

DEEP MULTI-SCALE VIDEO PREDICTION BEYOND MEAN SQUARE ERROR

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ABSTRACT

Learning to predict future images from a video sequence involves the construction of an internal representation that models the image evolution accurately, and therefore, to some degree, its content and dynamics. This is why pixel-space video prediction may be viewed as a promising avenue for unsupervised feature learning. In addition, while optical flow has been a very studied problem in computer vision for a long time, future frame prediction is rarely approached. Still, many vision applications could benefit from the knowledge of the next frames of videos, that does not require the complexity of tracking every pixel trajectory. In this work, we train a convolutional network to generate future frames given an input sequence. To deal with the inherently blurry predictions obtained from the standard Mean Squared Error (MSE) loss function, we propose three different and complementary feature learning strategies: a multi-scale architecture, an adversarial training method, and an image gradient difference loss function. We compare our predictions to different published results based on recurrent neural networks on the UCF101 dataset.

1 INTRODUCTION

Unsupervised feature learning of video representations is a promising direction of research because the resources are quasi-unlimited and the progress remaining to achieve in this area are quite important. In this paper, we address the problem of frame prediction. A significant difference with the more classical problem of image reconstruction (Vincent et al., 2008; Le, 2013) is that the ability of a model to predict future frames requires to build accurate, non trivial internal representations, even in the absence of other constraints (such as sparsity). Therefore, we postulate that the better the predictions of such system are, the better the feature representation should be. Indeed, the work of Srivastava et al. (2015) demonstrates that learning representations by predicting the next sequence of image features improves classification results on two action recognition datasets. In this work, however, we focus on predicting directly in pixel space and try to address the inherent problems related to this approach.

Top performing algorithms for action recognition exploit the temporal information in a supervised way, such as the 3D convolutional network of Tran et al. (2015), or the spatio-temporal convolutional model of Simonyan & Zisserman (2014), which can require months of training, and heavily labeled datasets. This could be reduced using unsupervised learning. The authors in (Wang & Gupta, 2015) compete with supervised learning performance on ImageNet, by using a siamese architecture (Bromley et al., 1993) to mine positive and negative examples from patch triplets of videos in an unsupervised fashion. Unsupervised learning from video is also exploited in the work of Vondrick et al. (2015), where a convolutional model is trained to predict sets of future possible actions, or in (Jayaraman & Grauman, 2015) which focuses on learning a feature space equivariant to ego-motion. Goroshin et al. (2015) trained a convolutional network to learn to linearize motion in the code space and tested it on the NORB dataset. Beside unsupervised learning, a video predictive system may find applications in robotics (Kosaka & Kak, 1992), video compression (Ascenso et al., 2005) and inpainting (Flynn et al., 2015) to name a few.

Recently, predicting future video sequences appeared in different settings: Ranzato et al. (2014) defined a recurrent network architecture inspired from language modeling, predicting the frames in a discrete space of patch clusters. Srivastava et al. (2015) adapted a LSTM model (Hochreiter & Schmidhuber, 1997) to future frame prediction. Oh et al. (2015) defined an action conditional auto-encoder model to predict next frames of Atari-like games. In the two works dealing with natural images, a blur effect is observed in the predictions, due to different causes. In (Ranzato et al., 2014), the transformation back and forth between pixel and clustered spaces involves the averaging of 64 predictions of overlapping tilings of the image, in order to avoid a blockiness effect in the result. Short term results from Srivastava et al. (2015) are less blurry, however the ℓ_2 loss function inherently produces blurry results. Indeed, using the ℓ_2 loss comes from the assumption that the data is drawn from a Gaussian distribution, and works poorly with multimodal distributions.

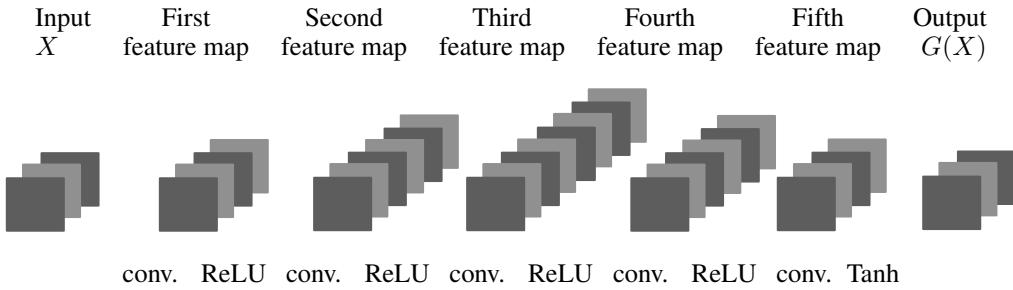
In this work, we address the problem of lack of sharpness in the predictions. We assess different loss functions, show that generative adversarial training (Goodfellow et al., 2014; Denton et al., 2015) may be successfully employed for next frame prediction, and finally introduce a new loss based on the image gradients, designed to preserve the sharpness of the frames. Combining these two losses produces the most visually satisfying results.

Our paper is organised as follows: the model section describes the different model architectures: simple, multi-scale, adversarial, and presents our gradient difference loss function. The experimental section compares the proposed architectures and losses on video sequences from the Sports1m dataset of Karpathy et al. (2014) and UCF101 (Soomro et al., 2012). We further compare our results with (Srivastava et al., 2015) and (Ranzato et al., 2014). We measure the quality of image generation by computing similarity and sharpness measures.

