## SHC 798 Assignment 2, 2025

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#### SHC 798 Assignment 2, 2025

Multiple Linear Analysis (MLR)

Question 2: # Energy consumption data from 80 office buildings

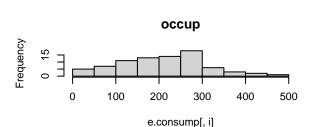
```
pacman::p_load(tidymodels)
# Getting started with the dataset in energy.csv :
e.consump <- read.csv(file.choose(), header = TRUE, na.strings = c("NA"))</pre>
head(e.consump) # View first few rows of the dataset
     energy area occup climate glazing insulation
## 1 1083.5 1887
                    174
                              2
                                   47.2
                                              108.5
                                   41.8
## 2 1560.9 5445
                    331
                              1
                                              101.4
## 3 1103.5 5576
                    246
                              1
                                   24.2
                                              115.3
## 4 1239.7 6304
                    132
                              3
                                   47.9
                                              124.9
## 5 1423.2 5749
                   260
                                   32.7
                                               61.7
                              1
## 6 1056.0 4778
                   102
                              1
                                   49.3
                                               79.0
```

summary(e.consump) # Get an overview of the dataset

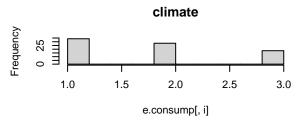
```
##
                                                      climate
                                                                    glazing
        energy
                          area
                                       occup
          : 448.7
                            :1500
                                         : 10.0
                                                                        :15.00
##
   Min.
                    Min.
                                   Min.
                                                   Min.
                                                          :1.0
                                                                 Min.
   1st Qu.:1095.3
                    1st Qu.:4101
                                   1st Qu.:133.0
                                                   1st Qu.:1.0
                                                                 1st Qu.:32.00
##
                    Median:4935
                                                   Median :2.0
##
  Median :1222.6
                                   Median :205.5
                                                                 Median :38.70
  Mean
          :1216.1
                    Mean
                          :5015
                                         :211.9
                                                          :1.8
                                                                 Mean
                                                                        :38.68
                                   Mean
                                                   Mean
##
  3rd Qu.:1379.9
                    3rd Qu.:6153
                                   3rd Qu.:281.0
                                                   3rd Qu.:2.0
                                                                 3rd Qu.:45.30
   Max.
           :1571.6
                    Max.
                          :8591
                                   Max.
                                          :469.0
                                                          :3.0
                                                                 Max.
##
                                                   Max.
                                                                        :57.20
##
      insulation
## Min.
          : 60.00
## 1st Qu.: 98.08
## Median :110.45
## Mean
          :115.33
## 3rd Qu.:128.22
## Max.
          :172.10
```

#### str(e.consump) # inspect the dataset and viewing column data types

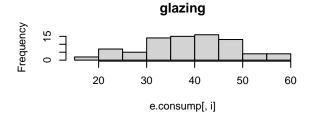
```
80 obs. of 6 variables:
   'data.frame':
##
##
    $ energy
                 : num
                        1084 1561 1104 1240 1423 ...
                        1887 5445 5576 6304 5749 4778 4291 8005 6446 4765 ...
##
    $ area
                        174 331 246 132 260 102 76 423 189 299 ...
    $ occup
                 : int
                        2 1 1 3 1 1 3 3 2 1 ...
    $ climate
                 : int
##
    $ glazing
                 : num
                        47.2 41.8 24.2 47.9 32.7 49.3 32 31.4 48.6 38.4 ...
                       108.5 101.4 115.3 124.9 61.7 ...
    $ insulation: num
# View variables
par(mfrow=c(3,2))
for (i in 1:6) hist(e.consump[,i], main=names(e.consump)[i])
                      energy
                                                                       area
Frequency
                                                Frequency
    0 20
                                                    0 20
                                                    0
                                  1400
        400
             600
                  800
                        1000
                            1200
                                        1600
                                                           2000
                                                                    4000
                                                                            6000
                                                                                    8000
```

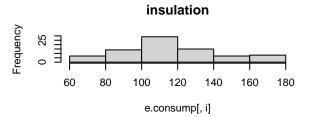


e.consump[, i]



e.consump[, i]



