

Green NFTs: A Study on the Environmental Impact of Cryptoart Technologies

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Abstract

We introduce a model of greenhouse gas emissions due to on-chain activity on Ethereum, focusing on cryptoart. We also estimate the impact of individual transactions on the environment, both before and after the London hard fork. We find that with the current fee mechanism, spending one dollar on transaction fees corresponds to emitting at least the equivalent of 1.151 kilograms of CO₂. We also describe several techniques to reduce cryptoart emissions, both in the short and long term.

1 Introduction

In the last year, there has been an exponential growth of cryptoart, a new blockchain-based art form. After the publication of several articles that aimed to raise awareness about its environmental impact [Akten, 2020] [Lemercier, 2021], there has also been a growing interest in developing solutions to reduce greenhouse gas (GHG) emissions due to cryptoart. A range of proposals have been advanced, from reducing gas usage [Pipkin, 2021] to switching to Proof of Stake blockchains [Wintermeyer, 2021] to carbon offsets [Kahn, 2021]. Others have even asserted that cryptoart has no impact on carbon emissions [Super-Rare, 2021] [Mattei, 2021]. We argue that a model of the environmental impact of cryptoart is fundamental to properly evaluate the effectiveness of potential solutions. We therefore introduce a model to compute the GHG emissions of cryptoart hosted on the Ethereum blockchain. We also analyze the impact of a single transaction, focusing on both the current fee mechanism and the soon to be implemented EIP-1559. By estimating the geographical distribution of Ether miners and their cost breakdown, we find that spending one dollar in transaction fees leads to additional GHG emissions amounting to 1.115 kgCO₂eq. Finally,

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we illustrate different solutions that would reduce the environmental impact of cryptoart, focusing on both individual and collective actions. A summary of our key conclusions can be found in Section 9.

2 Background

2.1 Cryptoart

Cryptoart is a category of art based on blockchain technology. Artworks are stored as Non-Fungible Tokens (NFTs), unique digital assets whose ownership and scarcity can be verified in a decentralized and trustless manner. The actions of creating (also known as "minting"), bidding, buying and transferring NFTs are performed by executing transactions on-chain. Some of the most known cryptoart platforms, such as OpenSea¹, Nifty Gateway² and SuperRare³ are currently hosted on the Ethereum network.

2.2 Block production

In order for a transaction to be accepted by the network, it must be included in a block. A block is a data structure containing a collection of transactions. Protocols define an entity, called validator, which appends new blocks to the blockchain. Since blocks are limited in size and frequency, validators prioritize inserting transactions that maximize their revenue. Users therefore pay fees to be included in new blocks. A transaction with a higher fee will be included sooner.

2.3 Proof of Work

Proof of Work (PoW) blockchains use a consensus algorithm where blocks are validated by solving an energy intensive computational puzzle. The protocol defines a value, block difficulty, which is adjusted in order to maintain a fixed block frequency. The energy consumption required to validate (or mine) a block is proportional to the block difficulty.

The computational power of a miner is measured by its hash rate. The difficulty of a block is proportional to the total hash rate of the network. The probability that a miner will mine a block is proportional to the percentage of their own hash rate compared to that of the network. Given a certain difficulty, both full and empty blocks require approximately the same amount of energy to be mined.

While Bitcoin is mined on application-specific integrated circuits (ASICs), Ethereum is relatively ASIC-resistant and is therefore mined on graphical processing units (GPUs).

¹Website: opensea.io

²Website: niftygateway.com

³Website: superrare.co

2.4 EIP-1559

EIP-1559 is an Ethereum update that will take place in July with the London hard fork.

The current fee mechanism is based on first-price auctions. A transaction requires a certain amount of block space, called gas, which is proportional to its complexity. Each user chooses the price paid per unit of gas. Miners prioritize transactions with the highest gas price; therefore, users have to estimate the minimum gas price required to be included. Since users do not have perfect information on other bids, this price tends to be overestimated.

EIP-1559 solves this problem by introducing a protocol-defined gas price, **BASEFEE**, which must be paid for a transaction to be included in the block. EIP-1559 defines a target block size T and a maximum block size $2T$. If the previous block was larger than T , **BASEFEE** is increased, and vice versa.

BASEFEE is computed as follows:

$$B_{n+1} = B_n \left(1 + \frac{1}{8} \frac{B_n - T}{T} \right)$$

where B_n is the **BASEFEE** of the n -th block.

The key difference between EIP-1559 and the current fee mechanism is that the transaction fee is burned. To incentivize miners to include transactions, users pay an additional **MINER_TIP**, which only covers execution costs.

