# Luca Benatti

☑ lbenatti.math@gmail.com
Sites.google.com/view/luca-benatti
0 0000-0002-4685-7443
☑ Luca Benatti
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Curriculum Vitae et Studiorum

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Feb 2024 - Current **Postdoctoral Researcher**, *University of Pisa*, Pisa (I), Principal Investigator: Prof. Giovanni Alberti.

# Previous positions

Feb 2023 - Jan 2024	Postdoctoral Researcher, University of Pisa, Pisa (I), founded at 50% by Starting
	Grant ERC "Variational approach to the regularity of the free boundaries". Principal
	Investigator: Prof. Bozhidar Velichkov.

Oct 2022 - Nov 2022 Long term visitor of the Thematic Program on Nonsmooth Riemannian and Lorentzian Geometry, Fields Institute, Toronto (CA)

Nov 2018 - Jun 2022 Ph.D. student with research fellowship, University of Trento, Trento (I)

#### Education

Nov 2018 - Jun 2022	Ph.D. in Mathematics, University of Trento, Trento (I), Ottimo cum Laude. Ad-
	visor: Prof. Lorenzo Mazzieri. Title: Monotonicity Formulas in Nonlinear Potential
	Theory and their geometric applications.

Oct 2016 - Sep 2018 Master's degree in Mathematics, University of Trieste, Trieste (I), 110/110 cum Laude. Thesis advisor: Prof. Nicola Gigli. Thesis Title: A review of differential calculus on metric measure spaces via  $L^0$ -normed modules.

Sep 2013 - Jul 2016 **Bachelor's degree in Mathematics**, *University of Modena and Reggio Emilia*, Modena (I), 110/110 cum Laude. Thesis advisor: Prof. Gian Paolo Leonardi. Thesis Title: Corpi galleggianti con equlibrio indifferente e una congettura di Auerbach.

#### Invited talks

- Sep 2024 **The Riemannian Penrose inequality**, Pisa-Freiburg school in Applied Analysis, Pisa (I), Lecture (2h) in Alessandra Pluda's course.
- Feb 2024 Nonlinear potential theory through the looking-glass and the Penrose inequality we found there, Recent Advances in Comparison Geometry, Hangzhou (CN)
- Sep 2022 Isoperimetric concept of mass in manifolds with nonnegative scalar curvature, University of Milano-Bicocca, Milano (I)
- Sep 2022 Bertie Bott's every flavour mass concepts in General Relativity, Another Pisan workshop in Geometric Analysis, Pisa (I)
- Aug 2022 Various concepts of mass in General Relativity, Three days between Analysis and Geometry in Trento, Trento (I)
- Oct 2021 From PDE's to Geometry: a new path towards the Minkowski, MAP Seminar, Pisa (I)
- Jun 2018 Differential calculus on metric measure spaces, University of Modena and Reggio Emilia, Modena (I)

Contributed talks

- Feb 2024 Isoperimetric concept of mass in manifolds with nonnegative scalar curvature, XXXIII Convegno Nazionale di Calcolo delle Variazioni, Riccione (I)
- Jun 2022 Minkowski Inequality in Riemannian manifolds with nonnegative Ricci curvature, Shape optimization, related topics and applications, Roscoff (FR)
- Oct 2021 Minkowski Inequality in Riemannian manifolds with nonnegative Ricci curvature, 9th GAMM-Workshop on Analysis of Partial Differential Equations, Freiburg im Breisgau (DE)
- Sep 2021 Minkowski Inequality in Riemannian manifolds with nonnegative Ricci curvature, Geometric theory of PDE's and sharp functional inequalities, Accademia Nazionale dei Lincei (Zoom Talk)

# Organisation of events

- Sep 2024 The Pisan workshop saga. Ep. V Geometric analysis strikes back., Pisa (I), with M. Fogagnolo e A. Pluda.
- Sep 2023 Guess what? A Pisan workshop in Geometric Analysis, Pisa (I), with M. Fogagnolo e A. Pluda.

