



CD LAB - PARTICULATE FLOW MODELLING

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Materials2Simulation2Application

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1 Behavior Investigation

This is the second draft of what should be the main topic of my PhD Thesis. The final version will enter and modify accordingly the ToC.

1.1 Investigation topics

In order to define the scientific core of my PhD Thesis the following themes could be investigated:

1. the micro-macro transition,
2. the influence of variations (distributions) of input parameters and poly-dispersity,
3. the behavior of the different properties in real life (e.g. segregation before doing the shear cell experiment),
4. the possibility to extrapolate (e.g. given 3 different fraction distributions, with known behaviors, extrapolate the behavior of a fourth fraction distribution).

Design of experiments and Oberkampf's guidelines will be used to perform the investigations. The selection and number of simulations necessary to accomplish the tasks have yet to be decided.

1.2 Micro - DEM parameters

The main micro parameters that characterize a single sphere in a simulation are:

- (A) the particle diameter distribution (*radii* (R),%) (0.00025 - 0.05 [m]),
- (B) the particle density (ρ_p) (2000-4000 [kg/m^3]),
- (C) the Young modulus (E) (5-10 [MPa]),
- (D) the Poisson ratio (ν) (0-0.5 [$-$]),
- (E) the coefficient of restitution (e) (0.1-1.0 [$-$]),
- (F) the sliding friction (sf) (0.1-1.0 [$-$]),
- (G) the rolling friction (rf) (0.1-1.0 [$-$]),
- (H) the domain edge dimension (D_{cyl}), proportional to R (76, 100, 124 times bigger).

The parameter that drives the simulation time is D_{cyl} . The number of particles is cubically proportional to its size. An estimation is given in Tab. 1 with 32 cores on gollum.

Table 1: Time estimation in hours for each shear cell simulation, see Draft 1

D_{cyl}	76	100	124
α	0.5	2	24
β	2	24	168
γ	168	336	?
δ	720	?	?

1.3 Macro - bulk parameters

The main macro parameters we experimentally determine for a bulk material are:

- (a) the particle diameter distribution (*radii*) (0.00001 - 0.05 [m]),(%),
- (b) the bulk density (ρ_b) (1000-3000 [kg/m³]),
- (c) the Young modulus (E) (5-10 [MPa]),
- (d) the Poisson ratio (ν) (0-0.5 [-]),
- (e) the coefficient of restitution (e) (0.1-1.0 [-]),
- (f) the cohesion in different loading conditions (c') (0-100 [kPa]),
- (g) the internal friction angle in different loading conditions (ϕ) (25-50 [°]).

Angle of Repose simulation, individual contacts micro-DEM parameters: Sliding friction: from 0.05 to 1, 0.05 interval = 20 possibilities; Rolling friction: from 0.05 to 1, 0.05 interval = 20 possibilities; Coefficient of restitution: from 0.5 to 1, 0.1 interval = 5 possibilities; Particle density: e.g. from 2500 to 3500 kg/m³, 100 interval = 11 possibilities; (Particle to geometry ratio: 50, 100, 150 = 3 possibilities;) 20 x 20 x 5 x 11 x 3 = 22000 possible combinations of parameter Each combination would require a simulation, each simulation requires 9 hours over 32 cores = 8250 days! All for only one material with a defined size distribution (e.g. from 3 to 10 mm)! We only consider p2g = 50, because otherwise with e.g. 100 the number of particles is 8 times higher, and so the time 8 times longer

Shear cell simulation, individual contacts micro-DEM parameters: Sliding friction: from 0.05 to 1, 0.05 interval = 20 possibilities; Rolling friction: from 0.05 to 1, 0.05 interval = 20 possibilities; Coefficient of restitution: from 0.5 to 1, 0.1 interval = 5 possibilities; Particle density: e.g. from 2500 to 3500 kg/m³, 100 interval = 11 possibilities; Normal stress: 1, 2, 5, 10 kPa = 4 possibilities; Shear (Particle to geometry ratio: 20, 36, 38, 40, 100, 150 = 6 possibilities;) 20 x 20 x 5 x 11 x 4 x 4 = 352000 possible combinations of parameter Each combination would require a simulation, each simulation requires 64 minutes over 32 cores = 15644 days! All for only one material with a defined size distribution (e.g. from 3 to 10 mm)!

