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Bloom Filters in MapReduce

Project report

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1 Introduction

A *Bloom Filter* is a space-efficient probabilistic data structure that is used to test whether an element is a member of a set. The cost paid for efficiency is that there might be some false positive results. False positive means, it might tell that an element is present but actually it is not.

It is initialized as an array of bits set to 0. Then some hashing functions are needed, each of which can map an element of the database to one of the m positions of the array. The mapping must also have a uniform distribution. To add an element the k hashing functions are recalculated to obtain the positions of the relative bits and setting them to 1. The verification of the presence of an element is accomplished by calculating the hashing functions on the controlled element, determining which bits should be set. The element is absent if even one of the bits is 0. For this reason, as the number of elements inserted in the *Bloom Filter* increases, the percentage of false positives becomes higher.

This data structure is efficient because the time needed to add or to find an element is constant and depending from the number of hash functions selected but independent from the number of elements that are already present.

In this project is presented a possible MapReduce implementation of a *Bloom Filter* using *Hadoop* and *Spark* and finally a comparison of the results obtained.

2 Design

The workflow that has been followed is structured in 3 stages: the first consists in the calibration of the parameters, then the Bloom Filters are created and populated and finally the performances are evaluated in terms of false positive rate.

2.1 Dataset

The dataset exploited is taken from IMDb and contains a list of films with the relative ratings. It is composed by the attributes [tconst, averageRating, numVotes] but only the first two have been considered in this work, i.e. id of the film and relative average rating.

In Figure 1 the bar diagram shows the films distribution considering their rounded ratings.

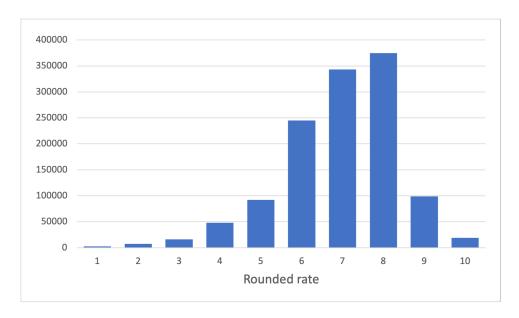


Figure 1: Rate distribution

2.2 Assumptions

To build a Bloom filter four main parameters are needed:

- p: false positive rate;
- k: number of hash functions;
- m: number of bits of the bloom filter;
- n: number of keys in input to the bloom filter.

The relations between these values can be expressed as:

$$m = -\frac{n \ln p}{(\ln 2)^2}$$
$$k = \frac{m}{n} \ln 2$$

$$p \approx (1 - e^{-\frac{kn}{m}})^k$$

To design a *Bloom Filter* with a given false positive rate p, first the number of keys n to be added have to be estimated, then the number of bits are computed and finally the number of hash functions k to use can be obtained.

The average ratings in the dataset are rounded to the closest integer value, and a $Bloom\ Filter$ is computed for each rating value. For this reason the number of $Bloom\ Filters$ will be 10, given that the rating value is in the range [1,10].

Given n and decided p a priori, the parameter m is dependent from both whereas k is only dependent from p as proved replacing m in its formula. Hence every $Bloom\ Filter$ may have a different m but all share the same number k of hash functions.

2.3 Parameter Calibration

The first stage calibrates the necessary parameters for the following steps.

Every **mapper** build an associative array counting how many films per rate. In particular, it parses each film of those that locally have, rounds its rating and increases the relative counter in the array. Then it emits < rate, count > pairs. The in-mapper combiner has been used in order to reduce the number of intermediate data produced.

```
class Mapper
 1: method Initialize
        counter \leftarrow \mathbf{new} \ Array[rates]
 2:
 3: method MAP (film f)
 4:
        rate \leftarrow round(f.rate);
 5:
        counter[rate] \leftarrow counter[rate] + 1;
 6: method Close
 7:
        for all r \in rates do
            Emit(r, counter[r])
 8:
        end for
 9:
```

The **reducer** takes in input the < rate, count > values, computes n for every Bloom Filter summing the counters of the mappers and define the relative m and k.

class Reducer

```
1: method Reduce (rate, counters[c1,c2,...])
2: n \leftarrow 0
3: for all c \in \text{counters } \mathbf{do}
4: n \leftarrow n + c
5: end for
6: m \leftarrow -n * \ln p / (\ln 2)^2
7: k \leftarrow \ln 2 * m / n
8: \text{EMIT}(rate, \{m, k, n\})
```

A second solution has been implemented in order to emit a lower number of bytes in output from each reducer. The **reducer** computes only the parameter n.

```
class Reducer
```

```
1: method REDUCE (rate, counters[c1,c2,...])
2: n \leftarrow 0
3: for all c \in \text{counters } \mathbf{do}
4: n \leftarrow n + c
5: end for
6: \text{EMIT}(rate, n)
```

2.4 Bloom Filters Creation

The second stage consists in the creation of the *Bloom Filter*. They have been implemented as arrays of bits filled with the result of the hashing functions generated for every film.