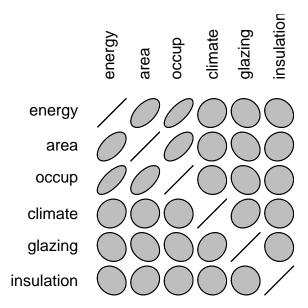


```
par(mfrow = c(1, 1))

# Part a): Multicollinearity
# (i) Pearson correlation coefficients
cor(e.consump, method = "pearson")
```

```
##
                                     occup
                                             climate
                                                       glazing
               energy
                           area
             1.0000000
                                           0.12451307 -0.1348882
## energy
                      0.56727188
                                0.71535501
## area
             0.5672719
                     1.00000000
                                1.00000000 -0.03118426 -0.1716492
## occup
             0.7153550 0.60076867
```

```
## climate
          -0.1348882 -0.23607748 -0.17164920 0.20012116 1.0000000
## glazing
##
          insulation
## energy
          -0.16816767
## area
          0.13148613
          0.02944892
## occup
## climate
          -0.03287315
## glazing
          -0.04479560
## insulation 1.0000000
# (ii) An ellipse plot to visualise collinearity
pacman::p_load(ellipse)
plotcorr(cor(e.consump))
```



```
# (iii) Variance Inflation Factors (VIFs)
pacman::p_load(car)
engy_model <- lm(energy ~ area + occup + climate + glazing + insulation, data = e.consump)
vif(engy_model)

## area occup climate glazing insulation
## 1.661848 1.579343 1.055096 1.111013 1.023478</pre>
```

Commenting on Multicollinearity In the correlogram (ellipse plot), narrow/elongated ellipses indicate stronger correlation. Energy has elongated ellipses with area (0.5672719) and occupancy (0.71535501),

indicating moderate to strong positive correlation. Also, area and occupancy are noticeably correlated with narrow tilted ellipse (0.60076867) which indicates collinearity. Therefore, there is some multicollinearity between area and occupancy, and to a lesser extent between energy and these two variables.

Since all VIF values are very well below 5, there is **no significant multicollinearity** among the predictors for the model, engy\_model. This suggests that the predictors can be considered independent of each other for this regression model.

```
# Part b): Model and Predictor Linearity
# Initial Model Output
summary(engy_model)
##
## Call:
## lm(formula = energy ~ area + occup + climate + glazing + insulation,
       data = e.consump)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -522.35 -74.40
                     11.52
                             93.61
                                    367.70
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 936.47055
                         115.55537
                                      8.104 8.23e-12 ***
                                      2.534 0.01338 *
## area
                 0.03186
                            0.01257
                 1.26073
                            0.19992
                                      6.306 1.87e-08 ***
## occup
## climate
                36.38855
                           21.04601
                                      1.729
                                            0.08798 .
## glazing
                -0.32620
                            1.73189
                                     -0.188
                                             0.85112
## insulation
                -1.73568
                            0.60284
                                     -2.879 0.00521 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 143.1 on 74 degrees of freedom
## Multiple R-squared: 0.6042, Adjusted R-squared: 0.5774
## F-statistic: 22.59 on 5 and 74 DF, p-value: 1.101e-13
confint(engy_model)
##
                      2.5 %
                                   97.5 %
## (Intercept) 706.22145364 1166.71964585
                 0.00681188
                               0.05690576
## area
                 0.86238033
                               1.65908800
## occup
## climate
                -5.54653691
                              78.32363945
                -3.77706386
## glazing
                               3.12466606
## insulation
                -2.93685538
                              -0.53449767
```

