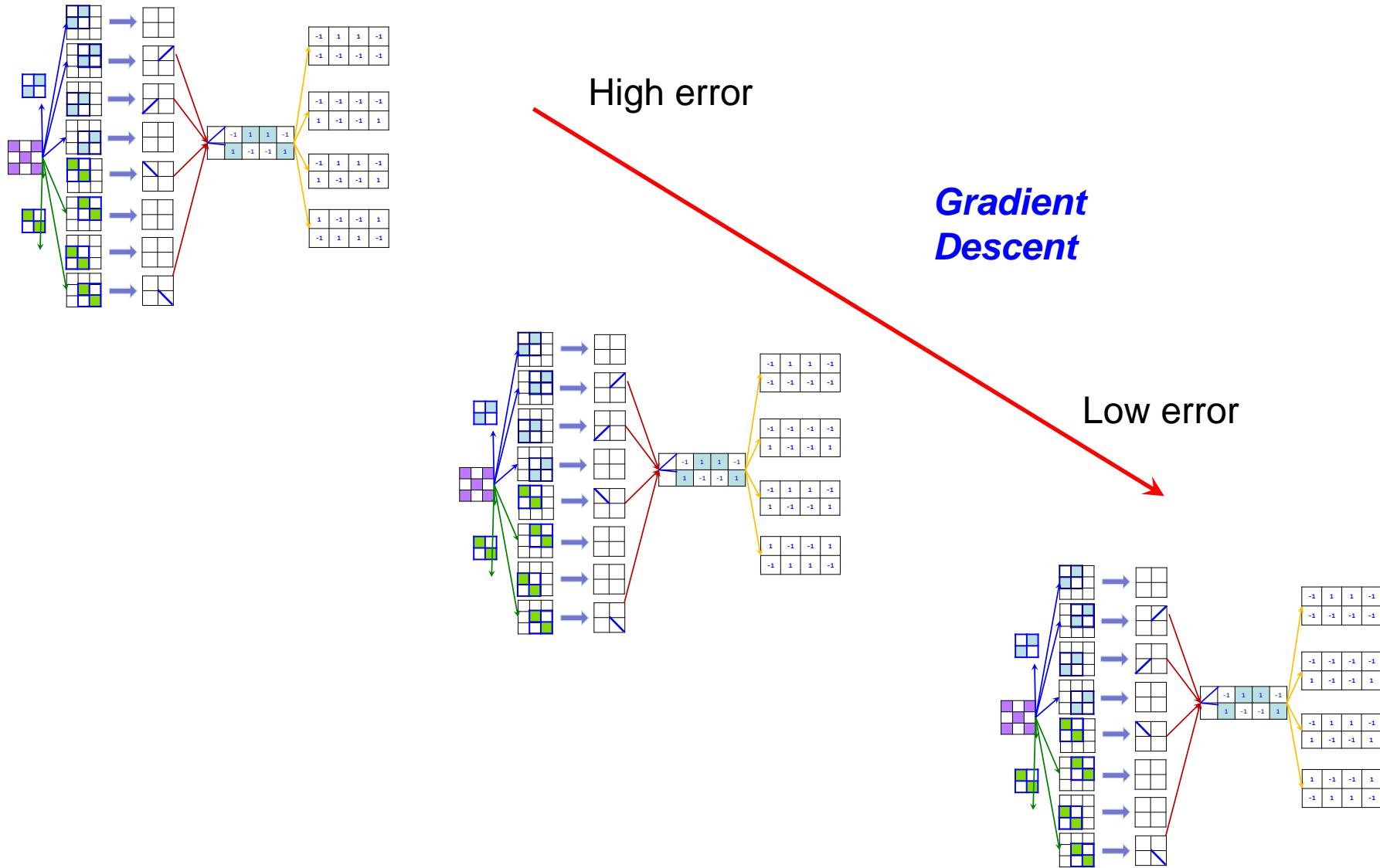
-1	1	-1
1	-1	1
-1	1	-1



A review of the process



How do we obtain filters?



Let's go back to real world!



