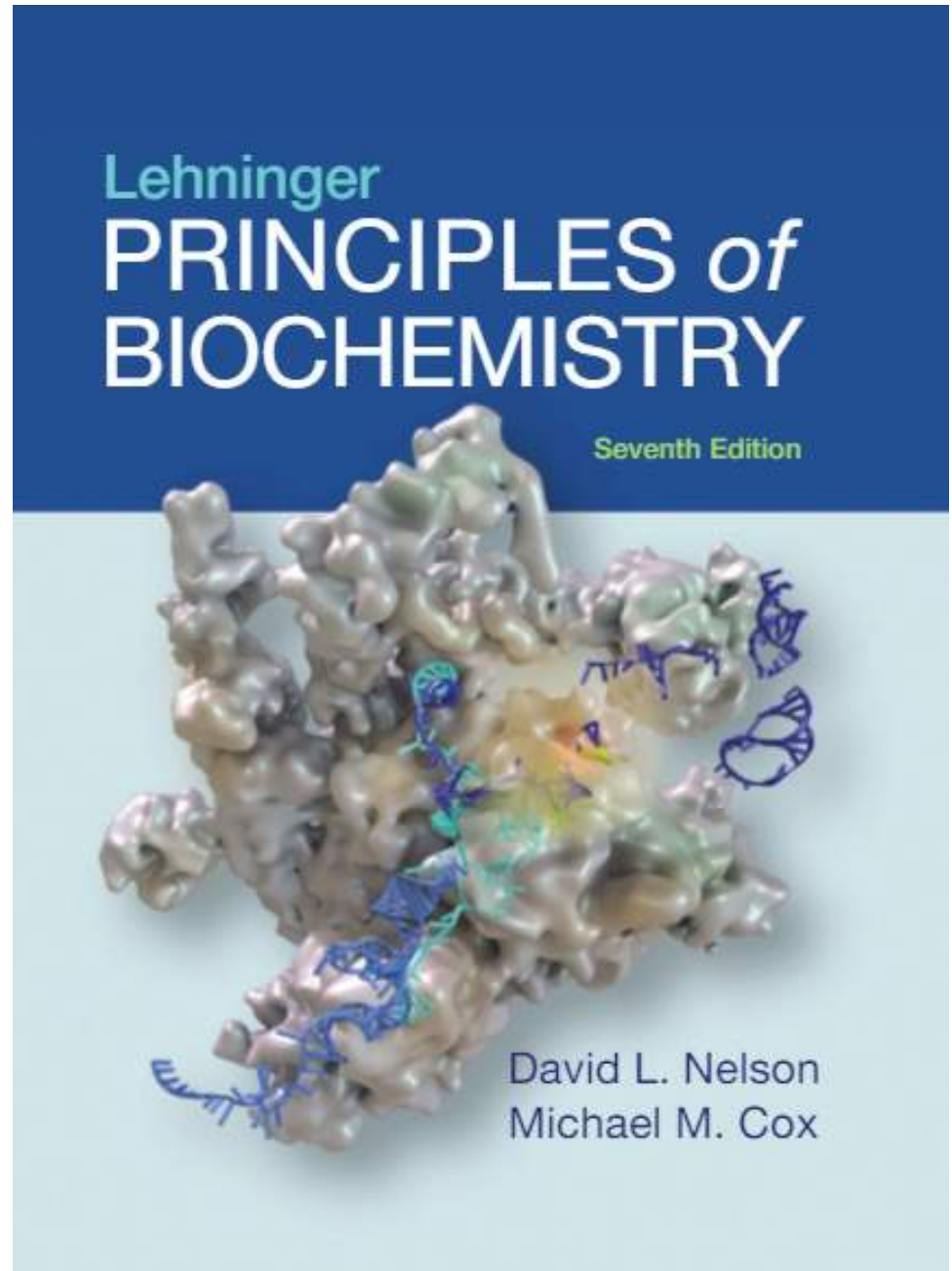




# 6 | Enzymes

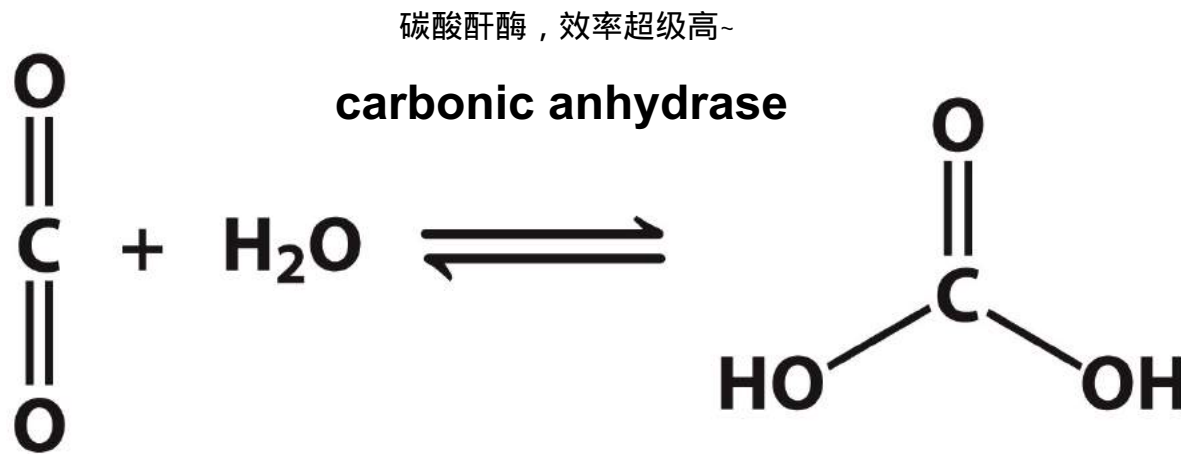
© 2017 W. H. Freeman and Company



# What are enzymes

- Enzymes are **catalysts**.
  - increase reaction rates without being used up
- **Most** enzymes are **proteins**.
  - However, some RNA (ribozymes and **ribosomal RNA**) also catalyze reactions.
- The study of enzymatic processes is the oldest field of biochemistry, dating back to late 1700s.
- The study of enzymes has dominated biochemistry in the past and continues to do so.

# Enzymes are macromolecular biological catalysts

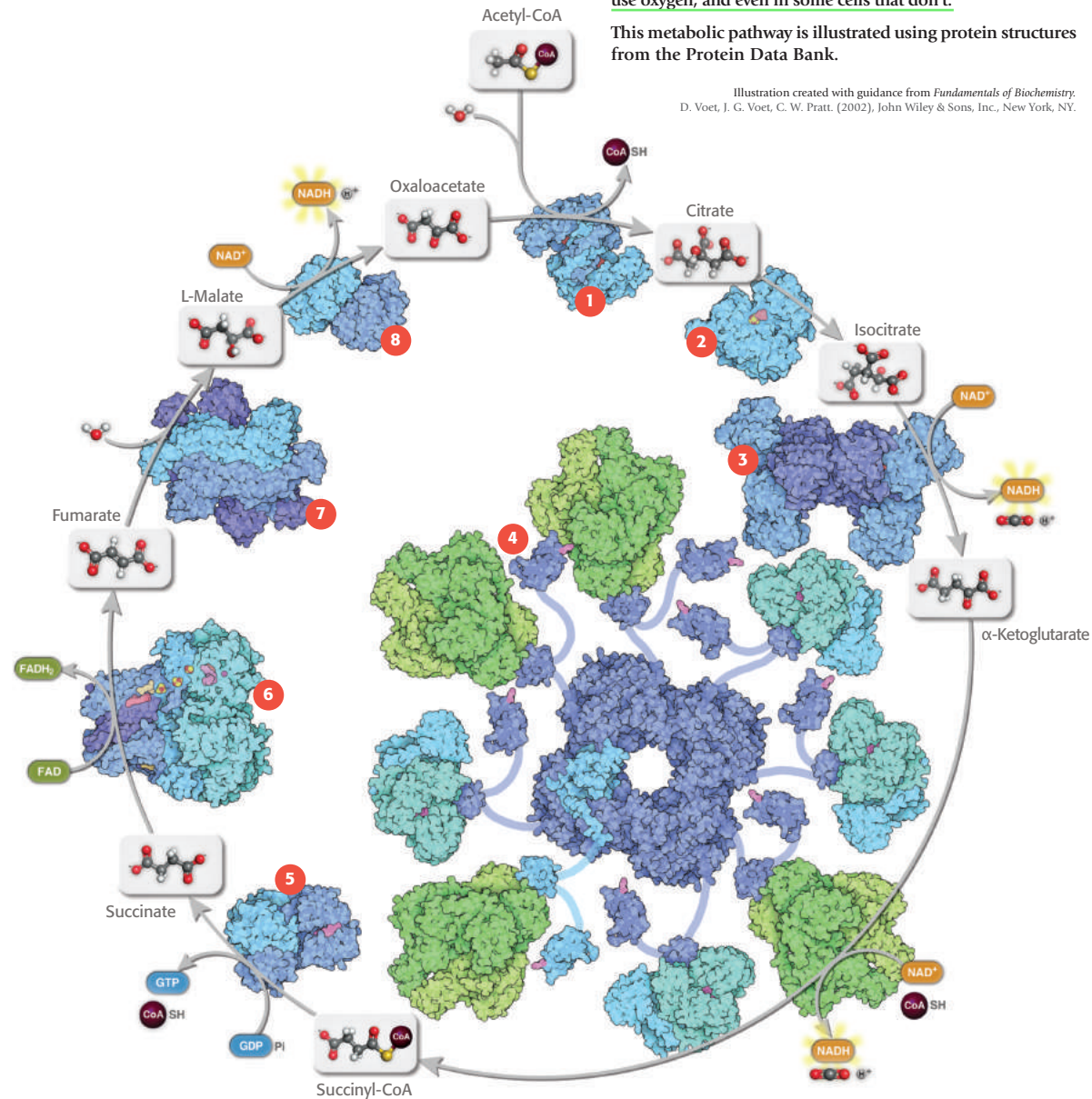


# The Structures of the Citric Acid Cycle

Also known as the Krebs cycle or the tricarboxylic acid cycle, the *citric acid cycle* is at the center of cellular metabolism. It plays a starring role in both the process of energy production and biosynthesis. The cycle finishes the sugar-breaking job started in glycolysis and fuels the production of ATP in the process. It is also a central hub in biosynthetic reactions, providing intermediates that are used to build amino acids and other molecules. Citric acid cycle enzymes are found in all cells that use oxygen, and even in some cells that don't.

This metabolic pathway is illustrated using protein structures from the Protein Data Bank.

Illustration created with guidance from *Fundamentals of Biochemistry*.  
D. Voet, J. G. Voet, C. W. Pratt. (2002), John Wiley & Sons, Inc., New York, NY.



# Enzymes are extraordinary catalysts

高效催化剂！

**TABLE 6-5**   **Some Rate Enhancements  
Produced by Enzymes**

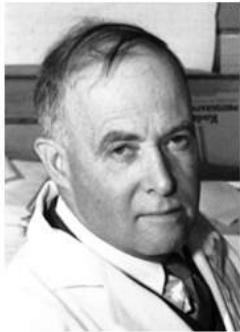
|  |                             |
|--|-----------------------------|
| <b>Cyclophilin</b>                           | <b><math>10^5</math></b>    |
| <b>Carbonic anhydrase</b>                    | <b><math>10^7</math></b>    |
| <b>Triose phosphate isomerase</b>            | <b><math>10^9</math></b>    |
| <b>Carboxypeptidase A</b>                    | <b><math>10^{11}</math></b> |
| <b>Phosphoglucomutase</b>                    | <b><math>10^{12}</math></b> |
| <b>Succinyl-CoA transferase</b>              | <b><math>10^{13}</math></b> |
| <b>Urease</b>                                | <b><math>10^{14}</math></b> |
| <b>Orotidine monophosphate decarboxylase</b> | <b><math>10^{17}</math></b> |

乳清酸脱羧酶（？）



# Most enzymes are proteins

## The Nobel Prize in Chemistry 1946



James Batcheller Sumner

Prize share: 1/2



John Howard Northrop

Prize share: 1/4



Wendell Meredith Stanley

Prize share: 1/4

The Nobel Prize in Chemistry 1946 was divided, one half awarded to James Batcheller Sumner *"for his discovery that enzymes can be crystallized"*, the other half jointly to John Howard Northrop and Wendell Meredith Stanley *"for their preparation of enzymes and virus proteins in a pure form"*.

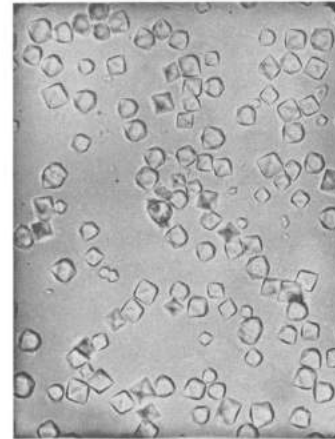
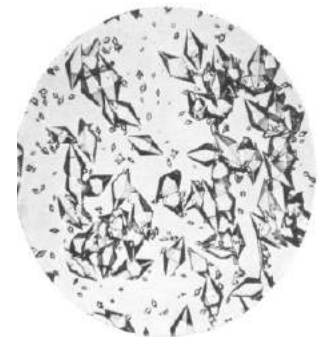


FIG. 1. Photomicrograph of urease crystals magnified 728 diameters.

Octahedral crystals  
of jack bean urease



Pepsin crystals

Some RNA can function as enzyme (**Ribozyme**):  
implications in the origin of life

## The Nobel Prize in Chemistry 1989



Sidney Altman

Prize share: 1/2

RNase P

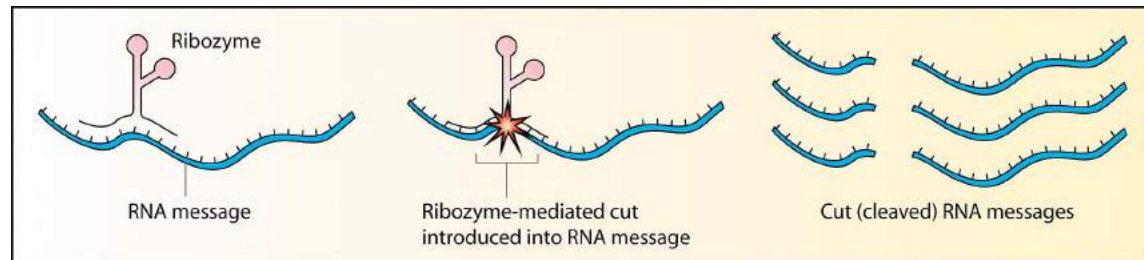


Thomas R. Cech

Prize share: 1/2

自剪切RNA (不算是真正的合酶, 反应前后化学性质改变了)

The Nobel Prize in Chemistry 1989 was awarded jointly to Sidney Altman and Thomas R. Cech *"for their discovery of catalytic properties of RNA"*



RNA催化功能的发现支持了RNA世界假说

# Vocabularies

- Reactants in enzyme-catalyzed reactions are called **substrates**.
- Enzymes bring substrates together to form an enzyme-substrate complex on a particular region of the enzyme called the **active site** (catalytic site + binding site).
- Many enzymes require cofactors for activity. Cofactors are small molecules that some enzymes require for activity. The two main classes of cofactors are **coenzymes** (organic molecules derived from vitamins) and **metals**.
- Tightly bound coenzymes are called **prosthetic groups**.
- An enzyme with its cofactor is a **holoenzyme**. Without the cofactor, the enzyme is called an **apoenzyme**.

apo : empty ( ? )



# PROTEIN STRUCTURE

Scaffold to support and  
position active site

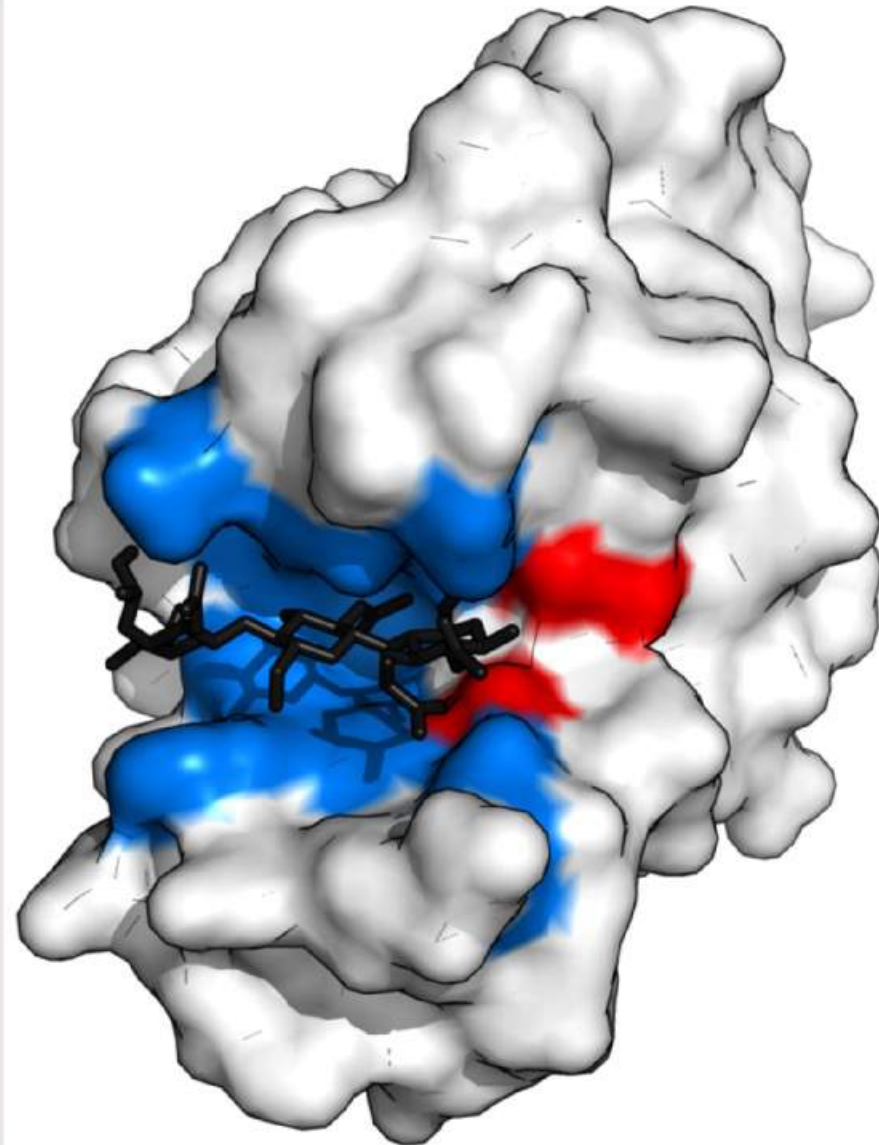
## ACTIVE SITE

### BINDING SITES

Bind and orient  
substrate(s)

### CATALYTIC SITE

Reduce chemical  
activation energy



# Cofactors and Coenzymes

**TABLE 6-2** Some Coenzymes That Serve as Transient Carriers of Specific Atoms or Functional Groups

| Coenzyme  | Examples of chemical groups transferred | Dietary precursor in mammals         |
|---|---|--------------------------------------|
| Biocytin 生物胞素   | CO <sub>2</sub> 一碳单位载体！                 | Biotin 泛酸                            |
| Coenzyme A  | Acyl groups 乙酰基                         | Pantothenic acid and other compounds |
| 5'-Deoxyadenosylcobalamin (coenzyme B <sub>12</sub> ) FAD | H atoms and alkyl groups H原子、烷基         | Vitamin B <sub>12</sub>              |
| Flavin adenine dinucleotide                               | Electrons                               | Riboflavin (vitamin B <sub>2</sub> ) |
| Lipoate 硫辛酸 NAD   | Electrons and acyl groups               | Not required in diet                 |
| Nicotinamide adenine dinucleotide                         | Hydride ion (:H <sup>-</sup> )          | Nicotinic acid (niacin)              |
| Pyridoxal phosphate 磷酸吡哆醛                                 | Amino groups                            | Pyridoxine (vitamin B <sub>6</sub> ) |
| Tetrahydrofolate 四氢叶酸                                     | One-carbon groups                       | Folate                               |
| Thiamine pyrophosphate TPP                                | Aldehydes 醛基                            | Thiamine (vitamin B <sub>1</sub> )   |

**Note:** The structures and modes of action of these coenzymes are described in Part II.

# Enzymes can be classified by the reactions they catalyze

**TABLE 6-3 International Classification of Enzymes**

|     | Class no. | Class name      | Type of reaction catalyzed   |
|-----|-----------|-----------------|--|
| 脱氢酶 | 1         | Oxidoreductases | Transfer of electrons (hydride ions or H atoms)  |
| 转移酶 | 2         | Transferases    | Group transfer reactions   |
| 水解酶 | 3         | Hydrolases      | Hydrolysis reactions ( <u>transfer of functional groups to water</u> )   |
| 裂合酶 | 4         | Lyases          | <u>Cleavage of C—C, C—O, C—N, or other bonds by elimination, leaving</u><br><u>bonds or rings, or addition of groups to double bonds</u> |
| 异构酶 | 5         | Isomerases      | Transfer of groups <u>within molecules</u> to yield isomeric forms   |
| 连接酶 | 6         | Ligases         | Formation of C—C, C—S, C—O, and C—N bonds by condensation reactions coupled to cleavage of <u>ATP or similar cofactor</u>                |



## IUBMB Enzyme Nomenclature

**EC 2.7.1.1**

2: class name (transferase);  
 7: subclass (phosphotransferase);  
 1: a hydroxyl group as acceptor;  
 1: D-hexose D-己糖

羟基作为磷酸受体

**Accepted name:** hexokinase

**Reaction:** ATP + D-hexose = ADP + D-hexose 6-phosphate

**Other name(s):** hexokinase type IV glucokinase; hexokinase D; hexokinase type IV; hexokinase (phosphorylating); ATP-dependent hexokinase; glucose ATP phosphotransferase