Every **mapper** creates an array of *Bloom Filters*, one for each rate, using the parameters calculated during the Parameter Calibration stage. In the *Map* function, for each film the indices of the correspondent *Bloom Filter* are set. At the end, in the *Close* function, for each rating is emitted the correspondent *Bloom Filter*.

class Mapper

```
1: method Initialize
       for all i \in rates do
2:
3:
           bf \leftarrow new BloomFilter(m,k)
       end for
 4:
5: method MAP (film f)
6:
       rate \leftarrow round(f.rate)
       bf[rate].insert(f);
 7:
8:
       method Close (film f)
       for all i \in rates do
9:
           Emit(rate, bf)
10:
       end for
11:
```

Each **reducer** computes the or operation between the partial $Bloom\ Filters$ for each rating in order to get the unified result.

class Reducer

```
1: method Reduce (rate, bf[bf1,bf2,...])
2: result \leftarrow \mathbf{new} \ BloomFilter(b1.m)
3: for all bf \in [bf1,bf2,...] do
4: result.or(bf)
5: end for
6: EMIT(rate, result)
```

Another solution for the creation $Bloom\ Filter$ has been implemented: every **mapper** computes the k hash functions on the films' ID and emits < rate, indices > pairs concerning the rounded rate and an integer array representing the binary configuration of the bits to set.

class Mapper

```
1: method Initialize
2: indices \leftarrow new Array[k]
3: method MAP (film f)
4: rate \leftarrow round(f.rate)
5: counter[rate] \leftarrow counter[rate] + 1;
6: for i \in 0,...,k do
7: indices[i] \leftarrow abs(MurmurHash(f.id) \% m[rate])
8: end for
9: EMIT(rate, indices)
```

The **reducer** receives the output of the mappers, creates the *Bloom Filters*, each with its own length m, fills them with the indices received and writes them to the HDFS.

class Reducer

```
1: method Reduce (rate, indices)
2:
       BitSet\ bs \leftarrow \mathbf{new}\ BitSet(m)
3:
       for all arr \in indices do
           for all i \in arr do
4:
               bs.set(arr[i])
5:
           end for
6:
       end for
7:
       BloomFilter\ bf \leftarrow \mathbf{new}\ BloomFilter(k, m, bs)
8:
       Emit(rate, bit)
9:
```

2.5 Bloom Filters Validation

The last stage is the evaluation of the false positive rate for each rating. First of all the *Bloom Filters* previously created and populated are taken from HDFS, then the MapReduce paradigm does what follows.

Every **mapper** builds an array containing a counter for each rate representing the number of false positives of the relative *Bloom Filter*.

```
class Mapper
```

```
1: method Initialize
        fp\_counters \leftarrow \mathbf{new} \ Array[rates]
 2:
        for all r \in rates do
 3:
 4:
            bf \leftarrow readFromFile()
            bloomFilters[r] \leftarrow \mathbf{new} \ BloomFilter(r, bf)
 5:
 6:
        end for
 7: method MAP (film f)
        rate \leftarrow round(f.rate) - 1
 8:
        for all r \in rates do
 9:
            if rate == r then
10:
               continue
11:
12:
            end if
           if bloomFilters[r].find(f) == true then
13:
                fp\_counters[r] + +
14:
           end if
15:
        end for
16:
17: method CLOSE
        for all r \in rates do
18:
19:
            Emit(rate, fp_counters)
20:
        end for
```

The **reducer** sums all the counters relative to the same rating and emits them.

class Reducer

```
1: \mathbf{method} Reduce (rate, mapper_counts[1,2,...])
```

- 2: counter = 0
- 3: for all $i \in mapper_counts$ do
- 4: counter + = i
- 5: end for
- 6: Emit(rate, counter)

3 Hadoop

3.1 Implementation

Concerning the hashing, the family org.apache.hadoop.util.hash.Hash.MURMUR_HASH hash function family has been used. This is a very fast, non-cryptographic hash suitable for general hash-based lookup.

For what concerns the different solutions compared in 7.1.1 and 7.1.2 they can be found in the *test* branch of the GitHub link. In particular, the *parametersDriver* module presents in both stages the implementation of the second solution, while the *sendBF* one has the combination of the others (all parameters evaluated in the Reducer phase and sending BF instead of indices).

3.1.1 Bloom Filter

The *Bloom Filter* class makes use of the object Bitset to implement the array of bits because it provides good results in terms of memory usage. It extends the Writable interface, so the methods for serialize and de-serialize objects over Hadoop have been redefined.

3.1.2 Parameter Calibration

Regarding the Calibration Reducer, two different solutions have been considered in order to compare the output bytes.

In the first solution, the Reducer compute the value of m and k starting from the total count of films per rate and emit, for each rate, an array of IntWritable objects (n, m, k).

In the second solution, the Reducer compute and emit only the total number of films per rate (n) and the values of m and k are computed on the driver allowing the reducer to emit a single IntWritable instead of an array. This solution is possible because the value of m depends on n and p, while the value of k only depends on p, so we avoid to emit it for each rate being equal for all of them.

3.1.3 Bloom Filter Creation

The creation stage also has two different implementations considering where the *Bloom-Filter* object is created.

In the first solution in the map phase a local ArrayList < BloomFilter > is created and sent to the reduce phase that does the or operation to create the final 10 filters.

In the second solution the *map* function emits an IntArrayWritable filled with the indices of the positions of the filter to be set. The BitSet object is then created and filled in the reduce phase and then passed to the *BloomFilter* constructor.

3.1.4 Parameter Validation

The last stage evaluates the false positive rate basing on the Bloom Filters and the parameters computed in the first two stages. It also exploits the MapReduce paradigm to parallelize the process. The filters just created are read and the **reduce** function takes care of the false positives count. This result is finally compared, for every rating, with the total number of film for each filter in the Driver.

3.2 Results

Using p = 0.01 the result is a value of k = 6 and the values of m are shown in Table 1.

Rating	n	m			
1	2555	24489			
2	6467	61986			
3	17051	163434			
4	42128	403799			
5	97625	935741			
6	215643	2066950			
7	369543	3542091			
8	352852	3382107			
9	118182	1132781			
10	19028	182384			

Table 1: m values for each rating

Table 2 shows the result in terms of false positive count and false positive rate for every class.

