$g(m)$ and $g(\beta(g(m)))$ are mapped to the same element in M_2, so their difference is zero. Therefore, $m - \beta(g(m)) \in \mathrm{Ker}(g)$.