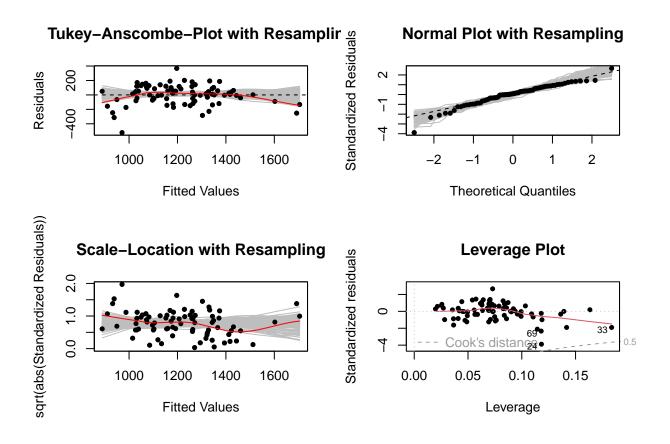
```
## 706.2215 1166.7196
```

2.5 %

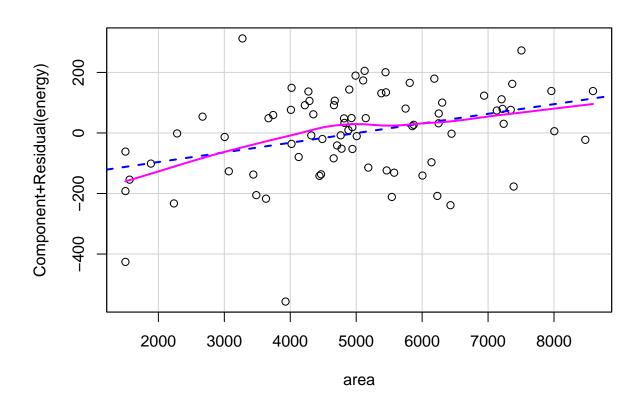
##

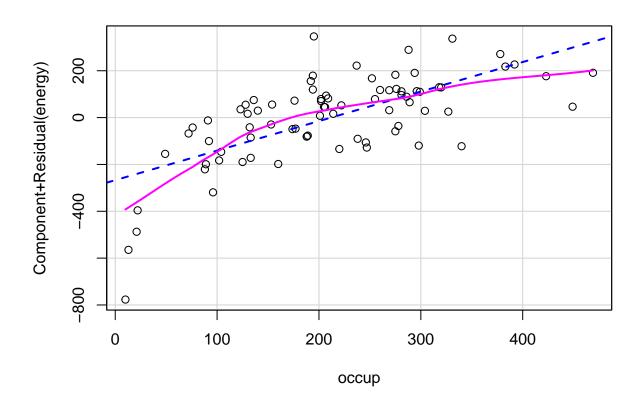
confint(engy\_model)["(Intercept)", ]