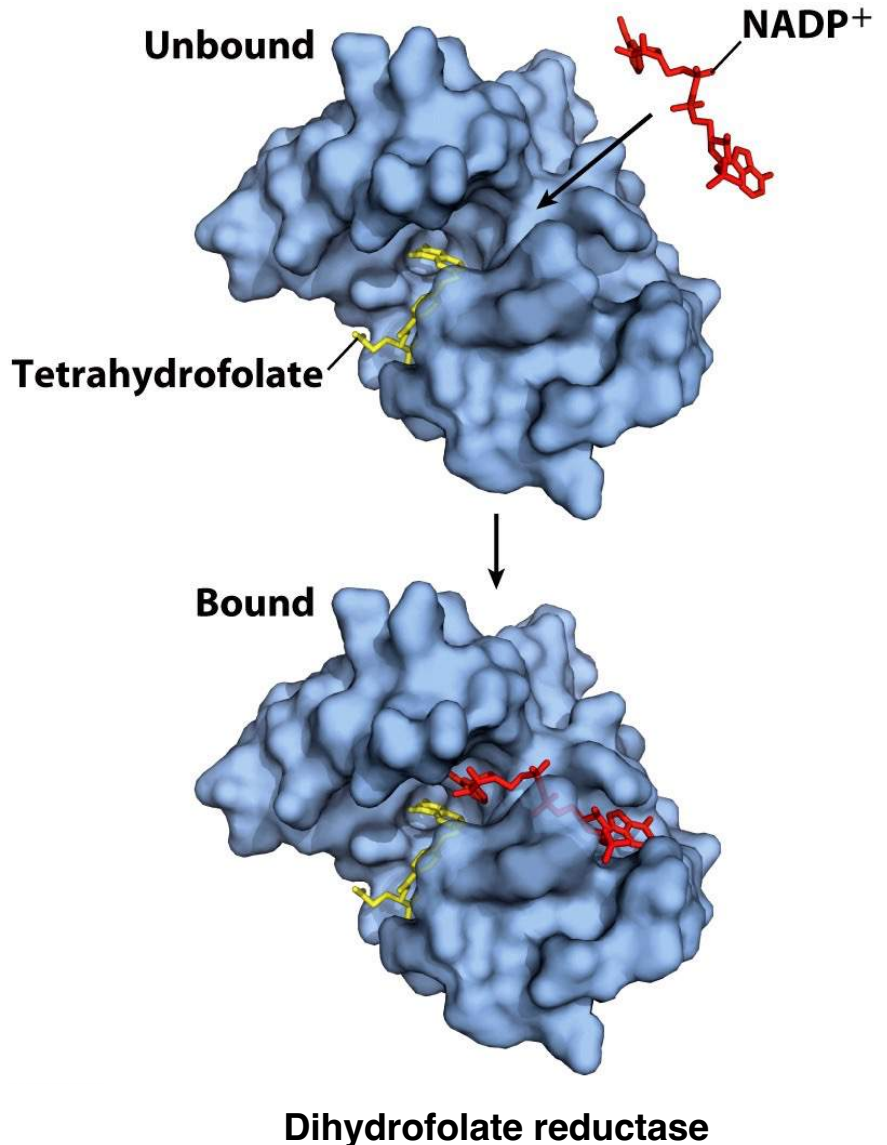
**Systematic name:** ATP:D-hexose 6-phosphotransferase

**Comments:** D-Glucose, D-mannose, D-fructose, sorbitol and D-glucosamine can act as acceptors; ITP and dATP can act as donors. The liver isoenzyme has sometimes been called glucokinase.

**Links to other databases:** [BRENDA](#), [EXPASY](#), [GTD](#), [KEGG](#), [Metacyc](#), [PDB](#), [UM-BBD](#), CAS registry number: 9001-51-8

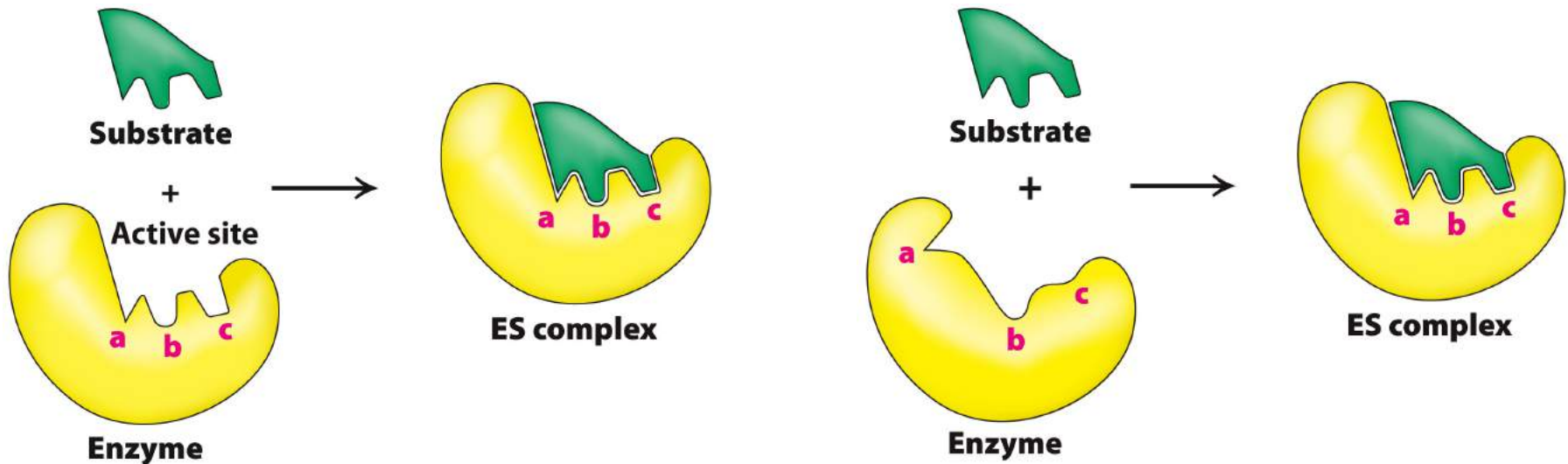
# Enzymes display a high degree of specificity

The specificity is due to the precise interaction of the enzyme and its substrate, achieved by binding pockets with complementary shape, charge and hydrophilic/hydrophobic properties of the substrates.





# “Lock and key” vs “induced fit”

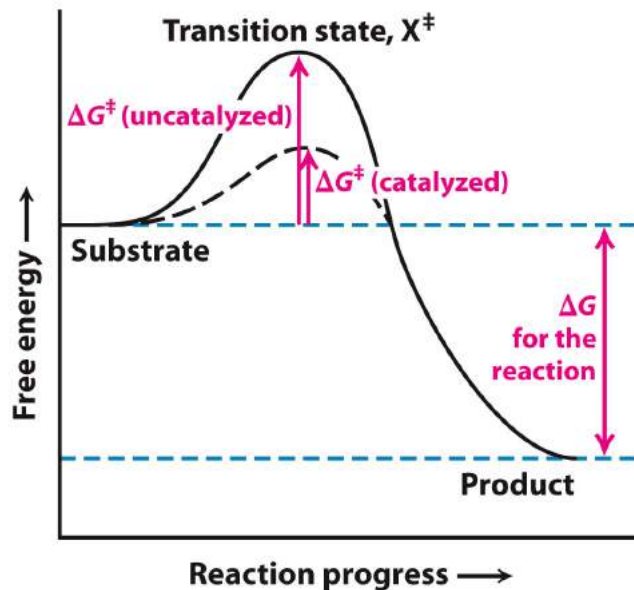


If so, there will not be catalysis.

Enzymes do not interact with their substrates like a lock and key. Rather, the enzyme changes shape upon substrate binding, a phenomenon called **induced fit**.

# Enzymes alter reaction rate, not equilibrium

- A chemical reaction proceeds through a **transition state**, a molecular form that is no longer substrate but not yet product.
- The **activation energy ( $\Delta G^\ddagger$ )** is the difference between the energy levels of the ground state and the transition state.

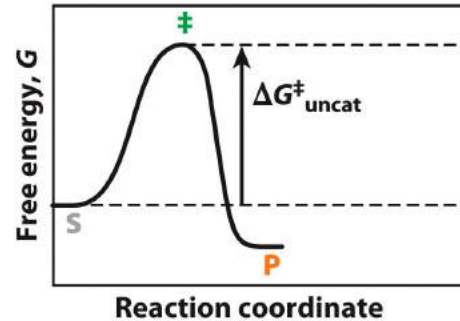
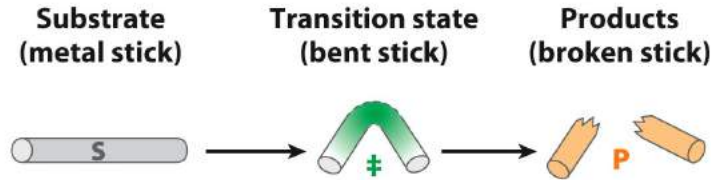


- Enzymes catalyze reaction by **lowering down the activation energy.**
- **The reaction equilibrium is determined only by the free-energy difference between the products and reactants. Enzymes cannot alter this difference.**
- In the presence of an enzyme, the reaction runs in the **same direction** as it would without the enzyme, just more **quickly.**

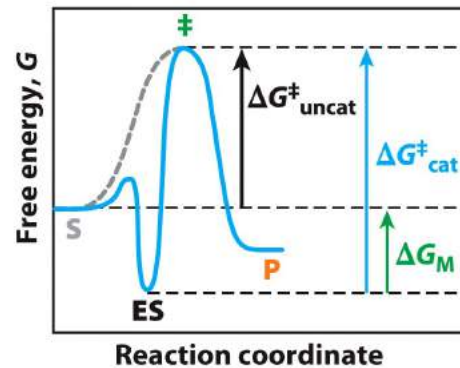
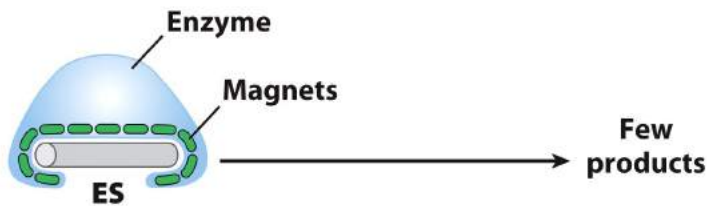


# Enzymes facilitate formation of the transition state

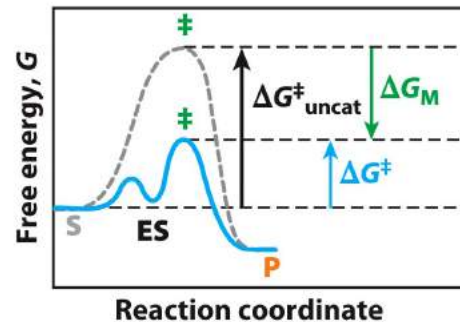
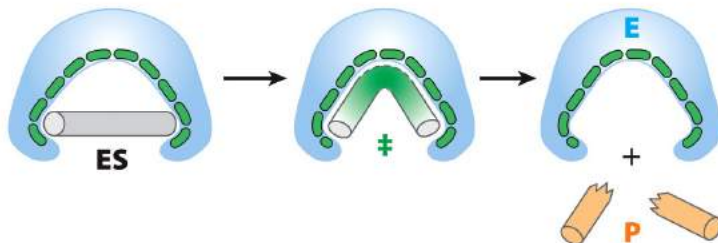
## (a) No enzyme



## (b) Enzyme complementary to substrate



## (c) Enzyme complementary to transition state



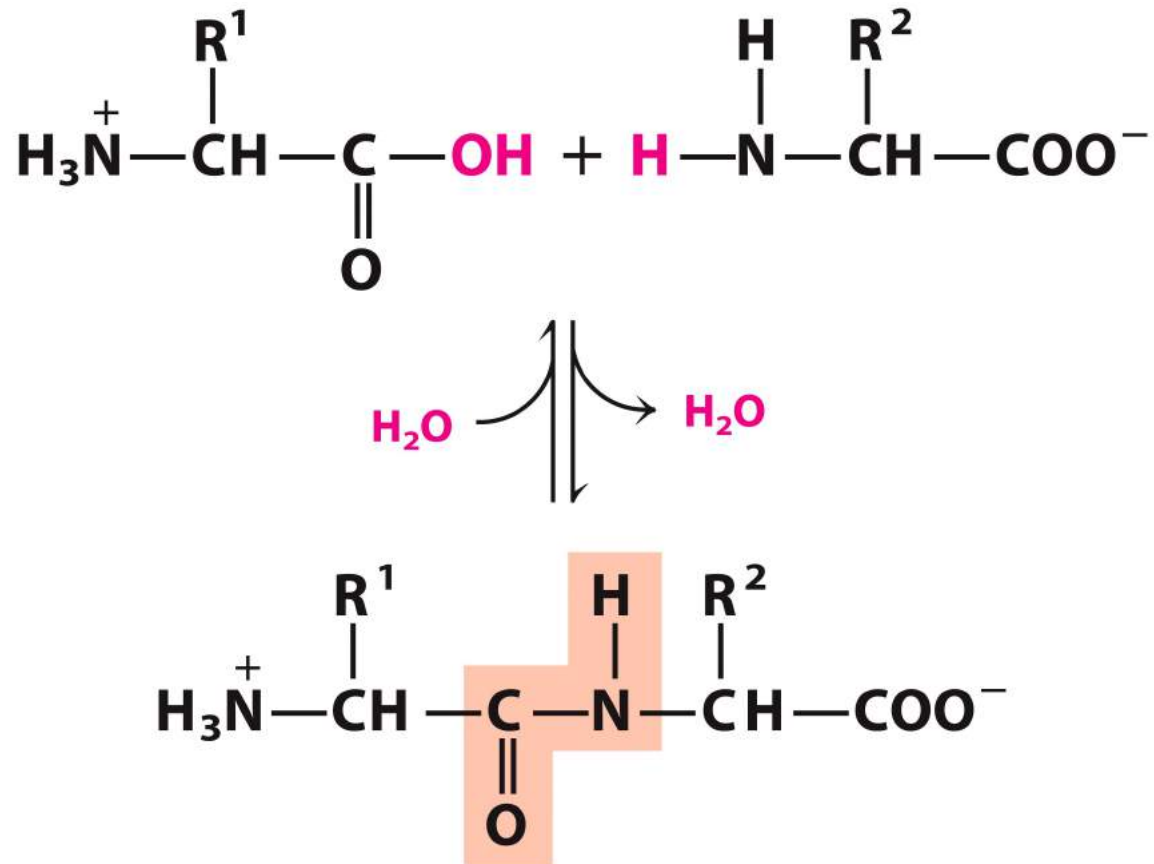
# Common catalytic strategies

- **General acid-base catalysis**: A molecule other than water donates or accepts a proton. 广义酸碱催化
- **Covalent catalysis**: The active site contains a nucleophile that is briefly covalently modified. 亲核基团  
共价催化
- **Metal ion catalysis**: Metal ions function in a number of ways, including serving as an electrophilic catalyst. 亲电催化  
金属离子催化
- **Catalysis by approximation**: The enzyme brings two substrates together in an orientation that facilitates catalysis.  
临近定向效应

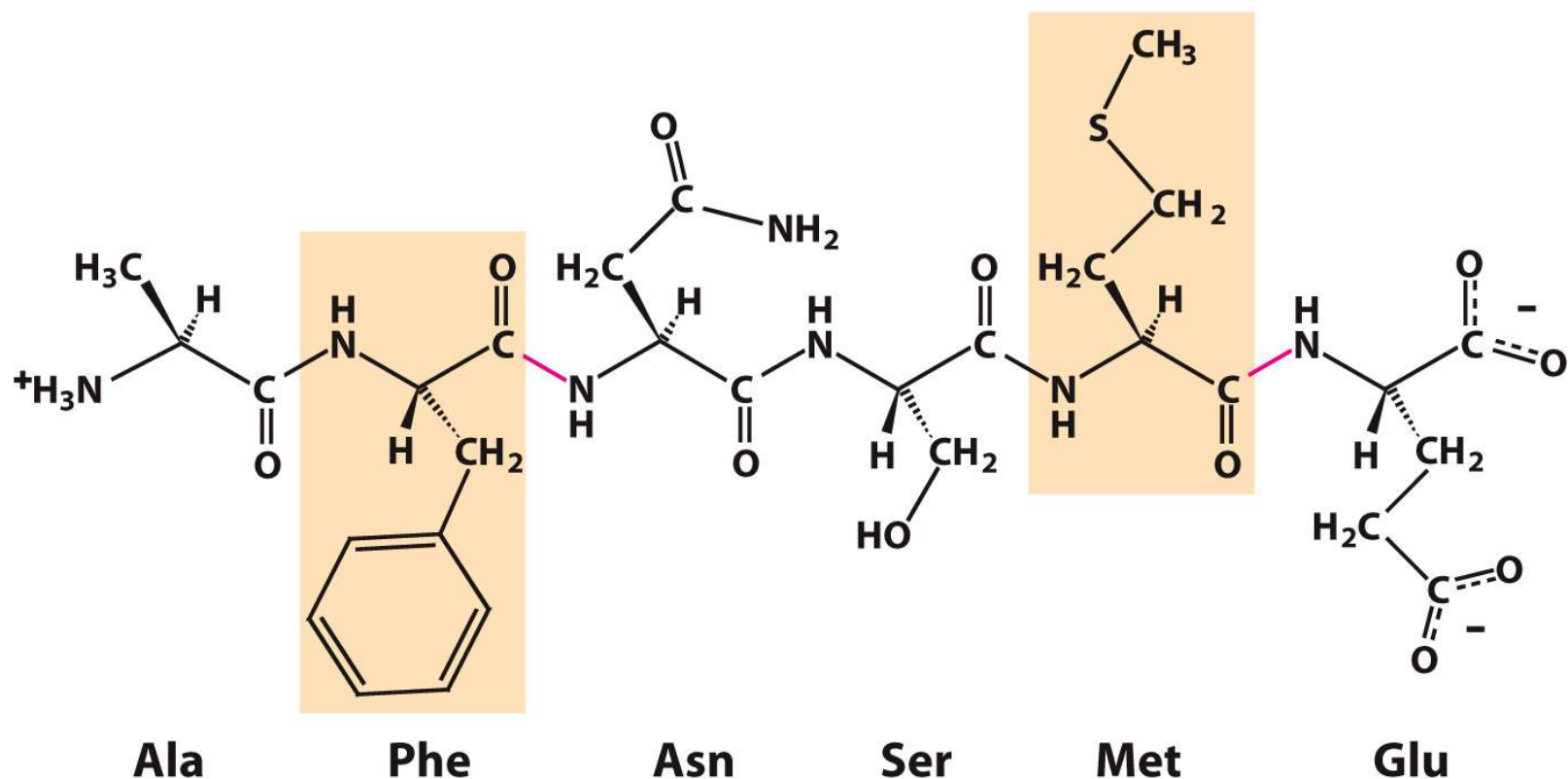
蛋白水解酶

Proteases catalyze an energetically favorable,  
but kinetically difficult reaction

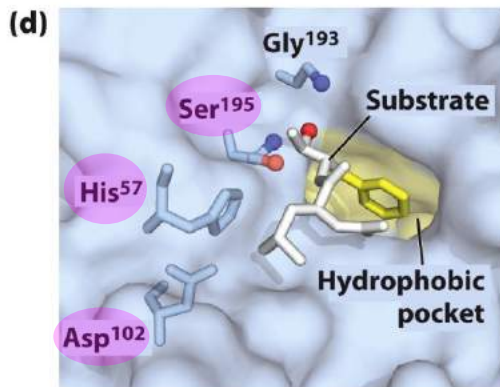
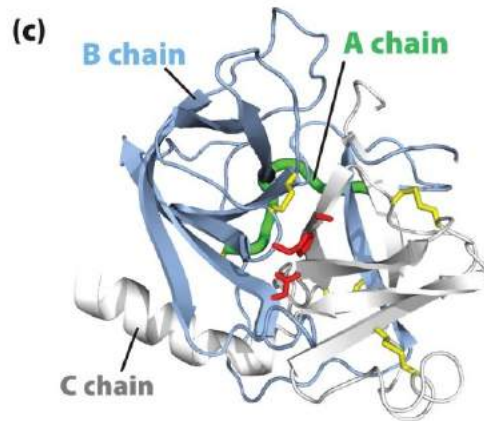
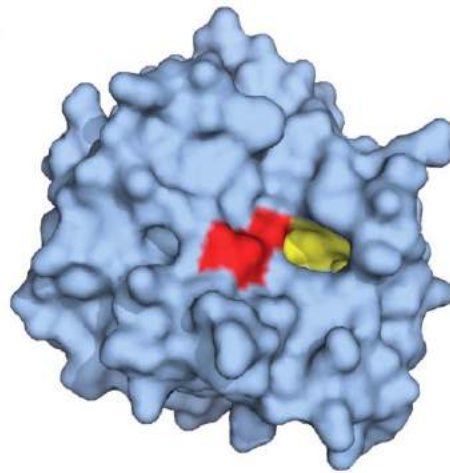
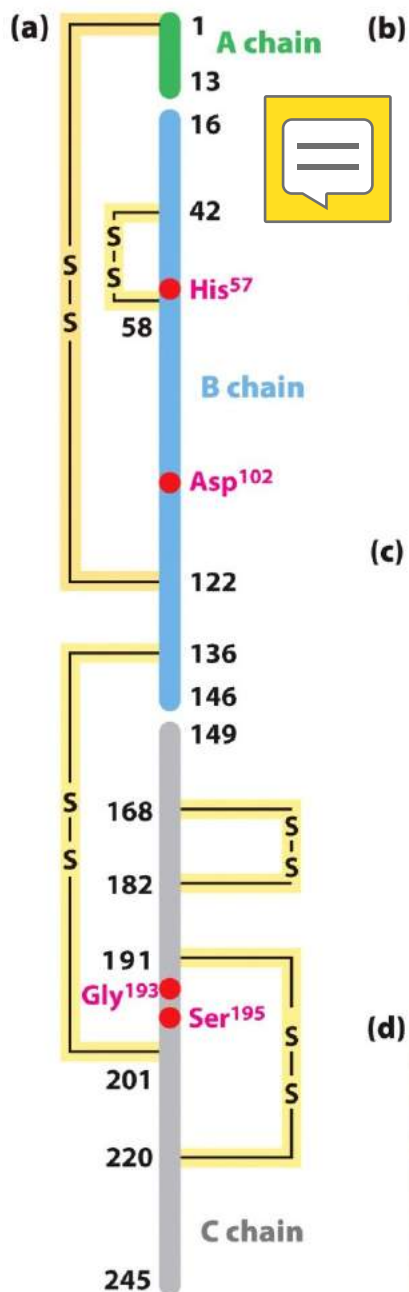
能量上有利，但是肽键稳定，不易反应



