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Intro. to Data Structures & Algorithms Project 1: Sudoku

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Due Date: Monday 27 September 2021, 08:00

1 Description

A Sudoku is a number-placement puzzle. An $n \times n$ grid has n rows, n columns and n blocks (which is made of a $k \times k$ grid of cells, where $n = k^2$). Some cells will have numbers in them already, and the goal of the puzzle is to place a number from $\{1, \ldots, n\}$ into each cell, such that each row, column and block contains every number once and only once. A valid Sudoku puzzle should have one unique solution.

For example, in Figure 1, there are 9 rows and columns, as well as 9.3×3 blocks. There are some cells with numbers in them already. The goal is to fill each empty cell with a number between 1 and 9 (inclusive). We can place the number 4 into the cell in the fourth row and first column (marked with a dot). This is a valid move because the relevant row and column do not currently contain a 4. The 3×3 block needs a 4, but there are already 4s in the fifth and sixth rows. Similarly, it cannot be placed to the right of the 7 as there is already a 4 in that column.

								8
1	8				2	3		
	6			5	7			1
•	7		9	6				
	9		7		4		1	
				8	1		4	
6			2	4			8	
		4	5				9	3
5								

Figure 1: 9 × 9 Sudoku - https://en.wikipedia.org/wiki/Sudoku

There are several logical techniques you can use to narrow down potential values for a cell and to solve a given Sudoku. However, in this project, you are going to implement a technique called a Depth First Search (DFS). A DFS is a backtracking algorithm where we make a decision and stick with it until we either solve the problem or discover that it was an incorrect choice. We then backtrack, or undo, that decision, make a different one, and then try again. We discussed this approach in Chapter 5 of the notes.

The Sudoku that you will be dealing with will either have a unique solution or no solution at all.

2 Input / Output

Input

Your program must read a Sudoku from stdin (using cin). You will read n integers each separated by spaces. It will contain values in $\{0, 1, \ldots, n\}$. If a cell contains a 0 then treat that cell as blank. Your program should be able to handle Sudokus of various sizes:

- $9 \times 9 \{0, 1, \dots, 9\},$
- $16 \times 16 \{0, 1, \dots, 9, A, \dots, F\}$, and
- $25 \times 25 \{0, 1, \dots, 9, A, \dots, P\}$.

The input will always be valid and you do not need to handle special cases with strange whitespace etc. Note that in competitive programming competitions and when programming generally, you should *always* check that the input is both valid and formatted correctly.

Output

Your program should output the solved Sudoku with all the values separated by spaces or if there is no solution you should output the text No Solution.