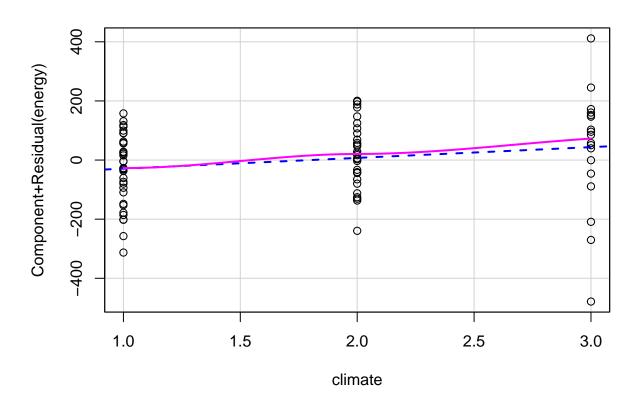
97.5 %

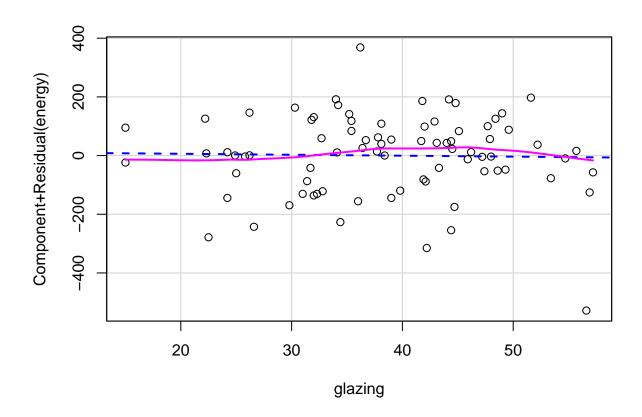


# Linearity of each predictor - Use of Partial Residual Plots
pacman::p\_load(car)
crPlots(engy\_model, layout = c(1,1))

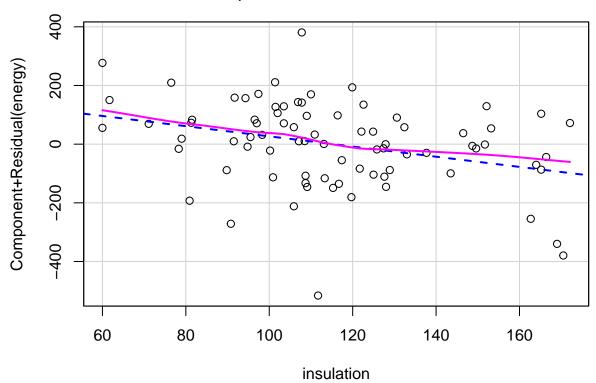








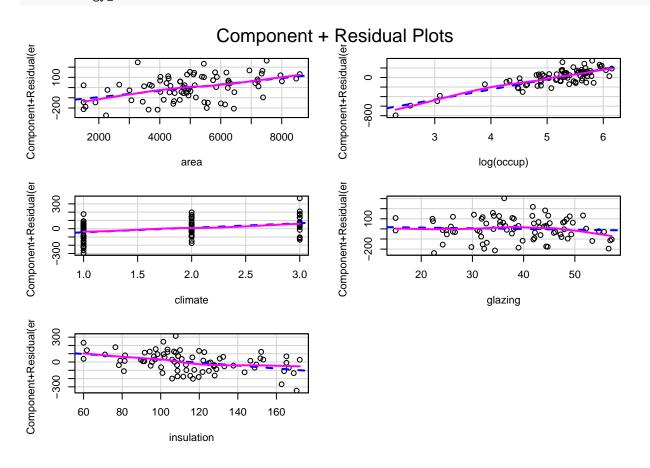
### Component + Residual Plots



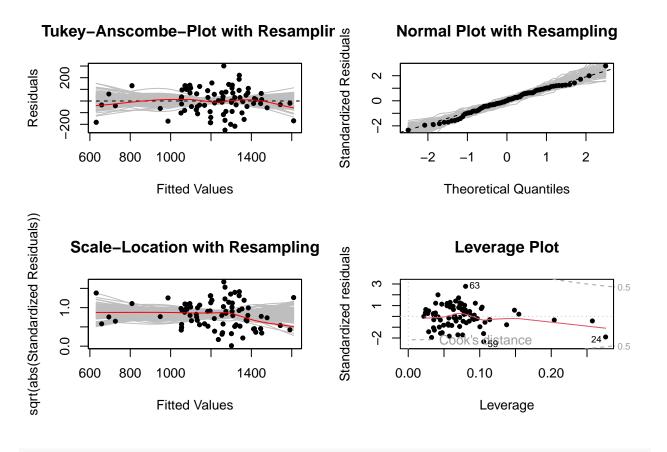
```
# crPlots(engy_model)
# Transformed Model 1
engy_model2 <- lm(energy ~ area + log(occup) + climate + glazing + insulation, data = e.consump)
summary(engy_model2)
##
## lm(formula = energy ~ area + log(occup) + climate + glazing +
##
       insulation, data = e.consump)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    ЗQ
                                            Max
##
  -250.129 -66.554
                        1.599
                                72.610
                                        301.157
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 89.134103 127.287741
                                       0.700 0.485963
                 0.031008
                            0.009216
                                       3.365 0.001217 **
## log(occup)
              212.531379
                          20.365584
                                     10.436 3.42e-16 ***
## climate
                55.078048
                          16.765693
                                       3.285 0.001559 **
## glazing
                -0.694371
                            1.365478
                                     -0.509 0.612602
## insulation
                -1.744152
                           0.474978
                                      -3.672 0.000452 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 112.9 on 74 degrees of freedom
## Multiple R-squared: 0.7538, Adjusted R-squared: 0.7371
## F-statistic: 45.31 on 5 and 74 DF, p-value: < 2.2e-16</pre>
```

#### crPlots(engy\_model2)



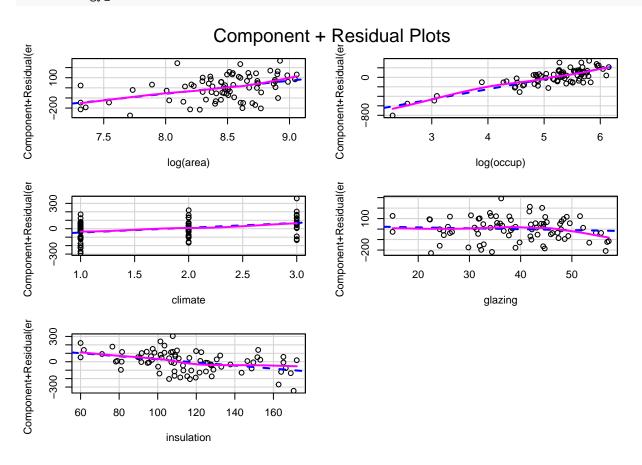
#### resplot(engy\_model2)



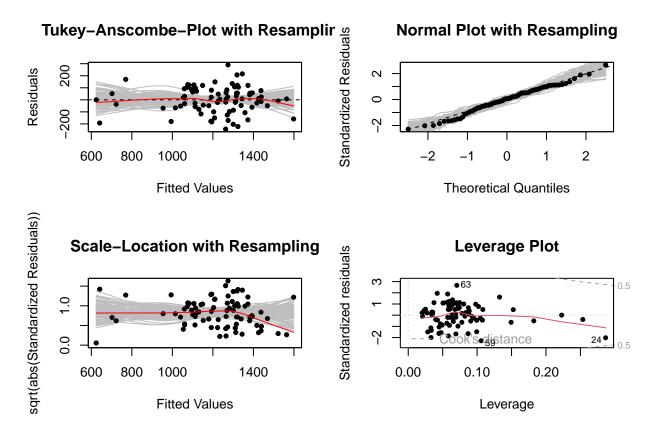
```
# Transformed Model 2
engy_model3 <- lm(energy ~ log(area) + log(occup) + climate + glazing + insulation, data = e.consump)
summary(engy_model3)</pre>
```

```
##
## Call:
## lm(formula = energy ~ log(area) + log(occup) + climate + glazing +
##
       insulation, data = e.consump)
##
## Residuals:
##
        Min
                                             Max
                  1Q
                       Median
                                     3Q
                         6.811
   -243.595
            -62.706
                                 77.199
                                         290.031
##
##
  Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -829.3248
                            295.0838
                                     -2.810 0.006327 **
## log(area)
                128.5629
                             38.1860
                                       3.367 0.001209 **
## log(occup)
                212.6420
                             20.3453
                                      10.452 3.19e-16 ***
## climate
                 56.9442
                             16.6877
                                       3.412 0.001047 **
                 -0.8729
                                      -0.644 0.521390
## glazing
                              1.3548
## insulation
                 -1.8293
                              0.4790
                                      -3.819 0.000276 ***
##
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 112.9 on 74 degrees of freedom
```

#### crPlots(engy\_model3)



resplot(engy\_model3)



From the partial plots of the initial/original (engy\_model) predictors, the variables area and occupancy clearly deviate from the dotted blue line which indicates non-linearity. In the first transformed model (engy\_model2), the linearity of both variables are seen to improve. Also, the model diagnostics are better for this transformed model. From the Adjusted R2, this model also fits the data better (0.7371 > 0.5774) than the original/initial model.