If, at any point in time, the total size of pending transactions is higher than $2T$, this new fee mechanism degrades to a first-price auction using **MINER_TIP**.

Roughgarden [2020] predicts that EIP-1559 will not affect the gas price.

3 Miners

In this section, we show that, under reasonable assumptions, the global mining cost of a PoW blockchain is approximately equal to the global mining revenue.

We treat miners as rational agents that aim to increase their profits. A rational agent would not undertake an activity which would result in a ongoing loss in doing so. This approach ignores other incentives that might motivate a miner, such as the desire for a more decentralized blockchain.

Miners have two main sources of revenue:

- The block reward, which consists of:
 - The fixed block reward;
 - The uncle block reward⁴;
 - The uncle block inclusion reward⁴;
- Transaction fees.

⁴Uncle block rewards and uncle block inclusion rewards [Wood et al., 2014] are mechanisms to promote decentralization. They are designed to reward miners that successfully mined a block which was not validated by the network.

and three main costs:

- Electricity cost;
- Hardware cost;
- Other types of costs, which we assume to be negligible.

The probability of a miner collecting the block reward and the transaction fees is equal to their hash rate divided by the global hash rate. More formally, we model the expected revenue of a miner k from a block as:

$$\mathbb{E}[R_k] = (R_{block} + R_{fees}) \frac{H_k}{\sum_i H_i} \quad (1)$$

where R_{block} is the revenue due to the block reward, R_{fees} is the revenue from transaction fees and H_i is the hash rate of the i -th miner.

Since miners have a negligible impact on R_{block} and R_{fees} , the only way to increase their revenue is to increase their relative hash rate. We treat variations in the per-unit cost of hardware and electricity due to economy of scale effects as negligible. If GPUs are being already used at maximum performance, a higher hash rate can only be achieved by acquiring more GPUs. Since the hardware cost of a typical mining setup is dominated by GPUs, doubling the number of GPUs also roughly doubles the hardware cost. Similarly, since the power requirements are dominated by GPUs, doubling their number would also approximately double the electricity cost. GPUs, however, have a limited life-time before becoming outdated or unusable. We therefore treat GPUs not as a one-time cost but as a recurring one.

More formally, we model the hash rate of a miner as directly proportional to both hardware and electricity costs.

Since Ether can be mined using consumer-grade hardware and with minimal technical skills, new miners can easily enter the market. We therefore model Ether mining as a competitive virtual commodity market, a market in which agents reach an equilibrium where the marginal revenue is equal to the marginal cost. In other words, the revenue of mining for an additional day is equal to the cost. The total mining revenue during a certain period of time is therefore equal to the total mining cost:

$$R_{tot} = C_{tot} \quad (2)$$

Our findings match the results obtained by Hayes [2017], who applied a similar model to estimate the GHG impact of Bitcoin.

Our model assumes that miners can quickly adapt their costs to market fluctuations. This is possible due to the existence of alternative sources of revenue (e.g. mining on other blockchains). If the profitability of Ether mining decreases, some miners will redirect their computational power towards other tasks, and vice versa. For the purpose of this paper, we ignore variations in the profitability of such activities.

4 GHG Impact of Proof of Work

In this section, we show that the GHG impact of a PoW blockchain is directly proportional to its global mining revenue.

First, we assume that variations in mining revenue do not significantly affect the distribution of energy sources, as well as of the hardware used.

Therefore, we treat the GHG impact of hardware and electricity as directly proportional to their costs. We model the GHG emissions due to mining as follows:

$$E_{tot} = \alpha_{hw}C_{hw} + \alpha_{el}C_{el} \quad (3)$$

where E_{tot} are the global mining emissions (in kgCO₂eq) of mining, C_{hw} is the global mining cost due to hardware, C_{el} is the global mining cost due to electricity, and α_{hw} and α_{el} are constants that represent the kgCO₂eq emitted per dollar spent respectively on hardware and electricity.

Assuming that variations in mining revenue do not meaningfully influence the ratio between hardware and electricity costs, we rewrite C_{hw} and C_{el} as follows:

$$C_{hw} = \beta C_{tot} \quad (4)$$

$$C_{el} = (1 - \beta)C_{tot} \quad (5)$$

where $C_{tot} = C_{hw} + C_{el}$ and $0 \leq \beta \leq 1$ is a constant.