Dating	p = 0.01		p = 0.05			p = 0.1		
Rating	FP	FPR		FP	FPR		FP	FPR
1	12690	0.0102		61008	0.0493		141458	0.1142
2	12523	0.0101		62557	0.0507		144156	0.1168
3	12208	0.0099		61982	0.0506		142771	0.1166
4	12024	0.0100		60186	0.0502		139430	0.1163
5	11638	0.0101		57499	0.0503		134094	0.1173
6	10536	0.0102		51551	0.0503		120113	0.1171
7	9015	0.0103		43675	0.0501		101586	0.1166
8	8796	0.0099		44940	0.0506		102946	0.1159
9	11406	0.0101		56570	0.0504		130603	0.1163
10	12117	0.0099		62011	0.0507		141230	0.1156

Table 2: FP and FPR with different p values

The different solutions for each stage were compared in terms of output bytes and execution time by varying the number of mappers and reducers. For each one, the one that guarantees the best trade off has been chosen.

For the first stage, we considered the two different implementations of the Reducer explained in 2.3: in the first solution (red one), the Reducer computes the values of n, m and k and emit, for each rate, an array of IntWritable objects (n, m, k); in the second solution (blue one), the Reducer compute only the total number n of films per rate, while the values of m and k are computed on the Driver, allowing the reducer to emit, for each rate, a single IntWritable instead of an array. This solution is possible because the value of m depends on n and p, while the value of k only depends on p, so we avoid to emit it for each rate being equal for all of them. In Figure 2 the execution time of the two different solutions have been compared using different numbers of mappers and reducers.

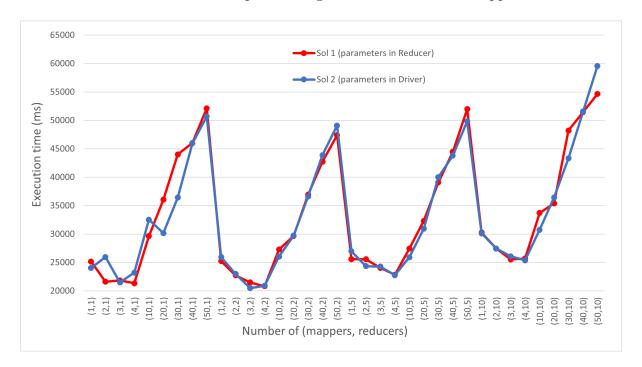


Figure 2: First stage solution execution time comparison

The two solutions have been compared also in terms of output bytes.

	Solution 1	Solution 2
Number of bytes written (HDFS)	374	252

As expected, the output bytes of the second solution are lower then the first. The second, indeed, needs to emit all the parameters computed, the first one emits only the n parameter.

The two solutions both provide comparable performances in terms of execution time, but the second one ensures also a lower number of output bytes. For this reason, **the second**

one has been chosen.

Regarding the second stage, the two solutions of 2.4 have been compared in terms of mapper output bytes. In the first solution (yellow one), each mapper creates a *Bloom Filter* for each rate and sends all of them to the reducer. In the second solution (green one) the mapper sends, for each film, the indices calculated with the hash function. As shown in Figure 3, the mapper output bytes of the second solution are constant. It was expected because the output bytes of the mapper are linear w.r.t. the input lines. Instead, in the first solution, increasing the number of mappers the number of output bytes emitted increases too because each mapper creates and emits ten *Bloom Filters*, one for each rate. For this reason, more mappers means more output bytes.

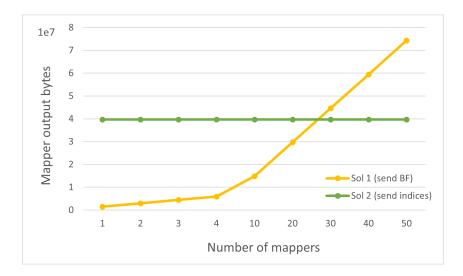


Figure 3: Second stage solution mapper bytes comparison

Considering the memory overhead, the first solution maintains as class fields the bloom filters and we can encounter scalability problems due to the store of all the Bloom Filters in memory, so the second solution has been preferred.

For the sake of completeness in Figure 4 the execution time of the two different solutions are shown using different numbers of mappers and reducers.

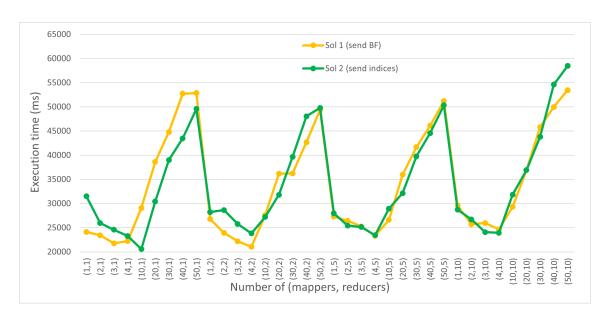


Figure 4: Second stage solution execution time comparison

Basing on the aspects previously highlighted, the second solution has been chosen because of the higher number of bytes emitted with a higher number of mappers and the memory overhead. Indeed, even if the execution time of the first solution is higher than the second, the difference becomes smaller with the increasing of the number of mapper.

4 Spark

4.1 Implementation

Following the implementation made in Hadoop, a similar one was built in the Spark framework. The following lineage graphs show the workflow of the the different stages.

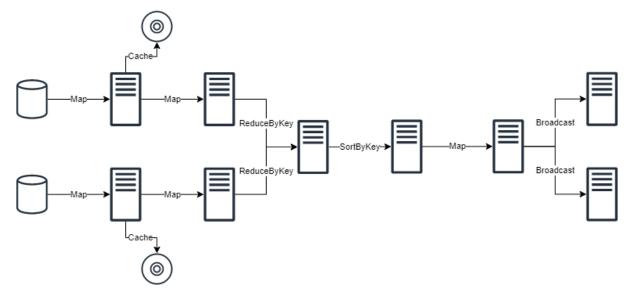


Figure 5: Spark's Parameter Calibration Workflow

The application takes as inputs the dataset and the value of p. In the Parameters Calibration stage (Figure 5) the data set is loaded and mapped inverting the original $\langle key, value \rangle$ pairs, caching it as it will be used in every stage. An aggregation is then executed in order to count for each vote the number of movies. Finally k, an array of m values and the number of films per vote are computed and saved in broadcast variables for all the worker to be accessed.