In the second transformed model (engy\_model3), the variable linearity, residual plots and model fit are better than both the original and the first transformed model (engy\_model2).

Therefore, this model is taken as the most appropriate.

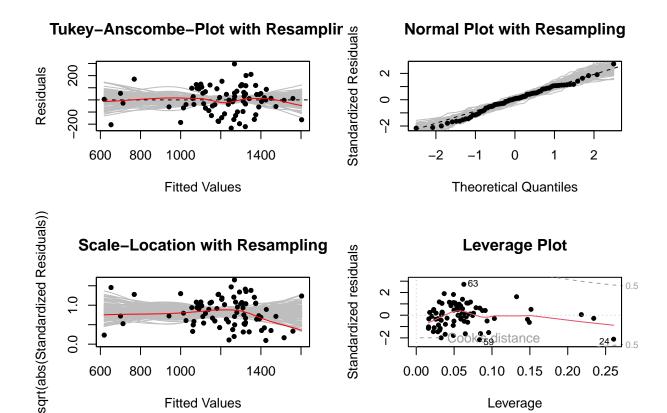
##

```
# Part c) Variable Selection starting with the transformed model
# Backward Elimination with AIC
engy.back <- stats::step(engy_model3, direction="backward")</pre>
## Start: AIC=761.97
## energy ~ log(area) + log(occup) + climate + glazing + insulation
##
##
                Df Sum of Sq
                                  RSS
                                          AIC
                         5288
                               948090 760.41
## - glazing
                 1
## <none>
                               942802 761.97
                       144415 1087217 771.37
## - log(area)
                 1
## - climate
                 1
                       148352 1091154 771.66
  - insulation
                 1
                       185826 1128628 774.36
  - log(occup)
                 1
                      1391746 2334548 832.50
```

```
## Step: AIC=760.41
## energy ~ log(area) + log(occup) + climate + insulation
##
##
               Df Sum of Sq
                               RSS
                                      AIC
## <none>
                            948090 760.41
## - climate
                    143097 1091187 769.66
               1
## - log(area) 1 159606 1107696 770.86
## - insulation 1
                   185718 1133808 772.73
## - log(occup) 1 1394266 2342356 830.77
summary(engy.back)
##
## Call:
## lm(formula = energy ~ log(area) + log(occup) + climate + insulation,
      data = e.consump)
##
## Residuals:
##
       Min
                1Q Median
                                  3Q
                                          Max
## -232.755 -60.103
                      8.202 75.275 296.391
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -897.3616 274.4641 -3.270 0.001628 **
              132.9696 37.4216 3.553 0.000662 ***
## log(area)
## log(occup)
               212.8157
                        20.2640 10.502 < 2e-16 ***
## climate
               54.7563
                          16.2747
                                   3.365 0.001211 **
## insulation -1.8288
                          0.4771 -3.833 0.000261 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

#### resplot(engy.back)

## Residual standard error: 112.4 on 75 degrees of freedom
## Multiple R-squared: 0.7524, Adjusted R-squared: 0.7392
## F-statistic: 56.99 on 4 and 75 DF, p-value: < 2.2e-16</pre>



```
# AIC Stepwise Model Search: Both Directions Approach
# starting with the null model
engy_null <- lm(energy ~ 1, data = e.consump) # Intercept-only model
sc <- list(lower=engy_null, upper=engy_model3)
engy.b1 <- stats::step(engy_null, scope = sc, direction = "both")</pre>
```

