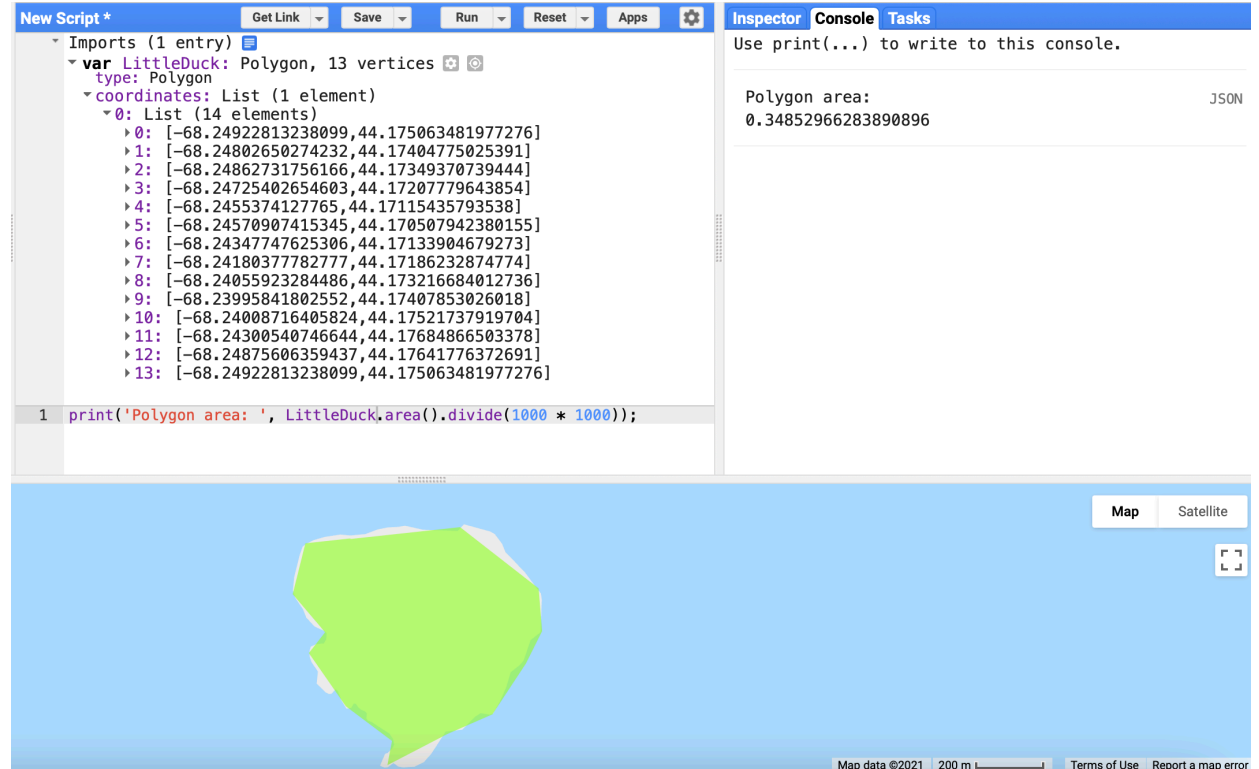


THE DEMOCRATIC REPUBLIC OF LITTLE DUCK ISLAND

```
In [8]: import math
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

Area of Duck Island



~ 349,000 m²

```
In [9]: Avg_elec_load = 1 # W/ft**2
Heat_load = 6 # W/ft**2
Air_condition_load = 0
```