1.4 Artificial neural network

The representation of a multi-sphere experiment through a mathematical model presents numerous complexities. Do we really need all these simulations? How to identify the effect (weight) each parameter? A different approach involves an artificial neural network, that can be realized to understand the relationship between the input

and the output parameters. An artificial neural network is composed of many artificial neurons that are linked together according to a specific network architecture. The objective of the neural network is to transform the inputs into meaningful outputs. The inputs are:

1. A , from real data a but simplified,
2. B, H ,
3. C, D , from literature,
4. E , from real data e ,
5. F, G , the main calibration parameters,

The outputs are f and g .

The idea would be to use a *backpropagation supervised learning*. The already performed simulations could be used as follows: given e.g. 5000 simulations, I will use 3000 of them as training set, and 1000 of the remaining ones could be used to validate the neural system from the *simulation* point of view. In this way I could study *the influence of variations of input parameters and poly-dispersity*.

Between the 1000 simulations remained, as hypothesis 100 of them are experimentally validated. I could use 80 of them to further refine the weights of the neural network functions, and the remaining 20 to validate this second step. At this point I should be able to *extrapolate the behavior of bulk with a volume too large to be simulated* with this complete neural network and to compare the results with the real scale experiments (Leoben).

The reliability of this work is deeply based on the already performed simulations: further numerical investigations as suggested in draft 1 could improve it.

By reserving a portion of the simulations, we can use them to establish the most effective number of neurons inside the hidden layer, for each bulk parameter, through maximization of R2.

Now that the networks have been trained, we can feed the networks with all the combination we need and receive reliable macro-BULK parameters as response. Especially, we can increase the parameter that account for the geometry dimension, without paying completely the price for it. E.g.: for the shear cell only 100 simulations can be done with $g2p > 20$, but thanks to them the network can be trained to understand how that parameter relates with the others = We can expand this consideration and evaluate the effect of the micro-DEM parameters over the large scale AOR test!

1.4.1 Test run with Matlab neural fitting tool

I tried a run with Matlab neural fitting tool. 773 simulations of the Jenike shear cell tester have been analyzed, with monodispersed spheres with the same radius, Young's modulus, ν , ρ_p , e and domain dimensions. The inputs values are F , G , the normal load until steady-state flow and the % of it during the second phase. Especially, these % are 40%, 60% and 80%. All other DEM values are identical for all the 773 simulations. The target value for each simulation is the coefficient of internal friction in the the

second phase. I use 10 hidden neurons in the hidden layer and 1 neuron in the output layer. Matlab "eats" 541 simulations to train the network, 116 to validate it and 116 to test it.

Now I use the network. The inputs values are F, G, the normal load until steady-state flow and the % of it during the second phase. Especially, this is only 100%. I have a total of 256 combinations. I compare the coefficient of internal friction in the second phase of the simulations and of the network in these 256 cases.

$$\left\langle \frac{\mu_{sh,sim} - \mu_{sh,neural}}{\mu_{sh,sim}} \right\rangle = -1.16\% \quad (1)$$

The average value is really promising for this approach.