```
## Start: AIC=864.1
## energy ~ 1
##
                Df Sum of Sq
##
                                  RSS
                                         AIC
## + log(occup)
                     2409474 1420285 786.75
## + log(area)
                     1164697 2665062 837.10
## + insulation
                      108307 3721452 863.81
## <none>
                              3829759 864.10
## + glazing
                       69682 3760078 864.63
## + climate
                       59375 3770385 864.85
##
## Step: AIC=786.75
  energy ~ log(occup)
##
##
                Df Sum of Sq
                                  RSS
                                         AIC
                      181658 1238627 777.80
## + climate
## + insulation 1
                      140139 1280146 780.44
## + log(area)
                 1
                      127714 1292571 781.21
                              1420285 786.75
## <none>
```

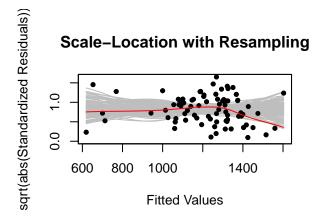
```
## - log(occup) 1
                   2409474 3829759 864.10
## Step: AIC=777.8
## energy ~ log(occup) + climate
##
               Df Sum of Sq
                                RSS
                     130931 1107696 770.86
## + insulation 1
## + log(area) 1
                     104819 1133808 772.73
## <none>
                            1238627 777.80
## + glazing
                     16872 1221755 778.70
                1
                     181658 1420285 786.75
## - climate
                1
## - log(occup) 1
                    2531758 3770385 864.85
##
## Step: AIC=770.86
## energy ~ log(occup) + climate + insulation
##
##
               Df Sum of Sq
                                RSS
                                       AIC
                1 159606 948090 760.41
## + log(area)
## <none>
                            1107696 770.86
## + glazing
                1
                     20479 1087217 771.37
## - insulation 1
                    130931 1238627 777.80
## - climate
                     172450 1280146 780.44
                1
## - log(occup) 1
                    2559478 3667174 864.63
##
## Step: AIC=760.41
## energy ~ log(occup) + climate + insulation + log(area)
##
##
               Df Sum of Sq
                                RSS
                                       AIC
## <none>
                             948090 760.41
## + glazing
                1
                       5288 942802 761.97
## - climate
                1
                     143097 1091187 769.66
## - log(area)
                1
                    159606 1107696 770.86
                     185718 1133808 772.73
## - insulation 1
## - log(occup)
                1
                    1394266 2342356 830.77
summary(engy.b1)
##
## Call:
## lm(formula = energy ~ log(occup) + climate + insulation + log(area),
##
      data = e.consump)
##
## Residuals:
                 1Q
                      Median
                                   3Q
## -232.755 -60.103
                       8.202
                              75.275 296.391
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -897.3616
                          274.4641 -3.270 0.001628 **
## log(occup)
              212.8157
                           20.2640 10.502 < 2e-16 ***
## climate
                54.7563
                         16.2747
                                    3.365 0.001211 **
## insulation
                -1.8288
                         0.4771 -3.833 0.000261 ***
## log(area)
                         37.4216
                                    3.553 0.000662 ***
               132.9696
```

2292 1417993 788.62

## + glazing

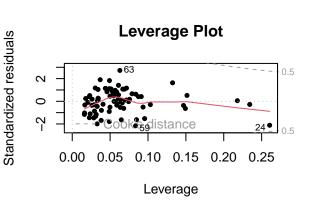
1

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 112.4 on 75 degrees of freedom
## Multiple R-squared: 0.7524, Adjusted R-squared: 0.7392
## F-statistic: 56.99 on 4 and 75 DF, p-value: < 2.2e-16
resplot(engy.b1)
  Tukey-Anscombe-Plot with Resamplir Standardized Residuals 1400
                                                        Normal Plot with Resampling
Residuals
                                                    \alpha
                                                    0
                                                    Ņ
```



# starting with the full model

Fitted Values



0

Theoretical Quantiles

-2

2

```
engy.b2 <- stats::step(engy_model3, scope = sc, direction = "both")</pre>
## Start: AIC=761.97
## energy ~ log(area) + log(occup) + climate + glazing + insulation
##
##
                Df Sum of Sq
                                  RSS
                                          AIC
                         5288
                               948090 760.41
## - glazing
## <none>
                               942802 761.97
                       144415 1087217 771.37
## - log(area)
## - climate
                       148352 1091154 771.66
## - insulation
                      185826 1128628 774.36
                 1
## - log(occup)
                      1391746 2334548 832.50
##
## Step: AIC=760.41
```

## energy ~ log(area) + log(occup) + climate + insulation

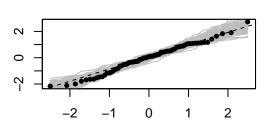
```
##
##
             Df Sum of Sq
                              RSS
                                    AIC
## <none>
                           948090 760.41
## + glazing 1 5288 942802 761.97
## - climate 1 143097 1091187 769.66
                    5288 942802 761.97
## - log(area) 1 159606 1107696 770.86
## - insulation 1 185718 1133808 772.73
## - log(occup) 1 1394266 2342356 830.77
summary(engy.b2)
##
## Call:
## lm(formula = energy ~ log(area) + log(occup) + climate + insulation,
##
      data = e.consump)
##
## Residuals:
               1Q Median
       Min
                                 3Q
## -232.755 -60.103 8.202 75.275 296.391
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -897.3616 274.4641 -3.270 0.001628 **
## log(area) 132.9696 37.4216 3.553 0.000662 ***
## log(occup) 212.8157 20.2640 10.502 < 2e-16 ***
## climate
              -1.8288
## insulation
                         0.4771 -3.833 0.000261 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

## Residual standard error: 112.4 on 75 degrees of freedom
## Multiple R-squared: 0.7524, Adjusted R-squared: 0.7392
## F-statistic: 56.99 on 4 and 75 DF, p-value: < 2.2e-16</pre>

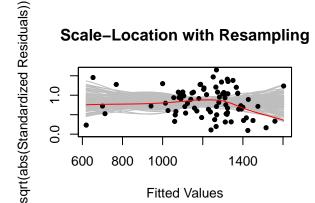
#### resplot(engy.b2)

# Tukey-Anscombe-Plot with Resamplir Standardized Residuals 1400 Residuals Fitted Values

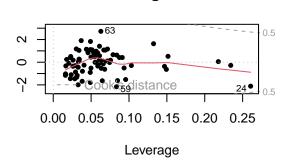
#### **Normal Plot with Resampling**



Theoretical Quantiles



#### Leverage Plot