Sample IO

In	put	[E	asy	/]:		Input [Medium]:										Input [Hard]:										Input [Easy]:									
0	4	0	0	0	0	1	7	9	0	9	0	3	8	4	0	0	0	7	9	0	0	0	0	0	0	3	0	0	0	0	0	0	0	0	7
0	0	2	0	0	8	0	5	4	0	0	2	0	7	0	0	0	0	0	0	0	0	0	0	0	6	0	7	2	0	3	0	9	0	0	1
0	0	6	0	0	5	0	0	8	0	0	0	0	0	0	0	7	1	8	0	1	0	0	4	0	0	2	0	0	8	7	0	5	0	6	0
0	8	0	0	7	0	9	1	0	5	0	0	0	0	3	2	4	0	0	0	5	0	0	0	0	0	0	5	0	2	8	9	0	0	0	0
0	5	0	0	9	0	0	3	0	0	3	0	0	0	0	0	0	0	3	0	0	1	0	0	0	0	0	0	4	0	5	0	1	0	9	0
0	1	9	0	6	0	0	4	0	0	0	1	0	0	5	0	9	0	0	4	0	0	0	6	2	0	9	0	0	0	0	6	3	7	0	5
3	0	0	4	0	0	7	0	0	0	0	0	8	0	0	0	0	0	2	0	0	0	3	0	0	0	6	0	3	0	9	0	6	1	7	0
5	7	0	1	0	0	2	0	0	7	0	6	5	2	0	0	0	0	0	3	0	6	0	5	4	2	1	2	0	0	1	0	7	0	5	3
9	2	8	0	0	0	0	6	0	0	0	0	0	0	6	4	0	0	0	0	0	0	0	0	0	0	0	9	0	0	0	0	0	0	0	0
					Output:											Output:									Output:										
O	utp	ut:							O	utp	ut:							Oı	utp	ut:							O	utp	ut:						
O 8	utp 4	ut: 5	6	3	2	1	7	9	O ₁	utp 9	ut: 7	3	8	4	5	6	2	O1	utp 9	ut: 2	5	6	8	1	4	3		_	ut:	Lut	cio	on			
	_		6	3	2	1	7 5	9	O1 1 8	_	ut: 7 2	3	8	4	5 9	6	2 4		_		5 2	6	8	1	4	3 7		_		Lut	cio	on			
	4	5		3 1 4	2 8 5	1 6 3	7 5 2		1	9	7	_	8 7 5	4 1 2	_	-		7	9	2	_	6 1 7		_	_	-		_		Lut	cio	on			
	4	5		3 1 4 7	-	1 6 3 9	_	4	1	9	7 2	6	7	1	9	-		7 4	9	2	2	6 1 7 9	9	8	6	7		_		Lut	cio	on			
8 7 1	4 3 9	5 2 6	9	3 1 4 7 9	5	3	_	4 8	1 8 4	9 5 6	7 2 3	6	7	1	9	3	4 1	7 4 8	9 5 6	2 3 1	2	1 7	9	8	6	7 2		_		Lut	ci(on			
8 7 1 6	4 3 9 8	5 2 6	9 7 5	1 4 7	5	3	2	4 8 2	1 8 4 5	9 5 6 8	7 2 3 9	6 9 7	7 5 1	1 2 3	9 8 2	3	4 1 6	7 4 8 6	9 5 6	2 3 1 5	2	1 7 9	9 4 3	8 9 7	6 5 1	7 2 4		_		Lut	cio	on			
8 7 1 6 4	4 3 9 8 5	5 2 6 3 7	9 7 5 2	1 4 7 9	5 4 1	3 9 8	2 1 3	4 8 2	1 8 4 5 6	9 5 6 8	7 2 3 9	6 9 7 2	7 5 1 9	1 2 3 8	9 8 2 7	3 7 4 1	4 1 6 5	7 4 8 6 3	9 5 6 2 7	2 3 1 5 9	2	1 7 9 4	9 4 3 2	8 9 7 6	6 5 1 8	7 2 4 5		_		Lut	cio	on			
8 7 1 6 4 2	4 3 9 8 5	5 2 6 3 7	9 7 5 2 8	1 4 7 9 6	5 4 1 3	3 9 8	2 1 3 4	4 8 2 6 7	1 8 4 5 6 2	9 5 6 8 3 7	7 2 3 9 4 1	6 9 7 2 4	7 5 1 9 6	1 2 3 8	9 8 2 7 3	3 7 4 1 9	1 6 5 8	7 4 8 6 3 1	9 5 6 2 7 4	2 3 1 5 9	2 3 8 1 7	1 7 9 4 5	9 4 3 2	8 9 7 6 2	6 5 1 8	7 2 4 5 9		_		Lut	cio	on			

3 Algorithm

You should implement a Depth First Search using either recursion (i.e. the call stack) or iteratively (i.e. using std::stack. In the iterative approach, consider using stack<pair<int,int>> which stores the row and column of the most recent cell to have been given a value. High-level pseudocode is given in Algorithm 1.

Algorithm 1 Iterative Depth First Search for Sudoku

```
1: function SOLVE(grid[N][N])
2:
        Initialise a stack
3:
        while the puzzle is not complete do
           if the puzzle is in an invalid state then
 4:
 5:
               The row/col for the most recent move if always at the top of the stack.
               while the most recent move involved a entering an N do
 6:
                   Pop from the stack and set the value at that position to be blank
 7:
               end while
 8:
               if the stack is empty then
9:
10:
                   return no solution
               else
11:
                   Increment the value stored at the most recent position
12:
               end if
13:
           else
14:
               Find an empty cell and insert the first value for that cell
15:
               Push this location onto the stack
16:
           end if
17:
18:
       end while
        return the resulting values
19:
20: end function
```

You should consider how to represent the various structures in memory efficiently. You may use any built-in structures in the C++11 STL.

4 Submission and Grading

There are 4 submissions on Moodle, you should submit the same Moodle file to all of them. The first submission is about correctness, while the remaining ones are competitive. Think of them as various leagues.

- 1. The first submission runs standard Input/Output test cases to ensure that you can solve the Sudoku of various sizes and difficulties correctly. The test cases here will be worth 75% of your grade.
- 2. The remaining 25% of your grade will be competitive. There will be separate submissions for competitions at 9×9 , 16×16 and 25×25 , your ranking in these competitions will earn you the remaining grades. Watch how different algorithms or aspects of your algorithm perform at different sizes. In the competitions, your program will be run on many different sudoku and Moodle will report the average time per sudoku. There will be a broad mix in terms of sudoku difficulty. You may implement any algorithmic optimisations that you like to improve the efficiency of your algorithm and outsmart your friends!

Your ranking in the competition will change as others submit or resubmit their programs. You may make as many submissions as you require. Note that the test cases on Moodle are valid but unseen input. Late submissions on the non-competitive part will be accepted for an additional 24h, but your grade will be capped at 50%. No late submissions will be accepted in the competitive submissions.