# Funded projects

2022 **GNAMPA Project: "Problemi al bordo e applicazioni geometriche"**, Joint project with V. Agostiniani, L. Benatti, S. Borghini, L. Mazzieri, F. Oronzio and A. Pinamonti.

# Teaching experience

- Spring 2023 Ph.D. Course (12 h): "Monotonicity formulas in nonlinear potential theory and their geometric applications", University of Pisa, Pisa (I), Department of Mathematics
- Winter 2021 Grader for Mathematical Analysis II, University of Trento, Trento (I), Department of Civil, Environmental and Mechanical
- Spring 2021 **TA for Geometric Analysis**, *University of Trento*, Trento (I), Department of Mathematics
- Winter 2020 Grader for Mathematical Analysis II, University of Trento, Trento (I), Department of Civil, Environmental and Mechanical
- Spring 2020 **TA for Geometric Analysis**, *University of Trento*, Trento (I), Department of Mathematics
- Autumn 2019 **TA for Mathematical Analysis I**, *University of Trento*, Trento (I), Department of Industrial Engineering
- Summer 2019 Grader for Geometry and Linear Algebra, University of Trento, Trento (I), Department of Industrial Engineering
- Spring 2019 IATEX mini-course, University of Trento, Trento (I), Department of Mathematics

#### Schools

- Sep 2024 Pisa-Freiburg school in Applied Analysis, University of Pisa, Pisa (I)
- Lug 2024 Bridging PDE and Geometric Flows An LMS-HIMR Research School, University of Cardiff, Cardiff (UK)
- Lug 2024 BIGW V Mathematical General Relativity, Birmingham (UK)
- Aug 2023 Three days between Analysis and Geometry in Trento, 2° edition, University of Trento, Trento (I)
- Aug 2022 Three days between Analysis and Geometry in Trento, University of Trento, Trento (I)

- Sep 2021 Convex Geometry, CIME, Cosenza (I)
- Sep 2019 Geometric Measure Theory and Applications, CIME, Cosenza (I)
- Jul 2019 Geometry and Gravity, ICTP, Trieste (I)

## Workshops

- Jun 2024 Regularity Theory for Free Boundary and Geometric Variational Problems IV, Trento (I)
- Jun 2024 CHANGE CHallenges in ANalysis and GEometry, Zürich (CH)
- Apr 2024 Workshop Calculus of Variations and Free Boundary Problems VIII, Pisa (I)
- Feb 2024 Recent Advances in Comparison Geometry, Hangzhou (CN)
- Feb 2024 XXXIII Convegno Nazionale di Calcolo delle Variazioni, Riccione (I)
- Dec 2023 Mathematical Relativity: Past, Present, Future, Wien (AT)
- Dec 2023 Curvature-driven geometric problems, Pisa (I)
- Jun 2023 Regularity Theory for Free Boundary and Geometric Variational Problems III, Trento (I)
- Jun 2023 Calculus of Variations & Geometric Measure Theory, Pisa (I)
- May 2023 Geometric Measure Theory, Bressanone (I)
- Nov 2022 Workshop on Aspects of Ricci Curvature Bounds, Toronto (CA)
- Oct 2022 Workshop on Mathematical Relativity, Scalar Curvature and Synthetic Lorentzian Geometry, Toronto (CA)
- Sep 2022 Another Pisan workshop in Geometric Analysis, Pisa (I)
- Jun 2022 Isoperimetric problems, Pisa (I)
- Jun 2022 Shape optimization, related topics and applications, Roscoff (FR)
- May 2022 XXXI Convegno Nazionale di Calcolo delle Variazioni, Levico (I)
- Oct 2021 A Pisan workshop in Geometric Analysis, Pisa (I)
- Oct 2021 9<sup>th</sup> GAMM-Workshop on Analysis of Partial Differential Equations, Freiburg im Breisgau (DE)
- Sep 2021 Geometric theory of PDE's and sharp functional inequalities, Zoom workshop
- Feb 2020 XXX Convegno Nazionale di Calcolo delle Variazioni, Levico (I)
- Feb 2019 XXIX Convegno Nazionale di Calcolo delle Variazioni, Levico (I)
- Jun 2019 Geometric Analysis and General Relativity. A conference in honour of G. Huisken's 60th, Zürich (CH)
- Jan 2019 Alessio Figalli, Fields Medallist 2018, Pisa (I)
- Feb 2018 XXVIII Convegno Nazionale di Calcolo delle Variazioni, Levico (I)