2 MODELS

Let $Y = \{Y^1, \dots, Y^n\}$ be a sequence of frames to predict from input frames $X = \{X^1, \dots, X^m\}$ in a video sequence. Our approach is based on a convolutional network (LeCun et al., 1998), alternating convolutions and Rectified Linear Units (ReLU) (Nair & Hinton, 2010).

Figure 1: A basic next frame prediction convnet



Such a network G , displayed in Figure 1, can be trained to predict one or several concatenated frames Y from the concatenated frames X by minimizing a distance, for instance ℓ_p with $p = 1$ or $p = 2$, between the predicted frame and the true frame:

$$\mathcal{L}_p(X, Y) = \ell_p(G(X), Y) = \|G(X) - Y\|_p^p, \quad (1)$$

However, such a network has at least two major flaws:

1. Convolutions only account for short-range dependencies, limited by the size of their kernels. However, using pooling would only be part of the solution since the output has to be of the same resolution as the input. There are a number of ways to avoid the loss of resolution brought about by pooling/subsampling while preserving long-range dependencies. The simplest and oldest one is to have no pooling/subsampling but many convolution layers (Jain et al., 2007). Another method is to use connections that “skip” the pooling/unpooling pairs, to preserve the high frequency information (Long et al., 2015; Dosovitskiy et al., 2015; Ronneberger et al., 2015). Finally, we can combine multiple scales linearly as in the reconstruction process of a Laplacian pyramid (Denton et al., 2015). This is the approach we use in this paper.

2. Using an ℓ_2 loss, and to a lesser extent ℓ_1 , produces blurry predictions, increasingly worse when predicting further in the future. If the probability distribution for an output pixel has two equally likely modes v_1 and v_2 , the value $v_{avg} = (v_1 + v_2)/2$ minimizes the ℓ_2 loss over the data, even if v_{avg} has very low probability. In the case of an ℓ_1 norm, this effect diminishes, but do not disappear, as the output value would be the median of the set of equally likely values.

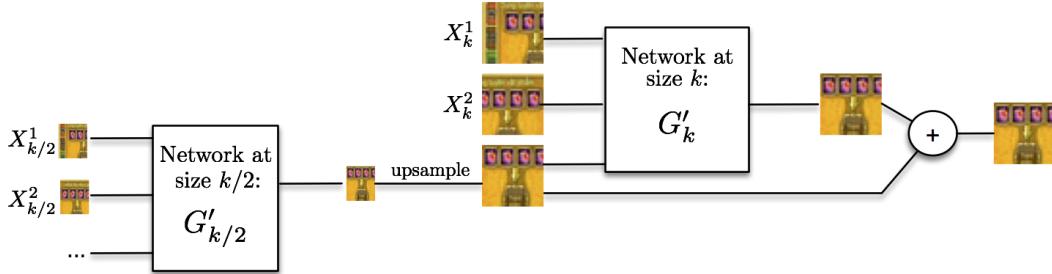
2.1 MULTI-SCALE NETWORK

We tackle Problem 1 by making the model multi-scale. A multi-scale version of the model is defined as follows: Let $s_1, \dots, s_{N_{\text{scales}}}$ be the sizes of the inputs of our network. Typically, in our experiments, we set $s_1 = 4 \times 4$, $s_2 = 8 \times 8$, $s_3 = 16 \times 16$ and $s_4 = 32 \times 32$. Let u_k be the upscaling operator toward size s_k . Let X_k^i, Y_k^i denote the downscaled versions of X^i and Y^i of size s_k , and G'_k be a network that learns to predict $Y_k - u_k(Y_{k-1})$ from X_k and a coarse guess of Y_k . We recursively define the network G_k , that makes a prediction \hat{Y}_k of size s_k , by

$$\hat{Y}_k = G_k(X) = u_k(\hat{Y}_{k-1}) + G'_k(X_k, u_k(\hat{Y}_{k-1})). \quad (2)$$

Therefore, the network makes a series of predictions, starting from the lowest resolution, and uses the prediction of size s_k as a starting point to make the prediction of size s_{k+1} . At the lowest scale s_1 , the network takes only X_1 as an input. This architecture is illustrated on Figure 2, and the specific details are given in Section 3. The set of trainable parameters is denoted W_G and the minimization is performed via Stochastic Gradient Descent (SGD).

Figure 2: Multi-scale architecture



not a necessity anymore. We trained the network with and without adding noise and did not observe any difference. The results we present are obtained without random noise.



Our main intuition on why to use an adversarial loss is that it can, **theoretically**, address the Problem 2 mentioned in Section 2. Imagine a sequence of frames $X = (X^1, \dots, X^m)$ for which, in the dataset, the next frames can either be $Y = (Y^1, \dots, Y^n)$ or $Y' = (Y'^1, \dots, Y'^n)$, with equal probability. As explained before, training the network with an ℓ_2 loss will result in predicting the average frames $Y_{avg} = (Y + Y')/2$. However, the sequence (X, Y_{avg}) , composed of the frames of X followed by the frames of Y_{avg} , is not a likely sequence, and D can discriminate them easily. The only sequences the model D will not be able to classify as fake are (X, Y) and (X, Y') .

The discriminative model D is a multi-scale convolutional network with a single scalar output. The training of the pair (G, D) consists of two alternated steps, described below. For the sake of clarity, we assume that we use pure SGD (minibatches of size 1), but there is no difficulty to generalize the algorithm to minibatches of size M by summing the losses over the samples.