**Chymotrypsin** selectively hydrolyzes peptide bonds on the carboxyl side of large hydrophobic amino acids



Chymotrypsin is a proteolytic enzyme secreted by the pancreas that hydrolyzes peptide bonds selectively on the carboxyl side of large hydrophobic amino acids

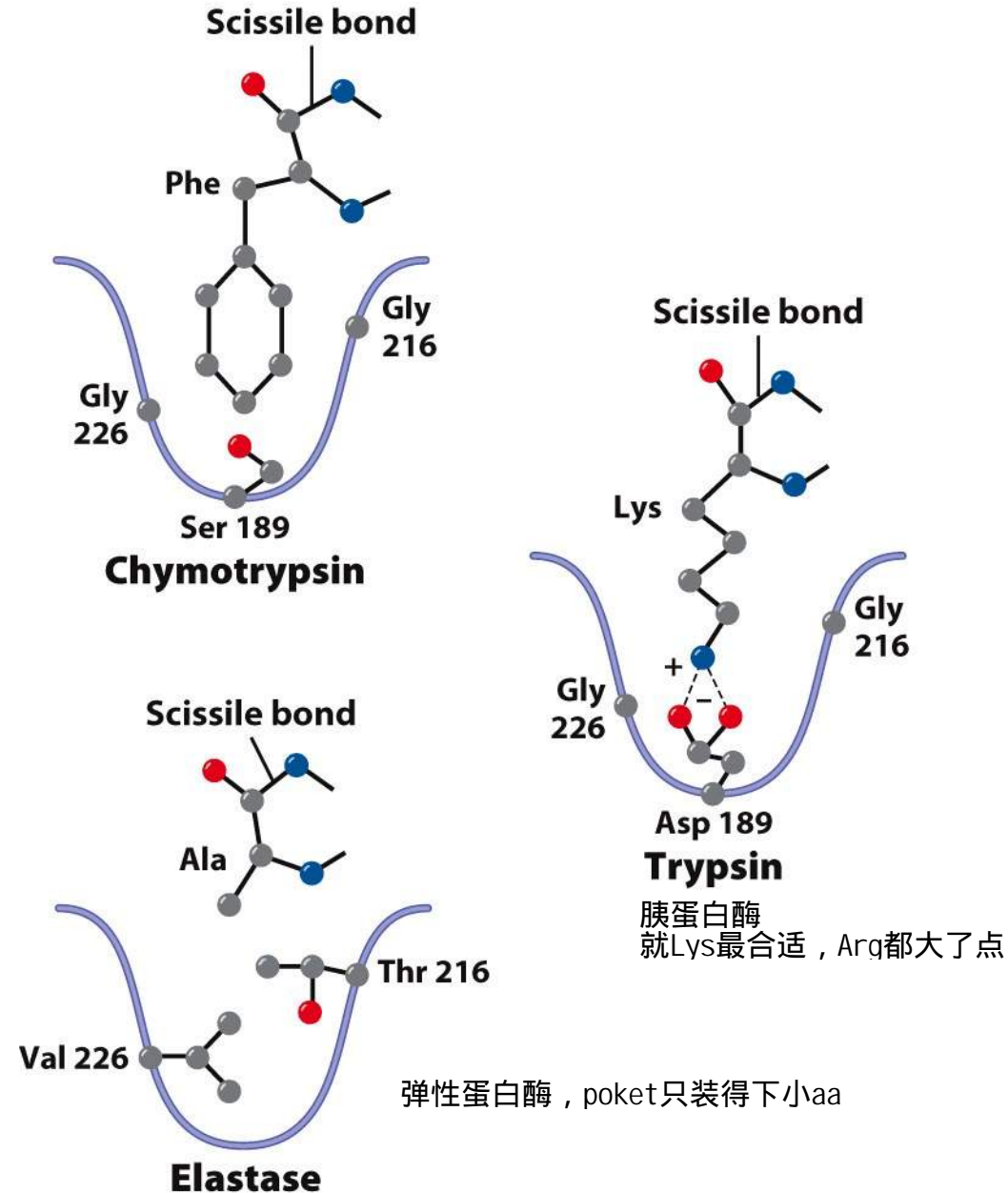


# Chymotrypsin structure

- A binding site recognizes a **large hydrophobic amino acids** especially **aromatic residues**;
- A catalytic site contains a **catalytic triad** (Ser, His, Asp), which acts via a mixture of **covalent** and **general acid-base catalysis** to cleave a peptide bond.

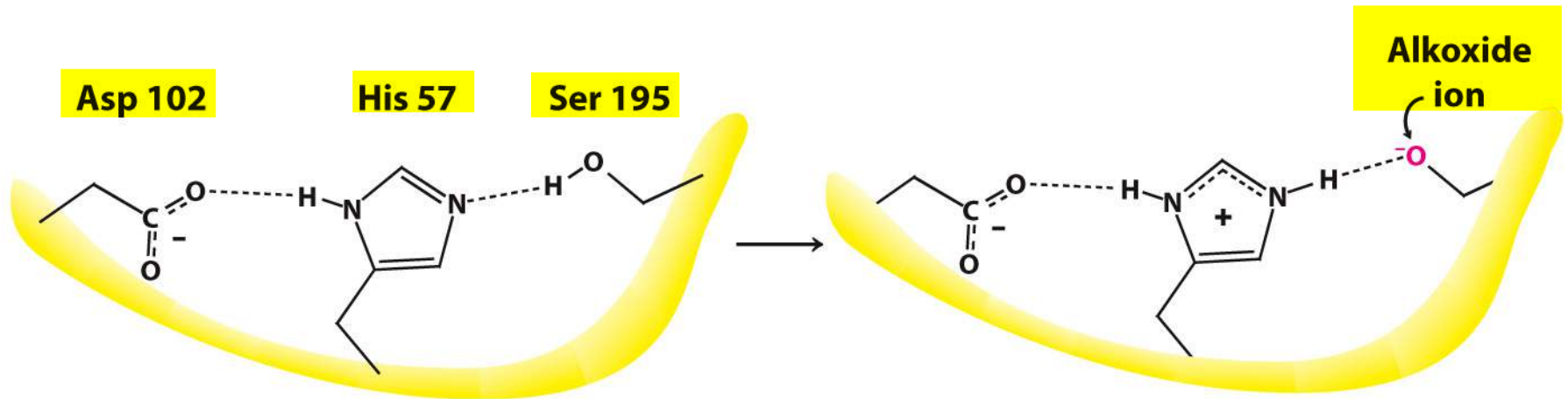
# Specificity of the serine proteases

口袋的形状及周围的aa决定了ser prE家族蛋白酶的特异性


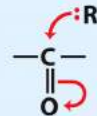

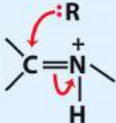
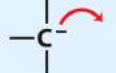
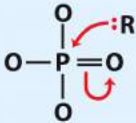


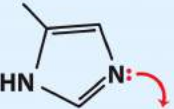





# Catalytic triad 催化三联体



- Aspartate orients the histidine and renders it a better proton acceptor.
- Histidine removes a proton from serine 195, generating a highly reactive alkoxide ion (RO<sup>-</sup>).
- The alkoxide ion attacks the peptide bond of the substrate.

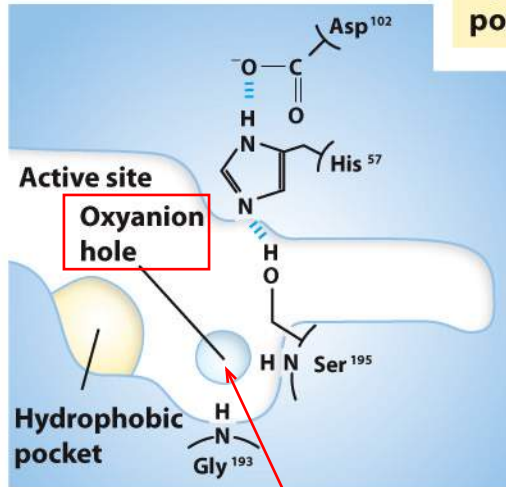
| Nucleophiles  | Electrophiles   |
|---|---|
| <br><b>Negatively charged oxygen</b><br>(as in an unprotonated hydroxyl group or an ionized carboxylic acid) | <br><b>Carbon atom of a carbonyl group</b><br>(the more electronegative oxygen of the carbonyl group pulls electrons away from the carbon) |
| <br><b>Negatively charged sulfhydryl</b>   | <br><b>Protonated imine group</b><br>(activated for nucleophilic attack at the carbon by protonation of the imine)                         |
| <br><b>Carbanion</b>   | <br><b>Phosphorus of a phosphate group</b>   |
| <br><b>Uncharged amine group</b>   | <br><b>Proton</b>  |
| <br><b>Imidazole</b>   |   |
| <br><b>Hydroxide ion</b>   |   |

- An **electron-rich** atom is called a **nucleophile** (Lewis base).
- An **electron-deficient** atom is called an **electrophile** (Lewis acid).
- Nonbonded electrons are designated by dots.
- Curved arrows represent the movement of electron pairs. (A single-headed arrow represents the movement of a single electron.)

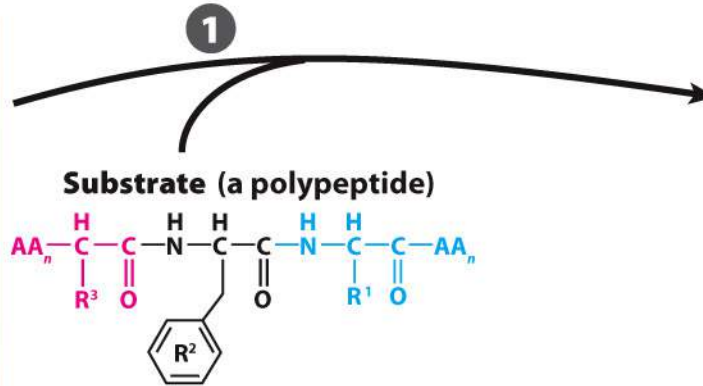
# Chymotrypsin Mechanism

## Step 1: Substrate Binding

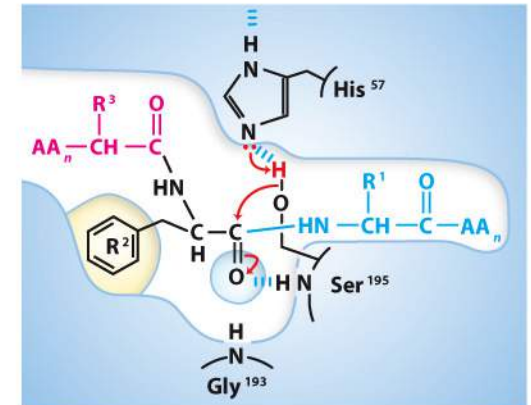
Chymotrypsin (free enzyme)



When substrate binds, the side chain of the residue adjacent to the peptide bond to be cleaved nestles in a hydrophobic pocket on the enzyme, positioning the peptide bond for attack.



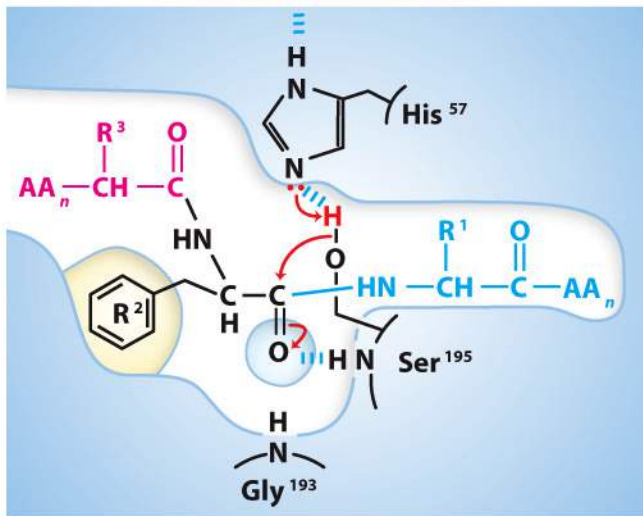
Enzyme-substrate complex



氧阴离子孔  
(Oxyanion hole)  
稳定之后会短暂出现的氧阴离子

## Step 2: Nucleophilic Attack

**Enzyme-substrate complex**

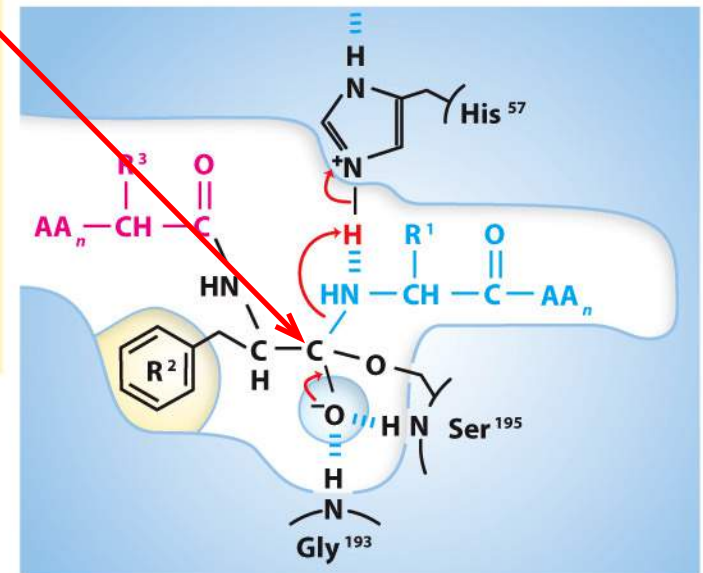


Interaction of Ser<sup>195</sup> and His<sup>57</sup> generates a strongly nucleophilic **alkoxide ion** on Ser<sup>195</sup>; the ion attacks the peptide carbonyl group, forming a **tetrahedral acyl-enzyme**. This is accompanied by formation of

a short-lived negative charge on the carbonyl oxygen of the substrate, which is stabilized by hydrogen bonding in the **oxyanion hole**.

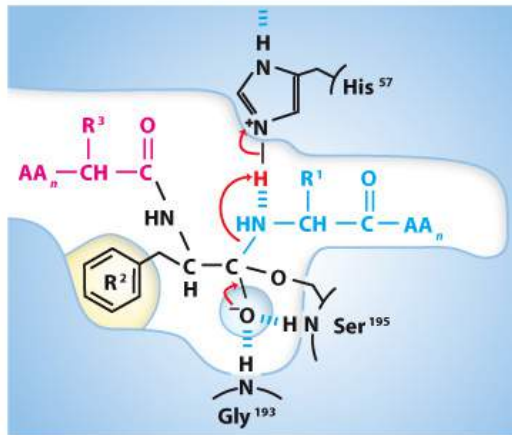
2

**Short-lived intermediate\* (acylation)**



**Short-lived intermediate\* (acylation)**

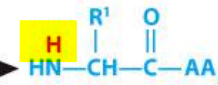
Instability of the negative charge on the substrate carbonyl oxygen leads to collapse of the tetrahedral intermediate; re-formation of a double bond with carbon displaces the bond between carbon and the amino group of the peptide linkage, breaking the peptide bond. The amino leaving group is protonated by His<sup>57</sup>, facilitating its displacement.



the amino group of the peptide linkage, breaking the peptide bond. The amino leaving group is protonated by His<sup>57</sup>, facilitating its displacement.

compared to C-O, C-N is easily to break (peptide bond)

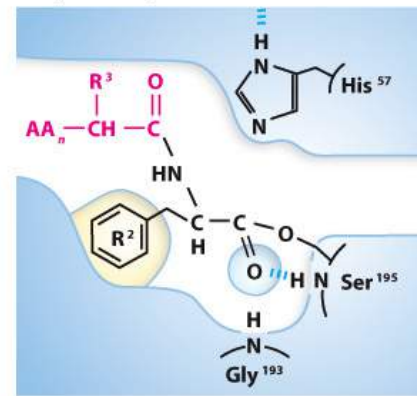
**Product 1**



3

## Step 3: Substrate Cleavage

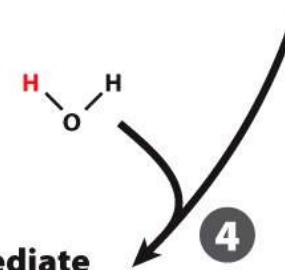
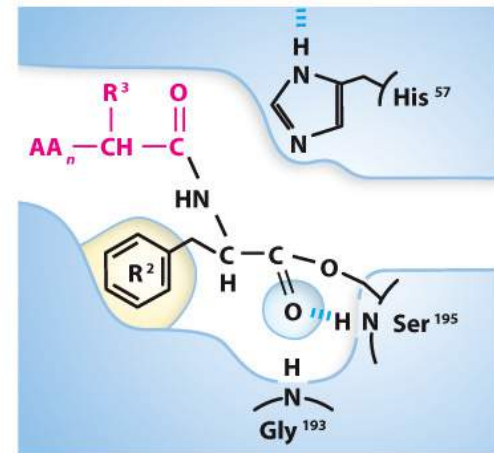
**Acyl-enzyme intermediate**



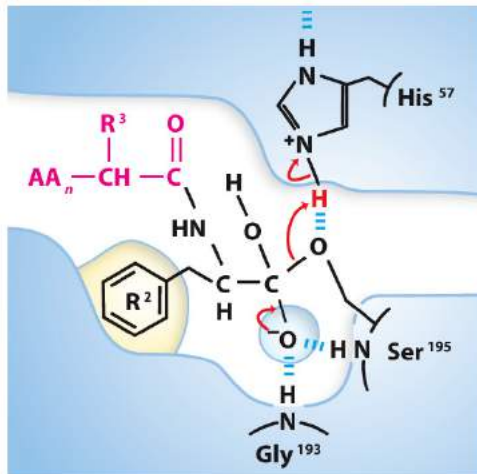


# Step 4&5: Water Comes In and attacks

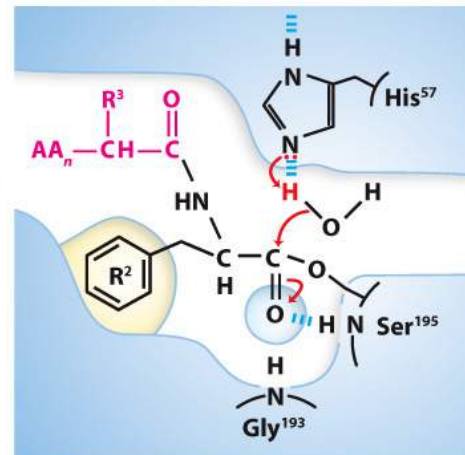
Acyl-enzyme intermediate



Short-lived intermediate \*  
(deacylation)



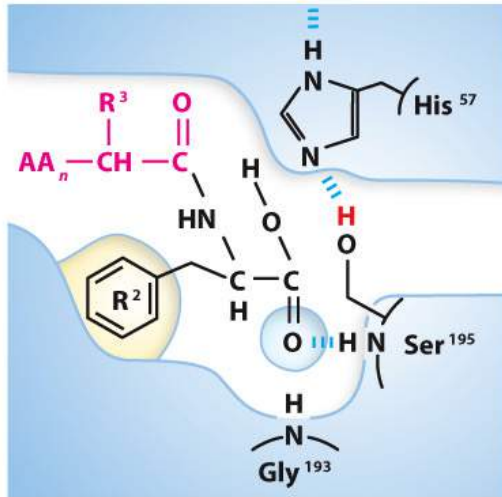
Acyl-enzyme intermediate



An incoming water molecule is deprotonated by general base catalysis, generating a strongly nucleophilic hydroxide ion. Attack of hydroxide on the ester linkage of the acyl-enzyme generates a second tetrahedral intermediate, with oxygen in the oxyanion hole again taking on a negative charge.

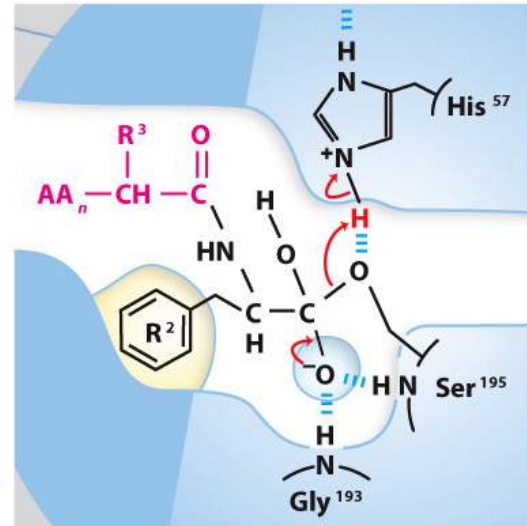


## Enzyme-product 2 complex



## Step 6: Break-off from the Enzyme

### Short-lived intermediate\* (deacylation)

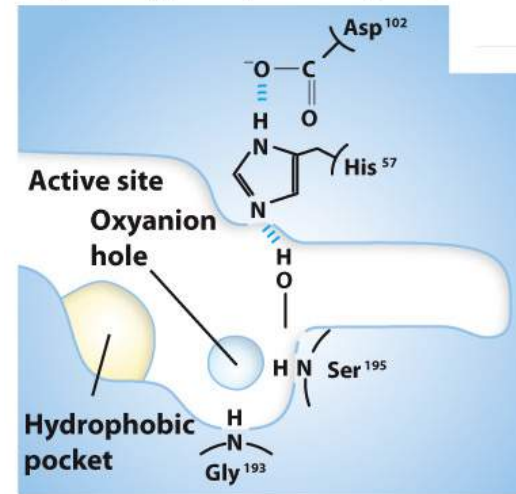


6

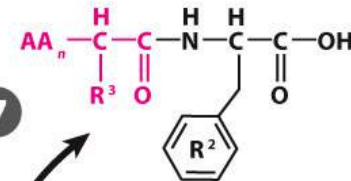
Collapse of the tetrahedral intermediate forms the second product, a carboxylate anion, and displaces  $Ser_{195}$ .