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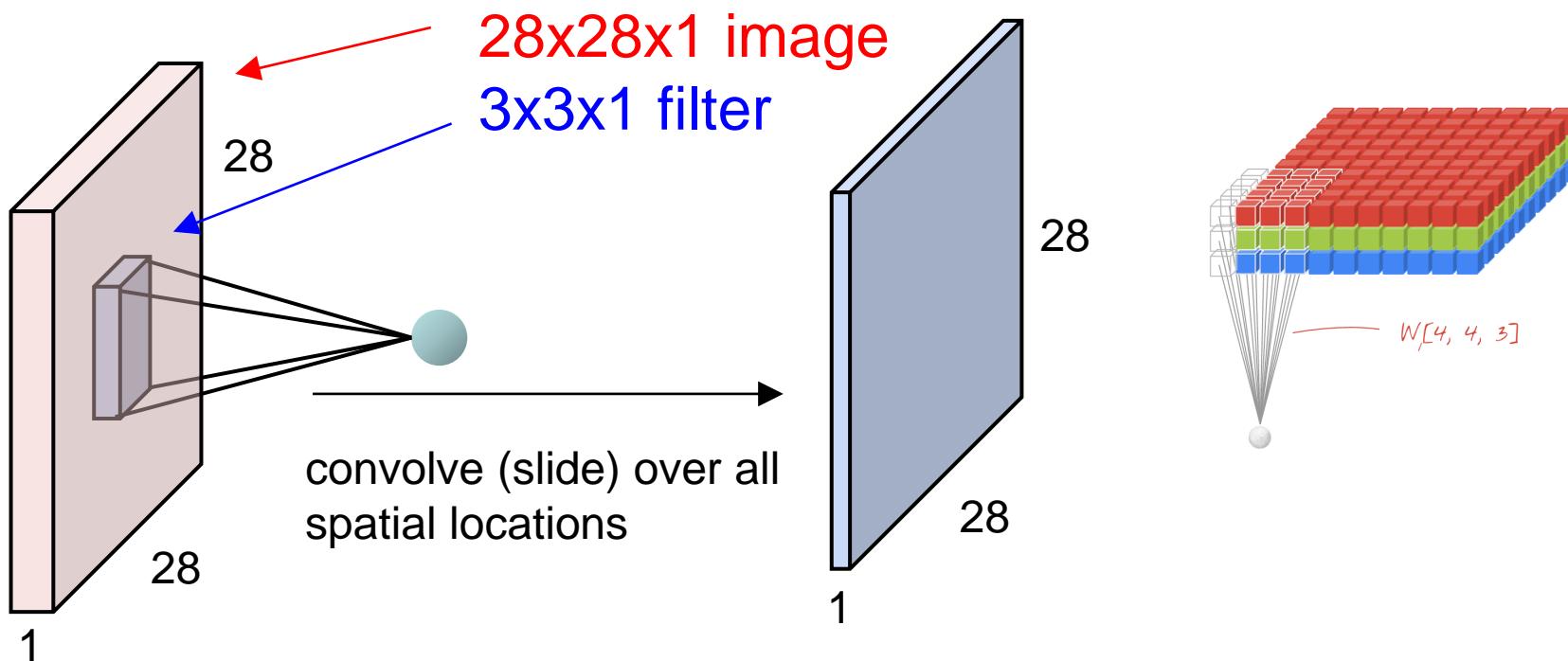


[This image by sare bear is licensed under CC-BY 2.0](#)



[This image by Tom Thai is licensed under CC-BY 2.0](#)

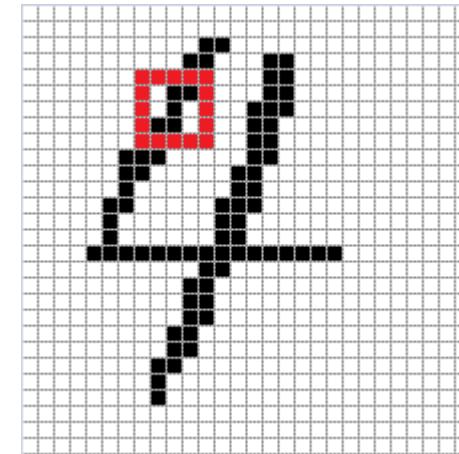
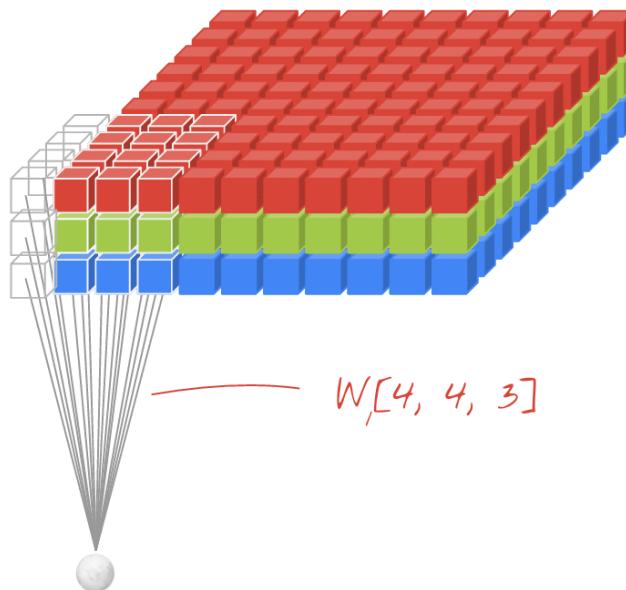
How Does CNN Work?



