$$\mathcal{C}^{\mathbb{R}} \stackrel{R}{\underset{E}{\longleftrightarrow}} \mathcal{C}^{S}$$
.