# Step 7: Product Dissociates

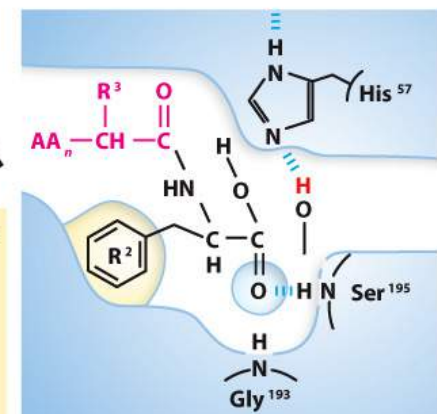
Chymotrypsin (free enzyme)



Product 2



Enzyme-product 2 complex

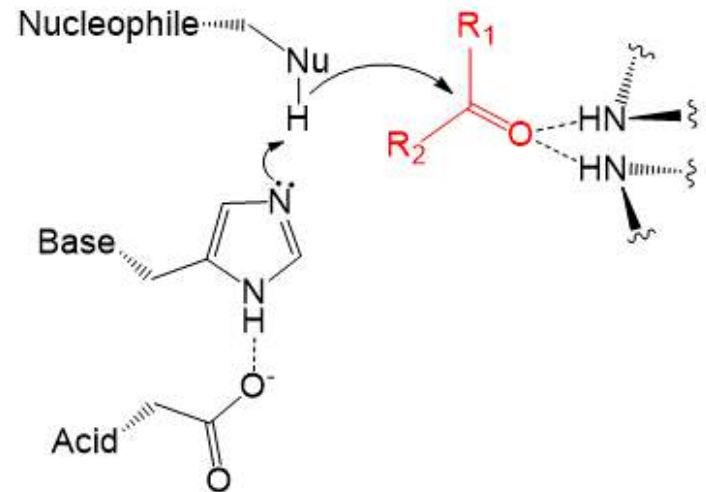


Dissociation of the second product from the active site regenerates free enzyme.

# Catalytic triad

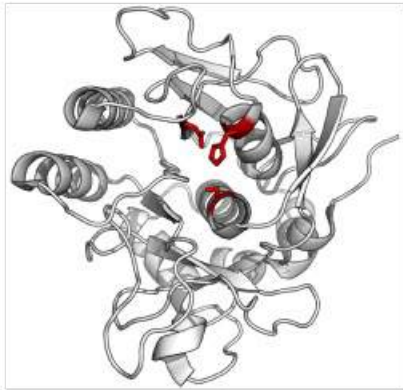
- An **Acid-Base-Nucleophile triad** is a common motif for generating a nucleophilic residue for covalent catalysis
- The acid residue (**Asp, Glu**) aligns and polarizes the base (**His, Lys**), which activates the nucleophile (**Ser, Cys, Thr**). The nucleophilic residue then attacks the substrate.
- An **oxyanion hole** in the enzyme (usually formed by backbone amides) stabilizes the negative charge on the **alkoxide ( $\text{RO}^-$ )** during catalysis.
- Present in many <sup>水解酶</sup>hydrolases, including proteases, amidases, esterases, acylases, lipases,  $\beta$ -lactamases, etc.

生成共价催化的亲核残基



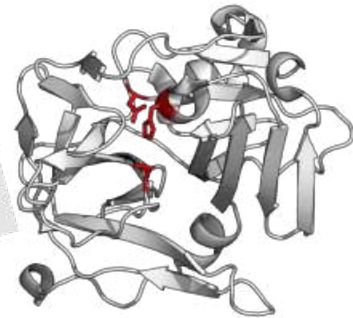
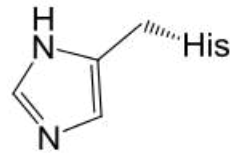
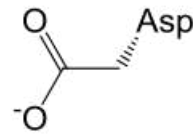
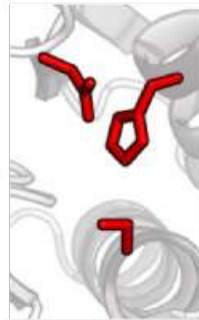
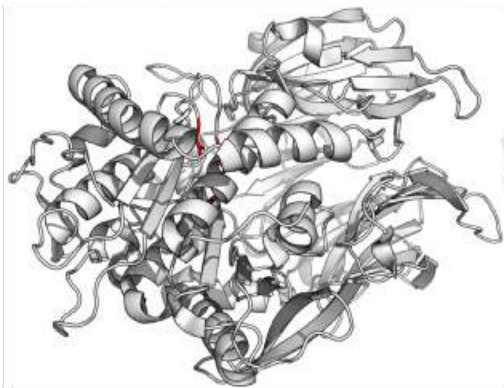
# Catalytic triad and Convergent evolution

催化三联体空间位置存在趋同演化



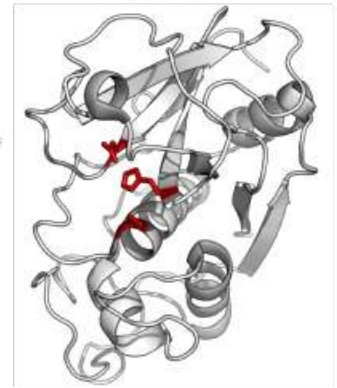
Subtilisin

Prolyl oligopeptidase

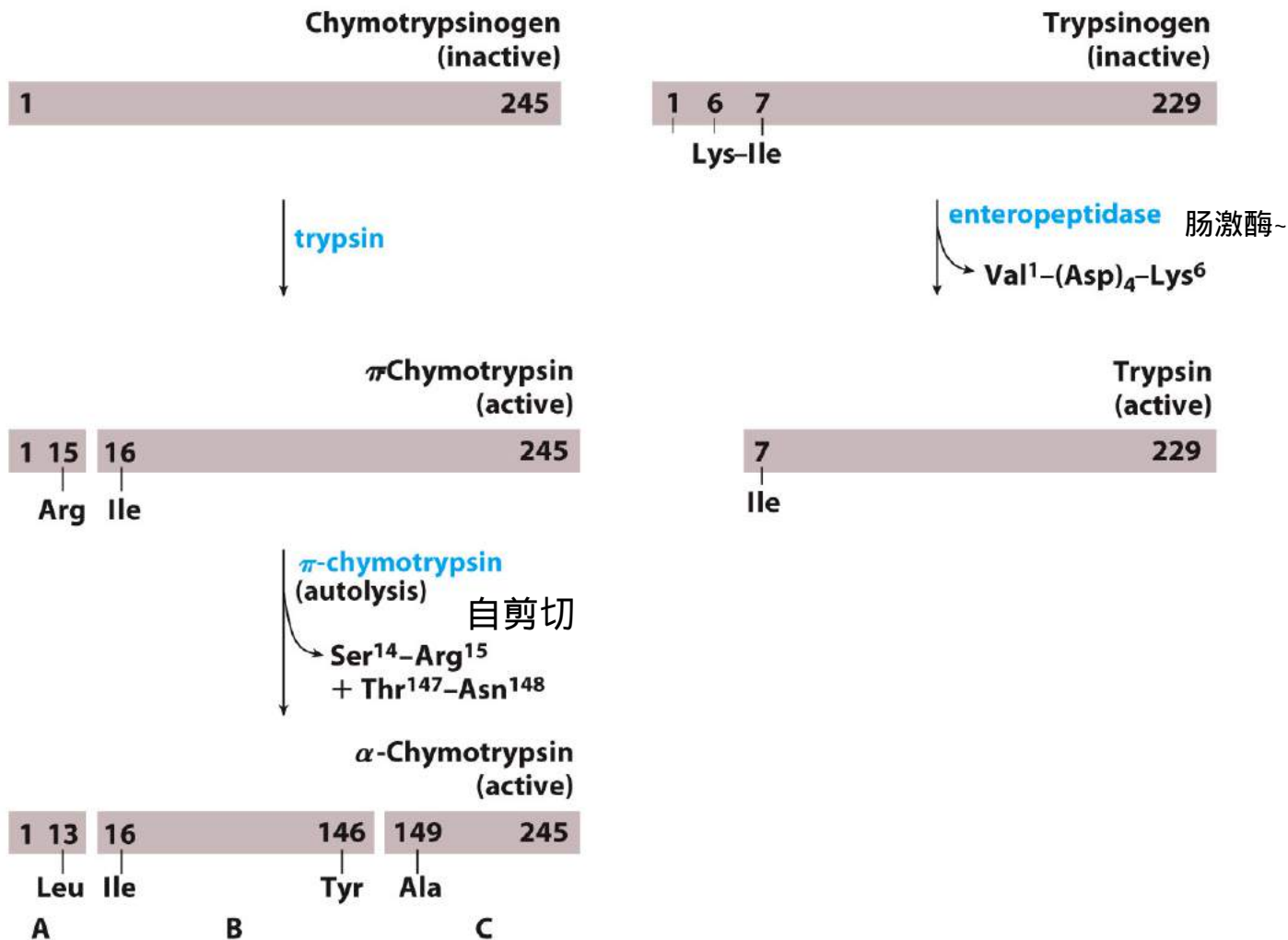


TEV protease

Papain



**Zymogens** are activated by irreversible covalent modification



# Control of Enzymes

Five means to regulate enzymatic activity:

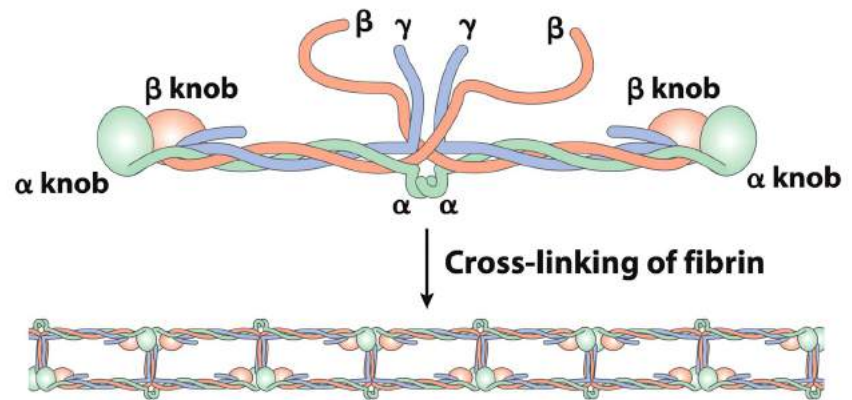
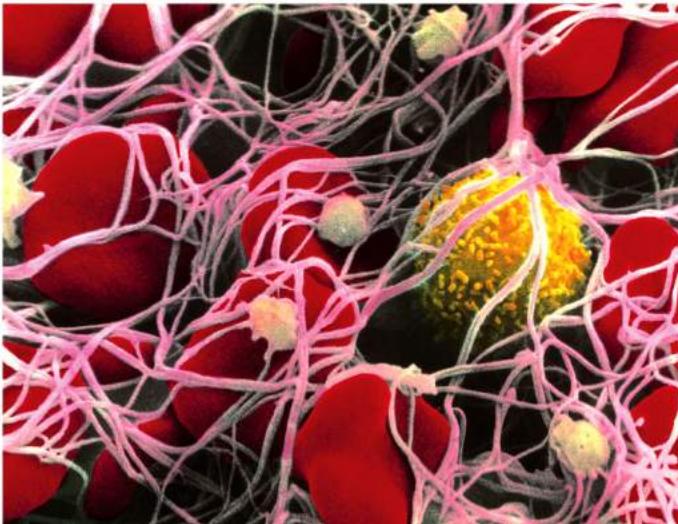
1. Multiple Forms of Enzymes 同工酶
2. Controlling the Amount of Enzyme Present
3. **Proteolytic Activation**
4. **Reversible Covalent Modification**
5. **Allosteric Control**

Many enzymes are regulated by multiple mechanisms.

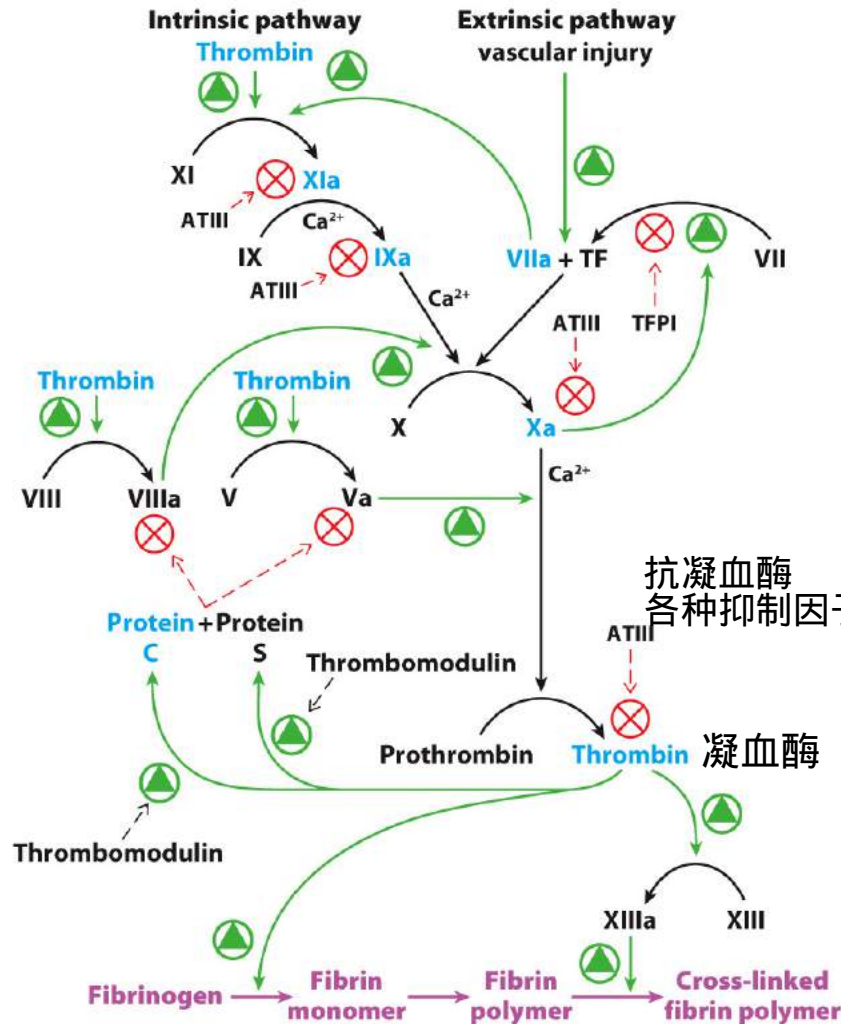


# Blood clotting (Coagulation)

- Coagulation (also known as clotting) is the process by which blood changes from a liquid to a gel, forming a blood clot.
- A blood clot consists of aggregated **platelets** and red blood cells (erythrocytes), which are tied together by cross-linked fibrin.



# The coagulation cascade



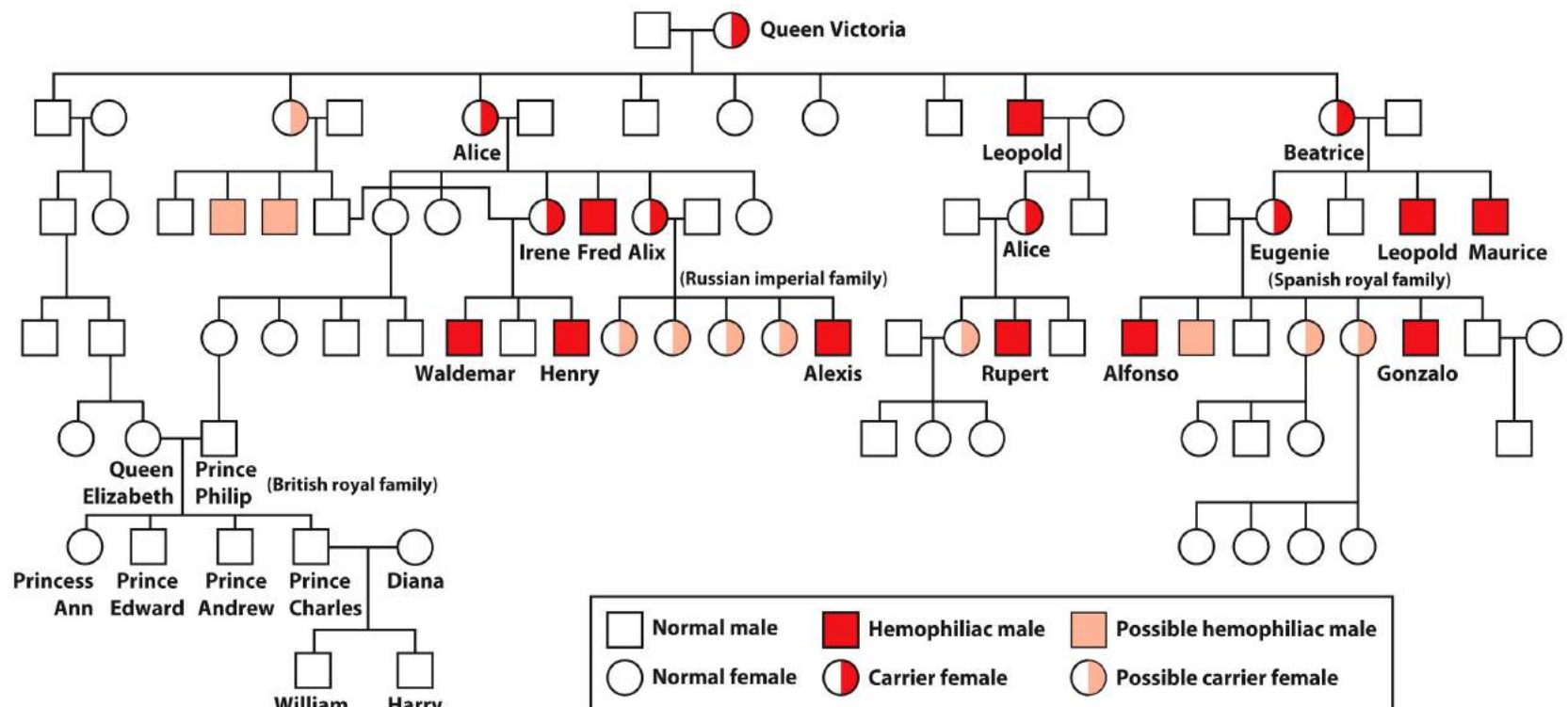
Blood clotting cascades can be initiated in two different ways that lead to a common end point.

- The **extrinsic pathway** is activated by the **tissue factor (TF)**.
- The **intrinsic pathway** is initiated by exposure of **anionic surfaces of damaged tissue**.

Most of the protein factors in the coagulation cascade are designated by Roman numerals.

Many of these factors are chymotrypsin-like serine proteases that have zymogen precursors (the activated forms are indicated by a subscript "a").

