This print-out should have 30 questions. Multiple-choice questions may continue on the next column or page - find all choices

001 10.0 points

Find y' when

$$xy + 5x + 4x^2 = 5$$
.

1.
$$y' = \frac{5 + 4x - y}{x}$$

2.
$$y' = \frac{y+5+4x}{x}$$

3.
$$y' = -(y+5+8x)$$

4.
$$y' = -\frac{y+5+4x}{x}$$

5.
$$y' = \frac{y+5+8x}{x}$$

6.
$$y' = -\frac{y+5+8x}{x}$$
 correct

Explanation:

Differentiating implicitly with respect to x

$$\frac{d}{dx}\left(xy+5x+4x^2\right) \; = \; \frac{d}{dx}\left(5\right) \; .$$

Thus

$$(xy'+y) + 5 + 8x = 0,$$

and so

$$xy' = -y - 5 - 8x.$$

Consequently,

$$y' = -\frac{y+5+8x}{x} \ .$$

002 10.0 points

Find dy/dx when

$$2x^2 + 3y^2 = 4.$$

1.
$$\frac{dy}{dx} = 3xy$$

2.
$$\frac{dy}{dx} = -\frac{2x}{x^2}$$

3.
$$\frac{dy}{dx} = \frac{x}{3x}$$

4.
$$\frac{dy}{dx} = -\frac{2x}{3y}$$
 correct

$$5. \ \frac{dy}{dx} = \frac{2x}{3y}$$

6.
$$\frac{dy}{dx} = -2xy$$

Explanation: Diferentiating

$$2x^2 + 3y^2 = 4$$

implicitly with respect to x we see that

$$4x + 6y \frac{dy}{dx} = 0.$$

Consequently,

$$\frac{dy}{dx} = -\frac{4x}{6y} = -\frac{2x}{3y}$$

10.0 points

Find $\frac{dy}{dx}$ when

$$\frac{3}{\sqrt{x}} + \frac{4}{\sqrt{y}} = 5.$$

1.
$$\frac{dy}{dx} = -\frac{4}{3} \left(\frac{x}{y}\right)^{3/2}$$

2.
$$\frac{dy}{dx} = \frac{3}{4}(xy)^{1/2}$$

$$3. \ \frac{dy}{dx} = \frac{4}{3} \left(\frac{x}{y}\right)^{3/2}$$

4.
$$\frac{dy}{dx} = \frac{4}{3}(xy)^{1/2}$$

5.
$$\frac{dy}{dx} = -\frac{3}{4} \left(\frac{y}{x}\right)^{3/2}$$
 correct

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If y = y(x) is defined implicitly by

$$3y^2 + xy - 2 = 0$$
,

find the value of dy/dx at the point (1, -1).

1.
$$\frac{dy}{dx}\Big|_{(1,-1)} = -\frac{1}{5}$$
 correct

2.
$$\frac{dy}{dx}\Big|_{(1,-1)} = \frac{2}{5}$$

3.
$$\frac{dy}{dx}\Big|_{(1,-1)} = -\frac{3}{5}$$

4.
$$\frac{dy}{dx}\Big|_{(1,-1)} = \frac{1}{5}$$

5.
$$\frac{dy}{dx}\Big|_{(1,-1)} = -\frac{2}{5}$$

6.
$$\frac{dy}{dx}\Big|_{(1,-1)} = \frac{3}{5}$$

Explanation:

Differentiating implicitly with respect to xwe see that

$$6y\frac{dy}{dx} + y + x\frac{dy}{dx} = 0,$$

$$\frac{dy}{dx} = -\frac{y}{6y + x}$$

At (1, -1), therefore,

$$\left. \frac{dy}{dx} \right|_{(1,-1)} = -\frac{1}{5}$$

10.0 points

Find
$$\frac{dy}{dx}$$
 when

$$2x^2 - xy + y^2 = 0.$$

$$\mathbf{1.} \ \frac{dy}{dx} \ = \ \frac{2y+x}{y-x}$$

$$2. \ \frac{dy}{dx} = \frac{2y - x}{y + x}$$

$$3. \frac{dy}{dx} = \frac{4x + y}{x - 2y}$$

5.
$$\frac{dy}{dx} = \frac{4x - y}{x - 2y}$$
 correct

$$6. \frac{dy}{dx} = \frac{4x - y}{x + 2y}$$

Explanation:

$$2x^2 - xy + y^2 = 0$$

implicitly we see that

$$4x - (xy' + y) + 2yy' = 0.$$

Thus

$$(4x - y) - y'(x - 2y) = 0.$$

Consequently,

$$\frac{dy}{dx} = \frac{4x - y}{x - 2y}$$

Find
$$\frac{dy}{dx}$$
 when

$$tan(xy) = 2x + y$$
.