Training D: Let (X, Y) be a sample from the dataset. Note that X (respectively Y) is a sequence of m (respectively n) frames. We train D to classify the input (X, Y) into class 1 and the input $(X, G(X))$ into class 0. More precisely, for each scale k , we perform one SGD iteration of D_k while keeping the weights of G fixed. It is trained with in the target 1 for the datapoint (X_k, Y_k) , and the target 0 for $(X_k, G_k(X_k))$. Therefore, the loss function we use to train D is

$$\mathcal{L}_{adv}^D(X, Y) = \sum_{k=1}^{N_{\text{scales}}} L_{bce}(D_k(X_k, Y_k), 1) + L_{bce}(D_k(X_k, G_k(X)), 0) \quad (3)$$

where L_{bce} is the **binary cross-entropy loss**, defined as

$$L_{bce}(Y, \hat{Y}) = - \sum_i \hat{Y}_i \log(Y_i) + (1 - \hat{Y}_i) \log(1 - Y_i) \quad (4)$$

where Y_i takes its values in $\{0, 1\}$ and \hat{Y}_i in $[0, 1]$.

Training G: Let (X, Y) be a *different* data sample. While keeping the weights of D fixed, we perform one SGD step on G to minimize the adversarial loss:

$$\mathcal{L}_{adv}^G(X, Y) = \sum_{k=1}^{N_{\text{scales}}} L_{bce}(D_k(X_k, G_k(X_k)), 1) \quad (5)$$

Minimizing this loss means that the generative model G is making the discriminative model D as “confused” as possible, in the sense that D will not discriminate the prediction correctly. However, in practice, minimizing this loss alone can lead to instability. G can always generate samples that “confuse” D , without being close to Y . In turn, D will learn to discriminate these samples, leading G to generate other “confusing” samples, and so on. To address this problem, we train the generator with a combined loss composed of the of the adversarial loss and the \mathcal{L}_p loss . The generator G is therefore trained to minimize $\lambda_{adv}\mathcal{L}_{adv}^G + \lambda_{\ell_p}\mathcal{L}_p$. There is therefore a tradeoff to adjust, by the mean of the λ_{adv} and λ_{ℓ_p} parameters, between sharp predictions due to the adversarial principle, and similarity with the ground truth brought by the second term. This process is summarized in Algorithm 1, with minibatches of size M .

2.3 IMAGE GRADIENT DIFFERENCE LOSS (GDL)



Another strategy to sharpen the image prediction is to directly penalize the differences of image gradient predictions in the generative loss function. We define a new loss function, the Gradient Difference Loss (GDL), that can be combined with a ℓ_p and/or adversarial loss function. The GDL function between the ground truth image Y , and the prediction $G(X) = \hat{Y}$ is given by

$$\begin{aligned} \mathcal{L}_{gdl}(X, Y) &= L_{gdl}(\hat{Y}, Y) = \\ &\sum_{i,j} \left| |Y_{i,j} - Y_{i-1,j}| - |\hat{Y}_{i,j} - \hat{Y}_{i-1,j}| \right|^{\alpha} + \left| |Y_{i,j-1} - Y_{i,j}| - |\hat{Y}_{i,j-1} - \hat{Y}_{i,j}| \right|^{\alpha}, \end{aligned} \quad (6)$$

Algorithm 1: Training adversarial networks for next frame generation

Set the learning rates ρ_D and ρ_G , and weights $\lambda_{adv}, \lambda_{\ell_p}$.

while not converged **do**

Update the discriminator D :

Get M data samples $(X, Y) = (X^{(1)}, Y^{(1)}), \dots, (X^{(M)}, Y^{(M)})$

$$W_D = W_D - \rho_D \sum_{i=1}^M \frac{\partial \mathcal{L}_{adv}^D(X^{(i)}, Y^{(i)})}{\partial W_D}$$

Update the generator G :

Get M new data samples $(X, Y) = (X^{(1)}, Y^{(1)}), \dots, (X^{(M)}, Y^{(M)})$

$$W_G = W_G - \rho_G \sum_{i=1}^M \left(\lambda_{adv} \frac{\partial \mathcal{L}_{adv}^G(X^{(i)}, Y^{(i)})}{\partial W_G} + \lambda_{\ell_p} \frac{\partial \mathcal{L}_{\ell_p}(X^{(i)}, Y^{(i)})}{\partial W_G} \right)$$

Table 1: Network architecture (Input: 4 frames – output: 1 frame)

Generative network scales	G_1	G_2	G_3	G_4
Number of feature maps	128, 256, 128	128, 256, 128	128, 256, 512, 256, 128	128, 256, 512, 256, 128
Conv. kernel size	3, 3, 3, 3	5, 3, 3, 5	5, 3, 3, 3, 5	7, 5, 5, 5, 7
Adversarial network scales	D_1	D_2	D_3	D_4
Number of feature maps	64	64, 128, 128	128, 256, 256	128, 256, 512, 128
Conv. kernel size (no padding)	3	3, 3, 3	5, 5, 5	7, 7, 5, 5
Fully connected	512, 256	1024, 512	1024, 512	1024, 512

where α is an integer greater or equal to 1, and $|.|$ denotes the absolute value function. To the best of our knowledge, the closest related work to this idea is the work of Mahendran & Vedaldi (2015), using a total variation regularization to generate images from learned features. Our GDL is fundamentally different: In (Mahendran & Vedaldi, 2015), the total variation takes only the reconstructed frame in input, whereas our loss penalises gradient differences between the prediction and the true output. Second, we chose the simplest possible image gradient by considering the neighbor pixel intensities differences, rather than adopting a more sophisticated norm on a larger neighborhood, for the sake of keeping the training time low.