References

- [1] Jun Ai et al. “Assessment of rolling resistance models in discrete element simulations”. In: *Powder Technology* 206.3 (2011), pp. 269–282.
- [2] Andreas Aigner et al. “Comparison of simulation and experimental results of a simplified jenike shear tester”. In: Colorado School of Mines, 2013.
- [3] Andreas Aigner et al. “Determining the coefficient of friction by shear tester simulation”. In: 2013, pp. 335–342.
- [4] A. Alenzi et al. “DEM validation using an annular shear cell”. In: *Powder Technology* 248.0 (Nov. 2013), pp. 131–142.
- [5] D. Aole, M. K. Jain, and M. Bruhis. “New characterization methods for powder die fill process for producing powder metallurgical components”. In: *Powder Technology* 232.0 (Dec. 2012), pp. 7–17.
- [6] International ASTM. *ASTM D6128 - 06 -Standard Test Method for Shear Testing of Bulk Solids Using the Jenike Shear Cell*. 2013.
- [7] Gabriel K. P. Barrios et al. “Contact parameter estimation for DEM simulation of iron ore pellet handling”. In: *Powder Technology* 248.0 (Nov. 2013), pp. 84–93.
- [8] Niranjana Behera et al. “Modeling and analysis of dilute phase pneumatic conveying of fine particles”. In: *Powder Technology* 249.0 (Nov. 2013), pp. 196–204.
- [9] R. J. Berry and M. S. A. Bradley. “Investigation of the effect of test procedure factors on the failure loci and derived failure functions obtained from annular shear cells”. In: *Powder Technology* 174.1-2 (2007), pp. 60–63.
- [10] Giuseppe Boccignone. *Computazione per interazione naturale: Regressione lineare Bayesiana*.
- [11] L. J. Briggs. “Methods for measuring the coefficient of restitution and the spin of a ball”. In: *Journal of Research of the National Bureau of Standards* 34 (1945).
- [12] Chris Brown and Randal Nelson. *Fitting Experimental Data*. 2011.
- [13] Petra Bubakova, Martin Pivokonsky, and Petr Filip. “Effect of shear rate on aggregate size and structure in the process of aggregation and at steady state”. In: *Powder Technology* 235.0 (Feb. 2013), pp. 540–549.
- [14] Jeffrey W. Bullard and Edward J. Garboczi. “Defining shape measures for 3D star-shaped particles: Sphericity, roundness, and dimensions”. In: *Powder Technology* 249.0 (Nov. 2013), pp. 241–252.
- [15] John W. Carson and Harald Wilms. “Development of an international standard for shear testing”. In: *Powder Technology* 167.1 (2006), pp. 1–9.
- [16] A. Lumin Chen, B. Zhen Chen, and C. Ansheng Feng. “Image analysis algorithm and verification for on-line molecular sieve size and shape inspection”. In: *Advanced Powder Technology* 0 ().
- [17] Sebastian Chialvo, Jin Sun, and Sankaran Sundaresan. “Bridging the rheology of granular flows in three regimes”. In: *Phys.Rev.E* 85.2 (2012), p. 021305. URL: <http://link.aps.org/doi/10.1103/PhysRevE.85.021305>.
- [18] Arthur Christopoulos and Michael J. Lew. “Beyond eyeballing: fitting models to experimental data”. In: *Critical reviews in biochemistry and molecular biology* 35.5 (2000), pp. 359–391.