E_{tot} can be therefore rewritten as:

$$E_{tot} = \alpha_{hw}\beta C_{tot} + \alpha_{el}(1 - \beta)C_{tot} = \alpha_{tot}C_{tot} = \alpha_{tot}R_{tot} \quad (6)$$

where $\alpha_{tot} = \alpha_{hw}\beta + \alpha_{el}(1 - \beta)$ is a constant measuring the kgCO₂eq emitted per dollar spent on mining.

5 Estimating α_{tot}

In this section, we estimate the kgCO₂eq emitted per dollar earned by Ether miners.

We compute a lower bound of α_{tot} by considering only two sources of GHG emissions, namely GPU production and electricity usage. In order to do so:

- We choose a representative mining GPU;
- We estimate the geographical distribution of Ether miners;
- We estimate the weighted average kgCO₂eq emitted per dollar spent on electricity;
- We estimate the average lifetime of a GPU and the ratio of C_{el} and C_{hw} compared to C_{tot} in that time frame;
- We use our gathered data to compute an estimate of α_{tot} .

Name	AMD RX 590
Launch quarter	Q4 2018
Current average price	USD 650
Hash rate	27.31 MH/s
Power consumption	163 W

Table 1: Specifications of an AMD RX 590 GPU. Since November 2020, a spike in demand has led to several shortages and an increase in average prices from USD 450 to USD 850. We therefore use an estimate of the average price in the last 6 months. Sources: AMD [2018], Minerstat [2021] CamelCamelCamel [2021].

5.1 Representative GPU

For the sake of modelling the role of GPUs in mining emissions, we use the AMD RX 590 as a representative GPU. As of May 2021, the RX 590 is the GPU with the highest Ethereum hash rate per Watt-hour Minerstat [2021]. The relevant specifications of an RX 590 are outlined in table 1.

Following De Vries [2018], we estimate a maximum GPU lifespan of 2 years. Ardenne and Talens Peiró [2015] estimate that producing a GPU has a GHG impact of 54 kgCO₂eq.

5.2 Geographical Distribution of Miners

While the approximate global hash rate of the Ethereum network is known, the inherent anonymity and decentralization of its protocol prevent accurate estimates of the geographical distribution of its nodes.

A naive approach would be to count the number of Ethereum nodes in each country. This technique, however, ignores potential differences in node hash rate between different countries.

A second approach involves using data on mining pools. Mining pools represent a large portion of the global hash rate [Lin et al., 2021] and often provide information on their hash rate share. However, several large mining pools are based in multiple countries and do not provide information regarding their internal geographical distribution. Moreover, if the increased payout and reliability outweigh the revenue loss due to connection delays, a miner might join a pool in a different country or continent.

We therefore follow a different strategy: we use the data collected by Silva et al. [2020] on block observation as a proxy of the true geographical distribution of Ether miners. In April 2019, the authors collected statistics on which of four nodes (located in Western Europe, Central Europe, North America and East Asia) was the first to receive updates on a newly mined block. While during the last two years there might have been shifts in the geographical distribution, we argue that, due to the relative stability of Ether mining economics⁵, such esti-

⁵Compare with Bitcoin, which saw a shift towards industrial, ASIC-based large scale mining

Region	Hash rate %	\$/kWh	kgCO ₂ eq/kWh	kgCO ₂ eq/\$
Europe	50	0.1419	0.230	1.621
East Asia	38	0.0916	0.582	6.354
North America	12	0.0815	0.331	4.061
Overall	~100	0.1155	0.376	3.255

Table 2: Industrial electricity prices and CIPK by region. We use average electricity prices in the European Union [Rademaekers et al., 2020], People’s Republic of China [ESCAP, 2018] and the United States [EIA, 2021]. Source for CIPK data: IEA [2020].

Name	Cost (USD)	GHG emissions (kgCO ₂ eq)
Hardware	650	54
Electricity	330	1074
Total	980	1128

Table 3: Final breakdown of costs and emissions for one RX 590 GPU over 2 years.

mates are still adequate for our purposes. In the context of impact estimation, we treat Western and Central Europe as the same region. We also consider the role of other regions negligible. We compute a weighted average of kgCO₂eq per dollar based on average industrial electricity prices and carbon-intensity-per-kilowatthour (CIPK), as outlined in table 2.

5.3 Global estimate

We conclude that, over a 2-year period, a single GPU will cost 980 dollars and have an impact of 1128 kgCO₂eq (see table 3). Our estimate of α_{tot} is therefore 1.151 kgCO₂eq/\$. In order to put this value into context, we apply it to the current Ethereum data. From April 29, 2021, to May 5, the average global daily revenue for Ethereum miners was 58.91 millions of dollars [EtherChain, 2021a] [EtherChain, 2021b], equivalent to a daily emission of 67.80 ktCO₂eq or an annual emission of 24.76 MtCO₂eq. The latter value is consistent with the 19.64 MtCO₂eq figure estimated by the Ethereum Energy Consumption Index over the same period [De Vries, 2021].