# Coagulation defects can cause hemorrhage or thrombosis



血友病A

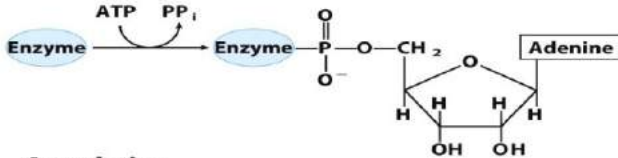
Hemophilia A, the royal disease, is caused by defect in the gene for factor **VIII**, which is located on the X chromosome

## Covalent modification (Target residues)

### Phosphorylation (Tyr, Ser, Thr, His)



### Adenylylation 腺苷化 (Tyr)



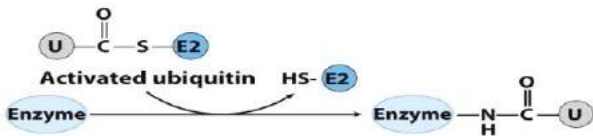
### Acetylation (Lys, α-amino (amino terminus))



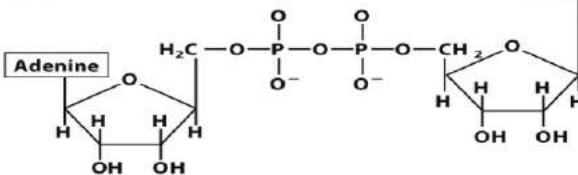
### Myristoylation (α-amino (amino terminus))



### Ubiquitination (Lys)

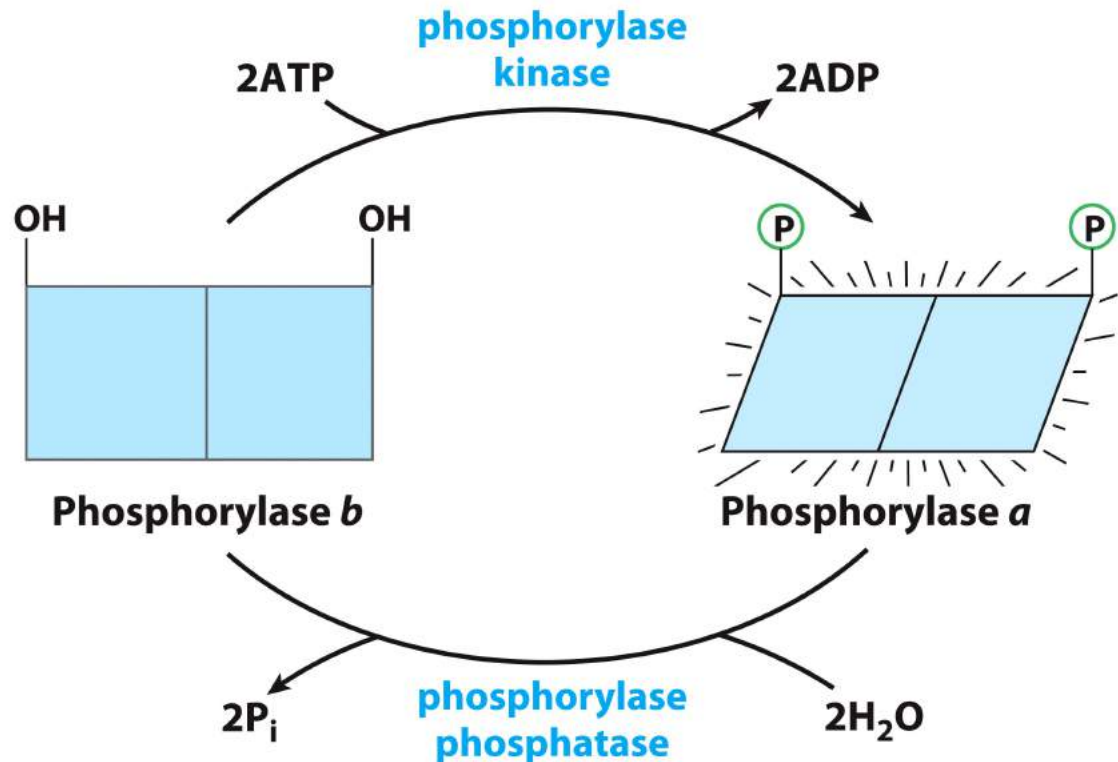


### ADP-ribosylation ADP核糖基化 (Arg, Gln, Cys, diphthamide—a modified His)

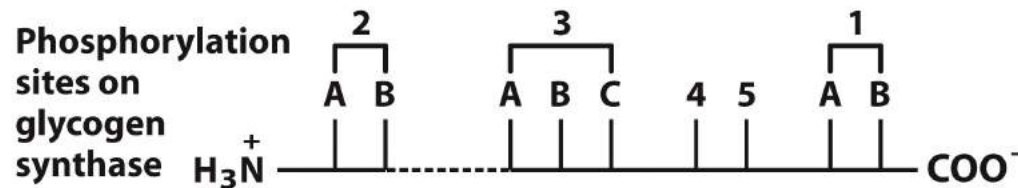


### Methylation (Glu)

# Enzyme regulation by covalent modification



# Multiple phosphorylation allow exquisite regulatory control



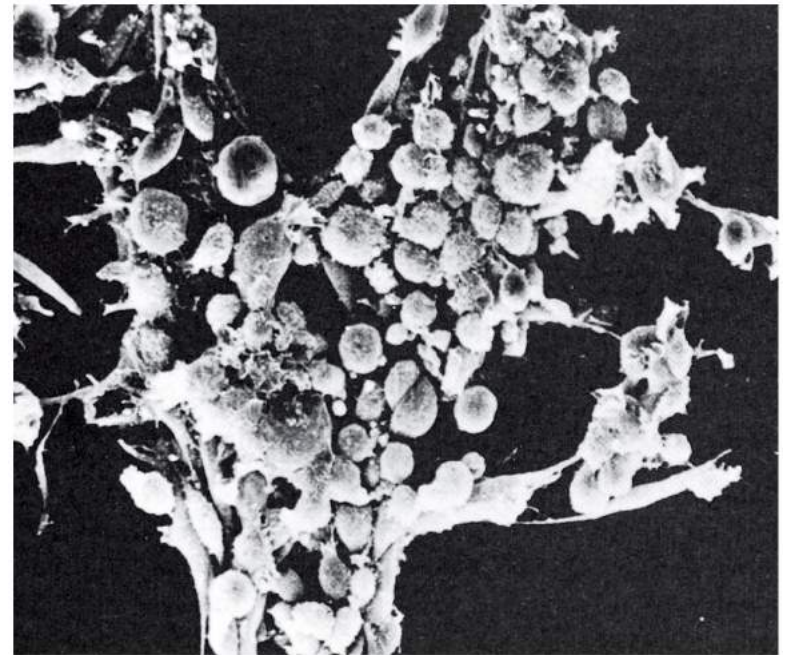
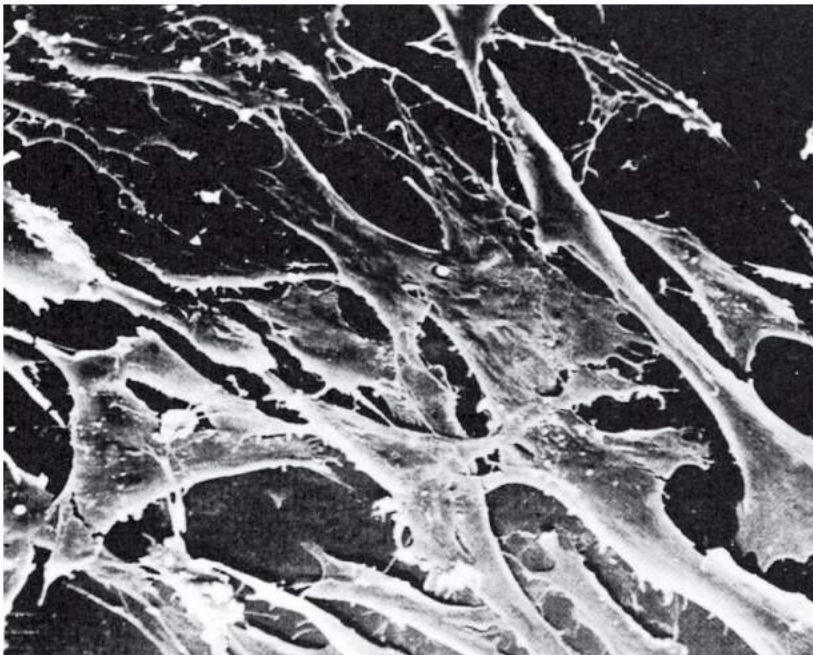
| Kinase                              | Phosphorylation sites | Degree of synthase inactivation |
|-------------------------------------|-----------------------|---------------------------------|
| Protein kinase A                    | 1A, 1B, 2, 4          | +                               |
| Protein kinase G                    | 1A, 1B, 2             | +                               |
| Protein kinase C                    | 1A                    | +                               |
| Ca <sup>2+</sup> /calmodulin kinase | 1B, 2                 | +                               |
| Phosphorylase <i>b</i> kinase       | 2                     | +                               |
| Casein kinase I                     | At least nine         | + + + +                         |
| Casein kinase II                    | 5                     | 0                               |
| Glycogen synthase kinase 3          | 3A, 3B, 3C            | + + +                           |
| Glycogen synthase kinase 4          | 2                     | +                               |

多种磷酸化位点  
多种激酶  
可以实现对酶活性的精细调控



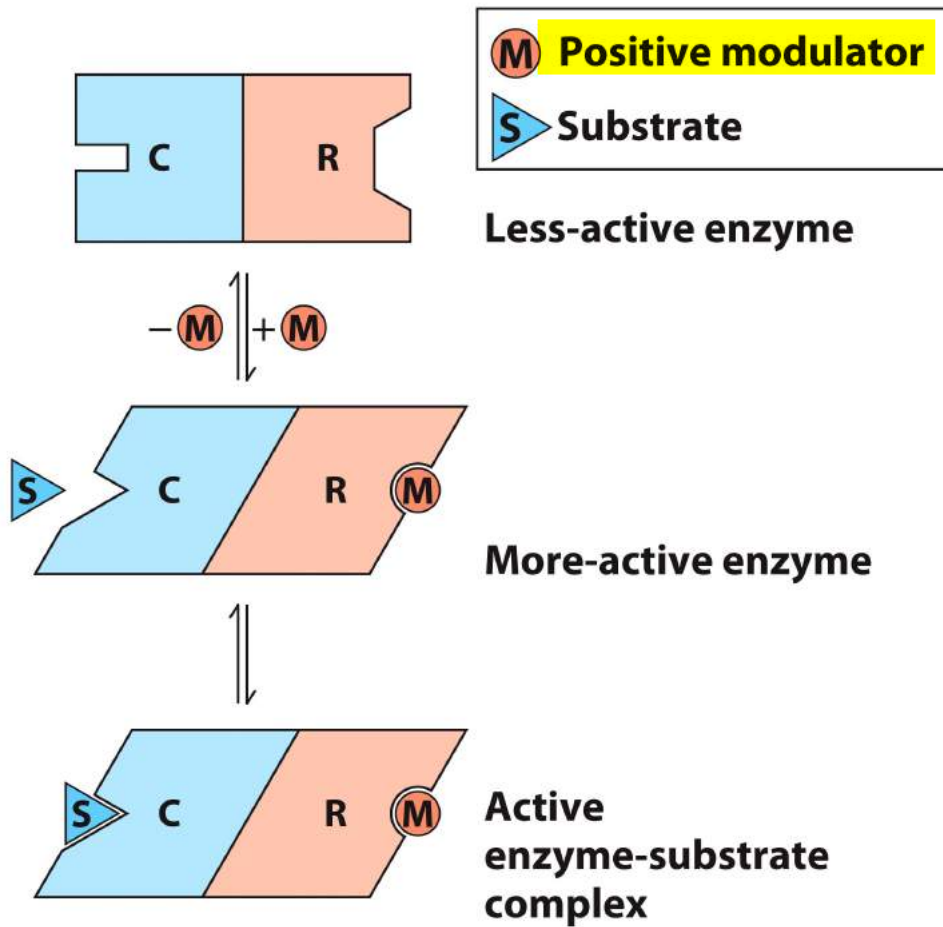
# Loss of normal regulatory control can cause cancer

eg. some kinase lose control, stay active, the cell may keep mitoticing

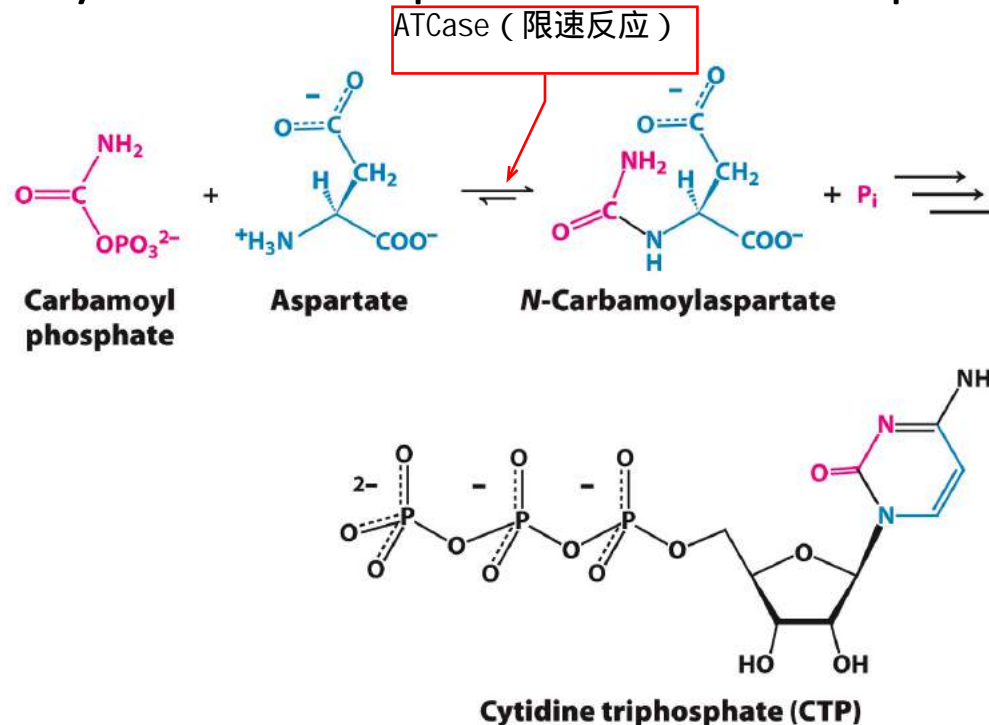




# Allosteric enzymes



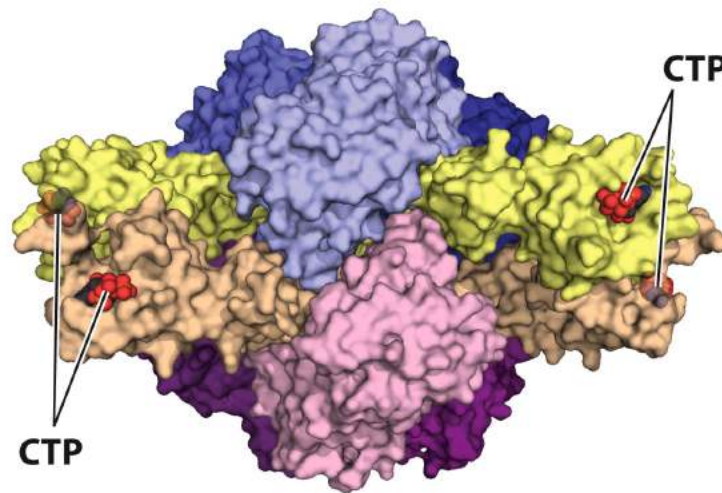
Aspartate transcarbamoylase is allosterically inhibited by the end product of its pathway



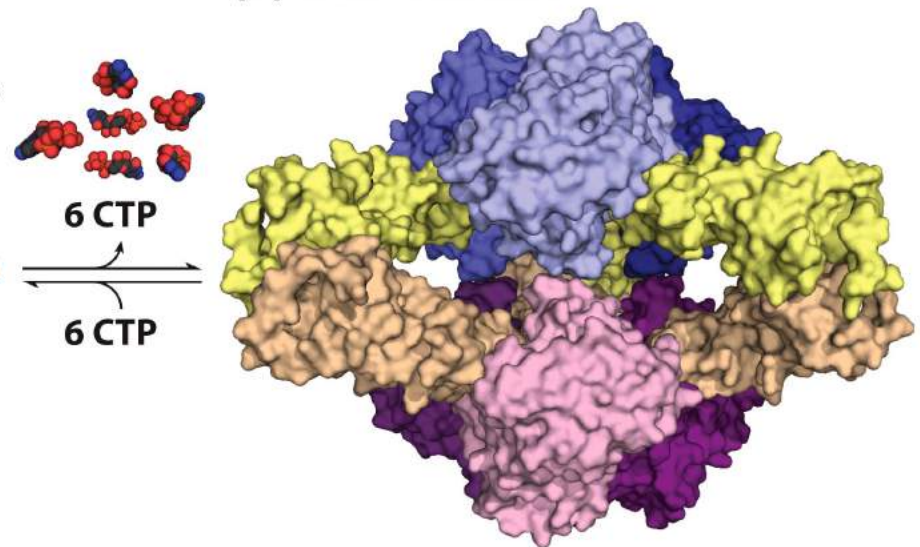
- Aspartate transcarbamoylase catalyzes the committed step, the condensation of aspartate and carbamoyl phosphate to form *N*-carbamoylaspartate, in pyrimidine synthesis.
- ATCase is activated by **ATP** and **Asp** (indicators of robust cellular metabolism), and inhibited by the end **product** of the pathway, **CTP**. 实现ATP\CTP数量的平衡
- ATP and CTP exert their effects by binding at distinct regulatory or allosteric sites on ATCase.

# Allosteric regulation is mediated by conformational changes

**(a) Inactive T state**

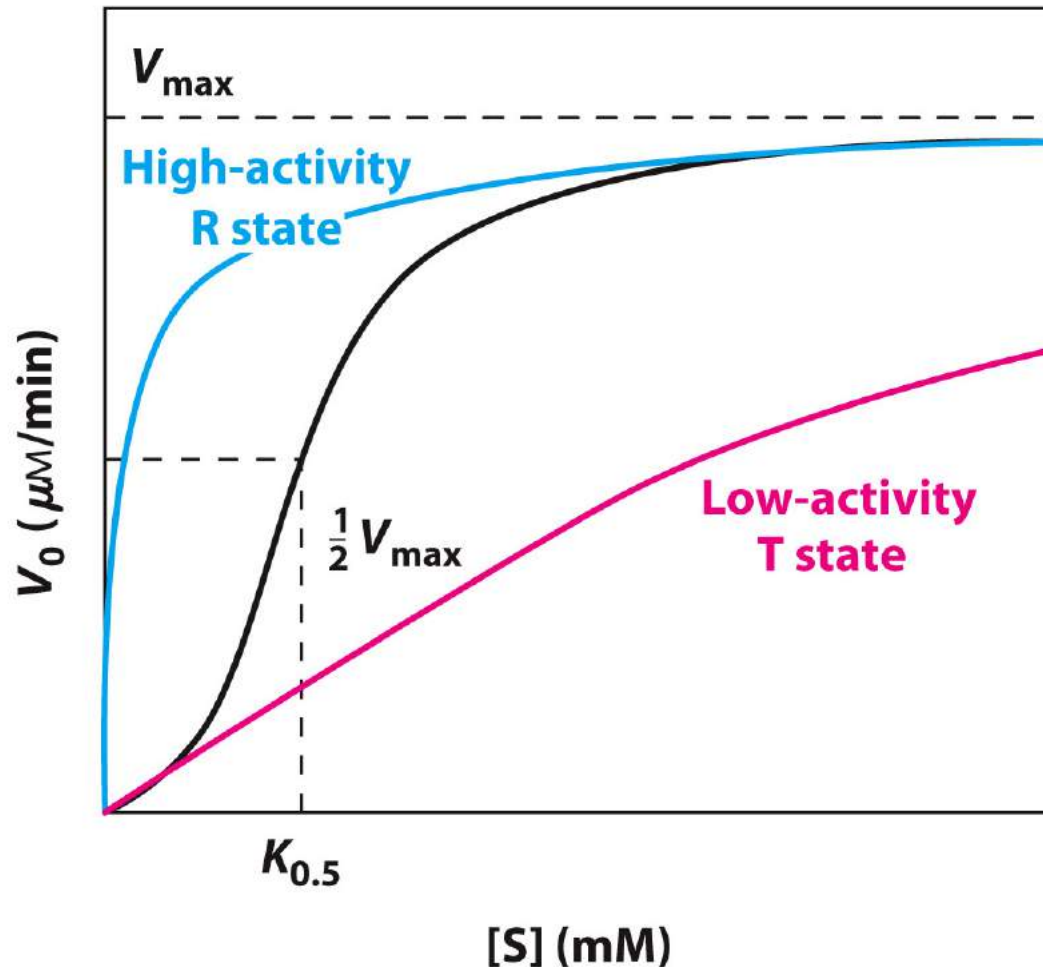


**(b) Active R state**



- Native ATCase consists of six catalytic and six regulatory subunits ( $c_6r_6$ ).
- Free ATCase is in equilibrium between the T state (low activity) and the R state (high activity), with the T state being more favored.
- Binding of CTP to the regulatory site of ATCase alters the T-to-R equilibrium in favor of the T state.
- ATP and Asp alters the T-to-R equilibrium in favor of the R state.

The kinetic properties of allosteric enzymes can diverge from Michaelis-Menten behavior

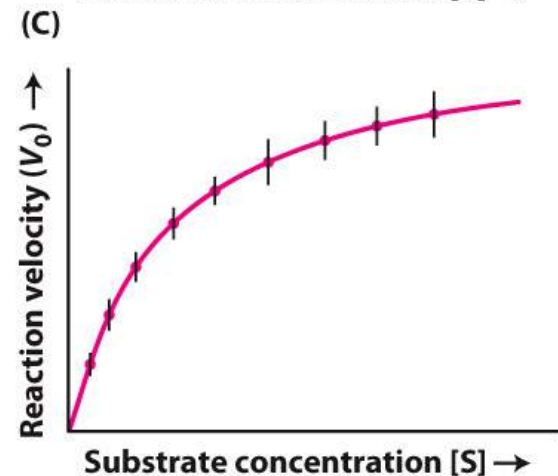
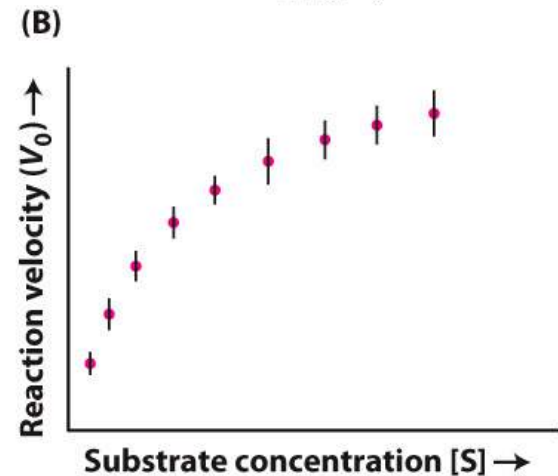
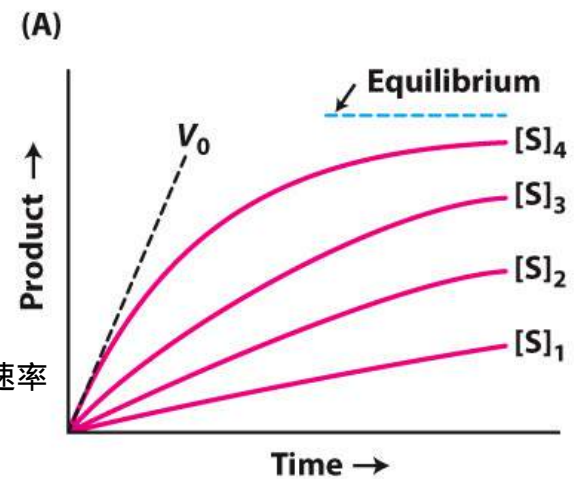


# Kinetics is the study of reaction rates

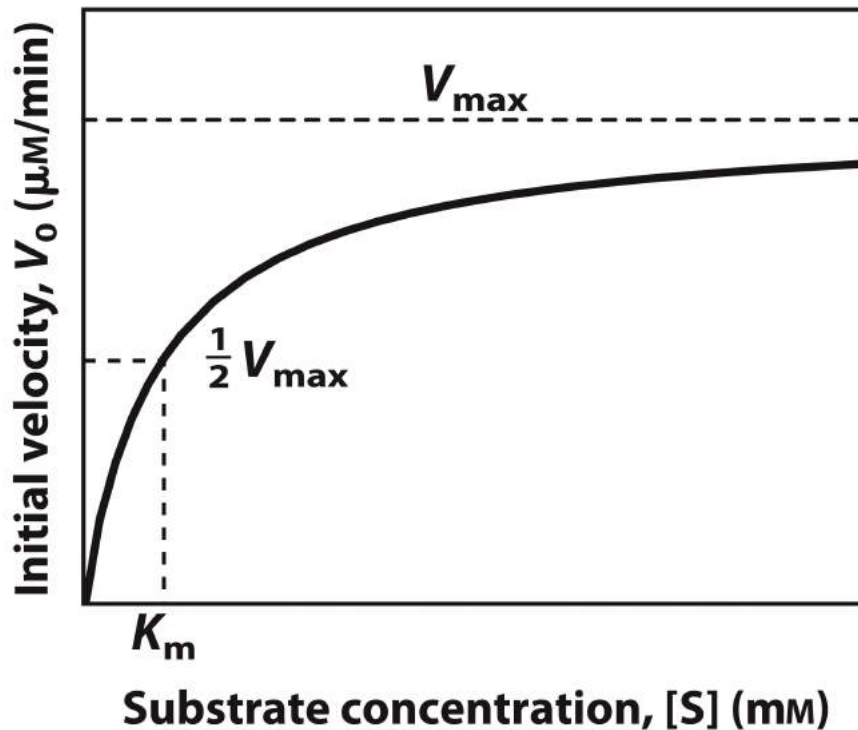
## Experiment:

1. Mix enzyme + substrate.
2. Record rate of substrate disappearance and/or product formation as a function of time (the velocity of reaction).
3. Plot initial velocity versus substrate concentration.