```
In [10]: class Info():
    def Trees():
        rho = 1/50 # tree/m^2
        regen_coEfficient = 0
        Tree_BioMass = 1000 # kg
        E_perTree = 20 # kJ/g
        return rho, regen_coEfficient, Tree_BioMass, E_perTree

    def Solar():
        Irradiance = 4 # kWh/day/m**2
        return Irradiance

    def Crib():
        Area = 2000 # ft**2
        HeatPump_COP = 3.0
        Fireplace_Efficiency = 0.7 # kJ/wood
        return Area, HeatPump_COP, Fireplace_Efficiency
```

Scenario 1:

1) In scenario 1, what is your yearly electricity and total energy requirement in kWh, and your yearly CO₂ production related to tree burning in kg , if you use only the fireplace during the heating season to heat the house.(30 pts)

2) In scenario 1, what is your yearly electricity and total energy requirement in kWh, and your yearly CO₂ production related to tree burning in kg , if you only run the heat pump during the heating season remarkably. (30 pts)

3) For both of the above cases in scenario 1, how many years can you run this operation before you run out of trees? (20 pts)

In [11]:

```
### 1 ###
```

Energy/Electricity Output Requirements

*heating.kwh(area, 0 < days < 121) : 6 * area*

*heating.kwh(area, 122 < days < 365) : 0 * area*

heating.kwh(2000, onDays) : 34848kWh

heating.w(2000, onDays) : 12000W

heating.kwh(2000, offDays) : 0kWh

heating.w(2000, offDays) : 0W

*electricity.kwh(area) : 1 * area*

electricity.kwh(2000) : 17520kWh

electricity.w(2000) : 2000W

```
In [12]: # Considering Generator with 0.5 efficiency of Carnot Efficiency that
ReqElec_Output = 17520 # kWh

# heat-to-electric generator
Th = 1000 # K
Tc = 293 # K
# convert heat to work at 1000K
CarnotE = (Th - Tc) / Th
GenEfficiency = 0.5 * CarnotE

#Heat requirement to produce required electricity given by:
ReqElec_Input = ReqElec_Output/GenEfficiency
print("The required annual energy input for matching electricity requi
```

The required annual energy input for matching electricity required is 49561.53 kWh.

```
In [13]: # Considering fireplace with 0.7 efficiency converting wood source to
ReqHeat_Output = 34848

Fireplace_efficiency = 0.7
ReqHeat_Input = ReqHeat_Output / Fireplace_efficiency
print("The required annual energy input for matching heating required
```

The required annual energy input for matching heating required during dec-apr is 49782.86 kwh.

Now for CO₂ !

TREE ANALYSIS

Assuming the total available biomass of trees on my island is convertible to energy:

Model energy by :

$$E_{perTree} = Mass_{Tree} * EnergyDensity$$

$$E_{perTree} = 20,000,000kJ$$

```
In [14]: # Calculating Energy available per tree
E_perTree = 20000000

P_watts_tree = E_perTree / 3600 # convert to kWh

print("Energy available on a per tree basis:\n -> {} kWh".format(round
```

Energy available on a per tree basis:
-> 5555.56 kWh

```
In [15]: # CALCULATING CO2 USING EFFICIENCY RATIO ON FUEL SOUCE INSTEAD OF MATC
```

```
In [16]: # for fireplace
TreeE_AvailableFireplace = P_watts_tree * Fireplace_efficiency
print("Heat energy produced by fireplace per tree:\n -> {} kWh".format

# given required heat output as ReqHeat_Output (34,848)...
No_Trees = ReqHeat_Output / TreeE_AvailableFireplace
print("\n \nI must chop {} trees down in order to meet my heating dema

Heat energy produced by fireplace per tree:
-> 3888.89 kWh
```

I must chop 9 trees down in order to meet my heating demand.

```
In [17]: # for generator
TreeE_GeneratorConversion = P_watts_tree * GenEfficiency
print("Electric energy produced by generator per tree:\n -> {} kWh".fo

# given required electric output as ReqElec_Output (17520)...
No_Trees = ReqElec_Output / TreeE_GeneratorConversion
print("\n \nI must chop {} trees down in order to meet my electricity

Electric energy produced by generator per tree:
-> 1963.89 kWh
```

I must chop 9 trees down in order to meet my electricity demand.

*So in order to satisfy my minimum heating/electricity requirements I must chop down **18 trees per year.***

```
In [18]: # CO2 from Trees
Total_mass = 18 * Info.Trees()[2] * 1000
C_mm = 12.011
C_moles = Total_mass / C_mm