1.
$$\frac{dy}{dx} = \frac{1 - x \sec^2(xy)}{y \sec^2(xy) + 2}$$

2.
$$\frac{dy}{dx} = \frac{1 - x \sec^2(xy)}{y \sec^2(xy) - 2}$$

3.
$$\frac{dy}{dx} = \frac{2 - y \sec^2(xy)}{x \sec^2(xy) + 1}$$

4.
$$\frac{dy}{dx} = \frac{2 - y \sec^2(xy)}{x \sec^2(xy) - 1}$$
 correct

$$5. \frac{dy}{dx} = \frac{2 + y \sec^2(xy)}{x \sec^2(xy) - 1}$$

6.
$$\frac{dy}{dx} = \frac{1 + x \sec^2(xy)}{y \sec^2(xy) + 2}$$

6.
$$\frac{dy}{dx} = \frac{3}{4} \left(\frac{y}{x} \right)^{3/2}$$

Explanation: Differentiating implicitly with respect to x,

$$-\frac{1}{2} \Big(\frac{3}{x\sqrt{x}} + \frac{4}{y\sqrt{y}} \frac{dy}{dx} \Big) \ = \ 0 \ .$$

Consequently,

$$\frac{dy}{dx} = -\frac{3}{4} \left(\frac{y}{x}\right)^{3/2}$$

004 10.0 points

Find $\frac{dy}{dx}$ when

$$3\sqrt{x} + 2\sqrt{y} = 4.$$

$$1. \ \frac{dy}{dx} = 3 + \frac{4}{\sqrt{x}}$$

2.
$$\frac{dy}{dx} = -\frac{3}{2} \left(3 - \frac{4}{\sqrt{x}} \right)$$

$$3. \frac{dy}{dx} = -\frac{3}{2} \left(4 - \frac{3}{\sqrt{x}} \right)$$

4.
$$\frac{dy}{dx} = -\frac{3}{4} \left(\frac{4 - 3\sqrt{x}}{\sqrt{x}} \right)$$
 correct
5.
$$\frac{dy}{dx} = 4 - \frac{3}{\sqrt{x}}$$

6.
$$\frac{dy}{dx} = \frac{3}{4} \left(4 + \frac{3}{\sqrt{x}} \right)$$

Explanation:

Differentiating implicitly with respect to x

$$\frac{1}{2} \Big(\frac{3}{\sqrt{x}} + \frac{2}{\sqrt{y}} \frac{dy}{dx} \Big) \ = \ 0 \ .$$

Thus

$$\frac{dy}{dx} = -\frac{3}{2} \left(\frac{\sqrt{y}}{\sqrt{x}} \right)$$

$$\sqrt{y} = \frac{4-3\sqrt{x}}{2}$$

$$\frac{dy}{dx} = -\frac{3}{4} \left(\frac{4 - 3\sqrt{x}}{\sqrt{x}} \right)$$

In this case, we can also begin by solving for y, using the Chain Rule, and simplifying

$$y = \left(\frac{4-3\sqrt{x}}{2}\right)^2$$

$$\frac{dy}{dx} = 2\left(\frac{4-3\sqrt{x}}{2}\right)\left(\frac{-3}{2\cdot2\sqrt{x}}\right)$$

005 10.0 points

If y is defined implicitly by

$$y^2 - xy - 12 = 0,$$

find the value of dy/dx at (4, 6)