估算 $v_0$ 时的反应速率



# The Michaelis-Menten equation



$$V_o = V_{\text{max}} \frac{[S]}{[S] + K_M}$$

When  $V_o = \frac{1}{2} V_{\text{max}}$ ,  $K_M = [S]$ .

$K_M$  is the substrate concentration that yields  $\frac{1}{2} V_{\text{max}}$ .



Leonor Michaelis  
1875–1949

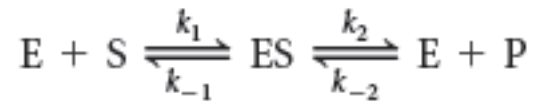


Maud Menten  
1879–1960

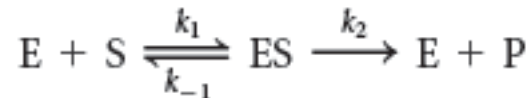


deduce(推导)

Consider a simple reaction in which the enzyme E catalyzes the conversion of  $S \rightarrow P$ .



with  $k_1$ ,  $k_2$ ,  $k_{-1}$  and  $k_{-2}$  being the rate constants for the indicated reaction steps. So as to ignore the reverse reaction of  $P \rightarrow S$ , we measure activity when  $[P] \approx 0$ .



Under these conditions, the velocity is called the **initial velocity** or  **$V_0$** .

初速度

$$V_0 = k_2[ES]$$

用产物生成的速率代表 $V_0$

At the **steady-state**, the rate of formation of ES is equal to the rate of its breakdown.  
Thus

$$k_1[E][S] = (k_{-1} + k_2)[ES]$$

This equation can be rearranged to

$$[E][S]/[ES] = (k_{-1} + k_2)/k_1$$

**We can define a new constant,  $K_M$ , called the Michaelis constant.**

$$K_M = \frac{k_{-1} + k_2}{k_1}$$

$K_M$ 的动力学含义

Thus

$$[E][S]/[ES] = (k_{-1} + k_2)/k_1$$

becomes

$$[ES] = \frac{[E][S]}{K_M}$$

The amount of free enzyme is equal to the total amount of enzyme present minus any enzyme bound to substrate.

$$[E] = [E]_T - [ES]$$

Substituting this equation for [E] in  $[ES] = \frac{[E][S]}{K_M}$

yields  $[ES] = \frac{([E]_T - [ES])[S]}{K_M}$

This equation can be rearranged to yield

$$[ES] = [E]_T \frac{[S]}{[S] + K_M}$$

Recall that

$$V_0 = k_2[ES]$$

Thus,

$$V_0 = k_2[E]_T \frac{[S]}{[S] + K_M}$$

# The Michaelis-Menten equation

The maximal rate of catalysis,  $V_{\max}$ , occurs when all of the enzyme is bound to substrate

$$[ES] = [E]_T$$

$$V_{\max} = k_2[E]_T$$

Substituting the equation for  $V_{\max}$  into  $V_0 = k_2[E]_T \frac{[S]}{[S] + K_M}$

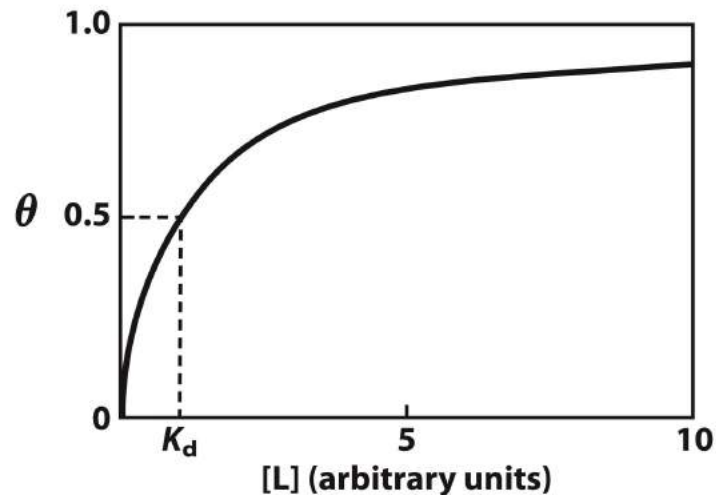
yields the **Michaelis-Menten equation**

$$V_0 = V_{\max} \frac{[S]}{[S] + K_M}$$

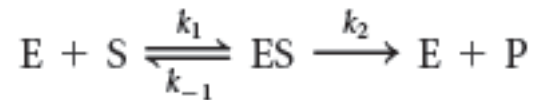
# Still remember $K_d$ ?

$K_d$  equals to the molar concentration of free ligand concentration at which half of available binding sites are occupied.

$$\theta = \frac{[L]}{[L] + K_d}$$



# $K_M$ vs. $K_d$



$$K_M = \frac{k_{-1} + k_2}{k_1}$$

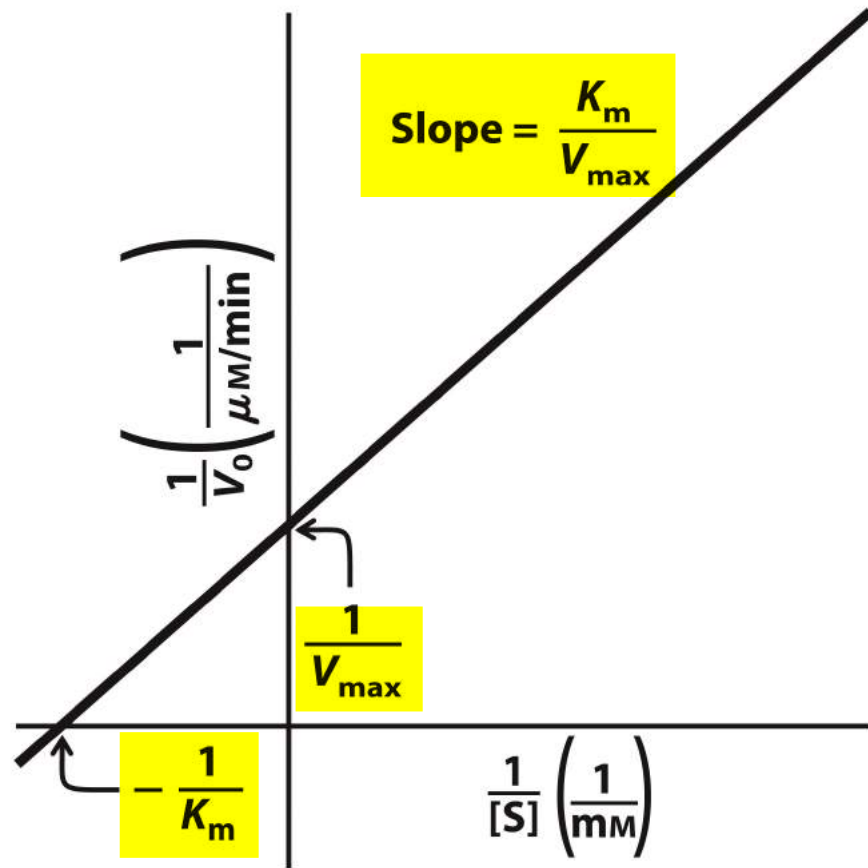
$$K_d = k_{-1}/k_1$$

- If  $k_2$  is rate-limiting,  $k_2 \ll k_{-1}$ ,  $K_M = k_{-1}/k_1$ , which equals to the dissociation constant ( $K_d$ ) of the ES complex. **Under this condition**,  $K_M$  represents a measure of affinity of the enzyme for its substrate in the ES complex (lower  $K_M$ , higher affinity and vice versa).
- If  $k_2 \gg k_{-1}$ , then  $K_M = k_2/k_1$ .
- If  $k_2$  and  $k_{-1}$  are comparable,  $K_M$  is a complex function of all three rate constants.



# The Lineweaver-Burk plot (Double-Reciprocal Plot)

双倒数作图



$$V = \frac{V_{\max}[S]}{K_m + [S]}$$

Taking the reciprocal gives

$$\frac{1}{V} = \frac{K_m + [S]}{V_{\max}[S]} = \frac{K_m}{V_{\max}} \frac{1}{[S]} + \frac{1}{V_{\max}}$$

Lineweaver & Burk (1934) The Determination of Enzyme Dissociation Constants, *J. Ame. Chem.Soc.* 56: 658–666.



Dean Burk  
(1904-1988)



Hans Lineweaver  
(1907-2009)

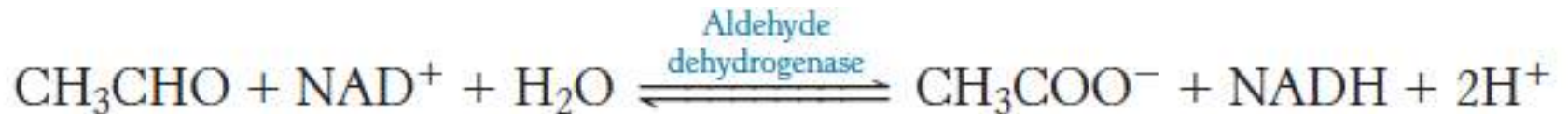
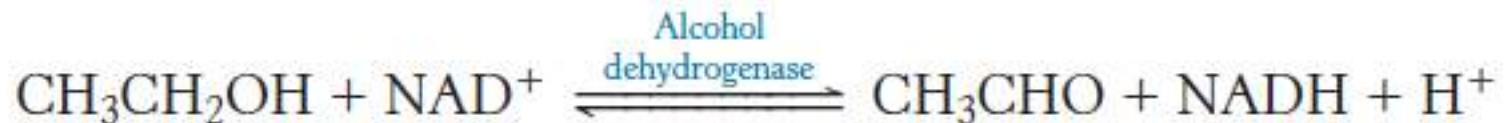
$K_M$  is a constant for each substrate of an enzyme at a defined condition

**TABLE 6-6**  $K_m$  for Some Enzymes and Substrates

| Enzyme                     | Substrate              | $K_m$ (mM) |
|----------------------------|------------------------|------------|
| Hexokinase (brain)<br>己糖激酶 | ATP                    | 0.4        |
|                            | D-Glucose              | 0.05       |
|                            | D-Fructose             | 1.5        |
| Carbonic anhydrase         | $\text{HCO}_3^-$       | 26         |
| Chymotrypsin               | Glycyltyrosinylglycine | 108        |
|                            | N-Benzoyltyrosinamide  | 2.5        |
| $\beta$ -Galactosidase     | D-Lactose              | 4.0        |
| Threonine dehydratase      | L-Threonine            | 5.0        |

# Physiological implications of $K_M$ : an example

Two enzymes play a key role in the metabolism of alcohol.



Some people respond to alcohol consumption with facial flushing and rapid heart beat, symptoms caused by excessive amounts of acetaldehyde in the blood. There are two different acetaldehyde dehydrogenase in most people, one with a low  $K_M$  and one with a high  $K_M$ . The low  $K_M$  enzyme is inactivated in susceptible individuals. The enzyme with the high  $K_M$  cannot process all of the acetaldehyde, and so some acetaldehyde appears in the blood.

# The turnover number

$$k_{\text{cat}} = V_{\text{max}} / [\text{Enzyme}]$$

$K_m$ 与酶浓度无关，但是 $V_{\text{max}}$ 与酶浓度有关  
把酶浓度除了就是常数了！

$k_{\text{cat}}$  is also called the **turnover number**. It is equivalent to the number of substrate molecules that are converted to product in a given unit of time on a single enzyme (when the enzyme is saturated with substrate)

**TABLE 6-7** Turnover Number,  $k_{\text{cat}}$ , of Some Enzymes

| Enzyme                   | Substrate              | $k_{\text{cat}}$ ( $\text{s}^{-1}$ ) |
|--------------------------|------------------------|--------------------------------------|
| Catalase                 | $\text{H}_2\text{O}_2$ | 40,000,000                           |
| Carbonic anhydrase       | $\text{HCO}_3^-$       | 400,000                              |
| Acetylcholinesterase     | Acetylcholine          | 14,000                               |
| $\beta$ -Lactamase       | Benzylpenicillin       | 2,000                                |
| Fumarase                 | Fumarate               | 800                                  |
| RecA protein (an ATPase) | ATP                    | 0.5                                  |

$k_{\text{cat}}/K_M$  (specificity constant) is a measure of catalytic efficiency

**TABLE 6-8** Enzymes for Which  $k_{\text{cat}}/K_M$  Is Close to the Diffusion-Controlled Limit ( $10^8$  to  $10^9 \text{ M}^{-1}\text{s}^{-1}$ )

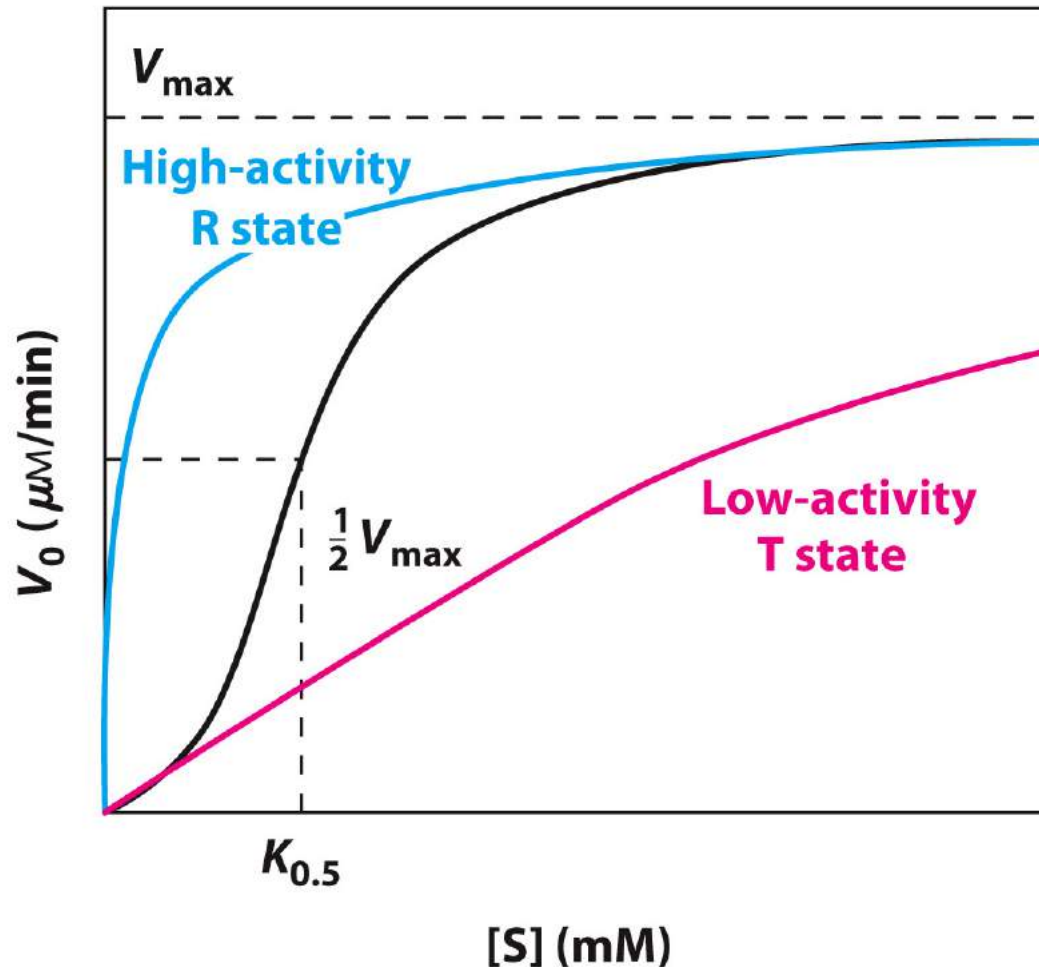
| Enzyme               | Substrate              | $k_{\text{cat}}$<br>( $\text{s}^{-1}$ ) | $K_M$<br>(M)         | $k_{\text{cat}}/K_M$<br>( $\text{M}^{-1}\text{s}^{-1}$ ) |
|----------------------|------------------------|---|----------------------|--|
| Acetylcholinesterase | Acetylcholine          | $1.4 \times 10^4$                       | $9 \times 10^{-5}$   | $1.6 \times 10^8$  |
| Carbonic anhydrase   | $\text{CO}_2$          | $1 \times 10^6$                         | $1.2 \times 10^{-2}$ | $8.3 \times 10^7$  |
|                      | $\text{HCO}_3^-$       | $4 \times 10^5$                         | $2.6 \times 10^{-2}$ | $1.5 \times 10^7$  |
| Catalase             | $\text{H}_2\text{O}_2$ | $4 \times 10^7$                         | $1.1 \times 10^0$    | $4 \times 10^7$  |
| Crotonase            | Crotonyl-CoA           | $5.7 \times 10^3$                       | $2 \times 10^{-5}$   | $2.8 \times 10^8$  |
| Fumarase             | Fumarate               | $8 \times 10^2$                         | $5 \times 10^{-6}$   | $1.6 \times 10^8$  |
|                      | Malate                 | $9 \times 10^2$                         | $2.5 \times 10^{-5}$ | $3.6 \times 10^7$  |
| $\beta$ -Lactamase   | Benzylpenicillin       | $2.0 \times 10^3$                       | $2 \times 10^{-5}$   | $1 \times 10^8$  |

Source: Fersht, A. (1999) *Structure and Mechanism in Protein Science*, p. 166, W. H. Freeman and Company, New York.

- The value of  $k_{\text{cat}}/K_M$  has an upper limit. It can be no greater than the rate at which E and S can diffuse together to form ES ( $k_1$ ).
- The most efficient enzymes have  $k_{\text{cat}}/K_M$  values near the diffusion-controlled limit of  $10^8$  to  $10^9 \text{ M}^{-1}\text{s}^{-1}$ . Such enzymes are catalytically perfect.

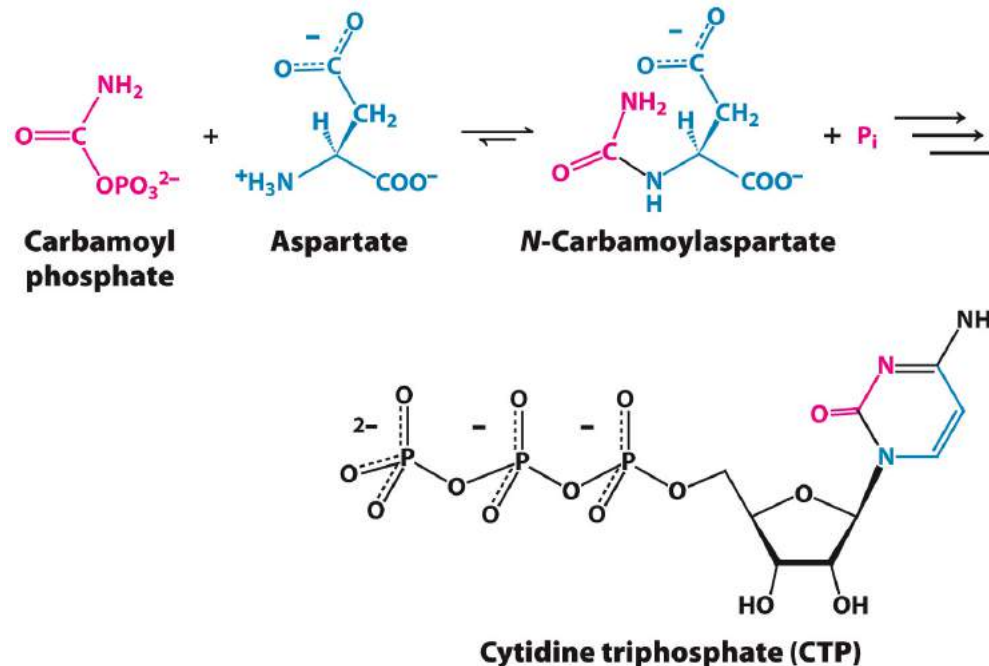
# Not all enzymes display Michaelis-Menten behavior

别构酶不遵循米氏方程！！





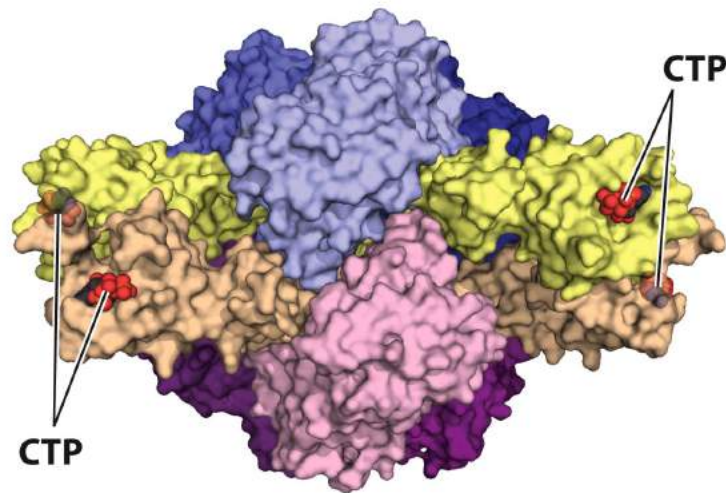
Aspartate transcarbamoylase is allosterically inhibited by the end product of its pathway



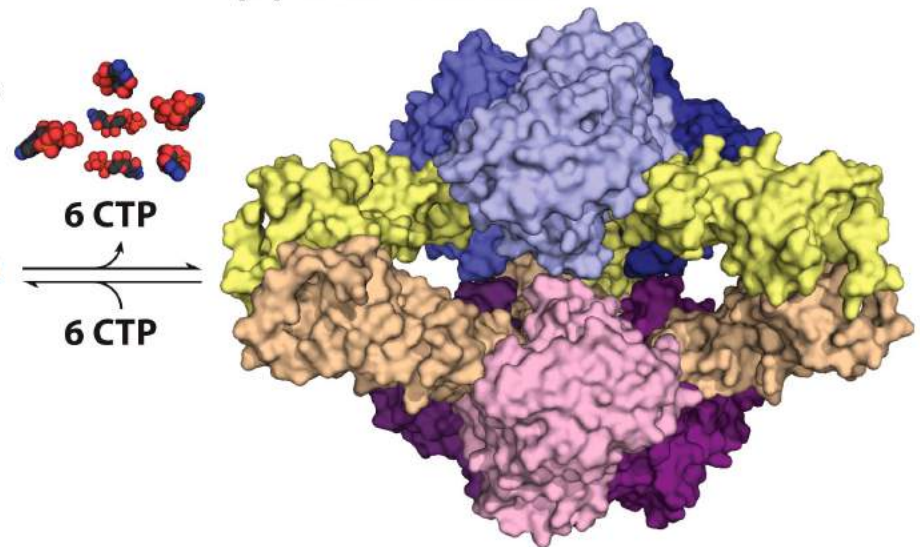
- Aspartate transcarbamoylase catalyzes the committed step, the condensation of aspartate and carbamoyl phosphate to form *N*-carbamoylaspartate, in pyrimidine synthesis.
- ATCase is activated by ATP and Asp (indicators of robust cellular metabolism), and inhibited by the end product of the pathway, CTP.
- ATP and CTP exert their effects by binding at distinct regulatory or allosteric sites on ATCase.