### Languages

English (competent), Italian (native)

# List of publications

- Fine properties of nonlinear potentials and a unified perspective on monotonicity formulas, joint with A. Pluda and M. Pozzetta, preprint
  DOI: 10.48550/arXiv.2411.06462. arXiv: 2411.06462
- 2024 A Note on Ricci-pinched three-manifolds, joint with C. Mantegazza and F. Oronzio and A. Pluda, preprint

  DOI: 10.48550/arXiv.2409.05078. arXiv: 2409.05078

- 2024 Second-order estimates for the p-Laplacian in RCD spaces, joint with I. Y. Violo, preprint
  - arXiv: 2401.09982 [math]. URL: http://arxiv.org/abs/2401.09982
- 2024 Minkowski inequality on complete Riemannian manifolds with nonnegative Ricci curvature, joint with M. Fogagnolo and L. Mazzieri, Analysis & PDE DOI: 10.2140/apde.2024.17.3039
- 2023 Isoperimetric sets in nonnegative scalar curvature and their role through various concepts of mass, joint with M. Fogagnolo, Accepted: Springer INdAM series
  - DOI: 10.48550/arXiv.2305.03643. arXiv: 2305.03643 [math]
- 2023 Nonlinear isocapacitary concepts of mass in 3-manifolds with nonnegative scalar curvature, joint with M. Fogagnolo and L. Mazzieri, SIGMA. Symmetry, Integrability and Geometry. Methods and Applications

  DOI: 10.3842/SIGMA.2023.091
- 2022 On the Isoperimetric Riemannian Penrose Inequality, joint with M. Fogagnolo and L. Mazzieri, Accepted: *CPAM*DOI: 10.48550/arXiv.2212.10215. arXiv: 2212.10215 [math]
- 2022 The asymptotic behaviour of *p*-capacitary potentials in asymptotically conical manifolds, joint with M. Fogagnolo and L. Mazzieri, *Mathematische Annalen*DOI: 10.1007/s00208-022-02515-4
- 2022 Monotonicity Formulas in Nonlinear Potential Theory and their geometric applications, Ph.D. thesis

  DOI: https://dx.doi.org/10.15168/11572\_346959

# Scholarships, awards and further information

- May 2023 Best Ph.D. Thesis in Mathematics of XXXIV cycle at University of Trento
- Nov 2018 Jan 2022 Ph.D. Scholarship "Departments of Excellence"
- Oct 2016 Sep 2018 SISSA scholarship
- Sep 2013 Jul 2016 INdAM scholarship
  - Since 2023 Reviewing activity for the following journals: Rendiconti Lincei, Mathematische Annalen, Journal of Differential Geometry.

## Professional references

Nicola Gigli, Mathematics Area, SISSA ngigli@sissa.it

Carlo Mantegazza, Dipartimento di Matematica e Applicazioni "Renato Caccioppoli", Università degli studi di Napoli Federico II c.mantegazza@sns.it

**Lorenzo Mazzieri**, *Dipartimento di Matematica*, Università degli studi di Trento lorenzo.mazzieri@unitn.it

**Alessandra Pluda**, *Dipartimento di Matematica*, Università di Pisa alessandra.pluda@unipi.it

**Bozhidar Velichkov**, *Dipartimento di Matematica*, Università di Pisa bozhidar.velichkov@unipi.it