6 Individual Impact

While estimating the total emissions of a network can be useful to compare entire blockchains, we also model the impact of a single transaction, both with the current fee mechanism and with EIP-1559. In order to isolate the effects of individual transactions, we treat the Ether demand as constant in time.

[Taylor, 2017].

6.1 First-Price Auction

Suppose that a user successfully executes a transaction that requires G gas at a price (in Gwei, equivalent to 10^{-9} Ether) of P_{gas} per unit of gas. We identify three main effects of this action:

1. The user paid their fee to a miner, thereby directly increasing the global mining revenue;
2. The user caused other transactions amounting to G gas to be left out of the block, which are then⁶:
 - (a) Accepted later at the same price;
 - (b) Accepted after their gas price is increased;
 - (c) Never accepted;
3. The user increased estimates of the gas price, leading other users to bid more in the following blocks.

On May 1, out of more than 1.1 billion total Ethereum transactions [Blockchair, 2021], roughly 190 thousand ($<0.02\%$) were still pending, the majority of which were accepted within 24 hours [Etherscan, 2021c]. We therefore treat case 2c as negligible.

We compute a lower bound of the increase in miner revenue by considering only cases 1, 2a and 2b. This approach ignores the long-term effects of a transaction, therefore providing a conservative estimate of the true impact.

Specifically, we model the lower bound of the overall increase in miner revenue (in dollars) ΔR as:

$$\Delta R \geq P_{Gwei}GP_{gas} + P_{Gwei} \sum_i g_i (p'_i - p_i) \quad (7)$$

where $G = \sum_i g_i$, P_{Gwei} is the price of one Gwei, and g_i , p_i and p'_i are respectively the gas amount, the old gas price and the new gas price of the i -th transaction that was excluded. For case 2a, $p'_i = p_i$, which means that the direct revenue impact of delaying such transactions is zero. We compute a looser lower bound by ignoring case 2b⁷.

We therefore simplify inequality 7 by rewriting it as:

$$\Delta R \geq GP_{Gwei}P_{gas} \quad (8)$$

In other words, the lower bound ΔE of the GHG impact of a transaction is:

$$\Delta E \geq \alpha_{tot}GP_{Gwei}P_{gas} \quad (9)$$

⁶Due to the specifications of the Ethereum protocol, it is not possible to reduce the gas price of a submitted transaction.

⁷We analyzed 20k transactions executed on May 3, 2021, finding that case 2b was responsible for an increase of less than 2% in transaction revenue. [Etherscan, 2021d]

6.2 EIP-1559

With EIP-1559, since the `MINER_TIP` only covers the execution costs, the total mining revenue is dominated by the block reward. Therefore, the only non-negligible impact that a transaction has on mining revenue is the deflationary effect of burning `BASEFEE` Ether.

Let s_t be the rate of growth of the Ether circulating supply after the t -th block has been mined:

$$s_t = \frac{u_t}{S_t} \quad (10)$$

where u_t is the absolute variation in the number of existing Ethers and S_t is the Ether circulating supply after the t -th block has been mined.

Since we treat the Ether demand as constant, the dollar value P_{t+1} of one Ether after the $t + 1$ -th block has been mined is [Sutherland, 2019]:

$$P_{t+1} = \frac{P_t}{s_t + 1} = P_t \frac{S_t}{S_t + u_t} \quad (11)$$

Let $V_t = P_t S_t$ be the total dollar value of the Ether circulating supply after the t -th block has been mined. Note that

$$V_{t+1} = P_{t+1} S_{t+1} = P_t \frac{S_t}{S_t + u_t} (S_t + u_t) = P_t S_t = V_t \quad (12)$$

In other words, V_t is constant. Let $V : \forall t. V_t = V$. P_t is therefore:

$$P_t = \frac{V}{S_t} \quad (13)$$

In EIP-1559, there are two factors that have opposite effects on the circulating supply. After each block is mined, $m = 2$ additional Ethers are created to reward the miners, while users burn the equivalent of b dollars in transaction fees. We assume m and b to be constant. u_t is therefore:

$$u_t = m - \frac{b}{P_t} = m - \frac{b}{V} S_t \quad (14)$$

S_{t+1} is then equal to:

$$S_{t+1} = S_t + u_t = S_t + m - \frac{b}{V} S_t \quad (15)$$

while the miner revenue R_{t+1} in USD after the $t + 1$ -th block has been mined is:

$$R_{t+1} = R_t + m \frac{V}{S_{t+1}} \quad (16)$$

Let S_0 be the Ether circulating supply at a $t = 0$.