2.4 COMBINING LOSSES

In our experiments, we combine the losses previously defined with different weights. The final loss is:

$$\mathcal{L}(X, Y) = \lambda_{adv} \mathcal{L}_{adv}^G(X, Y) + \lambda_{\ell_p} \mathcal{L}_p(X, Y) + \lambda_{gdl} \mathcal{L}_{gdl}(X, Y) \quad (7)$$

3 EXPERIMENTS

We now provide a quantitative evaluation of the quality of our video predictions on UCF101 (Soomro et al., 2012) and Sports1m (Karpathy et al., 2014) video clips. We train and compare two configurations: (1) We use 4 input frames to predict one future frame. In order to generate further in the future, we apply the model recursively by using the newly generated frame as an input. (2) We use 8 input frames to produce 8 frames simultaneously. This second configuration represents a significantly harder problem and is presented in Appendix.

3.1 DATASETS

We use the Sports1m for the training, because most of UCF101 frames only have a very small portion of the image actually moving, while the rest is just a fixed background. We train our network by randomly selecting temporal sequences of patches of 32×32 pixels after making sure they show enough movement (quantified by the ℓ_2 difference between the frames). The data patches are first normalized so that their values are comprised between -1 and 1.

3.2 NETWORK ARCHITECTURE

We present results for several models. Unless otherwise stated, we employed multiscale architectures. Our baseline models are using ℓ_1 and ℓ_2 losses. The GDL- ℓ_1 (respectively GDL- ℓ_2) model is using a combination of the GDL with $\alpha = 1$ (respectively $\alpha = 2$) and $p = 1$ (respectively $p = 2$) loss; the relative weights λ_{gdl} and λ_{ℓ_p} are both 1. The adversarial (Adv) model uses the adversarial loss, with $p = 2$ weighted by $\lambda_{adv} = 0.05$ and $\lambda_{\ell_p} = 1$. Finally, the Adv+GDL model is a combination of the adversarial loss and the GDL, with the same parameters as for Adv with $\alpha = 1$ and $\lambda_{gdl} = 1$.

Generative model training: The generative model G architecture is presented in Table 1. It contains padded convolutions interlaced with ReLU non linearities. A Hyperbolic tangent (Tanh) is added at the end of the model to ensure that the output values are between -1 and 1. The learning rate ρ_G starts at 0.04 and is reduced over time to 0.005. The minibatch size is set to 4, or 8 in the case of the adversarial training, to take advantage of GPU hardware capabilities. We train the network on small patches, and since it is fully convolutional, we can seamlessly apply it on larger images at test time.

Adversarial training: The discriminative model D , also presented in Table 1, uses standard non padded convolutions followed by fully connected layers and ReLU non linearities. For the largest scale s_4 , a 2×2 pooling is added after the convolutions. The network is trained by setting the learning rate ρ_D to 0.02.

3.3 QUANTITATIVE EVALUATIONS

To evaluate the quality of the image predictions resulting from the different tested systems, we compute the Peak Signal to Noise Ratio (PSNR) between the true frame Y and the prediction \hat{Y} :

$$\text{PSNR}(Y, \hat{Y}) = 10 \log_{10} \frac{\max_{\hat{Y}}^2}{\frac{1}{N} \sum_{i=0}^N (Y_i - \hat{Y}_i)^2}, \quad (8)$$

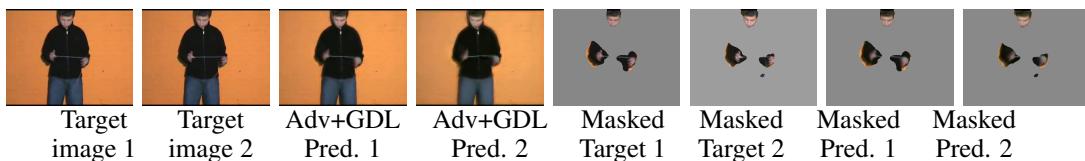
where $\max_{\hat{Y}}$ is the maximum possible value of the image intensities. We also provide the Structural Similarity Index Measure (SSIM) of Wang et al. (2004). It ranges between -1 and 1, a larger score meaning a greater similarity between the two images.

To measure the loss of sharpness between the true frame and the prediction, we define the following sharpness measure based on the difference of gradients between two images Y and \hat{Y} :

$$\text{Sharp. diff.}(Y, \hat{Y}) = 10 \log_{10} \frac{\max_{\hat{Y}}^2}{\frac{1}{N} \left(\sum_i \sum_j |(\nabla_i Y + \nabla_j Y) - (\nabla_i \hat{Y} + \nabla_j \hat{Y})| \right)}. \quad (9)$$

where $\nabla_i Y = |Y_{i,j} - Y_{i-1,j}|$ and $\nabla_j Y = |Y_{i,j} - Y_{i,j-1}|$.

Figure 3: Our evaluation of the accuracy of future frames prediction only takes the moving areas of the images into account. Left: example of our frame predictions in a entire image with ground truth; Right: images masked with thresholded optical flow.



