SHC 798 Assignment 2, 2025

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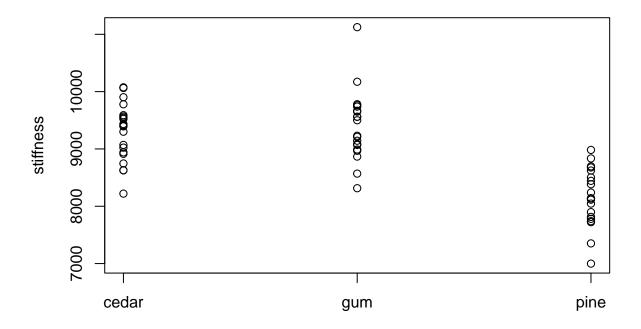
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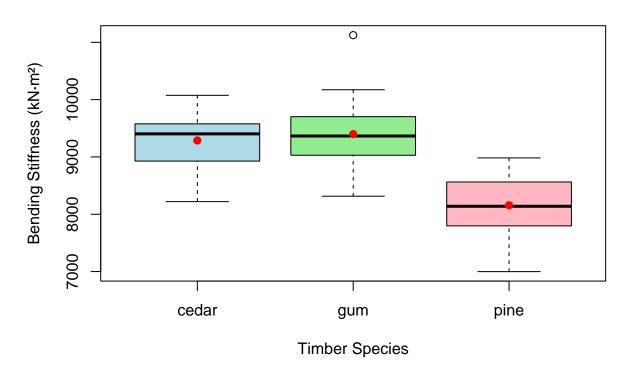
Analysis of Variance (ANOVA)

Question 4: # Compressive strength results

```
pacman::p_load(tidymodels)
# Getting started with the dataset in timber.csv :
timber <- read.csv(file.choose(), header = TRUE, na.strings = c("NA"))</pre>
# timber
head(timber)
     species stiffness
## 1
        pine
                7897.6
## 2
                8239.5
        pine
## 3
        pine
               7740.3
                7722.1
## 4
        pine
## 5
        pine
                8982.9
## 6
        pine
                8696.7
str(timber)
## 'data.frame':
                    60 obs. of 2 variables:
## $ species : chr "pine" "pine" "pine" "pine" ...
## $ stiffness: num 7898 8240 7740 7722 8983 ...
## Convert species column to a factor
timber$species <- factor(timber$species)</pre>
## Check levels
levels(timber$species)
## [1] "cedar" "gum"
                       "pine"
## Visualize data
stripchart(stiffness ~ species, data = timber, pch = 1, vertical = TRUE)
```



Bending Stiffness by Timber Species



```
# Annotate outliers on the plot # text(x = bp\$group, y = bp\$out, labels = bp\$out, pos = 3, cex = 0.7, col = "darkblue")
```

Commenting on Variability and Outliers Variability: Standard Deviation (SD): Gum has the highest variability (SD = $641.0 \text{ kN} \cdot \text{m}^2$), followed by cedar (SD = $572.8 \text{ kN} \cdot \text{m}^2$), and pine has the lowest (SD = $552.6 \text{ kN} \cdot \text{m}^2$). This suggests that gum's stiffness values are more spread out compared to pine and cedar.

Interquartile Range (IQR): Pine has the highest IQR (696.8 kN·m²), indicating a slightly wider spread of the middle 50% of stiffness values compared to gum (673.8 kN·m²) and cedar (659.1 kN·m²). However, the differences in IQR are small, suggesting comparable spread in the central data across species.

Range (Max - Min): Gum shows the largest range (11124.5 - 8314.9 = 2809.6 kN \cdot m²), followed by cedar (10074.9 - 8220.3 = 1854.6 kN \cdot m²), and pine (8982.9 - 6999.2 = 1983.7 kN \cdot m²). This reinforces that gum has the most extreme values.

Central Tendency: Gum has the highest median stiffness (9425.3 kN \cdot m²), followed by cedar (9387.7 kN \cdot m²), and pine (8139.2 kN \cdot m²). This indicates that gum and cedar generally have higher bending stiffness than pine.

In short;

Variability: Gum exhibits the highest variability in bending stiffness, as seen in its larger SD and range, suggesting less consistency in its mechanical properties compared to pine and cedar. Cedar and pine have similar variability, but pine's stiffness values are generally lower.

Outliers: Pine has one low outlier, indicating a single timber sample with unusually low stiffness, possibly due to defects or testing conditions. Gum has both a high and a low outlier, suggesting it can exhibit extreme

stiffness values (both stronger and weaker), which may reflect natural variability or quality differences in the samples. Cedar's lack of outliers suggests greater consistency in its stiffness properties.