```
# starting with a model somewhere in the middle
engy.mid <- lm(energy ~ climate + glazing, data = e.consump)</pre>
engy.b3<- stats::step(engy.mid, scope = sc, direction = "both")</pre>
```

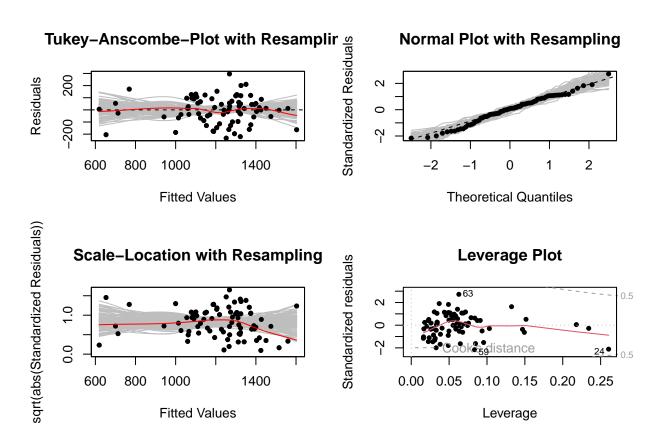
Standardized residuals

```
## Start: AIC=864.66
## energy ~ climate + glazing
##
##
                Df Sum of Sq
                                  RSS
                                         AIC
## + log(occup)
                     2446745 1221755 778.70
## + log(area)
                     1063969 2604532 839.26
## + insulation
                      111540 3556961 864.19
## - climate
                       91577 3760078 864.63
## <none>
                              3668500 864.66
##
  - glazing
                      101884 3770385 864.85
##
## Step: AIC=778.7
## energy ~ climate + glazing + log(occup)
##
##
                Df Sum of Sq
                                  RSS
                                         AIC
## + insulation
                      134538 1087217 771.37
                1
## + log(area)
                 1
                       93127 1128628 774.36
## - glazing
                       16872 1238627 777.80
## <none>
                              1221755 778.70
## - climate
                      196238 1417993 788.62
                 1
## - log(occup) 1
                     2446745 3668500 864.66
```

```
##
## Step: AIC=771.37
## energy ~ climate + glazing + log(occup) + insulation
##
               Df Sum of Sq
                                RSS
                     144415 942802 761.97
## + log(area)
                1
                      20479 1107696 770.86
## - glazing
                1
                            1087217 771.37
## <none>
## - insulation 1
                     134538 1221755 778.70
## - climate
             1
                    188917 1276134 782.19
## - log(occup) 1
                    2469744 3556961 864.19
##
## Step: AIC=761.97
## energy ~ climate + glazing + log(occup) + insulation + log(area)
##
                Df Sum of Sq
                                RSS
                                       AIC
                       5288 948090 760.41
## - glazing
## <none>
                             942802 761.97
## - log(area)
                     144415 1087217 771.37
                1
## - climate
                1
                     148352 1091154 771.66
## - insulation 1
                     185826 1128628 774.36
## - log(occup) 1
                    1391746 2334548 832.50
##
## Step: AIC=760.41
## energy ~ climate + log(occup) + insulation + log(area)
##
##
               Df Sum of Sq
                                RSS
                                        AIC
                             948090 760.41
## <none>
## + glazing
                       5288 942802 761.97
                1
## - climate
                1
                    143097 1091187 769.66
## - log(area)
                1
                     159606 1107696 770.86
## - insulation 1
                     185718 1133808 772.73
## - log(occup) 1
                    1394266 2342356 830.77
summary(engy.b3)
##
## lm(formula = energy ~ climate + log(occup) + insulation + log(area),
##
      data = e.consump)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -232.755 -60.103
                       8.202
                              75.275 296.391
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -897.3616 274.4641 -3.270 0.001628 **
## climate
                54.7563
                          16.2747
                                    3.365 0.001211 **
                           20.2640 10.502 < 2e-16 ***
## log(occup)
               212.8157
## insulation
                -1.8288
                           0.4771 -3.833 0.000261 ***
## log(area)
               132.9696
                           37.4216 3.553 0.000662 ***
## ---
```

## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