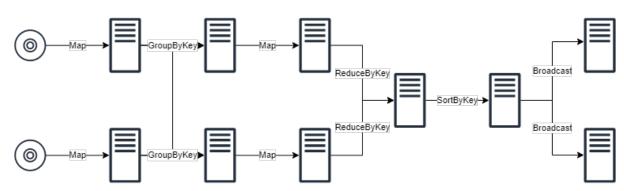


Figure 6: Spark's Bloom Filter Creation Workflow

In the Bloom Filter Creation stage (Figure 6) the partitioned data set is loaded from the cache and the different movies are grouped in lists by their respective keys, shuffling them between workers. Each list is the used to calculate the k hashes of each title in order

to populate local bloom filters. Finally the global bloom filters are created by aggregating the local ones and are then sent in broadcast to all workers following the same reasoning of the previous stage.

4.2 Results

Table 3 shows the result in terms of false positive count and false positive rate for every bloom filter at different values of p.

Rating	p = 0.01		p = 0.05			p = 0.1		
Rating	FP	FPR	FP	FPR		FP	FPR	
1	12466	0.0100	61435	0.0496		127149	0.1026	
2	12545	0.0101	60313	0.0488		123988	0.1005	
3	12244	0.0099	61709	0.0503		123247	0.1006	
4	12464	0.0104	60108	0.0503		120097	0.1006	
5	11838	0.0102	57728	0.0502		115003	0.1000	
6	10114	0.0101	50230	0.0503		100590	0.1008	
7	9222	0.0102	45259	0.0503		90746	0.1008	
8	8913	0.0102	43689	0.0502		87619	0.1008	
9	11591	0.0101	57485	0.0503		115517	0.1011	
10	12380	0.0101	61066	0.0499		123819	0.1013	

Table 3: Spark Framework FP and FPR with different p values

To check the correctness of the results an accumulator array was implemented and then populated by each worker by iterating the data set. In this last part the k hashes were computed on each film for each other vote different from its own, increasing the respective position of each vote in the accumulator in case of a False Positive.

5 Experimental results

In this paragraph the execution of the first two stages of the Hadoop and the Spark implementation are compared both in terms of FPR and execution time.

Rating	p = 0.01		p = 0.05			p = 0.1		
Training	Hadoop	Spark		Hadoop	Spark		Hadoop	Spark
1	0.0102	0.0100		0.0493	0.0496		0.1142	0.1026
2	0.0101	0.0101		0.0507	0.0488		0.1168	0.1005
3	0.0099	0.0099		0.0506	0.0503		0.1166	0.1006
4	0.0100	0.0104		0.0502	0.0503		0.1163	0.1006
5	0.0101	0.0102		0.0503	0.0502		0.1173	0.1000
6	0.0102	0.0101		0.0503	0.0503		0.1171	0.1008
7	0.0103	0.0102		0.0501	0.0503		0.1166	0.1008
8	0.0099	0.0102		0.0506	0.0502		0.1159	0.1008
9	0.0101	0.0101		0.0504	0.0503		0.1163	0.1011
10	0.0099	0.0101		0.0507	0.0499		0.1156	0.1013

Table 4: Hadoop and Spark FPR for different values of p

The obtained results concerning FPR shown in Table 4 are similar between the Hadoop and Spark implementation, specifically at p = 0.01 and p = 0.05, while at p = 0.1 there is an mean improvement of 0.016 on the Spark side.

In order to compare the results of the Hadoop and Spark implementations, it is necessary to choose a configuration of mappers-reducers for the Hadoop framework. In Figure 7 and Figure 8 are reported the selected solutions for stage 1 and stage 2 respectively. The trend shows that the execution time increases proportionally with the mappers if the number of reducers is fixed and, overall, also with the increasing of the number of reducers. From the plots a pattern can be identified: the execution time decreases from 1 to 4 mappers and increases from 4 to 10 so, at number of mappers equal to 4 the plot has its local minima and these local minima do not differ significantly from each other.

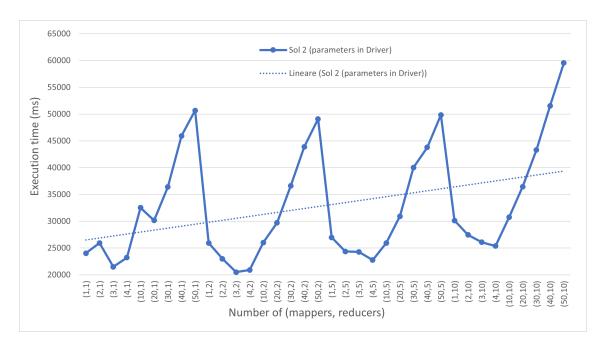


Figure 7: stage1



Figure 8: stage2

For simplicity, the configuration with the lowest total execution time of the algorithm (stage 1 and stage 2) has been chosen (Figure 9), corresponding to the one with 4 mappers and 2 reducers.

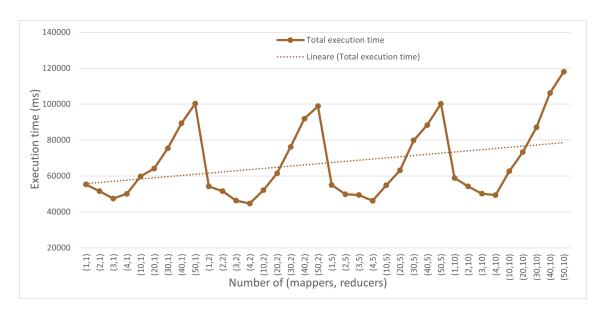


Figure 9: Total execution time plot

In Table 5 are shown the mean execution times of the different stages in both the Hadoop and Spark frameworks over 10 iterations. As expected, the execution times are lower in Spark, specifically in the second stage were more computation is needed for each row of the data set.

