## 作业1

Problem Set 9.1

3, (a) 
$$|z| = \sqrt{|z|^2 + 8^2} = 10$$
.  $z = 10(\frac{3}{5} - \frac{4}{5}i) = 10e^{i\theta}$ 

$$|z| = |z| = |z| = \frac{6+8i}{6-8i} = \frac{6+8i}{(6+8i)(6-8i)} = \frac{6+8i}{3b+64} = \frac{1}{100} \cdot |z| \cdot \frac{3}{5} + \frac{4}{5}i)$$

$$= \frac{1}{10}e^{7(-0)}$$

(d) 
$$z = (6+8i)^2 = (10 e^{i(-0)})(10 e^{i(-0)}) = 100 e^{i(20)}$$

## 10、 至十豆 为实数 is always !!!我这就去改好! 2-2为0或纯虚数

Z×至= (a+bi)(a-bi)= a+b2、又22+0, 12×至为正实数

$$\frac{Z}{\overline{Z}} = \frac{Z^{1}Z}{Z^{2}} = \frac{(a+bi)^{2}}{a^{2}+b^{2}} = \frac{1}{a^{2}+b^{2}} (a^{2}-b^{2}+2abi)$$

$$\frac{2}{|z|} = \frac{1}{a^2 + b^2} \sqrt{(a^2 + b^2)^2 + 4a^2b^2} = \frac{1}{a^2 + b^2} \sqrt{a^4 + b^4 + 2a^2b^2}$$

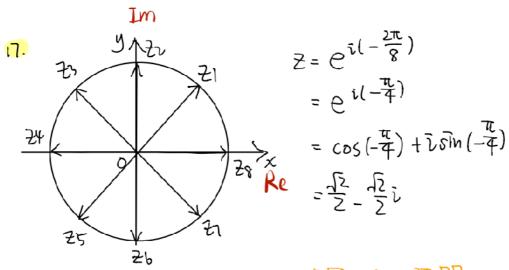
$$= \frac{1}{a^2 + b^2} \cdot a^2 + b^2 = 1$$

事方: $(e^{i2\theta})^2 = e^{i4\theta} = \cos 4\theta + i\sin 4\theta$ .

(d) 
$$5-5\hat{i}=512\left(\frac{12}{2}-\frac{12}{2}\hat{i}\right)=512e^{\hat{i}(-\frac{\pi}{4})}$$

平方= 
$$(556e^{7(-4)})^2 = 50.e^{7(-\frac{\pi}{2})} = 50(-i) = -50i$$

## 复于面貌似罗写上Re与Im的!



$$(Y1 = 1 = 2^8 = 1)$$
 解 = 几何上将图 8分 而证明:  $2^8 = 1 = e^{2\pi k \hat{i}}$  》  $2 = e^{\frac{2\pi k \hat{i}}{8}}/(ke^2)$ 

19. 
$$\cos 3\theta + i \sin 3\theta = e^{3i\theta} = (e^{i\theta})^3 = (\cos \theta + i \sin \theta)^3$$
 $= \cos^3 \theta - i \sin^3 \theta + 3 \cos^2 \theta i \sin \theta - 3 \cos \theta \sin^2 \theta$ .
 $= (\cos^3 \theta - 3 \cos \theta \sin^2 \theta) + i (-\sin^3 \theta + 3 \cos^2 \theta \sin^2 \theta)$ .
 $= \cot^3 \theta + 3 \cos \theta \sin^2 \theta$ .
 $= \cot^3 \theta + 3 \cos^3 \theta \sin^3 \theta + 3 \cos^3 \theta \sin^3 \theta$ .
 $= \cot^3 \theta + 3 \cos^3 \theta \cos$ 