CO2_moles = C_moles
CO2_mm = 44.009
CO2_mass = (CO2_moles * CO2_mm) / 1000

print("{} kg of CO2 produced during a one year cyle.".format(round(CO2

65953.04 kg of CO2 produced during a one year cyle.
```

1| Solution

Yearly Input Electricity Requirement: : 49561.53 KWH

~~Yearly Convertible Heating Requirement : 49782.86 KWH~~

TOTAL INPUT ENERGY REQUIREMENT : 99,344.39 KWH

Total CO2 Produced : 65,953.04 kg

In [19]:

```
### 2 ###
```

In [20]:

```
# NOW INSTEAD OF FIREPLACE HEATING, I ADOPT HEAT PUMP HEATING
# heat pump takes *Electricity* and produces *Heat*
```

```
COP = 3.0
```

```
PumpElec_Input = ReqHeat_Output / COP
```

```
print("The pump requires {} kWh of electricity to produce {} kWh of He
```

The pump requires 11616 kWh of electricity to produce 34848 kWh of Heat.

In [21]:

```
# Above covers heating requirements but not electric requirements, so
# requirements for total electricity:
```

```
TotalElec_InputReq = PumpElec_Input + ReqElec_Output
```

```
GenHeat_Input = TotalElec_InputReq / GenEfficiency
```

```
print("The generator requires {} kWh of heat to produce {} kWh of elec
```

The generator requires 82421.5 kWh of heat to produce 29136.0 kWh of electricity.

Just a bit of overview:

Yearly Elec. Consumption = 11616 + 17520

Yearly Energy. Consumption = 82421.5

Now for CO2 Analysis based on Energy Consumption

```
In [22]: # Generator supplies total electricity for both heating and consumption
# Input heat is sourced from the burning of trees:

Nos_Trees = GenHeat_Input / P_watts_tree

print("I must chop {} trees down in order to meet my total energy demand")
I must chop 15 trees down in order to meet my total energy demand.
```

```
In [23]: # CO2 from Trees
Total_mass = 15 * Info.Trees()[2] * 1000
C_mm = 12.011
C_moles = Total_mass / C_mm

CO2_moles = C_moles
CO2_mm = 44.009
CO2_mass = (CO2_moles * CO2_mm) / 1000

print("{} kg of CO2 produced during a one year cycle.".format(round(CO2_mass)))
54960.87 kg of CO2 produced during a one year cycle.
```

2| Solution

Yearly Consumable Electricity Requirement : 29,136 KWH

TOTAL ENERGY REQUIREMENT : 82,421.50 KWH

Total CO2 Produced : 54,960.87 kg

```
In [24]: ##### 3 #####
```

```
In [25]: # CASE 1| To calculate longevity of my time on LDI
Trees_req = 18
Area_LDI = 349000 #m**2
TreeDensity = Info.Trees()[0]
House_Size = 185.81 #m**2
ForestedArea = Area_LDI - House_Size

No_ofTreesLDI = ForestedArea * TreeDensity
print("There are {} trees on Little Duck Island (LDI)".format(round(No

# If I need 18 trees x year in Case 1, then ->

Years_RunOutFire = No_ofTreesLDI / 18
print("\nI will run out of trees in {} years using the fireplace and g

There are 6976 trees on Little Duck Island (LDI)

I will run out of trees in 388 years using the fireplace and generato
r.
```

```
In [26]: # CASE 2|
# If I need 15 trees x year to match total generation capabilities req

Years_RunOutPump = No_ofTreesLDI / 15
print("I will run out of trees in {} years using the generator and pump

I will run out of trees in 465 years using the generator and pump.
```

3| Solution

Case 1 Years Before Resource Exhaustion: : 388 years

Case 2 Years Before Resource Exhaustion: : 465 years

```
In [27]: ##### 4 #####
```


Scenario 2

4) how much land do you need for solar PV in m^2 , assuming you do not burn down any trees for heat? (20 pts)

1. 100% energy generation from Solar PV
2. Assume original 2,000 W electricity demand and 12,000 W heating demand.