- By sliding the patch of weights (filter) across the image in both directions (a convolution) you obtain as many output values as there were pixels in the image (some padding is necessary at the edges).

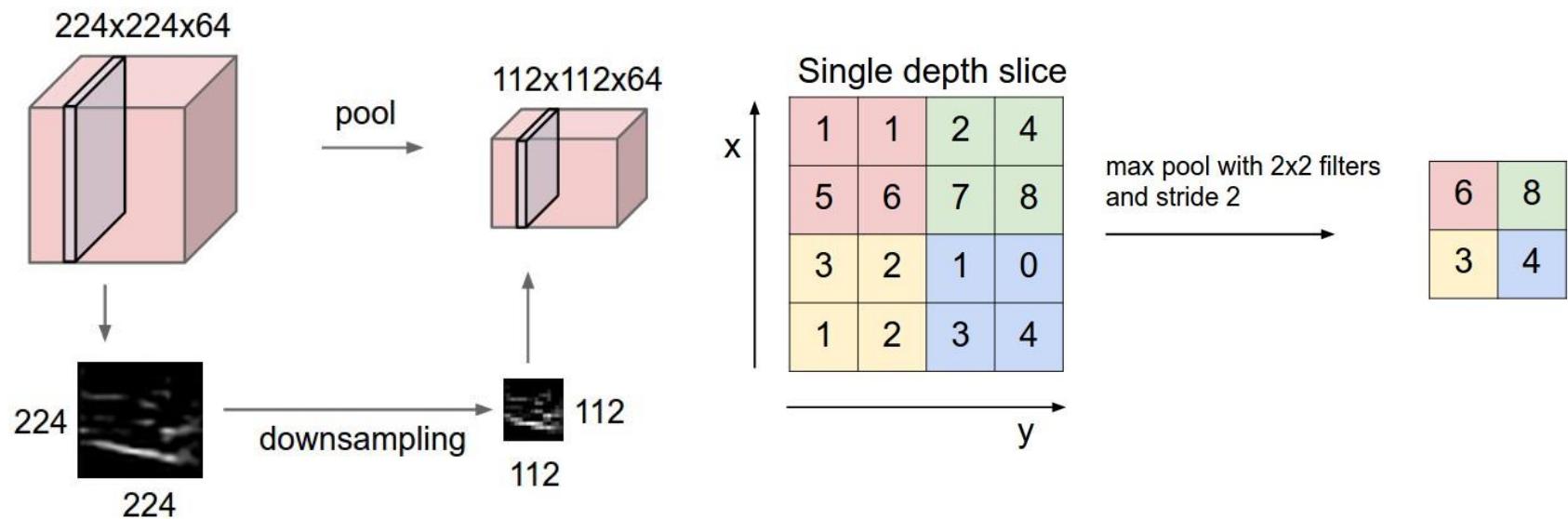
Three basic ideas about CNN

- Local receptive fields
- Shared weights and biases:
- Pooling



Pooling Layer

- Convolutional neural networks also contain pooling layers. Pooling layers are usually used immediately after convolutional layers.
- What the pooling layers do is simplify the information in the output from the convolutional layer.
- We can think of max-pooling as a way for the network to ask whether a given feature is found anywhere in a region of the image. It then throws away the exact positional information.