```
##
## Residual standard error: 112.4 on 75 degrees of freedom
## Multiple R-squared: 0.7524, Adjusted R-squared: 0.7392
## F-statistic: 56.99 on 4 and 75 DF, p-value: < 2.2e-16
resplot(engy.b3)</pre>
```



In all the reduced models from applying variable selection (i.e., engy.back, engy.b1, engy.b2 and engy.b3), the variable glazing was dropped. There are no major improvements in residual plots for all the models. Also, no noticeable changes on predictor significance or model fit.

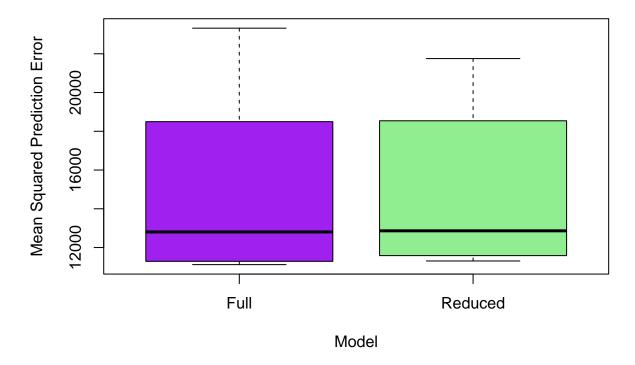
```
# Part d) 5-fold cross validation
set.seed(123) # Set seed for reproducibility
n <- nrow(e.consump) # Number of observations and folds
k <- 5 # Number of folds
sb <- round(seq(0, n, length = (k + 1))) # Fold boundaries

# Initialize vectors to store MSPE for each model
mspe_full <- numeric(k)
mspe_reduced <- numeric(k)

# 5-fold cross-validation for full model (engy_model3)
for (i in 1:k) {
   test <- (sb[k + 1 - i] + 1):sb[k + 2 - i]
   train <- (1:n)[-test]
   fit_full <- lm(energy ~ log(area) + log(occup) + climate + glazing + insulation, data = e.consump[tra</pre>
```

```
pred_full <- predict(fit_full, newdata = e.consump[test, ])</pre>
 mspe_full[i] <- mean((e.consump$energy[test] - pred_full)^2, na.rm = FALSE)</pre>
# 5-fold cross-validation for reduced model (dropping glazing)
for (i in 1:k) {
 test \leftarrow (sb[k + 1 - i] + 1):sb[k + 2 - i] # Same fold split for comparability
 train <- (1:n) [-test]
 fit_reduced <- lm(energy ~ log(area) + log(occup) + climate + insulation, data = e.consump[train, ])</pre>
 pred_reduced <- predict(fit_reduced, newdata = e.consump[test, ])</pre>
 mspe_reduced[i] <- mean((e.consump$energy[test] - pred_reduced)^2, na.rm = FALSE)</pre>
}
# Calculate overall MSPE for each model
mspe_full_mean <- mean(mspe_full, na.rm = TRUE)</pre>
mspe_reduced_mean <- mean(mspe_reduced, na.rm = TRUE)</pre>
# Report results
cat("MSPE per fold for Full Model:", mspe_full, "\n")
## MSPE per fold for Full Model: 12804.69 23320.92 11287.79 18497.25 11118.67
cat("MSPE per fold for Reduced Model:", mspe_reduced, "\n")
## MSPE per fold for Reduced Model: 12862.88 21751.54 11583.43 18541.62 11307.16
cat("MSPE for Full Model:", mspe_full_mean, "\n")
## MSPE for Full Model: 15405.86
cat("MSPE for Reduced Model:", mspe_reduced_mean, "\n")
## MSPE for Reduced Model: 15209.33
# Checking relative increase in MSPE
relative_increase <- ((mspe_reduced_mean - mspe_full_mean) / mspe_full_mean) * 100
cat("Relative increase in MSPE (%):", relative_increase, "\n")
## Relative increase in MSPE (%): -1.275735
# Box plots Using MSPEs
# Combining MSPEs into a data frame for plotting
mspe_data <- data.frame(</pre>
 MSPE = c(mspe_full, mspe_reduced),
 Model = factor(rep(c("Full", "Reduced"), each = k))
# Generating box plots
boxplot(MSPE ~ Model, data = mspe_data,
        main = "MSPE Comparison: Full vs Reduced Model",
        ylab = "Mean Squared Prediction Error",
        col = c("purple", "lightgreen"),
        border = "black")
```

# **MSPE Comparison: Full vs Reduced Model**



From the cross-validation exercise, The MSPE for the reduced is less (-1.275735%) than the full model. Therefore, the variable glazing can be said to reduce the predictive power in model. Therefore, the reduced model is preferable for prediction purposes.