# Allosteric regulation is mediated by conformational changes

**(a) Inactive T state**

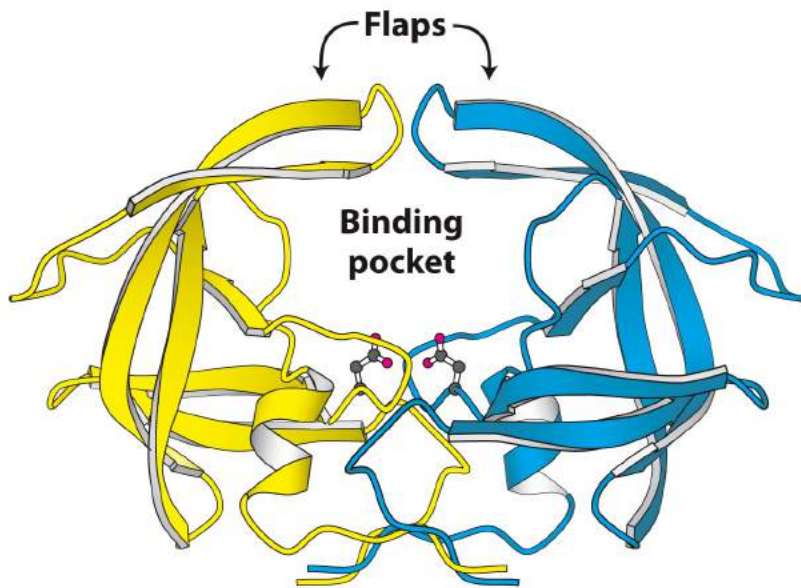


**(b) Active R state**

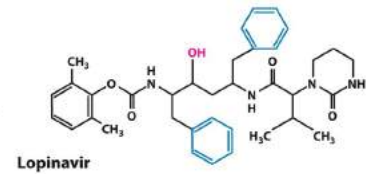


- Native ATCase consists of six catalytic and six regulatory subunits ( $c_6r_6$ ).
- Free ATCase is in equilibrium between the T state (low activity) and the R state (high activity), with the T state being more favored.
- Binding of CTP to the regulatory site of ATCase alters the T-to-R equilibrium in favor of the T state.
- ATP and Asp alters the T-to-R equilibrium in favor of the R state.

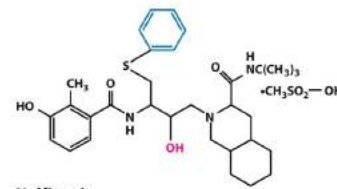
# Enzyme inhibitors



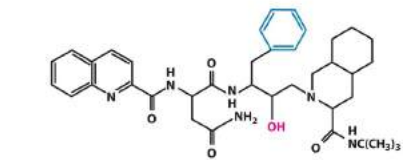
Indinavir



Lopinavir



Nelfinavir



Saquinavir

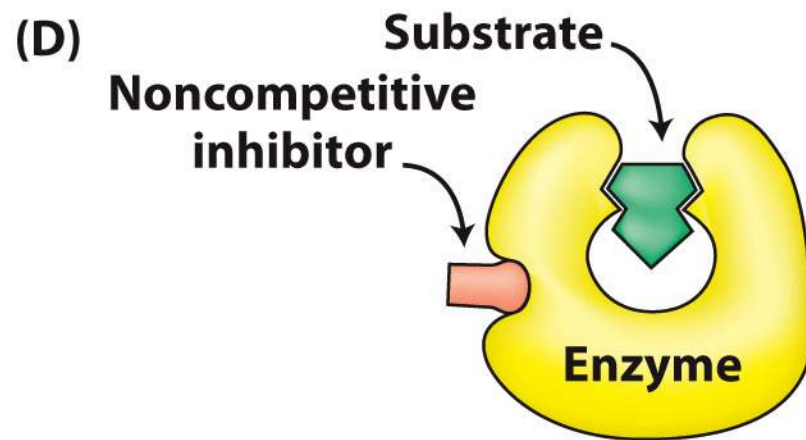
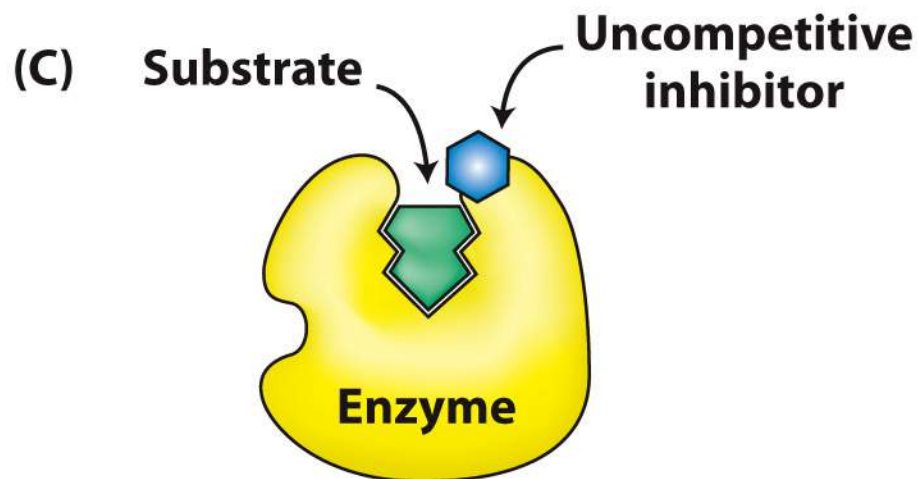
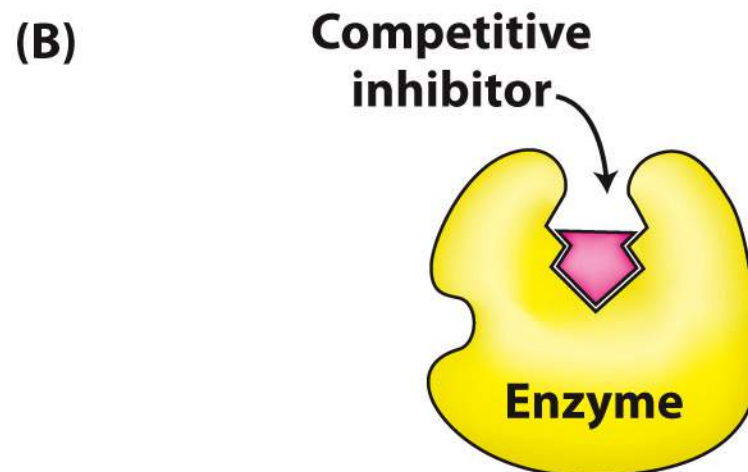
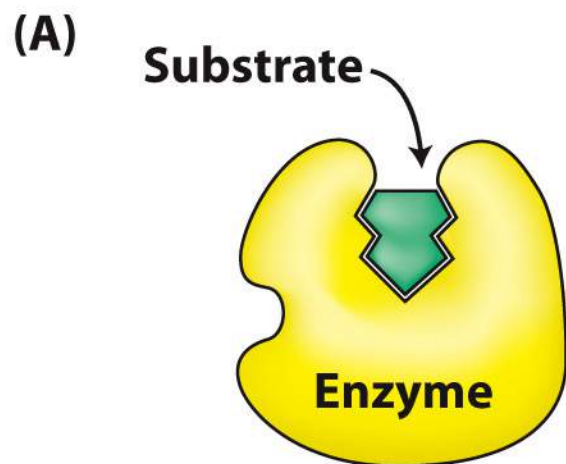
# Enzymes can be inhibited by specific molecules

**Reversible inhibition** is characterized by a rapid dissociation of the enzyme-inhibitor complex.

There are three common types of reversible inhibition:

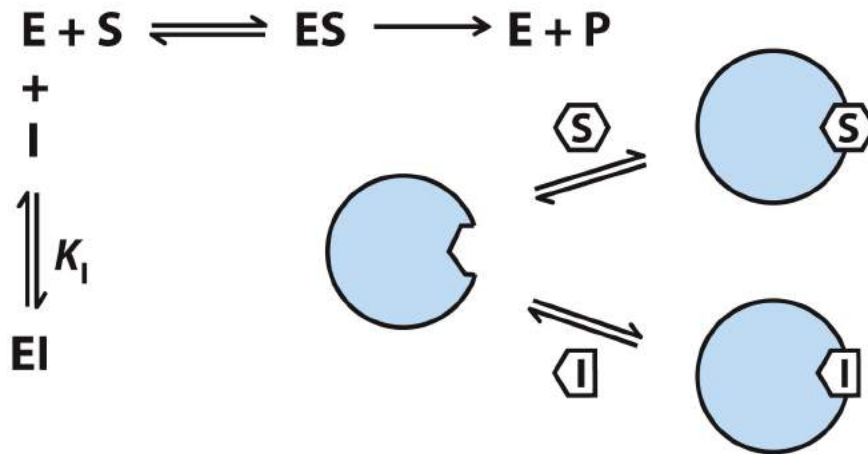
1. **Competitive inhibition**: The inhibitor is structurally similar to the substrate and can **bind to the active site**, preventing the actual substrate from binding.
2. **Uncompetitive inhibition**: The inhibitor **binds only to the enzyme-substrate complex** in what is essentially substrate-dependent inhibition.
3. A **mixed inhibitor** also binds to an allosteric site, but it binds to **either E or ES**. In **Noncompetitive inhibition**, the inhibitor binds to **either E or ES** equally well.

**Irreversible** enzyme inhibitors bind covalently, or noncovalently to the enzyme but with a negligible dissociation constant.



# Competitive Inhibition

## Competitive inhibition



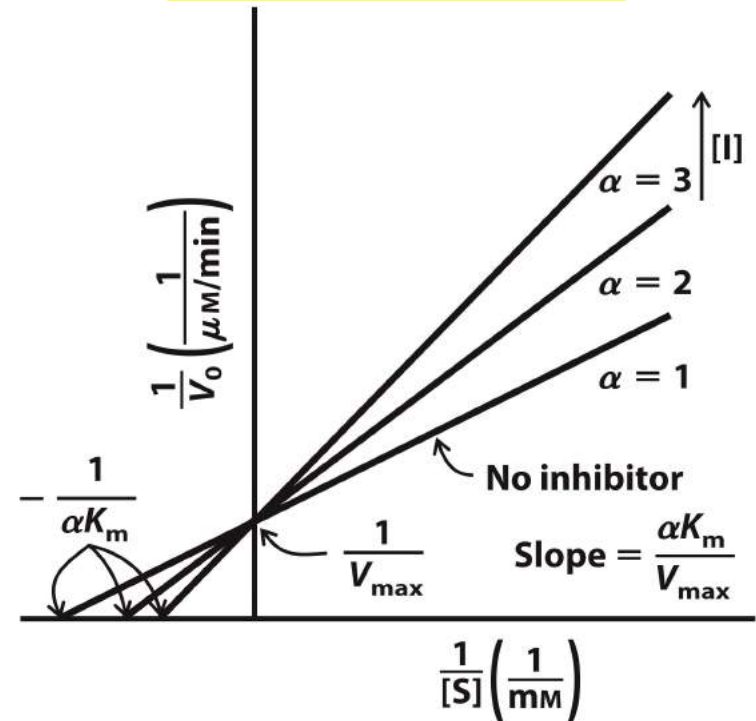
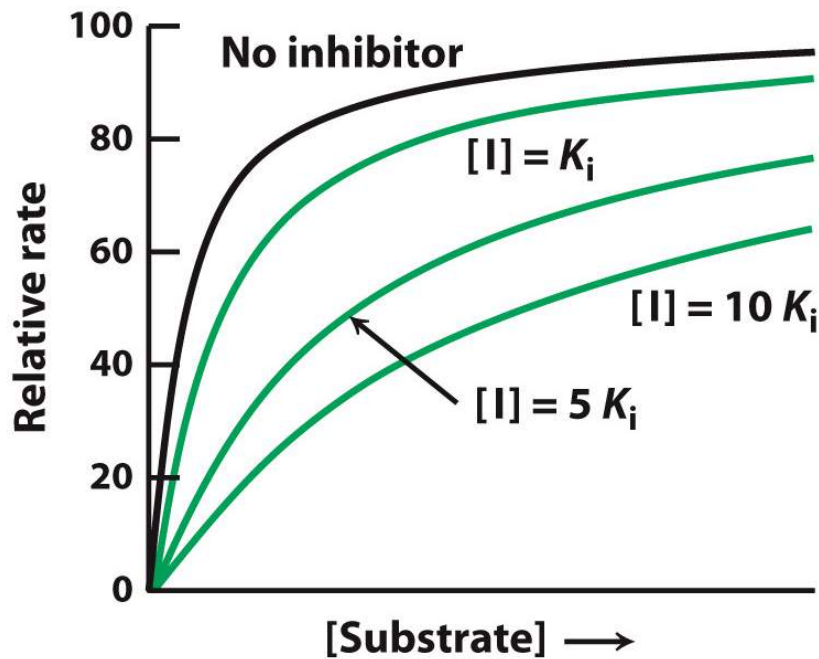
- Competes with substrate for binding
- Does not affect catalysis
- No change in  $V_{\max}$  (because the inhibition can be overcome by a sufficiently high concentration of substrate)
- Increase in apparent  $K_M$



# Competitive Inhibition

$$= (1 + [I] / K_i)$$

$$\frac{1}{V_0} = \left( \frac{\alpha K_m}{V_{\max}} \right) \frac{1}{[S]} + \frac{1}{V_{\max}}$$

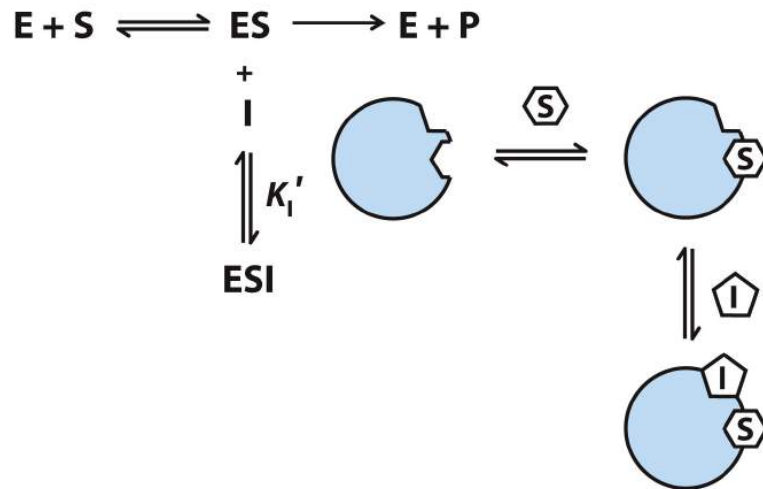


# Uncompetitive Inhibition

反竞争性抑制剂

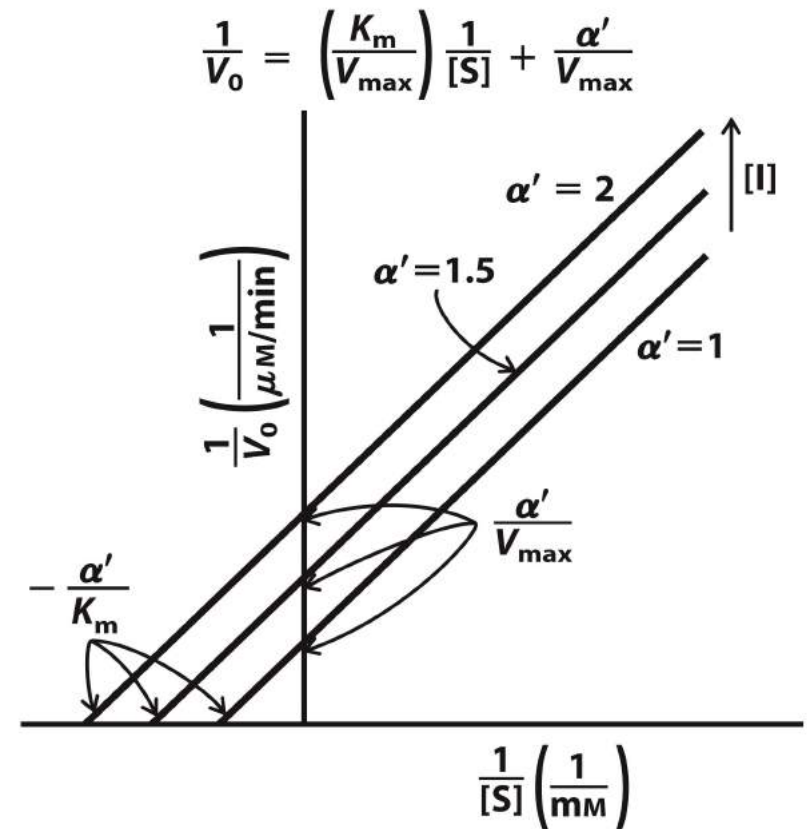
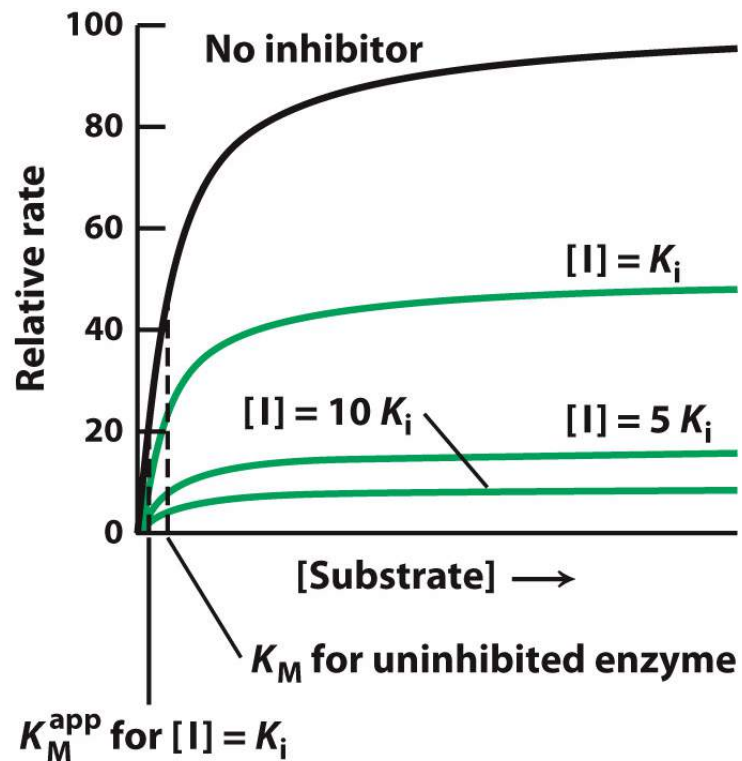