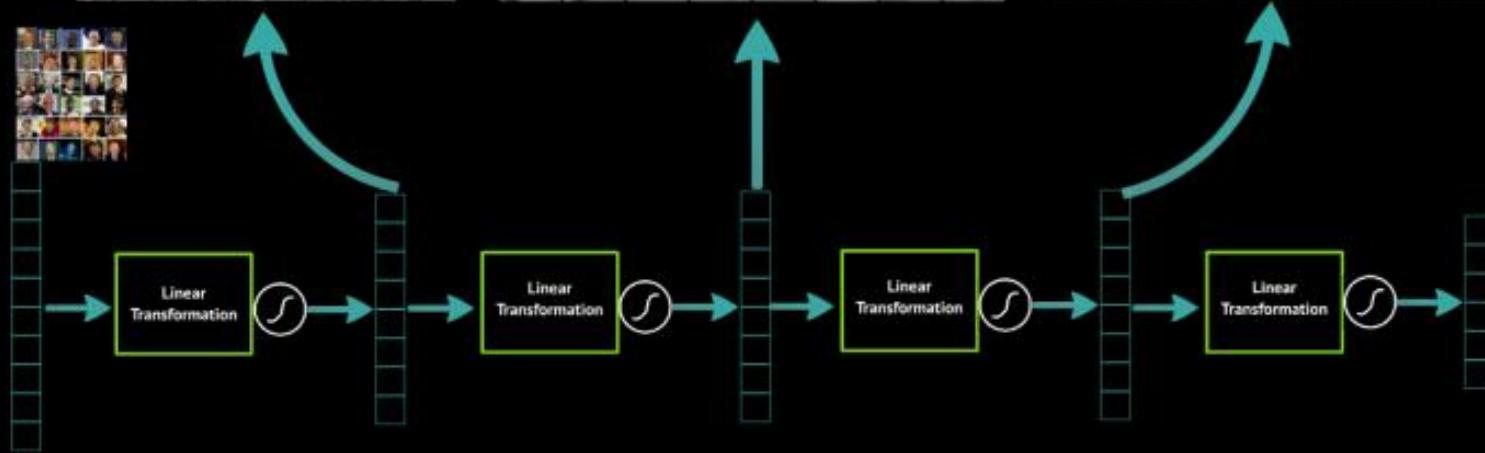
Feature Maps



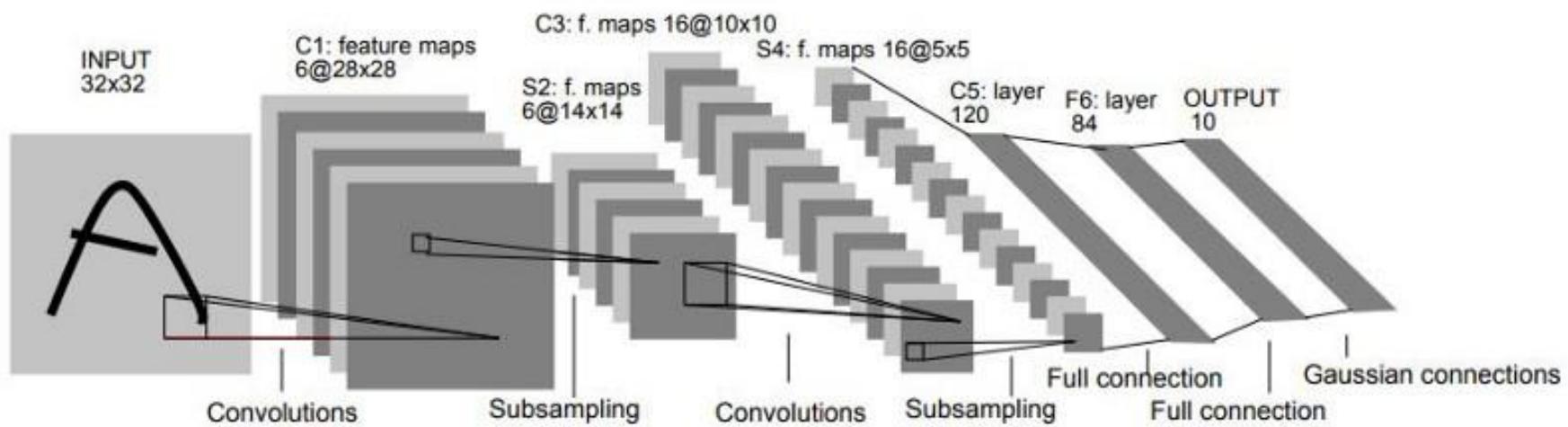
Source: https://medium.com/@chriskevin_80184/feature-maps-ee8e11a71f9e