	Stage 1 (ms)	Stage 2 (ms)	Total (ms)
Hadoop	20906	23821	44727
Spark	17833	7857	25690

Table 5: Hadoop-Spark comparison

6 Conclusion

In this report the Bloom Filter data structure was implemented and tested in both the Hadoop and Spark frameworks, considering both the False Positive Rate and execution time of the two to highlight the differences. Spark's capability of in-memory processing, exploited by caching the mapped input data set, built-in support for distributed computing, which allows it to divide the filter into smaller chunks and process them in parallel, and for iterative processing, which makes it more suitable for implementing algorithms that require multiple passes over the data, reduce the execution time needed for computing the parameters and filling the Bloom Filters of almost half compared to its Hadoop counterpart. Hadoop, on the other hand, is designed for batch processing and does not have native support for distributed computing and in-memory processing, which can make it less efficient for creating Bloom Filters and in general for computation on large data sets.

7 Hadoop Code

7.1 Driver

```
public class Driver {
   // files for input and output
   private static final String OUTPUT_FOLDER = "output/";
   private static final String OUTPUT_CALIBRATE = "outStage1";
   private static final String OUTPUT_CREATE = "outStage2";
   private static final String OUTPUT_FP = "fp";
   // configuration variables
   private static String INPUT;
   private static int N_RATES;
   private static int N_REDUCERS;
   private static double P;
   private static int N_LINES;
   public static void main(String[] args) throws IOException, InterruptedException,
   ClassNotFoundException {
       Configuration conf = new Configuration();
       String[] otherArgs = new GenericOptionsParser(conf, args).getRemainingArgs();
       if(otherArgs.length != 5) {
           print("Arguments required: <input> <n_rates> <n_reducers>  <n_lines>");
           System.exit(-1);
       }
       //print configuration
       System.out.println("-----");
       System.out.println("Configuration variables\n");
       System.out.println("Input\t\t\" + otherArgs[0]);
       System.out.println("Number of rates:\t" + otherArgs[1]);
       System.out.println("Number of reducers:\t" + otherArgs[2]);
       System.out.println("P:\t\t\t" + otherArgs[3]);
       System.out.println("Number of lines:\t" + otherArgs[4]);
       System.out.println("-----
       //get args from terminal
       INPUT = otherArgs[0];
       N_RATES = Integer.parseInt(otherArgs[1]);
       conf.set("n_rates", otherArgs[1]);
       N_REDUCERS = Integer.parseInt(otherArgs[2]);
       P = Double.parseDouble(otherArgs[3]);
       N_LINES = Integer.parseInt(otherArgs[4]);
```

```
//errors
    if(P < 0 || P > 1 || N_RATES <= 0 || N_REDUCERS <= 0 || INPUT.equals("")) {</pre>
       print("Configuration not valid: check the arguments passed.");
       System.exit(-1);
    }
    // Clean HDFS workspace
    print("Clean HDFS workspace");
    FileSystem fs = FileSystem.get(conf);
    if(fs.exists(new Path(OUTPUT_FOLDER)))
        fs.delete(new Path(OUTPUT_FOLDER), true);
    // first stage
    print("Parameter calibration stage...");
    if(!calibrateParams(conf)){
       fs.close();
       System.exit(-1);
    print("Parameters correctly calibrated!");
    // read output of first stage and add m, k to configuration
    FileStatus[] status = fs.listStatus(new Path(OUTPUT_FOLDER +
OUTPUT_CALIBRATE));
    int n, m, k=0;// for m, k, n
    double p = conf.getDouble("p", 0.01);
    for(FileStatus filestatus : status) {
       String f = String.valueOf(filestatus.getPath());
       if(f.contains("SUCCESS"))
           continue;
       IntWritable key = new IntWritable();
       IntWritable nWritable = new IntWritable();
       try (SequenceFile.Reader reader = new SequenceFile.Reader(conf,
SequenceFile.Reader.file(filestatus.getPath()))) {
           while (reader.next(key, nWritable)) {
               n = nWritable.get();
               m = (int) (- (n * Math.log(p)) / (Math.pow(Math.log(2),2)));
               k = (int) ((m/n) * Math.log(2));
               //conf.set("filter_n", String.valueOf(n));
               conf.set("filter_" + key.get()+ "_m", String.valueOf(m));
               rate_count[key.get()-1] = n;
               Driver.print("Rating " + key + "\tm: " + m + "\tk: " + k + "\tn:
" + n);
           conf.set("filter_k", String.valueOf(k));
       }
```

```
// second stage
    print("Bloom filters creation stage...");
    if (!createBloomFilters(conf)) {
        fs.close();
        System.exit(-1);
    print("BloomFilters correctly created!");
    // third stage
    print("FP computation stage...");
    conf.set("outStage2", OUTPUT_FOLDER+OUTPUT_CREATE);
    if (!computeFP(conf)) {
        fs.close();
        System.exit(-1);
    print("FP correctly computed!");
    // get fp from 3rd stage output and compute fpr for every rating
    status = fs.listStatus(new Path(OUTPUT_FOLDER + OUTPUT_FP));
    int[] falsePositiveCounter = new int[N_RATES];
    for(FileStatus filestatus : status) {
        String f = String.valueOf(filestatus.getPath());
        if(f.contains("SUCCESS"))
            continue;
        IntWritable key = new IntWritable();
        IntWritable value = new IntWritable();
        try (SequenceFile.Reader reader = new SequenceFile.Reader(conf,
SequenceFile.Reader.file(filestatus.getPath()))) {
            while (reader.next(key, value)) {
                falsePositiveCounter[key.get()-1] = value.get();
            }
        }
    double[] falsePositiveRate = new double[N_RATES];
    double tot = 0;
    for (int i=0; i<N_RATES; i++)</pre>
        tot += rate_count[i];
    for (int i=0; i<N_RATES; i++) {</pre>
        falsePositiveRate[i] = falsePositiveCounter[i]/(tot-rate_count[i]);
// fpr = fp / (tot - tp)
        print("Rating "+(i+1)+"\tfp: "+falsePositiveCounter[i]+"\tfpr:
"+String.format("%.4f", falsePositiveRate[i]));
    }
}
```

```
private static boolean calibrateParams(Configuration conf) throws IOException,
InterruptedException, ClassNotFoundException {
    Job job = Job.getInstance(conf, "calibrate");
    job.setJarByClass(Driver.class);
    job.setMapperClass(CalibrationMapper.class);
    job.setReducerClass(CalibrationReducer.class);
    // mapper's output key and output value
    job.setMapOutputKeyClass(IntWritable.class);
    job.setMapOutputValueClass(IntWritable.class);
    // reducer's output key and output value
    job.setOutputKeyClass(IntWritable.class);
    job.setOutputValueClass(IntWritable.class);
    job.setNumReduceTasks(N_REDUCERS);
    job.getConfiguration().setDouble("p", P);
    return configJob(job, OUTPUT_CALIBRATE);
}
private static boolean createBloomFilters(Configuration conf) throws IOException,
InterruptedException, ClassNotFoundException {
    Job job = Job.getInstance(conf, "create");
    job.setJarByClass(Driver.class);
    job.setMapperClass(CreationMapper.class);
    job.setReducerClass(CreationReducer.class);
    // mapper's output key and output value
    job.setMapOutputKeyClass(IntWritable.class);
    job.setMapOutputValueClass(IntArrayWritable.class);
    // reducer's output key and output value
    job.setOutputKeyClass(IntWritable.class);
    job.setOutputValueClass(BloomFilter.class);
    return configJob(job, OUTPUT_CREATE);
}
private static boolean computeFP(Configuration conf) throws IOException,
InterruptedException, ClassNotFoundException {
    Job job = Job.getInstance(conf, "fp");
    job.setJarByClass(Driver.class);
    job.setMapperClass(ValidationMapper.class);
    job.setReducerClass(ValidationReducer.class);
```

```
// mapper's output key and output value
        job.setMapOutputKeyClass(IntWritable.class);
        job.setMapOutputValueClass(IntWritable.class);
        // reducer's output key and output value
        job.setOutputKeyClass(IntWritable.class);
        job.setOutputValueClass(IntWritable.class);
        return configJob(job, OUTPUT_FP);
   }
   private static boolean configJob(Job job, String outputPath) throws IOException,
   InterruptedException, ClassNotFoundException {
        NLineInputFormat.addInputPath(job, new Path(INPUT));
        job.getConfiguration().setInt("mapreduce.input.lineinputformat.linespermap",
   N_LINES);
        job.setInputFormatClass(NLineInputFormat.class);
        job.setOutputFormatClass(SequenceFileOutputFormat.class);
        FileOutputFormat.setOutputPath(job, new Path(OUTPUT_FOLDER + outputPath));
        return job.waitForCompletion(true);
   }
}
```