```
In [28]: # Energy vals that I need to match:
Elec_Reqs = 2000 # W
Heat_Reqs = 12000 # W
Tot_UnconvertedReqs = Elec_Reqs + Heat_Reqs

# Looking at Solar energy conversions now:
Irradiance = Info.Solar() # kWh/day/m^2
PanelEfficiency = 0.18

# Assuming 24 hour solar day
Avg_Insolation = (Irradiance * 1000) / 24 # 24-hour solar day
Collected_PowerDensity = Avg_Insolation * PanelEfficiency
print("The maximum harvestable energy from solar panel is {} W/m^2".format(Collected_PowerDensity))

#LDI - Little Duck Island
LDI_SolarPowerArea = Tot_UnconvertedReqs / Collected_PowerDensity
print("\nNeeded area for matching energy requirements with solar panels is {} m^2".format(LDI_SolarPowerArea))
```

The maximum harvestable energy from solar panel is 30 W/m²

Needed area for matching energy requirements with solar panels is 467 m²

4| Solution

Land Required: : 467 m²

```
In [29]: ##### 5 #####
```

5) Estimate the amount of battery storage you need to install to smooth out the day night cycles year round. (10 pts)

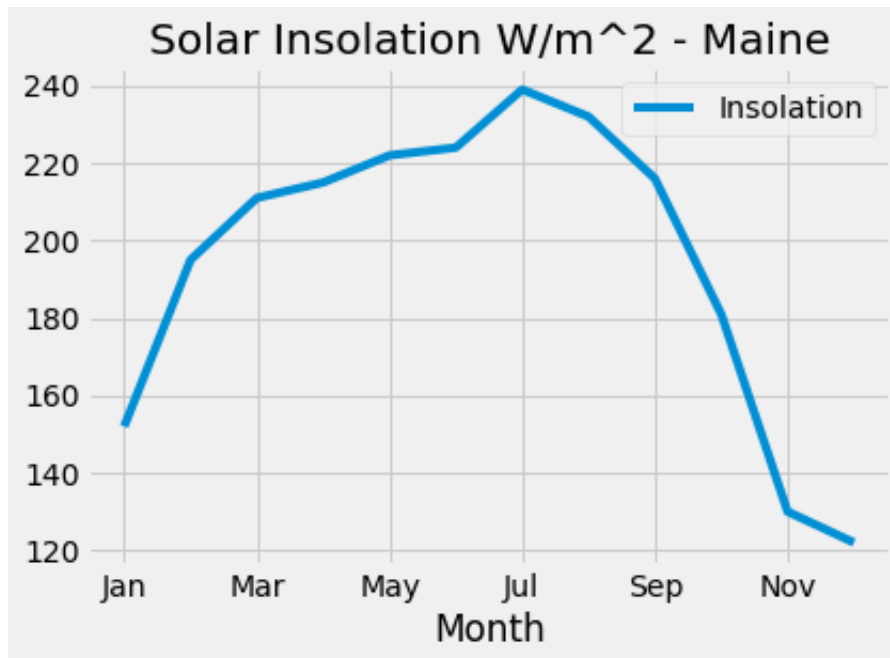
1. Batteries are 100% efficient

```
In [37]: # Maine Monthly Irradiance (12-hour x day cycle)

Mon_SolarRadiation = pd.DataFrame([['Jan', 3.64, ], ['Feb', 4.68], ['M
#Insolation in kWh/day/m2
Insolation_Conversion = Mon_SolarRadiation['Insolation']
Converted_Insolation = [round(x * 1000 / 24) for x in Insolation_Conve
#Now Insolation in W/m2

Mon_SolarRadiation['Insolation'] = Converted_Insolation

Mon_SolarRadiation.plot(x='Month', y='Insolation')
plt.title('Solar Insolation W/m^2 - Maine')
plt.style.use('fivethirtyeight')
plt.show()
```



```
In [38]: # Energy production cycles broken down by month:

# JAN
Jan = Mon_SolarRadiation.iloc[0]

Jan_Pd = Jan['Insolation'] * PanelEfficiency
# FEB
```

```
Feb = Mon_SolarRadiation.iloc[1]

Feb_Pd = Feb['Insolation'] * PanelEfficiency
# MAR
Mar = Mon_SolarRadiation.iloc[2]

Mar_Pd = Mar['Insolation'] * PanelEfficiency
# APR
Apr = Mon_SolarRadiation.iloc[3]

Apr_Pd = Apr['Insolation'] * PanelEfficiency
# MAY
May = Mon_SolarRadiation.iloc[4]

May_Pd = May['Insolation'] * PanelEfficiency
# JUN
Jun = Mon_SolarRadiation.iloc[5]

Jun_Pd = Jun['Insolation'] * PanelEfficiency
# JUL
Jul = Mon_SolarRadiation.iloc[6]

Jul_Pd = Jul['Insolation'] * PanelEfficiency
# AUG
Aug = Mon_SolarRadiation.iloc[7]

Aug_Pd = Aug['Insolation'] * PanelEfficiency
# SEP
Sep = Mon_SolarRadiation.iloc[8]

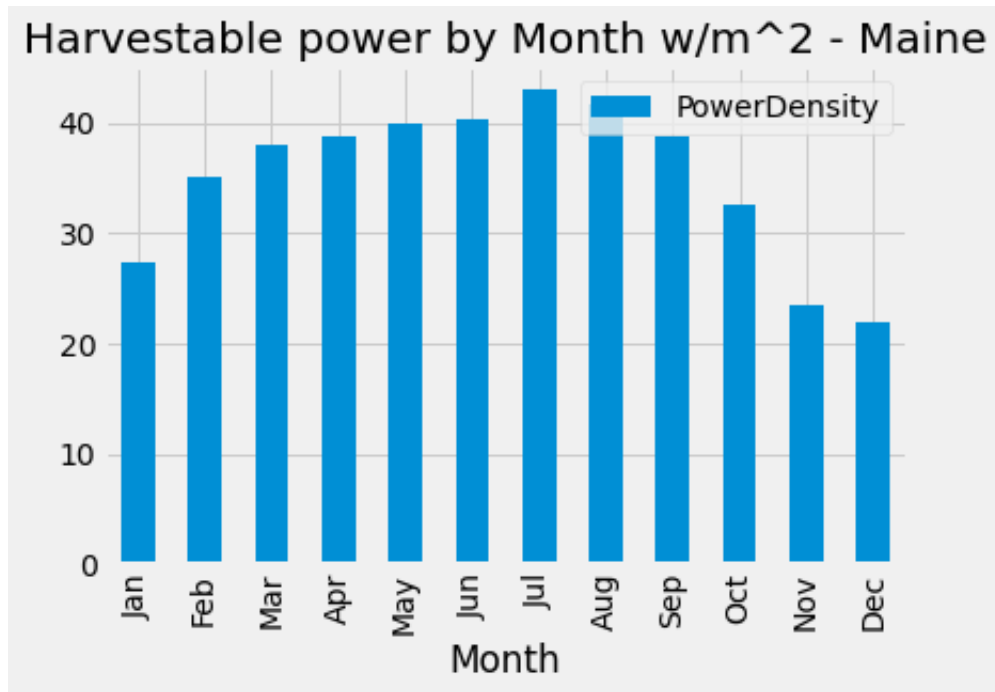
Sep_Pd = Sep['Insolation'] * PanelEfficiency
# OCT
Oct = Mon_SolarRadiation.iloc[9]

Oct_Pd = Oct['Insolation'] * PanelEfficiency
# NOV
Nov = Mon_SolarRadiation.iloc[10]

Nov_Pd = Nov['Insolation'] * PanelEfficiency
# DEC
Dec = Mon_SolarRadiation.iloc[11]