1.
$$\frac{dy}{dx}\Big|_{(4,6)} = \frac{3}{4}$$
 correct

2.
$$\frac{dy}{dx}\Big|_{(4,6)} = \frac{7}{8}$$

3.
$$\frac{dy}{dx}\Big|_{(4,6)} = -\frac{3}{4}$$

4.
$$\frac{dy}{dx}\Big|_{(4,6)} = \frac{2}{3}$$

5.
$$\frac{dy}{dx}\Big|_{(4,6)} = -\frac{7}{8}$$

Differentiating implicitly with respect to x

$$2y\frac{dy}{dx} - y - x\frac{dy}{dx} = 0.$$

$$\frac{dy}{dx} = \frac{y}{2y - x}.$$

At (4, 6), therefore

$$\left. \frac{dy}{dx} \right|_{(4,6)} = \frac{3}{4}$$

006 10.0 points

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Explanation:

. Differentiating implicitly with respect to $\boldsymbol{x},$

$$\sec^2(xy)\left(y + x\frac{dy}{dx}\right) = 2 + \frac{dy}{dx}.$$

After rearranging, this becomes

$$\frac{dy}{dx} \left(x \sec^2(xy) - 1 \right) = 2 - y \sec^2(xy).$$

Consequently,

$$\frac{dy}{dx} = \frac{2 - y \sec^2(xy)}{x \sec^2(xy) - 1}$$

keywords:

009 10.0 points

Determine dy/dx when

$$5\cos x\sin y = 1.$$

1.
$$\frac{dy}{dx} = \tan x \tan y$$
 correct

2.
$$\frac{dy}{dx} = \tan x$$

3.
$$\frac{dy}{dx} = \cot x \tan y$$

$$4. \frac{dy}{dx} = \tan xy$$

5. $\frac{dy}{dx} = \cot x \cot y$

Explanation: Differentiating implicitly with respect to x

$$5\left\{\cos x\cos y\frac{dy}{dx} - \sin y\sin x\right\} = 0.$$

$$\frac{dy}{dx}\cos x\cos y \ = \ \sin x\sin y \, .$$

Consequently.

$$\frac{dy}{dx} = \frac{\sin x \sin y}{\cos x \cos y} = \tan x \tan y$$

010 10.0 points

Determine dy/dx when

$$y \cos(x^2) = 5.$$

1.
$$\frac{dy}{dx} = -2xy \cot(x^2)$$
2.
$$\frac{dy}{dx} = 2xy \cot(x^2)$$

3.
$$\frac{dy}{dx} = 2xy \cos(x^2)$$

$$4. \ \frac{dy}{dx} = -2xy \tan(x^2)$$

5.
$$\frac{dy}{dx} = 2xy \tan(x^2)$$
 correct
6. $\frac{dy}{dx} = -2xy \sin(x^2)$

Explanation: After implicit differentiation with respect

$$-2xy \sin(x^2) + y' \cos(x^2) = 0.$$

Consequently,

$$\frac{dy}{dx} = \frac{2xy\,\sin(x^2)}{\cos(x^2)} = 2xy\,\tan(x^2)$$

011 10.0 points

Find the equation of the tangent line to the

$$3y^2 - xy - 8 = 0,$$

1.
$$5y = 2x$$

at the point P = (10, 4).

2.
$$7y + 2x = 8$$

3.
$$7y = 2x + 8$$
 correct

 $y^2 = 10x^4 - x^2$

 $2yy' = 10(4x^3) - 2x$

014 10.0 points

 $f(x) = 5 \arcsin \left(\frac{x}{2}\right)$

Determine the derivative of

1. $f'(x) = \frac{15}{\sqrt{9-x^2}}$

2. $f'(x) = \frac{3}{\sqrt{9-x^2}}$

3. $f'(x) = \frac{5}{\sqrt{1-x^2}}$

4. $f'(x) = \frac{3}{\sqrt{1-x^2}}$

6. $f'(x) = \frac{15}{\sqrt{1-r^2}}$

Explanation: Use of

5. $f'(x) = \frac{5}{\sqrt{9-x^2}}$ correct

 $y' = \frac{20x^3 - x}{y}$

So at the point (1,3) we have

5.
$$13y + 4x = 12$$

Explanation:

Differentiating implicitly with respect to x

$$6y\frac{dy}{dx} - y - x\frac{dy}{dx} \ = \ 0,$$

$$\frac{dy}{dx} = \frac{y}{6y - x}$$

At P = (10, 4), therefore,

$$\frac{dy}{dx}\Big|_P = \frac{2}{7}.$$

Thus by the point slope formula, the equation of the tangent line at P is given by

$$y-4 = \frac{2}{7}(x-10).$$

Consequently,

$$7y = 2x + 8$$

012 10.0 points

Find an equation for the tangent line to the

$$26x^2 + 5xy + 7y^2 = 38$$

at the point (1, 1).