As for the other measures, a larger score is better. These quantitative measures on 378 test videos from UCF101¹ are given in Table 2. As it is trivial to predict pixel values in static areas, especially on

¹We extracted from the test set list video files every 10 videos, starting at 1, 11, 21 etc.

Table 2: Comparison of the accuracy of the predictions on 10% of the UCF101 test images. The different models have been trained given 4 frames to predict the next one. Similarity and sharpness measures evaluated only in the areas of movement. Our best model has been fine-tuned on UCF101 after the training on Sports1m.

	1 st frame prediction scores			2 nd frame prediction scores		
	Similarity		Sharpness	Similarity		Sharpness
	PSNR	SSIM		PSNR	SSIM	
single sc. ℓ_2	26.5	0.84	24.7	22.4	0.82	24.2
ℓ_2	27.6	0.86	24.7	22.5	0.81	24.2
ℓ_1	28.7	0.88	24.8	23.8	0.83	24.3
GDL ℓ_1	29.4	0.90	25.0	24.9	0.84	24.4
GDL ℓ_1^*	29.9	0.90	25.0	26.4	0.87	24.5
Adv*	30.6	0.89	25.2	26.1	0.85	24.2
Adv+GDL*	31.5	0.91	25.4	28.0	0.87	25.1
Adv+GDL fine-tuned *	32.0	0.92	25.4	28.9	0.89	25.0
Last input	28.6	0.89	24.6	26.3	0.87	24.2
Optical flow	31.6	0.93	25.3	28.2	0.90	24.7

* models fine-tuned on patches of size 64×64 .

the UCF101 dataset where most of the images are still, we performed our evaluation in the moving areas as displayed in Figure 3. To this end, we use the EpicFlow method of Revaud et al. (2015), and compute the different quality measures only in the areas where the optical flow is higher than a fixed threshold². Similarity and sharpness measures computed on the whole images are given in Appendix.

The numbers clearly indicate that all strategies perform better than the ℓ_2 predictions in terms of PSNR, SSIM and sharpness. The multi-scale model brings some improvement, but used with an ℓ_2 norm, it does not outperform simple frame copy in the moving areas. The ℓ_1 model improves the results, since it replaces the mean by the median value of individual pixel predictions. The GDL and adversarial predictions are leading to further gains, and finally the combination of the multi-scale, ℓ_1 norm, GDL and adversarial training achieves the best PSNR, SSIM and Sharpness difference measure.

It is interesting to note that while we showed that the ℓ_2 norm was a poor metric for training predictive models, the PSNR at test time is the worst for models trained optimising the ℓ_2 norm, although the PSNR is based on the ℓ_2 metric. We also include the baseline presented in Ranzato et al. (2014) – courtesy of Piotr Dollar – that extrapolates the pixels of the next frame by propagating the optical flow from the previous ones.

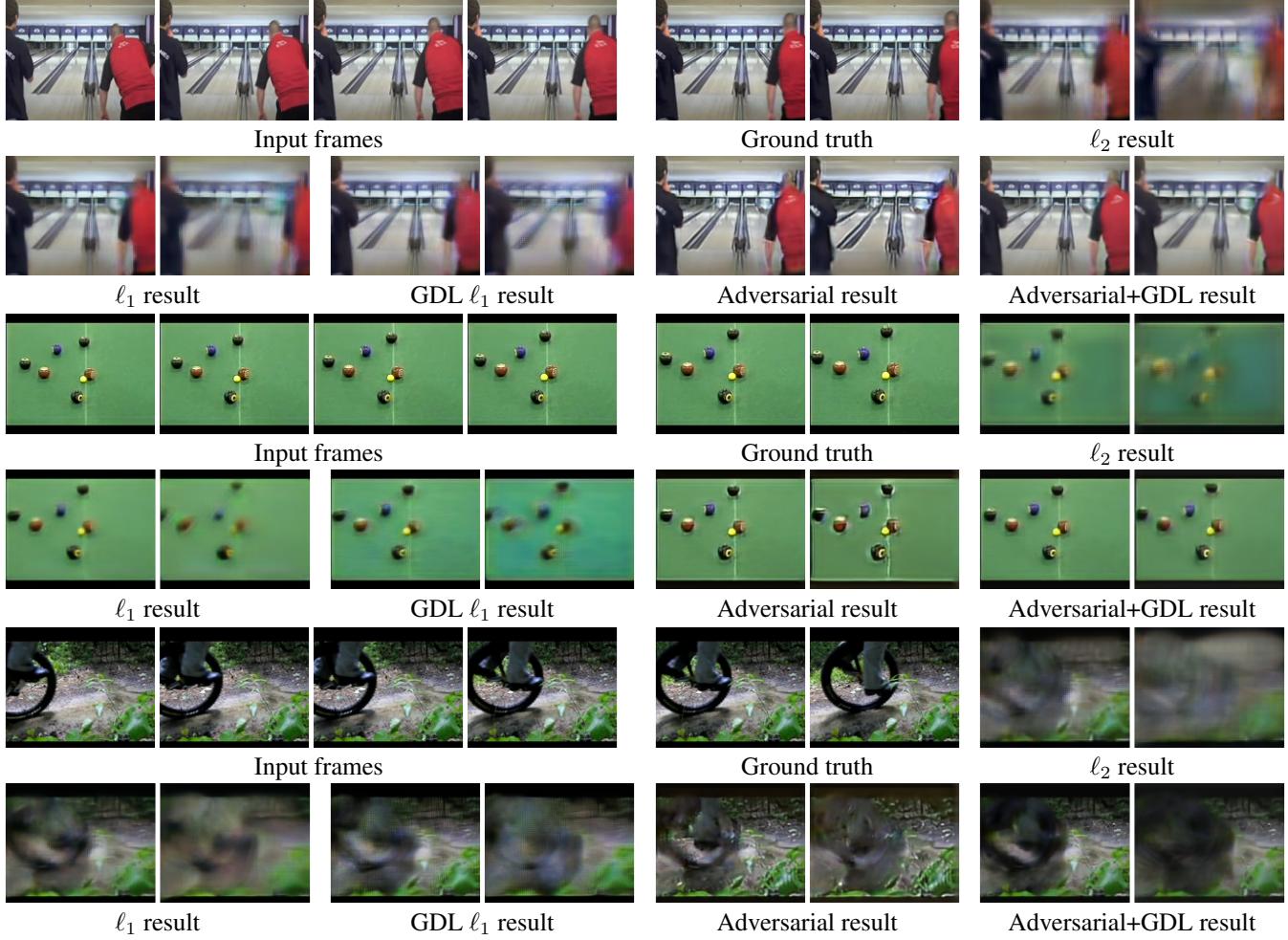
Figure 4 shows results on test sequences from the Sport1m dataset, as movements are more visible in this dataset.