- [19] Paul W. Cleary, Rob Morrisson, and Steve Morrell. “Comparison of DEM and experiment for a scale model SAG mill”. In: *International Journal of Mineral Processing* 68.1-4 (Jan. 2003), pp. 129–165.
- [20] Paul W. Cleary and Mark L. Sawley. “DEM modelling of industrial granular flows: 3D case studies and the effect of particle shape on hopper discharge”. In: *Applied Mathematical Modelling* 26.2 (Feb. 2002), pp. 89–111.
- [21] Kevin D. Costa, Steven Kleinstein, and Uri Hershberg. *Model Fitting and Error Estimation*. 2010.
- [22] Shyamal C. Das et al. “Importance of particle size and shape on the tensile strength distribution and de-agglomeration of cohesive powders”. In: *Powder Technology* 249.0 (Nov. 2013), pp. 297–303.
- [23] Niklas Engblom et al. “Segregation of powder mixtures at filling and complete discharge of silos”. In: *Powder Technology* 215-216.0 (Jan. 2012), pp. 104–116.
- [24] P. Frankowski et al. “Material characterisation for Discrete Element Modelling calibration”. In: *III International Conference on Particle-based Methods - Fundamentals and Applications PARTICLES 2013* (2013).
- [25] V. Ganesan, K. A. Rosentrater, and K. Muthukumarappan. “Flowability and handling characteristics of bulk solids and powders, a review with implications for DDGS”. In: *Biosystems Engineering* 101.4 (Dec. 2008), pp. 425–435.
- [26] LaTosha M. Gibson et al. “Image analysis measurements of particle coefficient of restitution for coal gasification applications”. In: *Powder Technology* 247.0 (Oct. 2013), pp. 30–43.
- [27] Yan Grasselli and Hans J. Herrmann. “On the angles of dry granular heaps”. In: *Physica A: Statistical Mechanics and its Applications* 246.3-4 (1997), pp. 301–312.
- [28] Yan Grasselli et al. “Effect of impact energy on the shape of granular heaps”. English. In: 2.2 (2000). journal: Granular Matter, pp. 97–100. URL: <http://dx.doi.org/10.1007/s100350050039>.
- [29] Pierre A. Gremaud, John V. Matthews, and Meghan O’Malley. “On the computation of steady Hopper flows: II: von Mises materials in various geometries”. In: *Journal of Computational Physics* 200.2 (2004), pp. 639–653.
- [30] Pierre A. Gremaud, John V. Matthews, and David G. Schaeffer. “On the computation of steady hopper flows III: Model comparisons”. In: *Journal of Computational Physics* 219.1 (2006), pp. 443–454.
- [31] A. P. Grima and P. W. Wypych. “Investigation into calibration of discrete element model parameters for scale-up and validation of particle-structure interactions under impact conditions”. In: *Powder Technology* 212.1 (2011), pp. 198–209.
- [32] Richard F. Grossman and R. J. Del Vecchio. “Chapter 22 : Design of Experiments”. In: *Handbook of Vinyl Formulating*. Wiley - Interscience, 2008, p. 515.
- [33] V. K. Gupta and Shivani Sharma. “Analysis of ball mill grinding operation using mill power specific kinetic parameters”. In: *Advanced Powder Technology* 0 ().
- [34] G. Gustafsson et al. “Determination of bulk properties and fracture data for iron ore pellets using instrumented confined compression experiments”. In: *Powder Technology* 241.0 (June 2013), pp. 19–27.
- [35] Kevin J. Hanley et al. “Application of Taguchi methods to DEM calibration of bonded agglomerates”. In: *Powder Technology* 210.3 (2011), pp. 230–240.

- [36] Johannes Hartl and Jin Y. Ooi. “Numerical investigation of particle shape and particle friction on limiting bulk friction in direct shear tests and comparison with experiments”. In: *Powder Technology* 212.1 (2011), pp. 231–239.
- [37] Jon Hilden et al. “Note on the interpretation of powder shear test data”. In: *Powder Technology* 182.3 (2008), pp. 486–492.
- [38] M. Hirota et al. “Proposal of an approximation equation for the yield locus to evaluate powder properties”. In: *Advanced Powder Technology* 18.3 (2007), pp. 287–302.
- [39] D. Hohner, S. Wirtz, and V. Scherer. “A numerical study on the influence of particle shape on hopper discharge within the polyhedral and multi-sphere discrete element method”. In: *Powder Technology* 226.0 (Aug. 2012), pp. 16–28.
- [40] Richard G. Holdich. *Fundamentals of Particle Technology*. Midland Information, Technology, and Publishing, 2002.
- [41] Etienne Horn. *The Calibration of Material Properties for Use in Discrete Element Models*. 2012.
- [42] S. Humby, U. Tuzun, and A. B. Yu. “Prediction of hopper discharge rates of binary granular mixtures”. In: *Chemical Engineering Science* 53.3 (Feb. 1998), pp. 483–494.
- [43] R. J. M. Janssen, M. J. Verwijs, and B. Scarlett. “Measuring flow functions with the Flexible Wall Biaxial Tester”. In: *Powder Technology* 158.1-3 (2005), pp. 34–44.
- [44] Kerry Johanson. “Effect of particle shape on unconfined yield strength”. In: *Powder Technology* 194.3 (2009), pp. 246–251.
- [45] Mohammad Khalilitehrani, Per J. Abrahamsson, and Anders Rasmuson. “The rheology of dense granular flows in a disc impeller high shear granulator”. In: *Powder Technology* 249.0 (Nov. 2013), pp. 309–315.
- [46] A. H. Kharaz, D. A. Gorham, and A. D. Salman. “Accurate measurement of particle impact parameters”. In: *Measurement Science and Technology* 10.1 (1999), p. 31. URL: <http://stacks.iop.org/0957-0233/10/i=1/a=009>.
- [47] A. H. Kharaz, D. A. Gorham, and A. D. Salman. “An experimental study of the elastic rebound of spheres”. In: *Powder Technology* 120.3 (2001), pp. 281–291.
- [48] Christoph Kloss and Christoph Goniva. *LIGGGHTS Manual*. URL: <http://www.cfdem.com/>.
- [49] Christoph Kloss et al. “Models, algorithms and validation for opensource DEM and CFDDEM”. In: *Progress in Computational Fluid Dynamics, an International Journal* 12.2 (2012), pp. 140–152. URL: <http://dx.doi.org/10.1504/PCFD.2012.047457>.
- [50] Matthew Krantz, Hui Zhang, and Jesse Zhu. “Characterization of powder flow: Static and dynamic testing”. In: *Powder Technology* 194.3 (2009), pp. 239–245.
- [51] M. Kheiripour Langroudi et al. “An investigation of frictional and collisional powder flows using a unified constitutive equation”. In: *Powder Technology* 197.1-2 (2010), pp. 91–101.
- [52] H. Li, G. R. McDowell, and I. S. Lowndes. “A laboratory investigation and discrete element modeling of rock flow in a chute”. In: *Powder Technology* 229.0 (Oct. 2012), pp. 199–205.