1.
$$y = 8x + 4$$

2.
$$y = -8x + 4$$

3.
$$y = -3x + 4$$
 correct

4.
$$y = 6x - 7$$

5.
$$y = -6x + 6$$

6.
$$y = 3x + 9$$

Differentiating implicitly, we see that

$$26x^{2} + 5xy + 7y^{2} = 38$$

$$52x + 5xy' + 5y \cdot 1 + 14yy' = 0$$

$$5xy' + 14yy' = -52x - 5y$$

$$y'(5x + 14y) = -52x - 5y$$

$$y' = \frac{-52x - 5y}{5x + 14y}$$

$$y' = \frac{-52 - 5}{5 + 14} = \frac{-57}{19} = -3$$

so an equation of the tangent line is

$$y-1=-3 (x-1)$$
$$y=-3x+4$$

keywords:

The curve with equation

$$y^2 = 10x^4 - x^2$$

is called a kampyle of Eudoxus.

Find an equation of the tangent line to this

1.
$$y = -\frac{25}{3}x + \frac{28}{3}$$

2.
$$y = \frac{25}{2}x - \frac{19}{2}$$

$$3. y = -\frac{19}{3}x - \frac{10}{3}$$

4.
$$y = \frac{25}{3}x + \frac{28}{3}$$

5.
$$y = \frac{19}{3}x - \frac{10}{3}$$
 correct

Explanation:

$$26x^{2} + 5xy + 7y^{2} = 38$$

$$52x + 5xy' + 5y \cdot 1 + 14yy' = 0$$

$$5xy' + 14yy' = -52x - 5y$$

$$y' (5x + 14y) = -52x - 5y$$

$$y' = \frac{-52x - 5y}{5x + 14y}$$

$$y' = \frac{-52 - 5}{5 + 14} = \frac{-57}{19} = -3$$

$$y = -3x + 4$$

013 10.0 points

curve at the point (1,3).

1.
$$y = -\frac{25}{3}x + \frac{28}{3}$$

2.
$$y = \frac{25}{3}x - \frac{19}{3}$$

$$3. y = -\frac{19}{3}x - \frac{10}{3}$$

4.
$$y = \frac{25}{3}x + \frac{28}{3}$$

5.
$$y = \frac{19}{3}x - \frac{10}{3}$$
 correc

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3.
$$f'(x) = \frac{1}{\sqrt{1 - e^{6x}}}$$

4.
$$f'(x) = \frac{1}{1 + e^{6x}}$$

5.
$$f'(x) = \frac{3e^{3x}}{1 + e^{6x}}$$

6.
$$f'(x) = \frac{e^{3x}}{1 + e^{6x}}$$

7.
$$f'(x) = \frac{e^{3x}}{\sqrt{1-e^{6x}}}$$

8.
$$f'(x) = \frac{3e^{3x}}{\sqrt{1-e^{6x}}}$$
 correct

Explanation:

$$\frac{d}{dx}\sin^{-1}x \; = \; \frac{1}{\sqrt{1-x^2}} \, , \quad \frac{d}{dx}e^{ax} \; = \; ae^{ax} \, ,$$

the Chain Rule ensures that

$$f'(x) = \frac{3e^{3x}}{\sqrt{1 - e^{6x}}}$$

017 10.0 points

Find the derivative of

$$f(x) = \tan^{-1}(e^{3x}).$$

1.
$$f'(x) = \frac{3e^{3x}}{\sqrt{1-e^{6x}}}$$

2.
$$f'(x) = \frac{e^{3x}}{\sqrt{1 - e^{6x}}}$$

3.
$$f'(x) = \frac{1}{1 + e^{6x}}$$

4.
$$f'(x) = \frac{3}{1 + e^{6x}}$$

5.
$$f'(x) = \frac{3}{\sqrt{1 - e^{6x}}}$$

6.
$$f'(x) = \frac{1}{\sqrt{1 - e^{6x}}}$$

7.
$$f'(x) = \frac{e^{3x}}{1 + e^{6x}}$$

8.
$$f'(x) = \frac{3e^{3x}}{1+e^{6x}}$$
 correct

Explanation:

$$\frac{d}{dx} \tan^{-1} x \; = \; \frac{1}{1+x^2} \, , \quad \frac{d}{dx} e^{ax} \; = \; a e^{ax} \, ,$$

the Chain Rule ensures that

$$f'(x) = \frac{3e^{3x}}{1 + e^{6x}}$$

018 10.0 points

Find the derivative of f when

$$f(x) = 2\sin^{-1}\frac{x}{2} - \sqrt{4 - x^2}$$

1.
$$f'(x) = \frac{x}{\sqrt{4-x^2}}$$

2.
$$f'(x) = \frac{2}{\sqrt{4-x^2}}$$

3.
$$f'(x) = \sqrt{\frac{2+x}{2-x}}$$
 correct

4.
$$f'(x) = \frac{1}{\sqrt{2-x}}$$

5.
$$f'(x) = \frac{1}{\sqrt{2+x}}$$

6.
$$f'(x) = \sqrt{\frac{2-x}{2+x}}$$

Explanation:

$$f'(x) = \frac{2}{\sqrt{4-x^2}} + \frac{x}{\sqrt{4-x^2}}$$
$$= \frac{2+x}{\sqrt{4-x^2}}.$$

On the other hand.

$$4 - x^2 = (2 - x)(2 + x)$$
.

$$f'(x) = \frac{5}{\sqrt{9-x^2}}$$

10.0 points

Find the derivative of

$$f(x) = (\sin^{-1}(3x))^2$$
.

1.
$$f'(x) = 6\cos(3x)\sin(3x)$$

2.
$$f'(x) = \frac{3}{\sqrt{1-9x^2}} \sin^{-1}(3x)$$

3.
$$f'(x) = \cos(3x)\sin(3x)$$

4.
$$f'(x) = \frac{6}{\sqrt{1-9x^2}} \sin^{-1}(3x)$$
 correct

5.
$$f'(x) = \frac{6}{\sqrt{9-x^2}} \sin^{-1}(3x)$$

6.
$$f'(x) = \frac{3}{\sqrt{9-x^2}} \sin^{-1}(3x)$$

Explanation:

The Chain Rule together with

$$\frac{d}{dx}\left(\sin^{-1}\left(ax\right)\right) = \frac{a}{\sqrt{1 - a^2x^2}}$$

$$f'(x) = \frac{6}{\sqrt{1 - 9x^2}} \sin^{-1}(3x)$$

Find the derivative of

$$f(x) = \sin^{-1}(e^{3x}).$$

1.
$$f'(x) = \frac{3}{\sqrt{1 - e^{6x}}}$$

2.
$$f'(x) = \frac{3}{1 + e^{6x}}$$

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Consequently,

$$f'(x) = \sqrt{\frac{2+x}{2-x}}$$

 $\frac{d}{dx} \arcsin(x) = \frac{1}{\sqrt{1-x^2}}$

 $f'(x) = \frac{5}{\sqrt{1 - (x/3)^2}} \left(\frac{1}{3}\right).$

together with the Chain Rule shows that

019 10.0 points

Find the derivative of f when

$$f(\theta) = \ln(\sin 3\theta)$$
.

1.
$$f'(\theta) = \frac{1}{\cos 3\theta}$$

2.
$$f'(\theta) = 3 \tan 3\theta$$

3.
$$f'(\theta) = 3 \cot 3\theta$$
 correct

4.
$$f'(\theta) = \frac{3}{\sin 3\theta}$$

5.
$$f'(\theta) = -\tan 3\theta$$

6. $f'(\theta) = \cot 3\theta$

Explanation:

$$f'(\theta) = \frac{1}{\sin(3\theta)} \frac{d}{d\theta} (\sin 3\theta) = \frac{3\cos 3\theta}{\sin 3\theta}$$

Consequently,

$$f'(\theta) = 3 \cot 3\theta$$

Find the derivative of f when

$$f(\theta) = \ln(\cos 3\theta)$$
.