## Uncompetitive inhibition



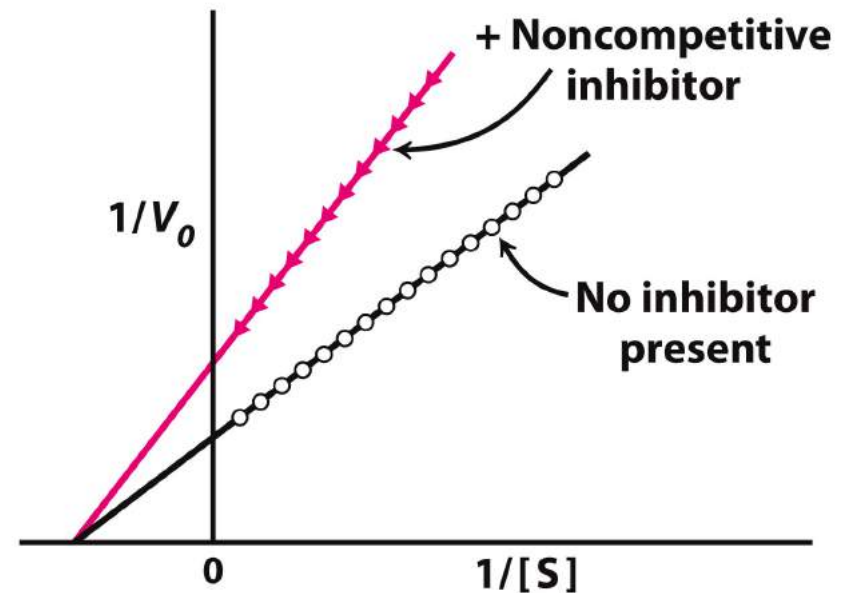
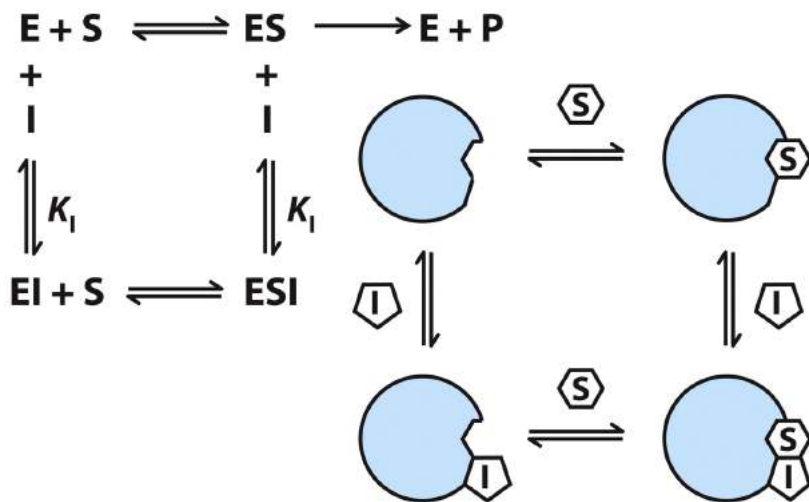
- Only binds to ES complex
- Decrease in  $V_{\max}$
- Apparent decrease in  $K_M$

# Uncompetitive Inhibition



# Noncompetitive inhibition 非竞争性抑制剂

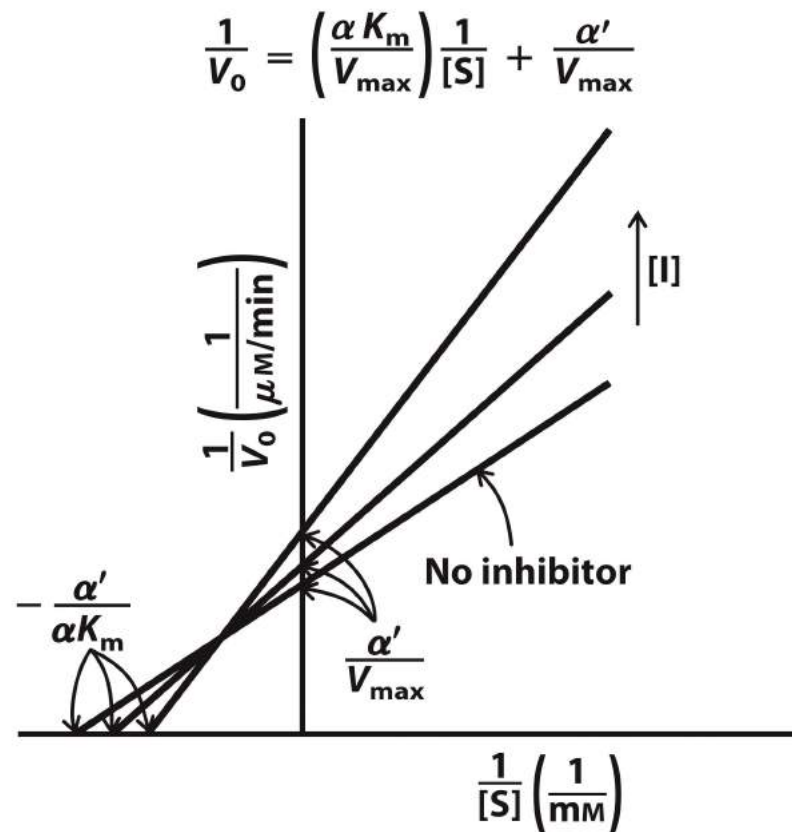
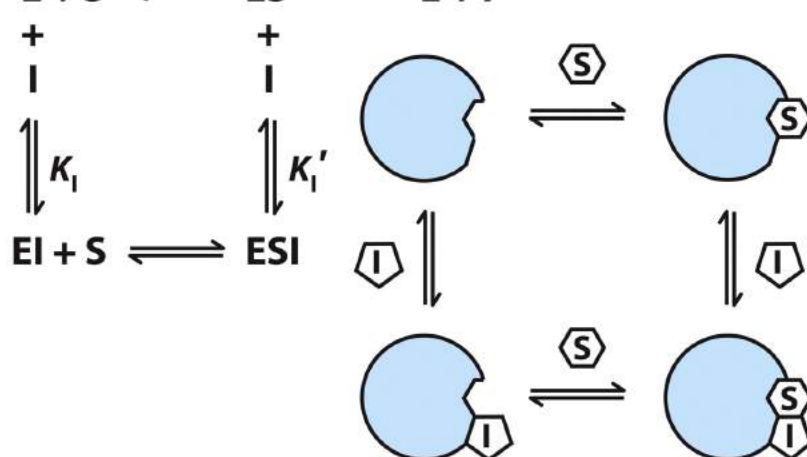
Noncompetitive inhibition



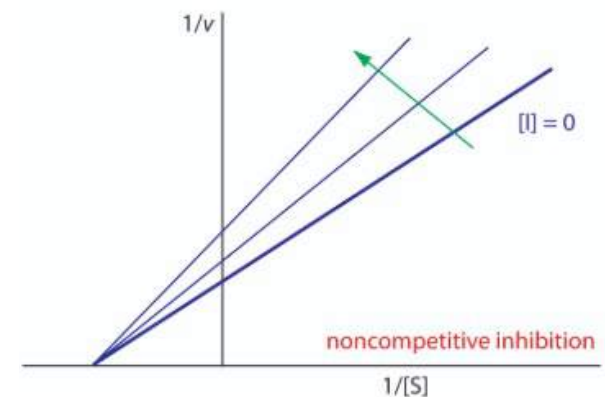
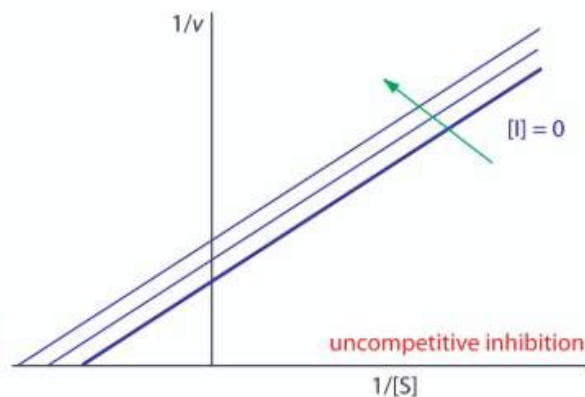
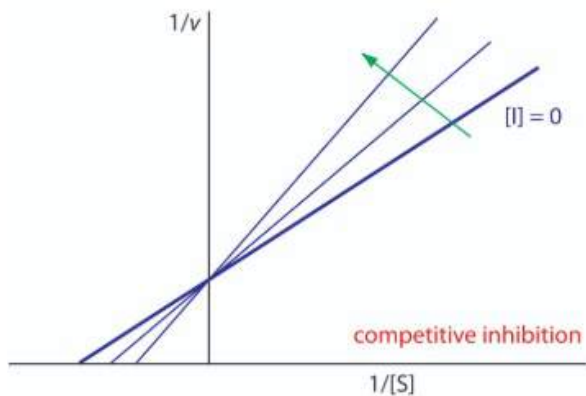
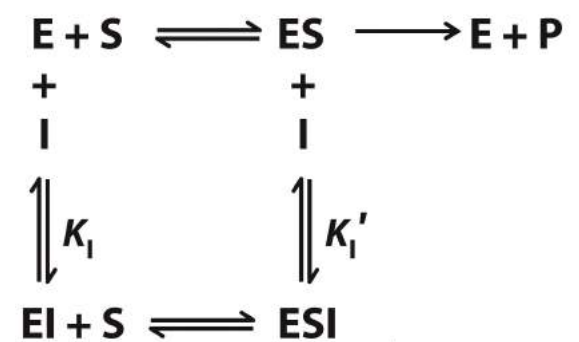
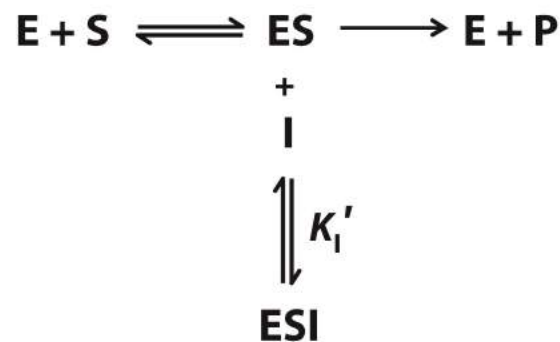
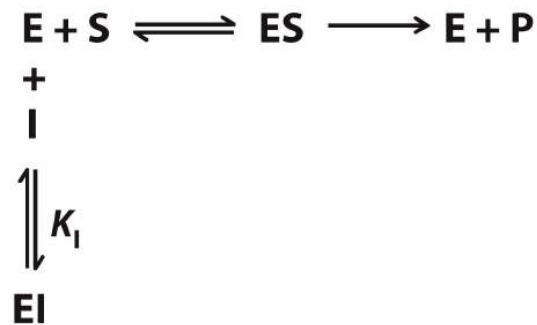
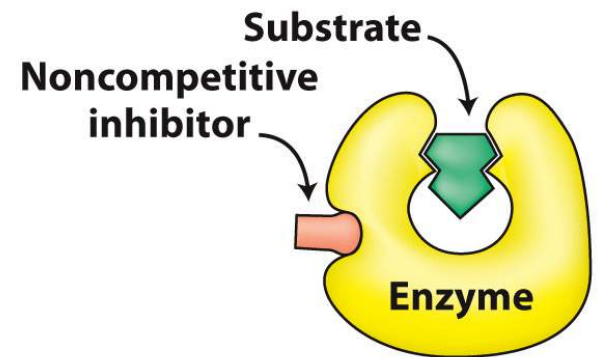
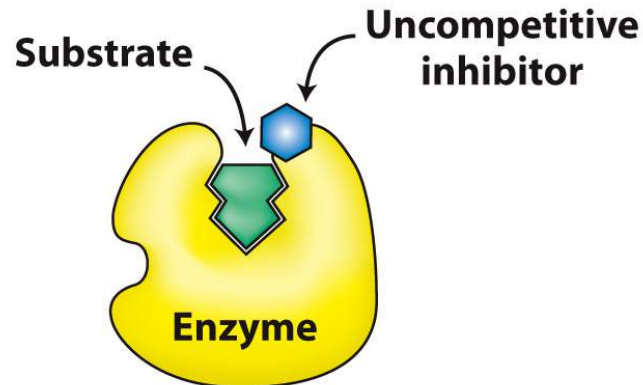
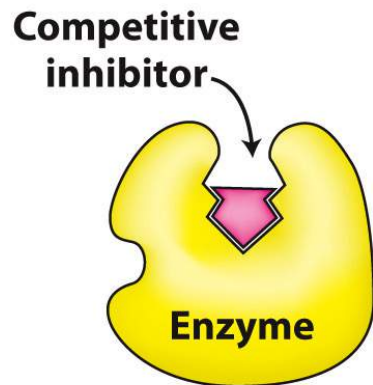
- $K_M$  is not changed.
- $V_{max}$  is lower.
- Lineweaver-Burk: lines intersect at the x-axis.

# A mixed inhibitor binds to either E or ES

## Mixed inhibition



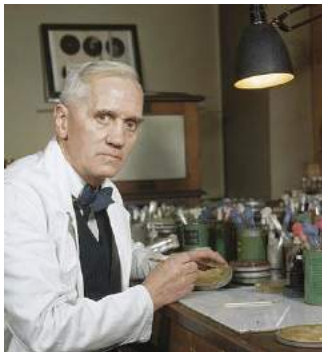
**Vmax下降, Km的改变看情况**  
 (结合E强点还是结合ES强点)  
 结合E强: Km升高, 交点在第二象限  
 结合ES强: Km降低, 交点在第三象限



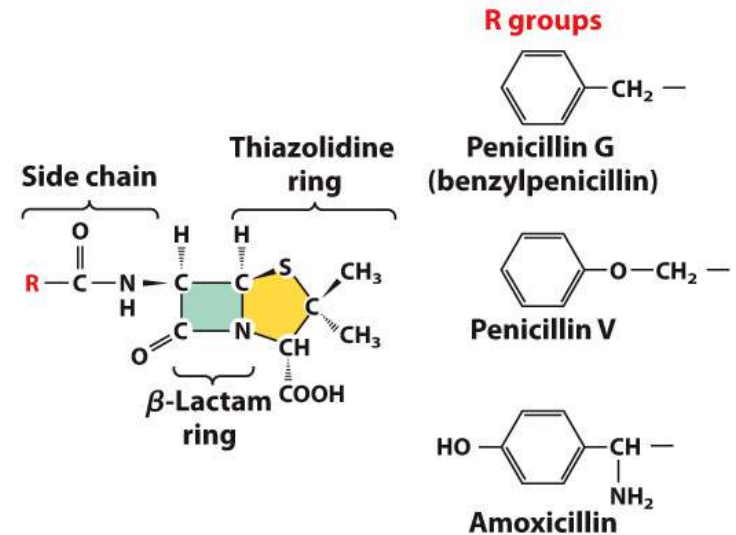


# An irreversible inhibitor: Penicillin

青霉素！

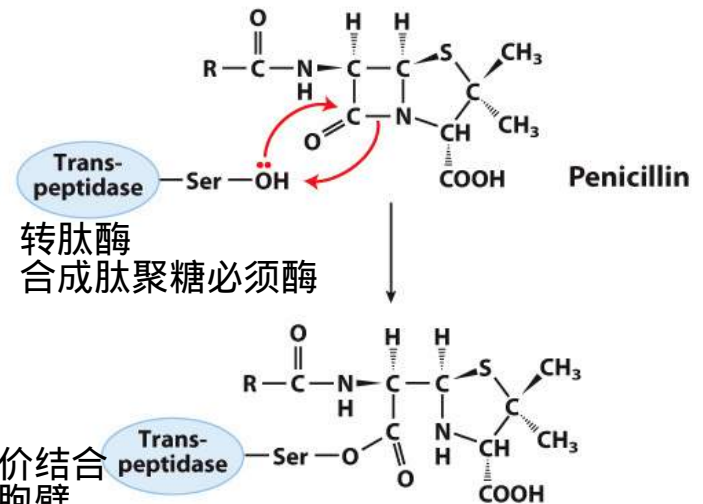


Alexander Fleming  
1945 Nobel Prize



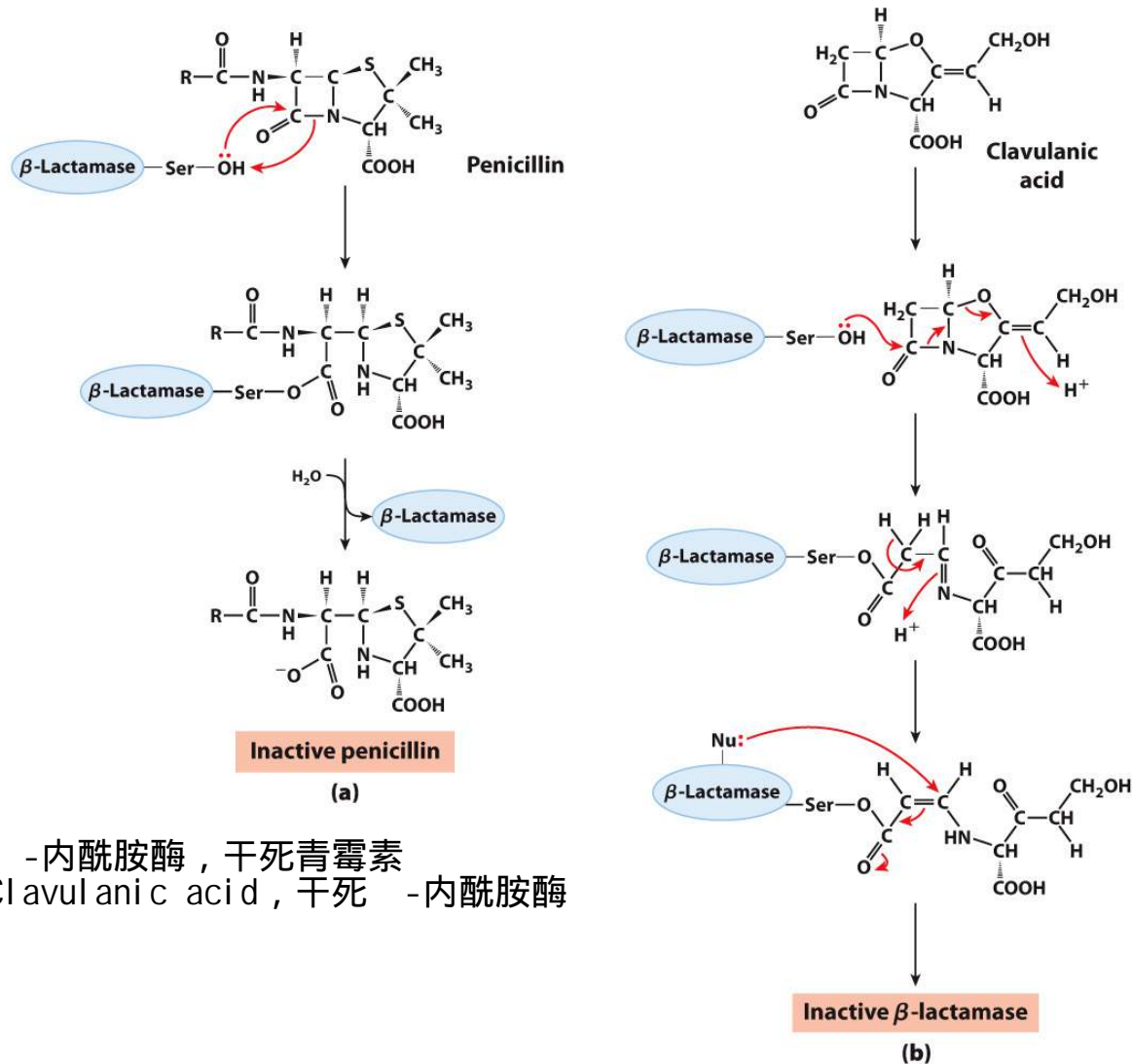
## General structure of penicillins

(a)



青霉素与转肽酶共价结合  
使细菌无法合成细胞壁

# Chemical warfare between us and bacteria continues



细菌产生  $\beta$ -内酰胺酶，干死青霉素  
人再搞出Clavulanic acid，干死  $\beta$ -内酰胺酶

# Most biochemical reactions include multiple substrates



There are two classes of multiple substrate reactions: sequential and double-displacement reactions.

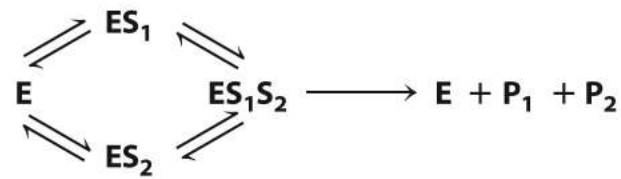
**Sequential reactions**, which may be **random or ordered**, are characterized by the formation of a ternary complex consisting of the enzyme and both substrates.

**Double-displacement reactions** are characterized by the formation of a substituted enzyme intermediate.

**(a) Enzyme reaction involving a ternary complex**



**Random order**

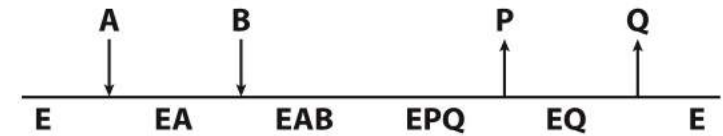


**(b) Enzyme reaction in which no ternary complex is formed**

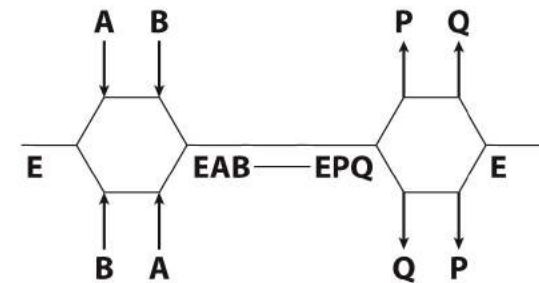


**(c) Cleland nomenclature**

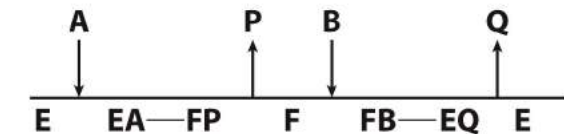
**Ordered bi bi**



**Random bi bi**



**(d) Ping-Pong in Cleland nomenclature**

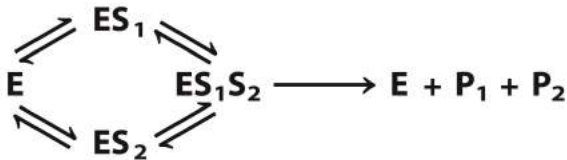


# Enzyme kinetics allows to distinguish between different kinetic mechanisms



## (a) Enzyme reaction involving a ternary complex

Random order



Ordered



## (b) Enzyme reaction in which no ternary complex is formed