Deep learning learns layers of features

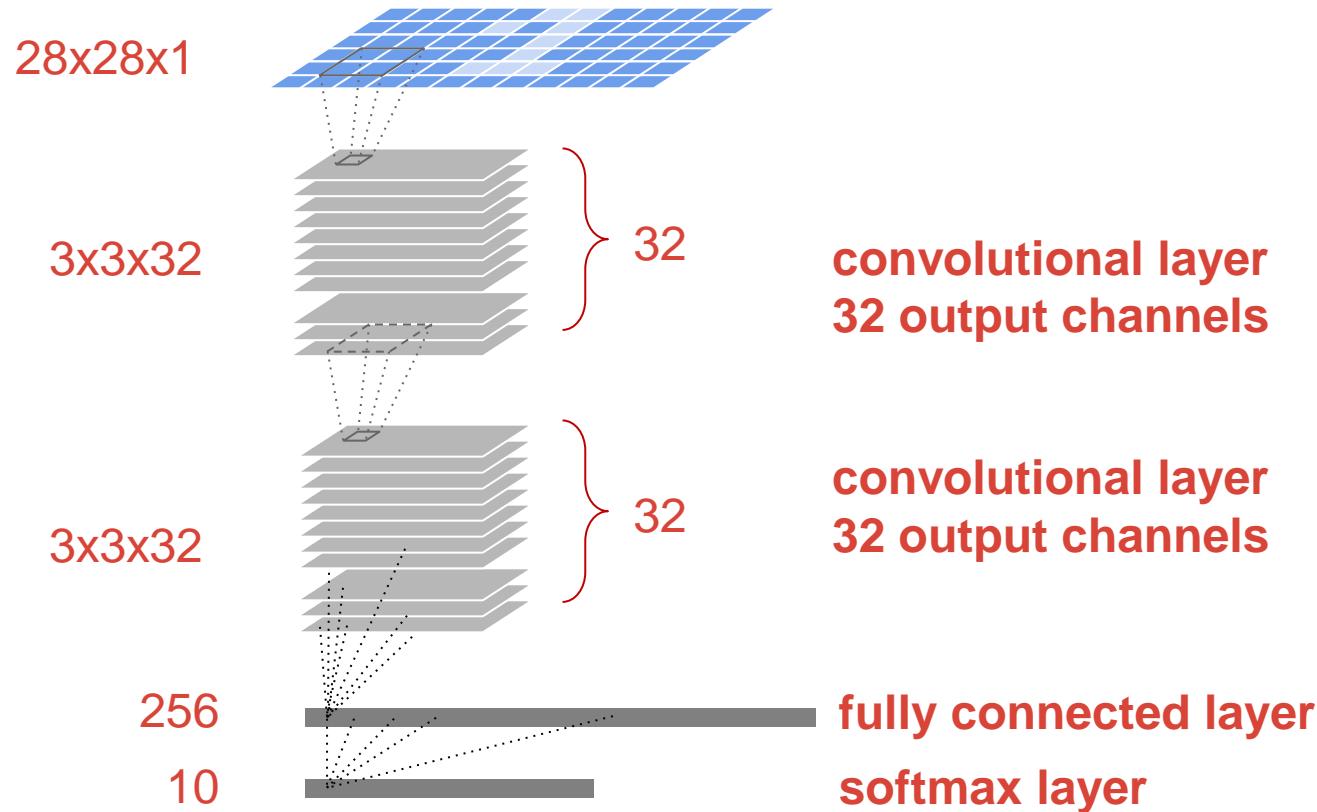
Deep Learning learns layers of features



A classical CNN example: LeNet (LeCun et al., 1998)