- [53] Stefan Luding. “Introduction to Discrete Element Methods, Basics of Contact Force Models and how to perform the MicroMacro Transition to Continuum Theory”. In: *EJECE* 12 (2008), pp. 785–826.
- [54] Mohan Medhe, B. Pitchumani, and J. Tomas. “Flow characterization of fine powders using material characteristic parameters”. In: *Advanced Powder Technology* 16.2 (2005), pp. 123–135.
- [55] J. Mellmann, T. Hoffmann, and C. Furl. “Flow properties of crushed grains as a function of the particle shape”. In: *Powder Technology* 249.0 (Nov. 2013), pp. 269–273.
- [56] Hiroshi Mio et al. “Validation of Particle Size Segregation of Sintered Ore during Flowing through Laboratory-scale Chute by Discrete Element Method”. In: *ISIJ International* 48.12 (2008). journal: ISIJ International, pp. 1696–1703.
- [57] B. K. Mishra and Raj K. Rajamani. “The discrete element method for the simulation of ball mills”. In: *Applied Mathematical Modelling* 16.11 (Nov. 1992), pp. 598–604.
- [58] Paul A. Moysey, Nadella V. Rama Rao, and Malcolm H. I. Baird. “Dynamic coefficient of friction and granular drag force in dense particle flows: Experiments and DEM simulations”. In: *Powder Technology* 248.0 (Nov. 2013), pp. 54–67.
- [59] Patric Muller et al. “Complex Velocity Dependence of the Coefficient of Restitution of a Bouncing Ball”. In: *Phys.Rev.Lett.* 110.25 (2013), p. 254301. URL: <http://link.aps.org/doi/10.1103/PhysRevLett.110.254301>.
- [60] Emilia Nowak et al. “Measurements of contact angle between fine, non-porous particles with varying hydrophobicity and water and non-polar liquids of different viscosities”. In: *Powder Technology* 250.0 (Dec. 2013), pp. 21–32.
- [61] J. R. Pillai, M. S. A. Bradley, and R. J. Berry. “Comparison between the angles of wall friction measured on an on-line wall friction tester and the Jenike wall friction tester”. In: *Powder Technology* 174.1-2 (2007), pp. 64–70.
- [62] S. J. Plimpton. “Fast Parallel Algorithms for Short-Range Molecular Dynamics”. In: *J Comp Phys* 117 (1995), pp. 1–19.
- [63] Yury V. Polezhaev and I. V. Chircov. “DRAG COEFFICIENT”. In: *Thermopedia* (2011). URL: <http://www.thermopedia.com/content/707/>.
- [64] Thorsten Poschel and Thomas Schwager. *Computational Granular Dynamics*. Springer, 2004.
- [65] C J Reagle et al. “Measuring the coefficient of restitution of high speed microparticle impacts using a PTV and CFD hybrid technique”. In: *Measurement Science and Technology* 24.10 (2013), p. 105303. URL: <http://stacks.iop.org/0957-0233/24/i=10/a=105303>.
- [66] Rudiger Schmitt and Hermann Feise. “Influence of Tester Geometry, Speed and Procedure on the Results from a Ring Shear Tester”. In: *Particle and Particle Systems Characterization* 21.5 (2004), pp. 403–410.
- [67] Dietmar Schulze. *Flow Properties of Powders and Bulk Solids*. 2011.
- [68] Dietmar Schulze. *Powders and bulk solids: behavior, characterization, storage and flow*. Springer, 2008.
- [69] Dietmar Schulze, H. Heinrich, and H. Zetzener. “The Ring Shear Tester as a Valuable Tool for Silo Design and Powder Characterization”. In: *Powder Handling and Processing* 13.19-26 (2001).