R_t can be rewritten as:

$$\begin{aligned}
R_t &= R_{t-1} + \frac{mV}{S_t} = \\
&= R_{t-2} + \frac{mV}{S_{t-1}} + \frac{mV}{S_t} = \\
&\vdots \\
&= R_0 + \sum_{j=1}^t \frac{mV}{S_j}
\end{aligned}$$

Since $R_0 = 0$:

$$R_t = mV \sum_{j=1}^t \frac{1}{S_j} \quad (17)$$

S_{t+1} can be rewritten as:

$$S_{t+1} = S_t + m - \frac{b}{V} S_t = S_t \underbrace{\left(1 - \frac{b}{V}\right)}_{:=K} + m = K S_t + m \quad (18)$$

which is equal to:

$$\begin{aligned}
S_{t+1} &= K S_t + m = \\
&= K^2 S_{t-1} + mK + m = \\
&= K^3 S_{t-2} + mK^2 + mK + m = \\
&\vdots \\
&= K^{t+1} S_0 + m \sum_{j=0}^t K^j
\end{aligned}$$

S_t is therefore equal to:

$$S_t = K^t S_0 + m \left(\frac{1 - K^t}{1 - K} \right) \quad (19)$$

Spending l dollars on transaction fees is equivalent to removing $lP_0 = l \frac{V}{S_0}$ Ethers from the initial circulating supply. Between the deployment of EIP-1559 (in July) and the transition to Proof of Stake (at the beginning of 2022, after which the additional environmental impact of the transaction will be negligible), only around 1.16 million blocks are expected to be mined. Since the closed-form expression of R_t (which we report in Appendix A) does not provide an intuition on the effect of a transaction, we instead plot the additional miner revenue ΔR_t . As shown in figure 1, the additional revenue is at least one to two orders of magnitude lower than with the current fee mechanism.

We estimate that, under our hypotheses, during the approximately 180 days between the introduction of EIP-1559 and the transition to PoS, the total miner revenue with the current fee mechanism would be 9.9 billion dollars. Over the same period, with EIP-1559 the miner revenue would be 6.8 billion dollars, corresponding to a reduction in the GHG emissions of Ethereum by approximately a third.

