CPSC 319 Tutorial 02
Finding Asymptotic Complexity: Exercises

Longsheng Zhou

Department of Computer Science
University of Calgary

January 25, 2015

8. Find the complexity of the function used to find the *k*th smallest integer in an unordered array of integers

```
int selectkth(int a[], int k, int n) {
    int i, j, mini, tmp;
    for (i = 0; i < k; i++) {
        mini = i;
        for (j = i+1; j < n; j++)
            if (a[j]<a[mini])
                mini = j;
        tmp = a[i];
        a[i] = a[mini];
        a[mini] = tmp;
    }
    return a[k-1];
}
```

9. Determine the complexity of the following implementations of the algorithms for adding, multiplying, and transposing $n \times n$ matrices:

```
for (i = 0; i < n; i++)
    for (j = 0; j < n; j++)
        a[i][j] = b[i][j] + c[i][j];

for (i = 0; i < n; i++)
    for (j = 0; j < n; j++)
        for (k = a[i][j] = 0; k < n; k++)
            a[i][j] += b[i][k] * c[k][j];

for (i = 0; i < n - 1; i++)
    for (j = i+1; j < n; j++) {
        tmp = a[i][j];
        a[i][j] = a[j][i];
        a[j][i] = tmp;
    }
```

10. Find the computational complexity for the following four loops:

a.
```
for (cnt1 = 0, i = 1; i <= n; i++)
    for (j = 1; j <= n; j++)
        cnt1++;
```

b.
```
for (cnt2 = 0, i = 1; i <= n; i++)
    for (j = 1; j <= i; j++)
        cnt2++;
```

c.
```
for (cnt3 = 0, i = 1; i <= n; i *= 2)
    for (j = 1; j <= n; j++)
        cnt3++;
```

d.
```
for (cnt4 = 0, i = 1; i <= n; i *= 2)
    for (j = 1; j <= i; j++)
        cnt4++;
```

Thank you!

AUTHOR: Longsheng Zhou
ADDRESS: ICT 609e
Department of Computer Science
University of Calgary
EMAIL: lozhou@ucalgary.ca