$$C_n(X) \xrightarrow{\partial_n} C_{n-1}(X)$$

$$C_n(f) \downarrow \qquad \qquad \downarrow^{C_{n-1}(f)}$$

$$C_n(Y) \xrightarrow{\partial_n} C_{n-1}(Y)$$