3.4 COMPARISON TO RANZATO ET AL. (2014)

In this section, we compare our results to (Ranzato et al., 2014). To obtain grayscale images, we make RGB predictions and extract the Y channel of our Adv+GDL model. Ranzato et al. (2014) images are generated by averaging 64 results obtained using different tiling to avoid a blockiness effect, however creating instead a blurriness effect. We compare the PSNR and SSIM values on the first predicted images of Figure 5.

²We use default parameters for the Epic Flow computation, and transformed the .flo file to png using the Matlab code <http://vision.middlebury.edu/flow/code/flow-code-matlab.zip>. If at least one color channel is lower than 0.2 (image color range between 0 and 1), we replace the corresponding pixel intensity of the output and ground truth to 0, and compute similarity measures in the resulting masked images.

Figure 4: Results on 3 video clips from Sport1m. Training: 4 inputs, 1 output. Second output computed recursively.

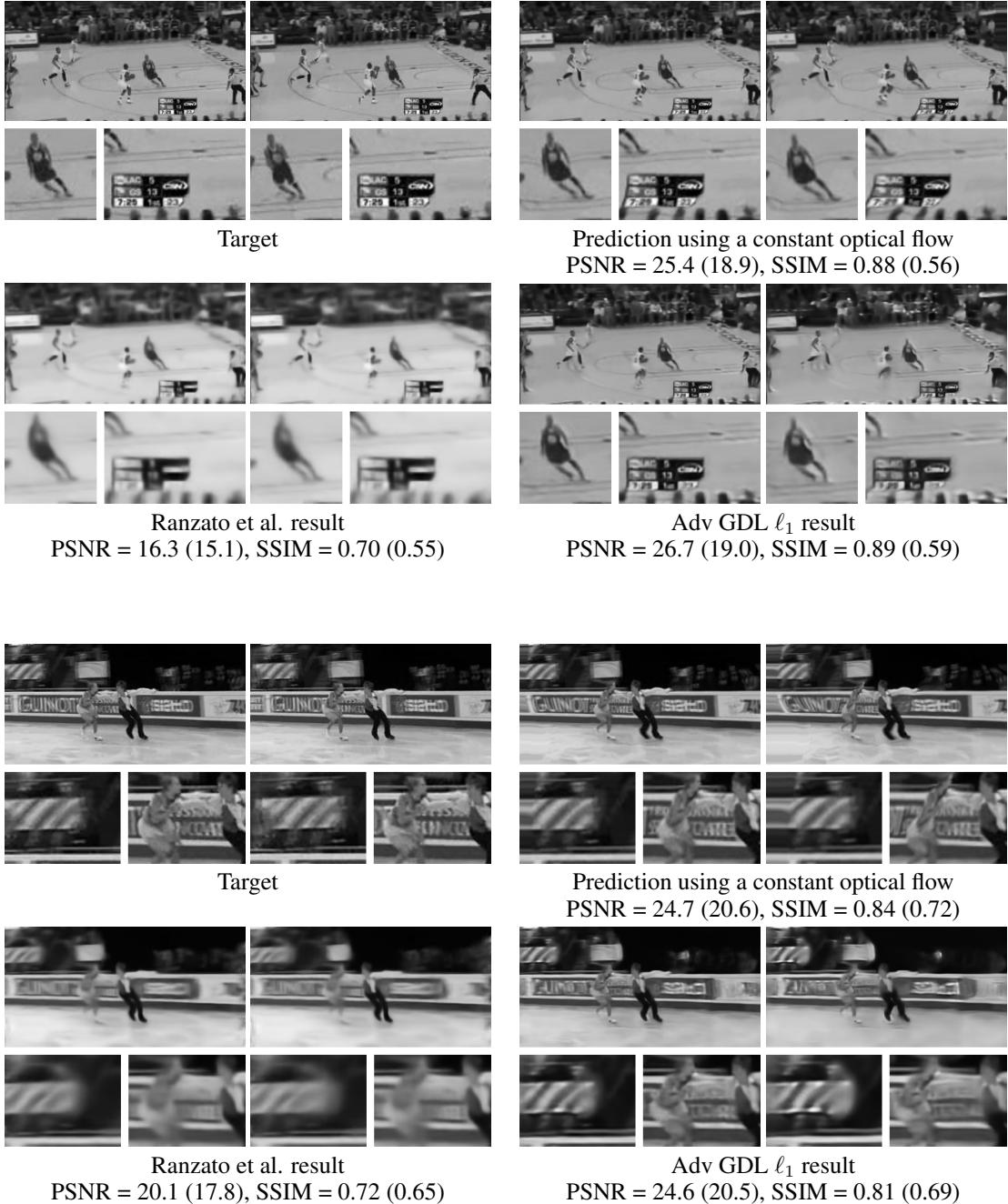


We note that the results of Ranzato et al. appear slightly lighter than our results because of a normalization that does not take place in the original images, therefore the errors given here are not reflecting the full capacity of their approach. We tried to apply the blind deconvolution method of Krishnan et al. (2011) to improve Ranzato et al. and our different results. As expected, the obtained sharpness scores are higher, but the image similarity measures are deteriorated because often the contours of the predictions do not match exactly the targets. More importantly, Ranzato et al. results appear to be more static in moving areas. Visually, the optical flow result appears similar to the target, but a closer look at thin details reveals that lines, heads of people are bent or squeezed.

4 CONCLUSION

We provided a benchmark of several strategies for next frame prediction, by evaluating the quality of the prediction in terms of Peak Signal to Noise Ratio, Structural Similarity Index Measure and image sharpness. We display our results on small UCF video clips at <http://cs.nyu.edu/~mathieu/iclr2016.html>. The presented architectures and losses may be used as building blocks for more sophisticated prediction models, involving memory and recurrence. Unlike most optical flow algorithms, the model is fully differentiable, so it can be fine-tuned for another task if necessary. Future work will deal with the evaluation of the classification performances of the learned

Figure 5: Comparison of results on the Basketball Dunk and Ice Dancing clips from UCF101 appearing in (Ranzato et al., 2014). We display 2 frame predictions for each method along with 2 zooms of each image. The PSNR and SSIM values are computed in the moving areas of the images (More than the 2/3 of the pixels in these examples). The values in parenthesis correspond to the second frame predictions measures.