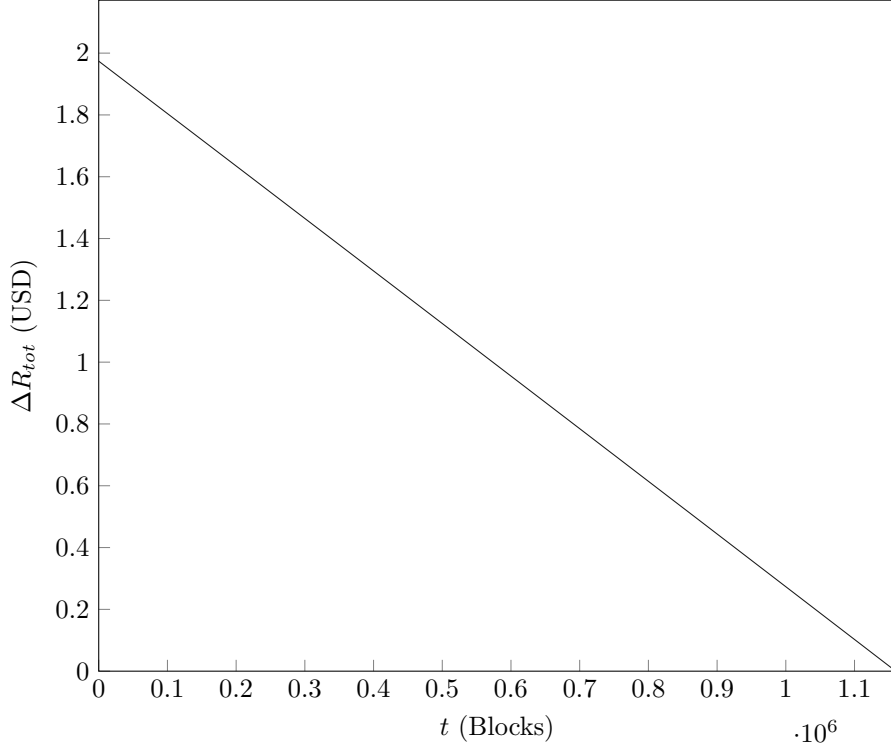


Figure 1: Difference in miner revenue due to the execution of a transaction which requires a fee of 100 dollars. The x axis represents the time of execution, with $t = 0$ corresponding to the first block after the introduction of EIP-1559. We set $S_0 = 115.7\text{M}$ Ether and $V_0 = 341\text{B}$ USD, corresponding to the average circulating supply and total value on May 1, 2021 [CoinGecko, 2021]. We use $b = 2650$ USD, equal to the average revenue per block due to transaction fees from April 29, 2021 to May 5, 2021 [Etherscan, 2021b].

7 Solutions

In this section, we present the most relevant solutions to reduce the GHG impact of NFTs, focusing on both individual and collective actions.

7.1 Individual Actions

From the model described in section 6, we deduce that any action to reduce transaction fees has a beneficial impact on GHG emissions. We therefore outline some practices to reduce the individual impact of a user.

A simple yet effective solution is to perform transactions using a lower gas price. This can be done by tolerating a longer confirmation time, executing transactions during times of the day with lower gas demand, or both.

Another way to reduce the environmental impact is by decreasing gas usage. For example, lazy minting minimizes gas requirements by treating the creation and sale of an NFT as a single transaction.

Additionally, artists often auction NFTs on-chain. Since on-chain bids require paying a transaction fee, we suggest using off-chain bids (supported for example by the Wyvern Protocol, implemented by OpenSea) to help reduce emissions.

Finally, most NFTs are sold through instant sales, where artists sell their work for a fixed price. If the artwork is particularly sought after, buyers are incentivized to use higher gas prices to outrun the others, therefore paying a much higher transaction fee than necessary. Moreover, buyers that fail to obtain a copy also pay transaction fees. In such cases, switching from instant sales to off-chain bids can significantly reduce the impact of cryptoart.

7.2 Proof of Stake

Proof of Stake (PoS) is a class of consensus algorithms that select and reward validators as a function of their economic stake in the network [Bentov et al., 2016]. Unlike PoW, the probability of creating a block in a PoS network does not depend on computational power, but rather on the staked amount that might be lost in case of fraudulent activity. A PoS node has minimal hardware and electricity requirements, and therefore has a significantly lower environmental impact. Moreover, increasing the stake has no effect on the energy consumption of the node. Ethereum 2.0, the upcoming PoS version of Ethereum, is expected to reduce the environmental impact of the network by 99% [Fairley, 2019].

7.3 Layer 2

Layer 2 is a collective term for solutions designed to help scale applications by handling transactions off the main chain (referred to as layer 1). Generally speaking, transactions are submitted to layer 2 nodes, which batch them into groups before storing them on layer 1.

Layer 2 technologies that are based on Ethereum have a nontrivial impact on the environment. However, layer 2 transactions require significantly less gas and therefore represent a preferable alternative to executing them directly on-chain. The main types of layer 2 solutions are sidechains and rollups.

7.3.1 Sidechains and Plasma

A sidechain is a separate blockchain which runs parallel to the layer 1 and operates independently, usually with a Proof of Stake consensus algorithm. Sidechains are connected to the main chain by a two-way bridge and are often less decentralized and therefore less secure than their layer 1.

Plasma, on the other hand, is a technology that provides a way to execute transactions off-chain at a higher frequency and lower cost. It regularly stores on layer 1 information such as asset ownership, protecting it from attacks. However, in extreme cases, it is not guaranteed that the full state of Plasma can be recovered [Poon and Buterin, 2017]. Sidechains and Plasma can be used together, such as in the case of Polygon, which features a hybrid protocol to mitigate the risk of information loss [Kanani et al., 2019].

7.3.2 Rollups

Rollups are a class of layer 2 technologies that execute transactions outside layer 1 but store their data on-chain. This approach guarantees that, even in case of attack, it is always possible to recover all performed transactions. The same transaction, if executed on a rollup, requires two to three orders of magnitude less gas compared to its layer 1 counterpart [Buterin, 2021]. Rollups can be divided into zero-knowledge and optimistic rollups.

Zero-knowledge (ZK) rollups bundle transactions off-chain and generate a cryptographic proof of their validity. This proof, known as a SNARK (Succinct Non-interactive ARgument of Knowledge), is then stored on layer 1. Being a relatively new technology, as of May 2021 the only known NFT platform hosted on ZK rollups is Immutable X⁸, which is currently in closed alpha. The main disadvantage of ZK rollups is that they do not support general computation. Because of this constraint, only basic NFT operations (e.g. minting and trading) can be executed. Extending ZK rollups is currently an active area of research.