Dec_Pd = Dec['Insolation'] * PanelEfficiency

Pd_df = pd.DataFrame(['Jan', Jan_Pd], ['Feb', Feb_Pd], ['Mar', Mar_Pd],
Pd_df.plot('Month', 'PowerDensity', kind='bar')
plt.title('Harvestable power by Month w/m^2 - Maine')
plt.style.use('fivethirtyeight')
plt.show()
```



SolarIntenseCurve()

requirements:

1. Elec : 1 W/ft² (Jan-Dec)
2. Heating : 6 W/ft² (Dec-Apr)
3. House size: 2000 ft²

ElecDemand: 1 W/ft² * 2000 ft² = 2000 W
 HeatingDemand: 6 W/ft² * 2000 ft² = 12000 W

Heating Energy Demand: 34848000 Wh (heating szn)
 Electricity Energy Demand: 17520000 Wh (year round)

Heating Energy Demand: 288000 Wh (x day during heating szn)
 Electricity Energy Demand: 48000 Wh (x day year round)

USING SOLAR LAND REQUIREMENT FROM Q4) But w/ a 12-hour window

In []:

```
In [33]: # Dec-Apr Calculations w/ Solar
PerDay_Demand = 14000 # watts

# function to break down 12-hour window into realistic intensities
def SolarDays(SolarMONTHpd):
    TwentyFourToOne = SolarMONTHpd * (Percents[0]/100)
    OneToTwoPD = SolarMONTHpd * (Percents[1]/100)
    TwoToThreePD = SolarMONTHpd * (Percents[2]/100)
    ThreeToFourPD = SolarMONTHpd * (Percents[3]/100)
    FourToFivePD = SolarMONTHpd * (Percents[4]/100)
    FiveToSixPD = SolarMONTHpd * (Percents[5]/100)
    SixToSevenPD = SolarMONTHpd * (Percents[6]/100)
    SevenToEightPD = SolarMONTHpd * (Percents[7]/100)
    EightToNinePD = SolarMONTHpd * (Percents[8]/100)
    NineToTennPD = SolarMONTHpd * (Percents[9]/100)
    TenToElevenPD = SolarMONTHpd * (Percents[10]/100)
    ElevenToTwelvePD = SolarMONTHpd * (Percents[11]/100)
    TwelveToThirtPD = SolarMONTHpd * (Percents[12]/100)
    ThirtToFourtPD = SolarMONTHpd * (Percents[13]/100)
    FourtToFiftPD = SolarMONTHpd * (Percents[14]/100)
    FiftToSixtPD = SolarMONTHpd * (Percents[15]/100)
    SixtToSeventPD = SolarMONTHpd * (Percents[16]/100)
    SeventToEighteenPD = SolarMONTHpd * (Percents[17]/100)
    EighteenToNinetPD = SolarMONTHpd * (Percents[18]/100)
    NinetToTwentyPD = SolarMONTHpd * (Percents[19]/100)
    TwentyToOnePD = SolarMONTHpd * (Percents[20]/100)
    TwentyToTwoPD = SolarMONTHpd * (Percents[21]/100)
```

```

TwentyToThreePD = SolarMONTHpd * (Percents[22]/100)
TwentyToFourPD = SolarMONTHpd * (Percents[23]/100)

return list([TwentyFourToOne, OneToTwoPD, TwoToThreePD, TwoToThreePD])

month_insolation = [Jan['Insolation'],Feb['Insolation'],Mar['Insolation']]

def GrouperFunc(varM):
    # Takes Calculated Fractional Insolation based upon time-of-day and month
    NewList = []
    for x in SolarDays(month_insolation[varM]):
        Insol = round(x) # W/m2
        EHarvest = Insol * PanelEfficiency * 467 # W
        NewList.append(EHarvest)
    return NewList

GrouperFunc(0)
# print('Daily Generative Capabilities for January is {} W.'.format(GrouperFunc(0)))
# print('Daily Generative Capabilities for February is {} W.'.format(GrouperFunc(1)))
# print('Daily Generative Capabilities for March is {} W.'.format(GrouperFunc(2)))
# print('Daily Generative Capabilities for April is {} W.'.format(GrouperFunc(3)))
# print('Daily Generative Capabilities for December is {} W.'.format(GrouperFunc(11)))