representations in a weakly supervised context, for instance on the UCF101 dataset. Another extension of this work could be the combination of the current system with optical flow predictions. Alternatively, we could replace optical flow predictions in applications that does not explicitly re-

quire optical flow but rather next frame predictions. A simple example is causal (where the next frame is unknown) segmentation of video streams.

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5 APPENDIX

5.1 PREDICTING THE EIGHT NEXT FRAMES

In this section, we trained our different multi-scale models – architecture described in Table 3– with 8 input frames to predict 8 frames simultaneously. Image similarity measures are given between the ground truth and the predictions in Table 4.

Table 3: Network architecture

Models 8 frames in input – 8 frames in output				
Generative network scales	G_1	G_2	G_3	G_4
Number of feature maps	16, 32, 64	16, 32, 64	32, 64, 128	32, 64, 128, 128
Conv. kernel size	3, 3, 3, 3	5, 3, 3, 3	5, 5, 5, 5	7, 5, 5, 5, 5
Adversarial network scales	D_1	D_2	D_3	D_4
Number of feature maps	16	16, 32, 32	32, 64, 64	32, 64, 128, 128
Conv. kernel size (no padding)	3	3, 3, 3	5, 5, 5	7, 7, 5, 5
Fully connected	128, 64	256, 128	256, 128	256, 128

For the first and eighth predicted frames, the numbers clearly indicate that all strategies perform better than the ℓ_2 predictions in terms of PSNR and sharpness. The ℓ_1 model, by replacing the mean intensity by the median value in individual pixel predictions, allows us to improve results. The adversarial predictions are leading to further gains, and finally the GDL allows the predictions to achieve the best PNSR and sharpness. We note that the size of the network employed in the simultaneous prediction configuration is smaller than in the unique frame prediction setting.

Table 4: Comparison of the accuracy of the predictions on 10% of the UCF101 test images. The different models have been trained given 8 frames to predict the 8 next ones.

	1 st frame prediction scores		8 th frame prediction scores			
	Similarity		Similarity			
	PSNR	SSIM	PSNR	SSIM		
ℓ_2	18.3	0.59	17.5	0.51	17.4	
Adv	21.1	0.61	17.6	0.52	17.4	
ℓ_1	21.3	0.66	17.7	0.55	17.5	
GDL ℓ_1	21.4	0.69	17.9	0.58	17.5	
Last input	30.6	0.90	22.3	0.74	18.5	

Figure 6 shows a generation result of eight frames simultaneously, using a large version of the GDL ℓ_1 model in which all the number of feature maps were multiplied by four.

Figure 6: Results on a UCF101 video using a large GDL- ℓ_1 model. Training: 8 inputs, 8 outputs. First line: target, second line: our predictions.