Convolutional Network With Fully Connected Layers

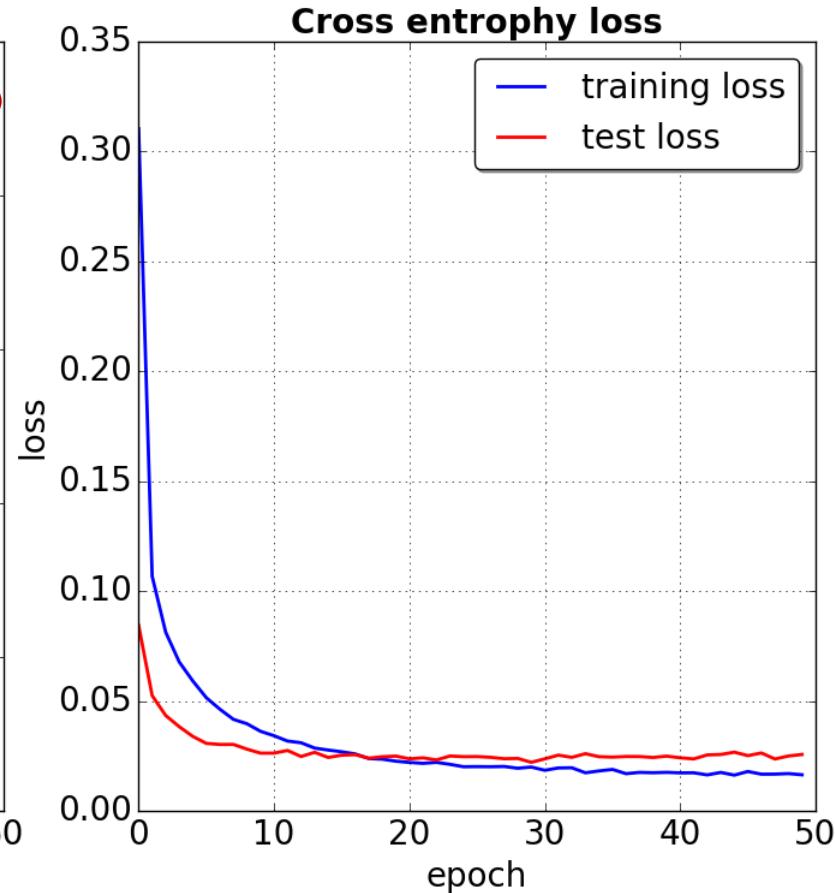
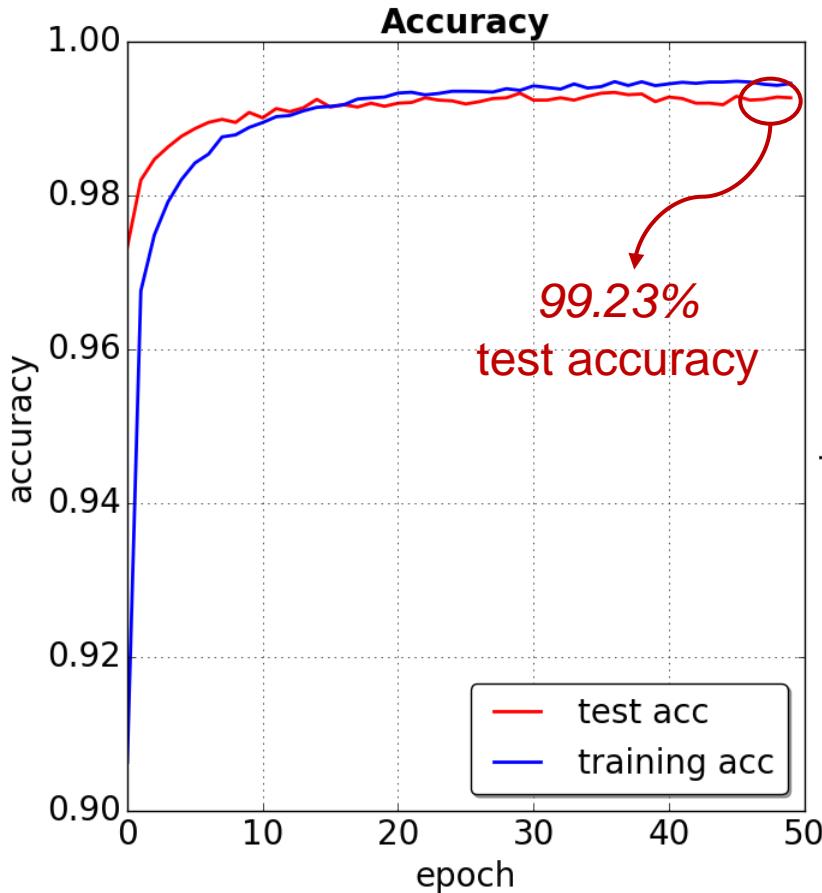