Optimistic rollups, on the other hand, assume that all transactions are valid (hence the name "optimistic"). In optimistic rollups, anyone can submit a new transaction batch. However, if a user (also known as "fraud verifier") suspects that a batch is fraudulent, it is possible to prove it by executing the entire computation using the stored data. Fraud verifiers are usually rewarded financially at the expense of malicious users. Unlike ZK rollups, optimistic rollups support general computation, but, before withdrawing assets, users must wait a "challenge period" during which other users can claim fraudulent activity.

The two most known optimistic rollups, Optimism⁹ and Arbitrum¹⁰, are currently in development. Optimism is expected to launch in July, while, as of May 2021, the team behind Arbitrum has not provided a launch date yet.

⁸Website: immutable.com

⁹Website: optimism.io

¹⁰Website: arbitrum.io

7.4 Carbon Offsets

Carbon offsets represent an alternative way to reduce the GHG impact of blockchains. By purchasing carbon offsets, a user compensates for their emissions by funding activities that have a negative GHG balance, such as planting trees or increasing the commercial viability of renewable energy. Several initiatives that use blockchains as a tool to complement carbon markets have been introduced [Howson et al., 2019] [Kahn, 2021]. Moreover, some NFT platforms, such as Immutable X, compensate for their GHG emissions by automatically purchasing carbon offsets [Immutable, 2020].

Another, more indirect, method to reduce the environmental impact is to donate to climate non-profits. The cryptoart platform KnownOrigin¹¹, for example, offers an interface for artists to donate part of their revenue to sustainable causes [KnownOrigin, 2021].

8 Example

To put our results in context, we use our model to estimate the environmental impact of a hypothetical cryptoart piece, focusing on Ethereum PoW with the current fee mechanism. Consider an NFT with the following gas requirements:

- Minting: 450k gas
- Buying: 300k gas
- Transferring: 80k gas
- Bidding: 100k gas

Refer to table 4 for an estimate of the impact of these transactions.

Suppose that after minting the artwork, the creator auctions it on-chain, receiving 10 bids. The winning bidder then purchases the NFT and transfers it to a secondary account. The impact of this art piece is therefore equal to the sum of the impacts of 1 mint, 10 bids, 1 purchase and 1 transfer. In other words, the impact of our hypothetical NFT is 412.09 kgCO₂eq, equivalent to driving a typical passenger vehicle for 1020 miles (or 1642 km) [EPA, 2018].

There are several simple actions that can be taken to reduce this figure:

- Using off-chain bids would reduce emissions by 55%;
- Executing transactions using the minimum required gas price (which, during April 29, 2021 - May 5, 2021, was on average 45 Gwei [GasNow, 2021]) would reduce transaction fees, and therefore emissions, by 26%;
- Similarly, executing these transactions during times of the day with a lower minimum gas price, such as at 5 p.m. UTC (see table 2), would reduce emissions by an additional 31%;

¹¹Website: knownorigin.io

Transaction	Gas usage	Cost (USD)	Impact (kgCO ₂ eq)
Minting	450k	88.03	101.33
Buying	300k	58.69	67.55
Transferring	80k	15.65	18.01
Bidding	100k	19.56	22.52

Table 4: Impact of different transactions of a hypothetical cryptoart piece. We use the average gas price from April 29, 2021 to May 5, 2021 of 61 Gwei [Etherscan, 2021a], as well as the average Ether price of 3207 USD in the same period [YCharts, 2021].

All these actions together would reduce emissions to 94.69 kgCO₂eq (-77%), equivalent to driving for 234 miles (or 377 km). Assuming 0.004 \$/kgCO₂eq [SavingNature, 2021], offsetting these emissions would cost approximately 0.38 dollars.