Listing 1: Driver

7.1.1 Parameter Calibration

```
String record = value.toString();
   if (record == null || record.startsWith("tconst"))
       return;
   String[] tokens = record.split("\t");
   int rate = Math.round(Float.parseFloat(tokens[1])); // <title, rating,</pre>
numVotes>
   counter[rate - 1]++;
}
@Override
protected void cleanup(Context context) throws IOException, InterruptedException {
   for (int i = 0; i < n_rates; i++) {</pre>
       outputKey.set(i + 1);
       outputVal.set(counter[i]);
       }
}
```

Listing 2: CalibrationMapper

```
public class CalibrationReducer extends Reducer<IntWritable, IntWritable,
   IntWritable, IntWritable> {
   private static double p;
   private static IntWritable outputValue = new IntWritable();
   @Override
   protected void setup(Context context) {
        p = context.getConfiguration().getDouble("p", 0.01);
   @Override
   public void reduce(IntWritable key, Iterable<IntWritable> values, Context
   context) throws IOException, InterruptedException {
                       // sum of all counters relative to the key
        int n = 0;
        while(values.iterator().hasNext())
           n += values.iterator().next().get();
        outputValue= new IntWritable(n);
        context.write(key, outputValue);  // n for every bloom filter
   }
```

Listing 3: CalibrationReducer

7.1.2 Bloom Filter Creation

```
public class CreationMapper extends Mapper<Object, Text, IntWritable,</pre>
   IntArrayWritable> {
                                            // k value
   private static int k;
   private static IntWritable[] indices; // bit positions to set
   private static final IntWritable outputKey = new IntWritable();
   private static final IntArrayWritable outputValue = new IntArrayWritable();
   @Override
   protected void setup(Context context) {
        k = Integer.parseInt(context.getConfiguration().get("filter_k"));
        indices = new IntWritable[k];
   }
   @Override
   public void map(Object key, Text value, Context context) throws IOException,
   InterruptedException {
        if(value.toString().startsWith("tconst"))
                                                       // skip the header
            return;
        String[] tokens = value.toString().split("\t"); // <title, rating, numVotes>
        int roundedRating = (int) Math.round(Double.parseDouble(tokens[1]));
        int m = Integer.parseInt(context.getConfiguration().get("filter_" +
   roundedRating + "_m"));
        for(int i = 0; i < k; i++)</pre>
            indices[i] = new
   IntWritable(Math.abs(MurmurHash.getInstance(MURMUR_HASH).hash(tokens[0].getBytes(),
   i) % m));
        outputKey.set(roundedRating);
        outputValue.set(indices);
        context.write(outputKey, outputValue);
   }
```