Stacking And Chaining Convolutional Layers in Keras

```
model = Sequential()  
# Adding the convolution layers  
model.add(Convolution2D(nb_filters, kernel_size[0], kernel_size[1],  
                      border_mode='valid',  
                      input_shape=input_shape))  
model.add(Activation('relu'))  
model.add(Convolution2D(nb_filters, kernel_size[0], kernel_size[1]))  
model.add(Activation('relu'))  
model.add(MaxPooling2D(pool_size=pool_size))  
model.add(Dropout(0.25))  
# Fully connected layers  
model.add(Flatten())  
model.add(Dense(256,activation='relu'))  
model.add(Dropout(0.25))  
model.add(Dense(nb_classes,activation('softmax')))  
model.compile(loss='categorical_crossentropy', optimizer='adadelta',  
              metrics=['accuracy'])  
  
h = model.fit(X_train, Y_train, batch_size=batch_size, nb_epoch=nb_epoch,  
               verbose=1, callbacks=[history], validation_data=(X_test, Y_test))
```

Challenging The 99% Testing Accuracy

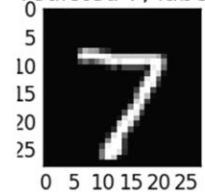
- By using the convolution layer and the fully connected layers, we reach a test accuracy of 99.23%