1.
$$f'(\theta) = -\frac{1}{\sin 3\theta}$$

2.
$$f'(\theta) = \cot 3\theta$$

3.
$$f'(\theta) = -3 \tan 3\theta$$
 correct

4. $f'(\theta) = 3 \tan 3\theta$

5.
$$f'(\theta) = -3 \cot 3\theta$$

6. $f'(\theta) = \frac{3}{\cos^{3\theta}}$

Explanation: By the Chain Rule,

$$f'(\theta) = \frac{1}{\cos(3\theta)} \frac{d}{d\theta} (\cos 3\theta) = -\frac{3\sin 3\theta}{\cos 3\theta}$$

Consequently,

$$f'(\theta) = -3 \tan 3\theta$$

021 10.0 points Differentiate the function

$$f(x) = \cos(\ln 6x)$$
.

1.
$$f'(x) = -\frac{6\sin(\ln 6x)}{x}$$

2.
$$f'(x) = \frac{1}{\cos(\ln 6 x)}$$

3.
$$f'(x) = -\sin(\ln 6 x)$$

4. $f'(x) = \frac{\sin(\ln 6 x)}{x}$

5.
$$f'(x) = -\frac{\sin(\ln 6 x)}{x}$$
 correct

6. $f'(x) = \frac{6\sin(\ln 6x)}{}$

Explanation: By the Chain Rule

$$f'(x) = -\frac{\sin(\ln 6x)}{x}$$

022 10.0 points

After successive applications of the Chain

 $f'(x) = \frac{8}{2x+1}$, $f''(x) = -\frac{16}{(2x+1)^2}$.

 $f''(1) = -\frac{16}{9}$

025 10.0 points

At x = 1, therefore,

Find the derivative of

1. $f'(t) = -\frac{5}{t(4-\ln t)^2}$

3. $f'(t) = \frac{4}{t(1+\ln t)^2}$

4. $f'(t) = -\frac{4 \ln t}{t (1 + \ln t)^2}$

5. $f'(t) = -\frac{5}{(4-\ln t)^2}$

6. $f'(t) = \frac{4 \ln t}{(1 + \ln t)^2}$

By the Quotient Rule,

 $f'(t) = \frac{(4 - \ln t)(1/t) + (1 + \ln t)(1/t)}{-}$

 $f(x) = 4 \ln(2x + \sqrt{6 + 4x^2})$

Explanation:

Consequently.

2. $f'(t) = \frac{5}{t(4-\ln t)^2}$ correct

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Find the slope of the line tangent to the

$$\ln(xy) + 2x = 0$$

at the point where x = 1.

$$\mathbf{1.} \text{ slope } = -3e^2$$

2. slope =
$$-\frac{3}{2}e^2$$

3. slope =
$$3e^{-2}$$

4. slope =
$$\frac{3}{9}e^{-2}$$

5. slope =
$$-3e^{-2}$$
 correct

6. slope =
$$\frac{3}{2}e^2$$

Explanation:

Differentiating implicitly with respect to x

$$\frac{1}{xy}\Big(\,y+x\frac{dy}{dx}\,\Big)+2 \ = \ 0 \ ,$$

in which case

$$\frac{dy}{dx} = -\frac{y(1+2x)}{x} = -\frac{e^{-2x}(1+2x)}{x^2}$$

$$y \;=\; \frac{e^{-2x}}{x} \,.$$

Consequently, at x = 1

slope =
$$\frac{dy}{dx}\Big|_{x=1} = -3e^{-2}$$

Determine the value of f'''(1) when

$$f(x) = 5 \ln (x+3).$$

1.
$$f'''(1) = \frac{5}{16}$$

2.
$$f'''(1) = -\frac{5}{64}$$

3.
$$f'''(1) = -\frac{5}{32}$$

4.
$$f'''(1) = -\frac{5}{16}$$

5.
$$f'''(1) = \frac{5}{64}$$

6.
$$f'''(1) = \frac{5}{32}$$
 correct

$$f'(x) = \frac{5}{x+3}$$
, $f''(x) = -\frac{5}{(x+3)^2}$

$$f'''(x) = \frac{10}{(x+3)^3}.$$

At x = 1, therefore,

$$f'''(1) = \frac{5}{32}$$

Determine the value of f''(1) when

$$f(x) = 4 \ln (2x + 1)$$
.