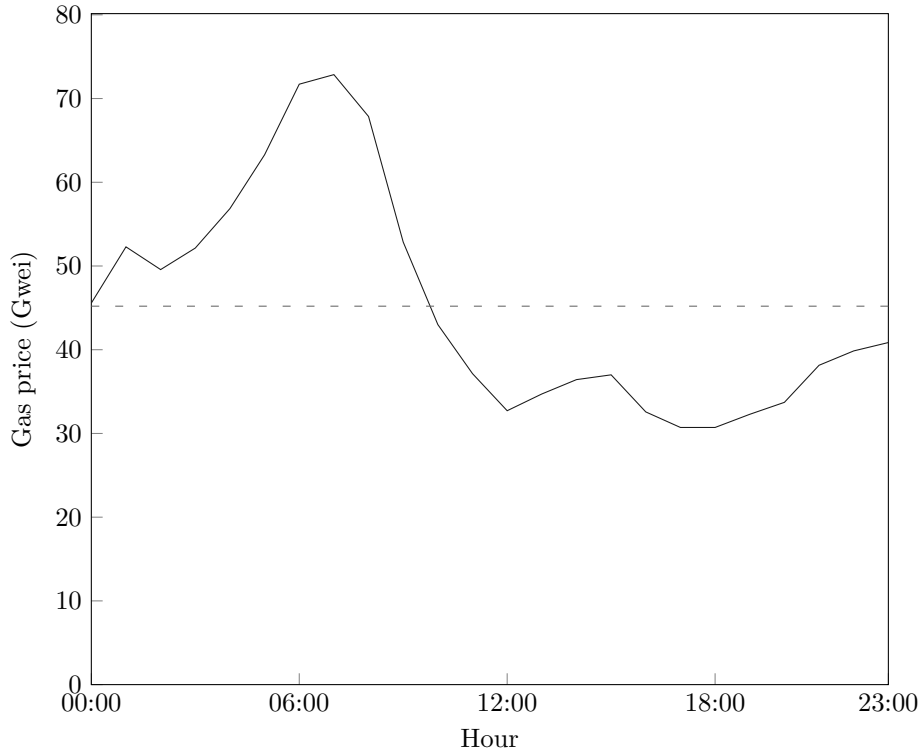


Figure 2: Minimum gas price required to be included in a block by time of the day, with daily average. The data was collected from April 29, 2021 to May 5, 2021. All times are in UTC. Source: GasNow [2021].

9 Key Takeaways

In this section, we list the most meaningful results of our study.

1. The impact of a transaction does not depend only on the gas used, but is instead proportional to the transaction fee;
2. Spending 1 dollar on transaction fees on Ethereum is equivalent to emitting at least 1.115 kgCO₂eq;
3. A blockchain with full blocks pollutes more than one with empty blocks;
4. The single most effective action that a user can take to reduce their own impact is to pay a reasonably lower gas price;
5. Variations in the price of Ether influence the greenhouse gas emissions of the Ethereum network;
6. As of early May 2021, Ethereum emits 24.76 MtCO₂eq per year;
7. EIP-1559 is expected to reduce global Ethereum emissions by about a third;
8. Using Layer 2 technologies significantly reduces the impact of transactions;
9. Transitioning to Proof of Stake remains the best long-term solution for Ethereum.

10 Conclusion

Our figure of 24.76 MtCO₂eq per year represents a grim remainder of the need for scalable solutions to reduce Ethereum emissions.

In this paper, we developed a model that can be used by cryptoartists to not only estimate the emissions of the entire network, but also measure their own environmental impact. We found that, in the short term, the most effective way for a user to reduce their emissions is to execute transactions with longer waiting times or during low-activity hours.

Our model, while designed with cryptoart in mind, can be easily applied to other areas, such as decentralized finance or games. The focus on transactions allows researches and members of the art community to evaluate the effectiveness of new solutions (both on and off chain), providing an immediate feedback and highlighting which research directions are worth pursuing.

A key limitation of our model is that it only takes into account the main factors that influence the behaviour of miners. Future studies might expand upon our work by considering other costs (e.g. human labour) or sources of revenue (e.g. Miner-Extractable Value [Daian et al., 2020]). Since the GHG emissions of the Ethereum blockchain also depend on the price of Ether, modelling the role of activities that influence its value (e.g. financial speculation) could provide a more complete picture of their environmental impact.

We hope that this paper will provide a basis for further developments in the field, with the eventual goal of building decentralized art platforms that unite artist empowerment and sustainable emissions.

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A Closed-Form Expression of R_t

Let $\psi_q(x) = \frac{d}{dx}\Gamma_q(x)$ be the q -digamma function. Let

$$h = \frac{\log\left(\frac{m}{m+KS_0-S_0}\right)}{\log K} \quad (20)$$

The closed-form expression of R_t is:

$$mV\left(\frac{(K-1)\psi_K(t-h+1)}{m\log K} + \frac{(1-K)\psi_K(-h)}{m\log K} - \frac{(K-1)(t+1)}{m}\right) \quad (21)$$

where \log is the natural logarithm.