

 $\alpha(m)$ and $\alpha(f(\alpha(m)))$ are mapped to the same element. Therefore, their difference is zero, so that $m - f(\alpha(m)) \in \operatorname{Ker}(\alpha)$.