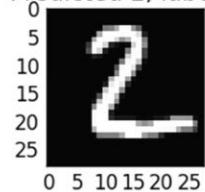
Review The Classified Results of CNN

Correctly classified

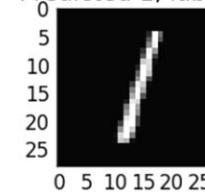
Predicted 7, label 7



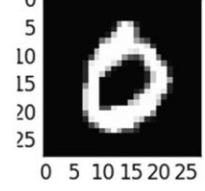
Predicted 2, label 2



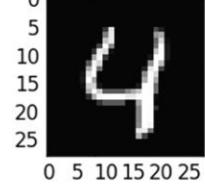
Predicted 1, label 1



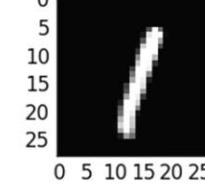
Predicted 0, label 0



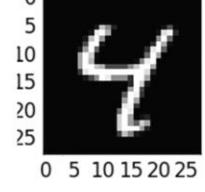
Predicted 4, label 4



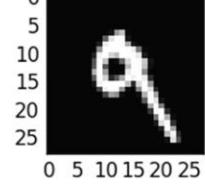
Predicted 1, label 1



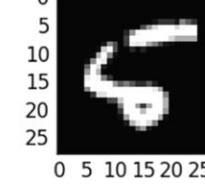
Predicted 4, label 4



Predicted 9, label 9

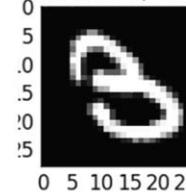


Predicted 5, label 5

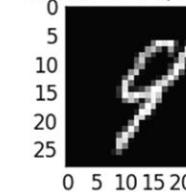


Incorrectly classified

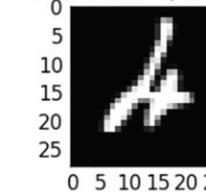
Predicted 5, label 3



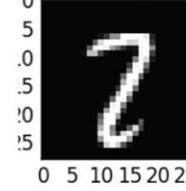
Predicted 4, label 9



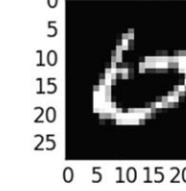
Predicted 6, label 4



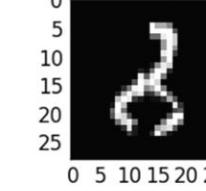
Predicted 7, label 2



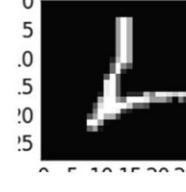
Predicted 0, label 6



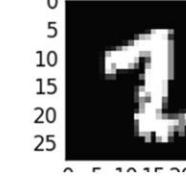
Predicted 2, label 8



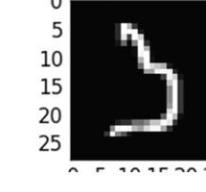
Predicted 6, label 2



Predicted 1, label 2

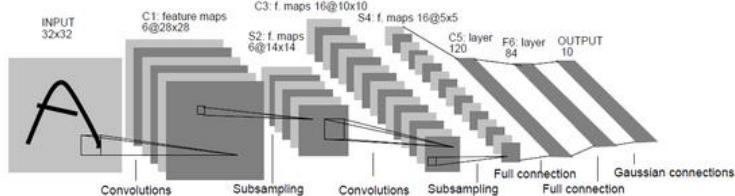


Predicted 5, label 3

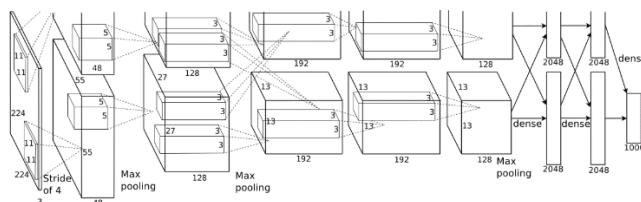


Examples of Convolution NN

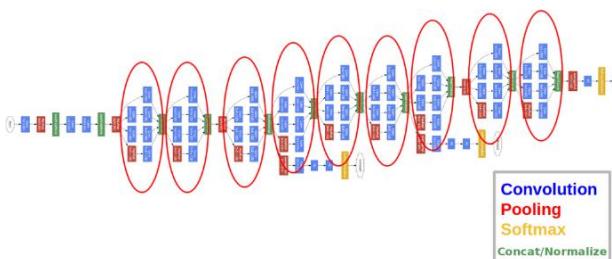
➤ LeNet (1998)



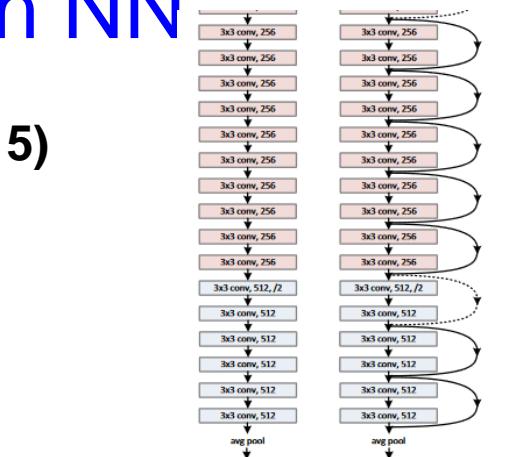
➤ AlexNet (2012)



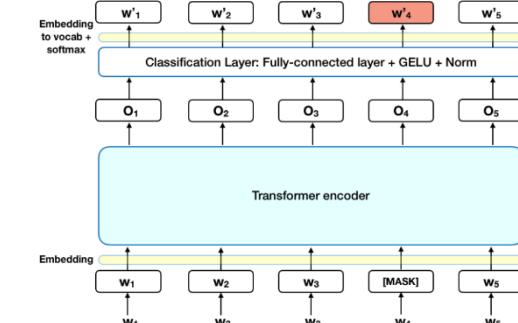
➤ GoogleLeNet (2014)



➤ ResNet (2015)



➤ Bert (2018)



➤ Transformer (2017)

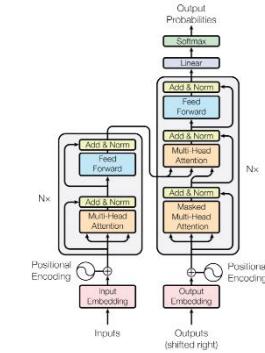


Figure 1: The Transformer - model architecture.

Machine Learning Courses List

- **Machine Learning in Coursera**
<https://www.coursera.org/learn/machine-learning>
- **Learning from Data (Caltech)**
<https://work.caltech.edu/telecourse.html>
- **Convolutional Neural Networks for Visual Recognition**
<http://cs231n.github.io/>
- **Deep Learning for Natural Language Processing**
<https://cs224d.stanford.edu/>
- **Dive into Deep Learning**
<http://d2l.ai/index.html>

Problems

1. Try to complete the gradient descent exercise in Colab notebook:
https://github.com/lsuhpc/help/lbrnloniworkshop2022/blob/main/day5-6/gradient_descent_y_fx.ipynb, if your answer is correct, you should be able to reproduce the animation in slide 17.
2. Play with the fully connected 5-layer neural network
https://github.com/lsuhpc/help/lbrnloniworkshop2022/blob/main/day5-6/2022_keras_mnist_v2_5layer_fc.ipynb, try different number of neurons/layers/activation functions, what do you see?
3. Try to build a LeNet to classify MNIST using this jupyter notebook
https://github.com/lsuhpc/help/lbrnloniworkshop2022/blob/main/day5-6/2022_keras_mnist_v5_cnn_lenet.ipynb as a starting point, you can refer to below link as a reference:
<https://medium.com/@mgazar/lenet-5-in-9-lines-of-code-using-keras-ac99294c8086>
4. Think about a workflow (just a workflow) to solve the problem in slide page 7, how to recognize handwritten characters and cat faces?