1.
$$f''(1) = -\frac{16}{3}$$

2.
$$f''(1) = \frac{32}{9}$$

3.
$$f''(1) = \frac{16}{9}$$

4.
$$f''(1) = -\frac{16}{9}$$
 correct

5.
$$f''(1) = -\frac{32}{9}$$

6.
$$f''(1) = \frac{16}{3}$$

Explanation:

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6.
$$f'(x) = 14x^{15}$$

Explanation:

$$r \ln x = \ln x^r$$
 $e^{\ln x} = x$

we see that

$$f(x) = e^{(\ln x^{15})} = x^{15}$$
.

Consequently,

$$f'(x) = 15x^{14}$$

028 10.0 points

Calculate $f'(\ln 3)$ when

$$f(x) = \ln \left(\sqrt{8 + e^x}\right)$$
.

1.
$$f'(\ln 3) = \frac{3}{44}$$

2.
$$f'(\ln 3) = -\frac{3}{22}$$

3.
$$f'(\ln 3) = \frac{3}{22}$$
 correct

4.
$$f'(\ln 3) = \frac{3}{11}$$

5.
$$f'(\ln 3) = \frac{1}{22}$$

Explanation:

By properties of logarithms,

$$f(x) = \frac{1}{2} \ln \left(8 + e^x \right).$$

Using the Chain Rule, we now see that

$$\frac{df}{dx} = \frac{e^x}{2(8+e^x)}.$$

Thus, at $x = \ln 3$,

$$f'(\ln 3) = \frac{3}{2(8+3)} = \frac{3}{22}$$

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since
$$e^{\ln x} = x$$
.

029 10.0 points

Determine the value of the third derivative of f at x = 1 when

$$f(x) = 3\ln(3x+2),$$

1.
$$f'''(x) = -\frac{162}{125}$$

2.
$$f'''(x) = \frac{486}{125}$$

3.
$$f'''(x) = \frac{81}{125}$$

4.
$$f'''(x) = -\frac{81}{125}$$

5.
$$f'''(x) = \frac{162}{125}$$
 correct

Explanation:

After successive applications of the Chain Rule

$$f'(x) = \frac{9}{3x+2}$$
, $f''(x) = -\frac{27}{(3x+2)^2}$

$$f'''(x) = \frac{162}{(3x+2)^3}$$

The value of f''' at x = 1 is thus given by

$$f'''(1) = \frac{162}{125}.$$

030 10.0 points

Determine f'(e) when

$$f(x) = x^2(2 + (\ln x)^3).$$

1.
$$f'(e) = 8e$$

1. $f'(x) = \frac{8}{\sqrt{6+4x^2}}$ correct

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 correc
2. $f'(x) = \frac{8}{6+4x^2}$

3.
$$f'(x) = -\frac{8}{\sqrt{6+4x^2}}$$

4.
$$f'(x) = \frac{4}{2x + \sqrt{6 + 4x^2}}$$

5.
$$f'(x) = 8\sqrt{6+4x^2}$$

Explanation:

$$\frac{d}{dx} \ln(2x + \sqrt{6 + 2x^2})$$

$$= \left(2 + \frac{4x}{\sqrt{6 + 4x^2}}\right) \left(\frac{1}{2x + \sqrt{6 + 4x^2}}\right)$$

$$= \frac{2}{\sqrt{6x + x^2}}.$$

Consequently,

$$f'(x) = \frac{8}{\sqrt{6+4x^2}}$$

027 10.0 points

Determine f'(x) when

$$f(x) = e^{(3\ln(x^5))}$$
.

1.
$$f'(x) = \frac{3}{x^2}e^{3\ln(x^5)}$$

2.
$$f'(x) = e^{15/x}$$

3.
$$f'(x) = 15x^{14}$$
 correct

4.
$$f'(x) = 15(\ln x)e^{3\ln(x^5)}$$

5.
$$f'(x) = \frac{1}{x}e^{3\ln(x^5)}$$

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2.
$$f'(e) = 5e$$

3. f'(e) = 9e correct

Find the derivative of

4.
$$f'(e) = 7e$$

5.
$$f'(e) = 6e$$

Explanation:

Using the Product and Power rules we see

$$f'(x) = 2x(2 + (\ln x)^3) + \frac{3x^2(\ln x)^2}{x}$$
$$= x(4 + 2(\ln x)^3 + 3(\ln x)^2).$$

At x = e, therefore,

$$f'(e) = 9e.$$