#Create two plots and distance between them is battery storage requirement

listoNos = []

for x in range(0,25):
    listoNos.append(14000)

listoPos = []

for y in range(0,25):
    listoPos.append(2000)

#-----
JanuaryTest = pd.DataFrame([GrouperFunc(0), listoNos]).T

JanuaryReal = JanuaryTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis=1)

JanuaryReal.plot()
plt.title('Solar Generation vs. Demand | Jan')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()

#-----
FebruaryTest = pd.DataFrame([GrouperFunc(1), listoNos]).T

```

```

FebruaryReal = FebruaryTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis='column')

FebruaryReal.plot()
plt.title('Solar Generation vs. Demand | Feb')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
MarchTest = pd.DataFrame([GrouperFunc(2), listoNos]).T

MarchReal = MarchTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis='column')

MarchReal.plot()
plt.title('Solar Generation vs. Demand | Mar')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
AprilTest = pd.DataFrame([GrouperFunc(3), listoNos]).T

AprilReal = AprilTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis='column')

AprilReal.plot()
plt.title('Solar Generation vs. Demand | Apr')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
MayTest = pd.DataFrame([GrouperFunc(4), listoPos]).T

MayReal = MayTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis='column')

MayReal.plot()
plt.title('Solar Generation vs. Demand | May')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
JuneTest = pd.DataFrame([GrouperFunc(5), listoPos]).T

JuneReal = JuneTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis='column')

JuneReal.plot()
plt.title('Solar Generation vs. Demand | Jun')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
JulyTest = pd.DataFrame([GrouperFunc(6), listoPos]).T

JulyReal = JulyTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis='column')

```



```
JulyReal.plot()
plt.title('Solar Generation vs. Demand | Jul')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
AugustTest = pd.DataFrame([GrouperFunc(7), listoPos]).T

AugustReal = AugustTest.rename({0:'SolarWatts', 1:'WattDemand'}, axis=

AugustReal.plot()
plt.title('Solar Generation vs. Demand | Aug')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
SeptemberTest = pd.DataFrame([GrouperFunc(8), listoPos]).T

SeptemberReal = SeptemberTest.rename({0:'SolarWatts', 1:'WattDemand'},

SeptemberReal.plot()
plt.title('Solar Generation vs. Demand | Sep')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
OctoberTest = pd.DataFrame([GrouperFunc(9), listoPos]).T

OctoberReal = OctoberTest.rename({0:'SolarWatts', 1:'WattDemand'}, axi

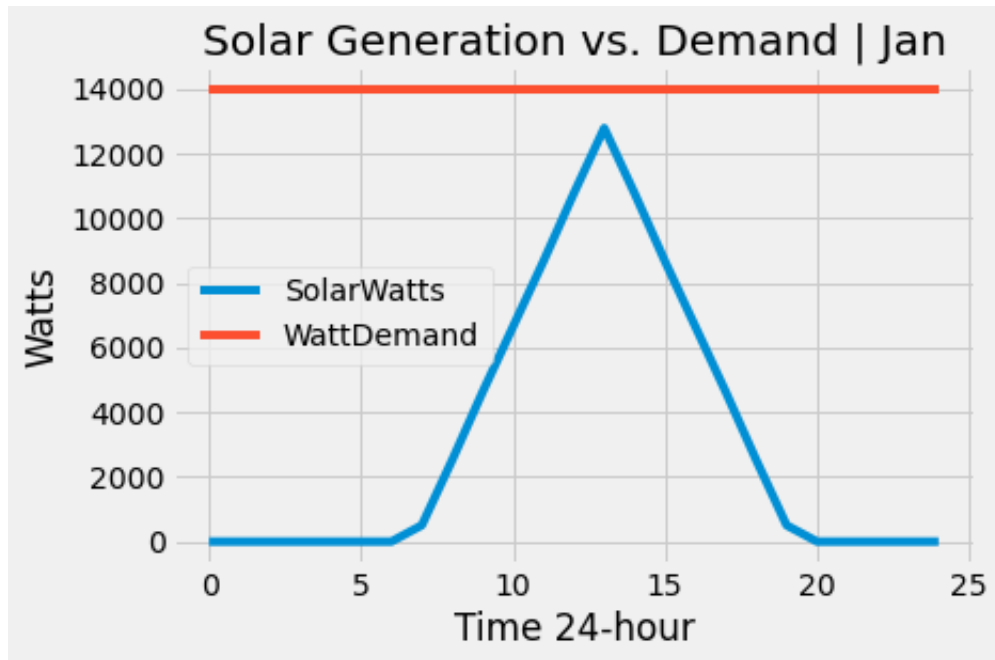
OctoberReal.plot()
plt.title('Solar Generation vs. Demand | Oct')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
NovemberTest = pd.DataFrame([GrouperFunc(10), listoPos]).T