- [70] Jorg Schwedes. “Measurement of flow properties of bulk solids”. In: *Powder Technology* 88.3 (Sept. 1996), pp. 285–290.
- [71] Jorg Schwedes. “Review on testers for measuring flow properties of bulk solids”. English. In: 5.1 (2003). journal: Granular Matter, pp. 1–43. URL: <http://dx.doi.org/10.1007/s10035-002-0124-4>.
- [72] A. Schweiger and I. Zimmermann. “A new approach for the measurement of the tensile strength of powders”. In: *Powder Technology* 101.1 (1999), pp. 7–15.
- [73] Erdem Simsek et al. “Influence of particle diameter and material properties on mixing of monodisperse spheres on a grate: Experiments and discrete element simulation”. In: *Powder Technology* 221.0 (May 2012), pp. 144–154.
- [74] U. Sindel and I. Zimmermann. “Measurement of interaction forces between individual powder particles using an atomic force microscope”. In: *Powder Technology* 117.3 (2001), pp. 247–254.
- [75] Dale M. Snider. “Three fundamental granular flow experiments and CPFD predictions”. In: *Powder Technology* 176.1 (2007), pp. 36–46.
- [76] R. Sondergaard, K. Chaney, and C. E. Brennen. “Measurements of Solid Spheres Bouncing Off Flat Plates”. In: *Journal of Applied Mechanics* 112.3 (1990), p. 694. URL: <http://resolver.caltech.edu/CaltechAUTHORS:SONjam90>.
- [77] Jin Sun and Sankaran Sundaresan. “Radial hopper flow prediction using a constitutive model with microstructure evolution”. In: *Powder Technology* 242.0 (July 2013), pp. 81–85.
- [78] K. Takenaka et al. “Shape Effects of the Yield Locus on the Rankine Coefficient”. In: *Advanced Powder Technology* 19.1 (2008), pp. 25–37.
- [79] Gabriel I. Tardos. “A fluid mechanistic approach to slow, frictional flow of powders”. In: *Powder Technology* 92.1 (June 1997), pp. 61–74.
- [80] Jose’ M. Torralba et al. “Development of high performance powder metallurgy steels by high-energy milling”. In: *Advanced Powder Technology* 24.5 (Sept. 2013), pp. 813–817.
- [81] C. M. Wensrich and A. Katterfeld. “Rolling friction as a technique for modelling particle shape in DEM”. In: *Powder Technology* 217.0 (Feb. 2012), pp. 409–417.
- [82] C. M. Wensrich and A. Katterfeld. “Rolling friction as a technique for modelling particle shape in DEM”. In: *Powder Technology* 217.0 (Feb. 2012), pp. 409–417.
- [83] Wikipedia. *Discrete element method*. URL: http://en.wikipedia.org/wiki/Discrete_element_method.
- [84] M. Wojcik, J. Tejchman, and G. G. Enstad. “Confined granular flow in silos with inserts - Full-scale experiments”. In: *Powder Technology* 222.0 (May 2012), pp. 15–36.
- [85] Y. C. Zhou et al. “An experimental and numerical study of the angle of repose of coarse spheres”. In: *Powder Technology* 125.1 (2002), pp. 45–54.