Listing 4: CreationMapper

```
public class CreationReducer extends Reducer<IntWritable, IntArrayWritable,
    IntWritable, BloomFilter> {
    private static MultipleOutputs mos;
    private static int k;

    @Override
    protected void setup(Context context) {
        mos = new MultipleOutputs(context);
    }
}
```

```
k = Integer.parseInt(context.getConfiguration().get("filter_k"));
   }
   @Override
   public void reduce(IntWritable key, Iterable<IntArrayWritable> values, Context
   context) throws IOException, InterruptedException {
        int m = Integer.parseInt(context.getConfiguration().get("filter_" + key +
   "_m"));
        BitSet bitset = new BitSet(m);
        for(IntArrayWritable arr: values) {
            for (Writable writable : arr.get()) {
                IntWritable intWritable = (IntWritable)writable;
                bitset.set(intWritable.get());
            }
        BloomFilter bloomfilter = new BloomFilter(k, m, bitset);
        mos.write(key, bloomfilter, "rate"+key);
   @Override
   protected void cleanup(Context context) throws IOException, InterruptedException {
        mos.close();
   }
}
```

Listing 5: CreationReducer

7.1.3 Parameter Validation

```
public class ValidationMapper extends Mapper<Object, Text, IntWritable, IntWritable> {
    private static int n_rates;
    private static final IntWritable outputKey = new IntWritable();
    private static final IntWritable outputValue = new IntWritable();

    private static int[] fp_counters;
    private final ArrayList<BloomFilter> bloomFilters = new ArrayList<>();

    @Override
    protected void setup(Context context) throws IOException {
        n_rates = context.getConfiguration().getInt("n_rates", 0);
        if(n_rates == 0)
            System.exit(-1);

        fp_counters = new int[n_rates];

        for(int i=0; i<n_rates; i++)
            bloomFilters.add(new BloomFilter());</pre>
```

```
// read bloom filters from creation stage and reconstruct them
   FileSystem fs = FileSystem.get(context.getConfiguration());
   FileStatus[] status = fs.listStatus(new
Path(context.getConfiguration().get("outStage2")));
   for(FileStatus filestatus : status) {
       String f = String.valueOf(filestatus.getPath());
       if(f.contains("_SUCCESS") || f.contains("part"))
           continue;
       IntWritable key;
       BloomFilter bf;
       try (SequenceFile.Reader reader = new
SequenceFile.Reader(context.getConfiguration(), SequenceFile.Reader.file(new
Path(f)))) {
           key = new IntWritable();
           bf = new BloomFilter();
           reader.next(key, bf);
       bloomFilters.set(key.get()-1, bf);
   }
}
@Override
public void map(Object key, Text value, Context context) {
   String record = value.toString();
   String[] tokens = record.split("\t");
                                                // token : <title, rating,</pre>
numVotes>
   int roundedRating = (int) Math.round(Double.parseDouble(tokens[1]))-1;
   for(int i = 0; i < n_rates; i++) {</pre>
       if (roundedRating == i)
                                   // skip the true positive
           continue;
       positives
          fp_counters[i]++;
   }
}
@Override
protected void cleanup(Context context) throws IOException, InterruptedException {
   for(int i = 0; i < n_rates; i++) {</pre>
       outputKey.set(i+1);
       outputValue.set(fp_counters[i]);
       context.write(outputKey, outputValue);
   }
```

}

Listing 6: ValidationMapper

```
public class ValidationReducer extends Reducer < IntWritable, IntWritable, IntWritable,
   IntWritable> {
   private static final IntWritable outputKey = new IntWritable();
   private static final IntWritable outputValue = new IntWritable();
   // rating and mappers count in input
   @Override
   public void reduce(IntWritable key, Iterable<IntWritable> mapper_counts, Context
   context) throws IOException, InterruptedException {
                               // sum of all the false positives relative to the key
        int counter = 0;
        for (IntWritable value : mapper_counts)
            counter += value.get();
        outputKey.set(key.get());
        outputValue.set(counter);
        context.write(outputKey, outputValue); // write rating and number of fp
   }
```