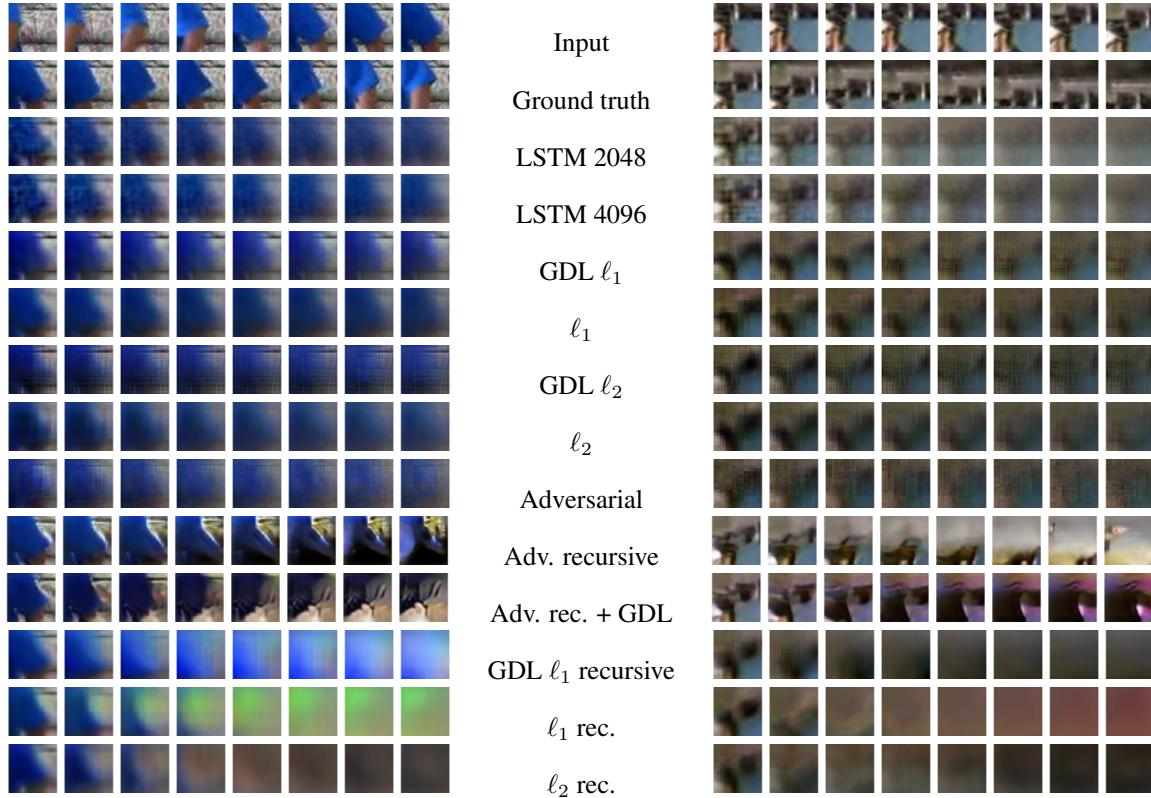


Compared to the recursive frame prediction as employed in the rest of the paper, predicting several input simultaneously leads to better long term results but worst shorter term ones. The gap between the two performances could be reduced by the design of time multi-scale strategies.

5.2 COMPARISON TO THE LSTM APPROACH OF SRIVASTAVA ET AL. (2015)

Figure 7 shows a comparison with predictions based on LSTMs using sequences of patches from (Srivastava et al., 2015). The model ranking established on UCF101 in terms of sharpness and PSNR remains unchanged on the two sequences. When we employ the setting 8 inputs-8 output described in Table 3, we note that the LSTM first frame prediction is sharper than our models predictions, however when looking at a longer term future, our gradient difference loss leads to sharper results. Comparing visually the GDL ℓ_1 and GDL ℓ_2 , we notice that the predictions suffer from a chessboard effect in the ℓ_2 case. On the other hand, when employing the recursive strategy (4 inputs, 1 output), the adversarial training lead to much sharper predictions. It does not look like anything close to the ground truth on the long term, but it remains realistic.

Figure 7: Comparison of different methods to predict 32×32 patches from UCF101. The LSTM lines are from (Srivastava et al., 2015). Baseline results with pure ℓ_1 and ℓ_2 losses are shown in Appendix.



5.3 ADDITIONAL RESULTS ON THE UCF101 DATASET

We trained the model described in Table 1 with our different losses to predict 1 frame from the 4 previous ones. We provide in Table 5 similarity (PSNR and SSIM) and sharpness measures between the different tested models predictions and frame to predict. The evaluation is performed on the full images but is not really meaningful because predicting the future location of static pixels is most accurately done by copying the last input frame.

Table 5: Comparison of the accuracy of the predictions on 10% of the UCF101 test images. The different models have been trained given 4 frames to predict the next one. Similarity and sharpness measures on full images.

	1 st frame prediction scores			2 nd frame prediction scores		
	Similarity		Sharpness	Similarity		Sharpness
	PSNR	SSIM		PSNR	SSIM	
single sc. ℓ_2	19.0	0.59	17.8	14.2	0.48	17.5
ℓ_2	20.1	0.64	17.8	14.1	0.50	17.4
ℓ_1	22.3	0.74	18.5	16.0	0.56	17.6
GDL ℓ_1	23.9	0.80	18.7	18.6	0.64	17.7
Adv	24.4	0.77	18.7	18.9	0.59	17.3
Adv+GDL	27.2	0.83	19.6	22.6	0.72	18.5
Adv+GDL fine-tuned	29.6	0.90	20.3	26.0	0.83	19.4
Last input	30.0	0.90	22.1	25.8	0.84	20.3