



$\alpha(m)$  and  $\alpha(f(\alpha(m)))$  are mapped to the same element. Therefore, their difference is zero, so that  $m - f(\alpha(m)) \in \text{Ker}(\alpha)$ .