NovemberReal = NovemberTest.rename({0:'SolarWatts', 1:'WattDemand'}, a

NovemberReal.plot()
plt.title('Solar Generation vs. Demand | Nov')
plt.xlabel('Time 24-hour')
plt.ylabel('Watts')
plt.show()
#-----
DecemberTest = pd.DataFrame([GrouperFunc(11), listoNos]).T

DecemberReal = DecemberTest.rename({0:'SolarWatts', 1:'WattDemand'}, a
```

```
DecemberReal.plot()  
plt.title('Solar Generation vs. Demand | Dec')  
plt.xlabel('Time 24-hour')  
plt.ylabel('Watts')  
plt.show()
```



It's clear to see that harvestable watts fluxuates dependant on the month.

```
In [34]: # a, b, c, d = points of intersection between demand and solar watts c
# HEATING SZN

a = [10.06, 14000]
b = [15.94, 14000]
Base = math.dist(a,b)
Height = 25250 - 14000
OverSupplyW = round((Base * Height) / 2)
print('From 10am to 4pm, the solar panels oversupply {} W of electricity')

c = [7, 1008]
d = [7, 14000]
```

```
BaseUnder = math.dist(d,a)
HeightUnder = math.dist(d, c)
UnderSupplyHeat = round((BaseUnder * HeightUnder) / 2)
print('From 6pm < time < 6am, the demand is undersupplied by {} W of electricity')
```

From 10am to 4pm, the solar panels oversupply 33075 W of electricity
 From 6pm < time < 6am, the demand is undersupplied by 19878 W of electricity

```
In [35]: # w, x = points of intersection between demand and solar watts curve u

w = [7.1, 2000]
x = [18.9, 2000]
y = [6,1600]
BaseWX = math.dist(w,x)
HeightWY = 2000-1600
UnderSupplyNoHeat = round((BaseWX * HeightWY) / 2)
print('From 6pm < time < 6am, the demand is undersupplied by {} W of electricity')
```

From 6pm < time < 6am, the demand is undersupplied by 2360 W of electricity

Now, take Li-ion batteries as our super-efficient storage device -->

Power Density of Li-ion batteries (source: cei.washington.edu): 250-270 Wh/kg

```
In [36]: # BATTERIES MUST HARVEST >19878 W OF ENERGY IN ORDER TO BALANCE THE DA  
# Take Lithium Ion Battery with 250 Wh/kg Energy Density
```

```
BatteryPD = 250 * 12 # W/kg - 12hour cycle for batteries
```

```
TotalBatteryStorageReq = round(UnderSupplyHeat / BatteryPD, 2) # cancell
```

```
TotBatStoReq = round(UnderSupplyNoHeat / BatteryPD, 2)
```

```
print("I will need {} kg of Li-ion batteries to account for my day-night i
```

```
print("I will need {} kg of Li-ion batteries to account for my day-night i
```

I will need 6.63 kg of Li-ion batteries to account for my day-night imbalance w/ solar during the heating season.

I will need 0.79 kg of Li-ion batteries to account for my day-night imbalance w/ solar during the non-heating season.

```
In [ ]:
```

```
In [ ]:
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In [ ]:
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In [ ]:
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