Listing 7: ValidationReducer

8 Spark Code

```
# Accumulator array of False Positives counts, each position in the accumulator
    corresponds to the false positive
# count of each bloom filter
class FalsePositiveAccumulatorParam(AccumulatorParam):
    def zero(self, value):
        return [0] * len(value)
    def addInPlace(self, acc, fp):
        for i in range(len(acc)):
             acc[i] += fp[i]
        return acc
# Function that computes m (the dimension of each bloom filter)
def compute_m(count, fpr):
    return math.ceil(-((count * math.log(fpr)) / math.pow(math.log(2), 2))), count
# Function that computes k (the number of hashes to compute for each title)
def compute_k(fpr):
    return int(-math.log(fpr) / math.log(2))
# Function that creates the bloom filters. It takes as input the list of titles for
    each vote and populate a
# local bloom filter of that vote
def create_bf(row): -> crea il bit array
    global broadcast_m, broadcast_k
    key = row[0] 4 Voto
    titles = row[1] & lista titoli
    bf = bitarray(broadcast_m.value[key - 1])
    bf.setall(0)
    for title in titles: & per agni lista di titoli (per agni usto)
        for i in range(broadcast_k.value):
            \begin{array}{ll} \text{hash}\_i = \text{abs}(\text{mmh3.hash}(\text{title, i})) \text{ % broadcast\_m.value[key - 1]} \end{array} \\ \begin{array}{ll} \text{colcola } \kappa \text{ hash } \geq \\ \text{setta bitset} \end{array}
    return key, bf
# Function that populates the accumulator of false positives. It takes as input a row
    of the RDD, computes the k
# hashes for each film and check the all bloom filters different from its own,
    finding false positives and
# increasing the respective position in the accumulator
def add_fp(row):
global fps_acc, broadcast_bfs 4 prende l'accumulatore e il bot
```

```
key = row[0]
    title = row[1]
    counter = [0 for _ in range(10)]
    for i in range(10): 4 Per ogni yoto
       if i == key - 1: Ur Se la Chiave e' la Stessa, voi avonti
       for j in range (broadcast_k.value): * altriments se le k hash sono true increments fp
            continue
            hash_j = mmh3.hash(title, j) % broadcast_m.value[i]
            if broadcast_bfs.value[i][hash_j]:
                pos_count += 1
        if pos_count == broadcast_k.value:
            counter[i] = 1
    fps_acc += counter
if __name__ == "__main__":
    # Checks if the number of inputs in right
    if len(sys.argv) != 3:
        print("Input list: <script.py> <dataset> <fpr>")
   # Save the dataset path and the False Positive Rate
   path = sys.argv[1]
   fpr = float(sys.argv[2])
   # Set the working environment to the virtual one installed on the VMs
   os.environ['PYSPARK_PYTHON'] = './pyspark_venv/bin/python'
    # Set in the configuration the master as yarn cluster and the name of the
   application
    conf = (SparkConf()
            .setMaster("yarn")
            .setAppName("BFSpark"))
   # Initialize a new Spark Context to use for the execution of the script
    sc = SparkContext(conf=conf)
    spark = SparkSession(sc)
    # Set the log level to 'WARN' in order to have a cleaner output
    spark.sparkContext.setLogLevel('WARN')
    # STAGE 1
    # loading the csv removing numVotes
   print("\n\nStarting STAGE 1...")
    # Start the timer for stage 1
    start1 = time.time()
    # Load the csv removing numVotes
```

```
carico csv togliendo
rdd = spark.read.csv(path, sep='\t',
                                                                          num voti
header=True).drop('numVotes').select("tconst", "averageRating").rdd
# Map the dataset as < vote, title > and save cache it
new_dataset = rdd.map(lambda x: (int(round(float(x[1]))), x[0])).cache()

& scambia chiawe e valore it was coche
                                                             nuova chiale, e poi metto in cache
print("Counting the films per vote...")
# Counting the number of movies per vote
vote_count = new_dataset.map(lambda x: (x[0], 1)).reduceByKey(lambda x, y: x +
                                            (voto,2) & ordina per chiave e somma
y).sortByKey()
print("Computing M values...")
# Computing the M and N values for each vote \sim calcola m.n
mn = vote_count.map(lambda x: (x[0], compute_m(x[1],
                       importanoperationi una dopo l'altra (altrimenti rad)
counts per vote ")
fpr))).sortByKey().values().collect()
print("Computing movie counts per vote...")
# Zip the M and N in two different arrays
m_values, tot_values = map(list, zip(*mn))
print("Broadcasting variables...")
# Compute k
k = compute_k(fpr)
# Broadcasts the array of M values, N values and K to all workers
broadcast_m = sc.broadcast(m_values)
print("M: " + str(m_values))
broadcast_k = sc.broadcast(k)
print("K: " + str(k))
broadcast_tot = sc.broadcast(tot_values)
print("N: " + str(tot_values))
# End the timer for stage 1 and print the execution time
elapsed_time_stage1 = time.time() - start1
print(elapsed_time_stage1, "seconds elapsed for completing STAGE 1\n")
# STAGE 2
print("Starting STAGE 2...")
# Start the timer for stage 2
start2 = time.time()
print("Grouping titles...")
# Groups titles in lists by their key
                                          lista di titoli roggi upati
per chiave (rating)
title_lists = new_dataset.groupByKey() &-
print("Creating bloom filters...")
                                                                         or bit a bit train bfs
# Compute the hashes for the titles of each list and populate local bloom
filters, the aggregate them
bloom_filters = title_lists.map(create_bf).reduceByKey(lambda x, y: x |
y).sortByKey().values().collect()
```

```
# Print the length of each bloom filter just populated
j = 0
for i in bloom_filters:
    print("[" + str(j + 1) + "]: " + str(len(i)))
    j = j + 1
print("Broadcasting bloom filters...")
# Instantiate globally the bloom filters
broadcast_bfs = sc.broadcast(bloom_filters)
# End the timer for stage 2 and print the execution time
elapsed_time_stage2 = time.time() - start2
print(elapsed_time_stage2, "seconds elapsed for completing STAGE 2\n")
# STAGE 3
print("Starting STAGE 3...")
# Start the timer for stage 3
start3 = time.time()
print("Checking False Positive Rates...")
# Initialise a global accumulator for the false positives count
fps_acc = sc.accumulator([0] * 10, FalsePositiveAccumulatorParam())
# Iterate the dataset and recompute the hashes of each title to check if it's a
false positive in other bloom
# filters
new_dataset.foreach(add_fp)
# Compute the total sum of films
tot = sum(broadcast_tot.value)
# Print the 10 False Positive Rates
for i in range(10):
    print("[" + str(i + 1) + "]: " + str(fps_acc.value[i] / (tot -
broadcast_tot.value[i])))
# Remove the global variables
broadcast_m.destroy()
broadcast_k.destroy()
broadcast_tot.destroy()
broadcast_bfs.destroy()
# End the timer for stage 3 and print the execution time
elapsed_time_stage3 = time.time() - start3
print(elapsed_time_stage3, "seconds elapsed for completing STAGE 3\n\n")
```