Practical Implications: If consistency is desired, cedar may be preferable due to its lack of outliers and moderate variability. Gum's higher median stiffness is appealing for strength, but its outliers and variability suggest a need for quality control. Pine's lower stiffness and single outlier may indicate it's less suitable for applications requiring high or consistent stiffness.

```
# Part b):# Fit a one-way ANOVA test
timber$species <- relevel(timber$species, ref = "gum")</pre>
options(contrasts = c("contr.sum", "contr.poly"))
# options(contrasts = c("contr.treatment", "contr.poly")) # used as default anyway
stiff <- aov(stiffness ~ species, data = timber)</pre>
summary(stiff) ## ANOVA table including F-test
##
              Df
                   Sum Sq Mean Sq F value
                                            Pr(>F)
               2 18889629 9444815
                                    32.17 4.45e-10 ***
## species
             57 16734248 293583
## Residuals
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Extract coefficients
coef(stiff)
            ## be careful with interpretation
## (Intercept)
                             species2
                 species1
    8947.4233
                             340.1017
                 450.8267
dummy.coef(stiff) ## full coefficients, easier to interpret
## Full coefficients are
##
## (Intercept):
                   8947.423
## species:
                             cedar
                                           pine
                        gum
##
                   450.8267 340.1017 -790.9283
```

Model Interpreation

 $Null\ hypothesis\ (H\): \ _{pine} = \ _{gum} = \ _{cedar}\ (All\ species\ have\ the\ same\ mean\ bending\ stiffness)$

Alternative hypothesis (H_A): At least one species has a different mean stiffness.

**F-statistic*: 32.17; Large F-value indicates that between-species variability is much greater than within-species variability.

p-value: 4.45×10^{-1} ; Extremely small (< 0.001), so we reject H at any conventional significance level (e.g., 0.05 or 0.01).

Conclusion: There is strong statistical evidence that the mean bending stiffness differs significantly between timber species.

```
# Part c) # A pairwise two-sample t-tests (with multiple comparison correction)
# Perform pairwise t-tests with Bonferroni correction
tapply(timber$stiffness, timber$species, sd) # check for group SD
```

```
gum
               cedar
                         pine
## 607.0210 505.7786 506.4222
tapply(timber$stiffness, timber$species, var) # check for group var
##
               cedar
        gum
                         pine
## 368474.5 255812.0 256463.4
pairwise_results <- pairwise.t.test(timber$stiffness, timber$species,</pre>
                                     p.adjust.method = "bonferroni",
                                    pool.sd = FALSE, # Welch's t-test (unequal variances)
                                     paired = FALSE, # Independent samples
                                     conf.level = 0.95)
# Print the results
print("Pairwise t-test results with Bonferroni correction:")
## [1] "Pairwise t-test results with Bonferroni correction:"
print(pairwise_results)
##
##
   Pairwise comparisons using t tests with non-pooled SD
##
## data: timber$stiffness and timber$species
##
##
         gum
                 cedar
## cedar 1
## pine 8.1e-08 6.0e-08
```

Test Interpretation

P value adjustment method: bonferroni

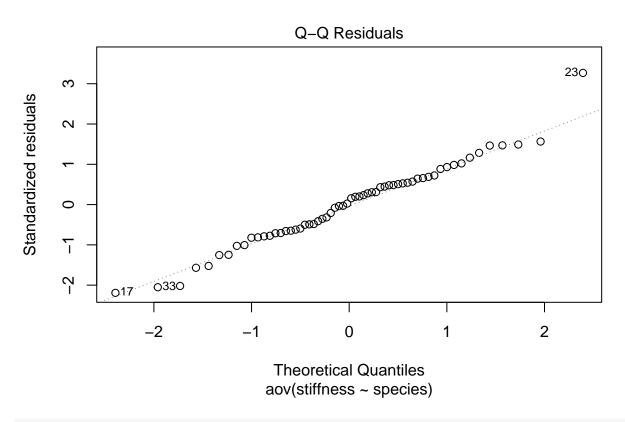
**Test method*: Welch-adjusted pairwise t-tests because the groups have unequal variances. This adjusts the degrees of freedom for each pair according to Welch's formula.

```
NNull\ hypothesis\ (H\ ): _{pine} = _{gum} = _{cedar}\ (All\ species\ have\ the\ same\ mean\ bending\ stiffness) Reject H if p < 0.05.
```

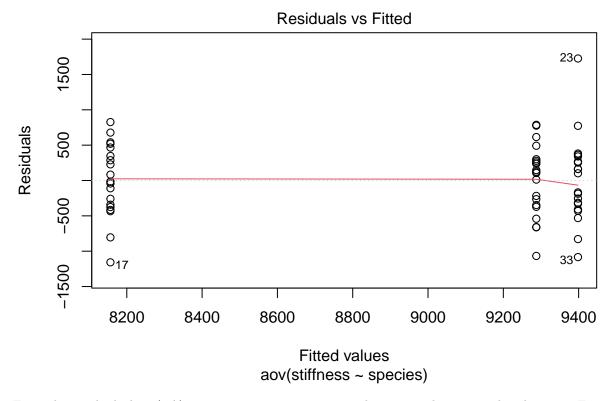
Interpretation of each pair pine vs gum: $p = 8.1 \times 10^{\circ} < 0.05 \rightarrow \text{significant}$; Mean stiffness differs between pine and gum, hence gum is stiffer than pine (looking at raw data: gum 9500 vs pine 8100). pine vs cedar: $p = 6.0 \times 10^{\circ} < 0.05 \rightarrow \text{significant}$, Mean stiffness differs between pine and cedar hence cedar is stiffer than pine (cedar 9400).

**gum vs cedar*: $p = 1 \rightarrow \text{not significant}$, No evidence that gum and cedar differ in mean stiffness. Their stiffness values are roughly similar (gum 9500, cedar 9400).

Therefore, In practical terms, pine is the softest, while gum and cedar have similar higher stiffness.



plot(stiff, which = 1)



From the residual plots (TA), error variance is constant and error can be expected to be zero. Errors are i.i.d (from Q-Q plot). No autocorrelation.